

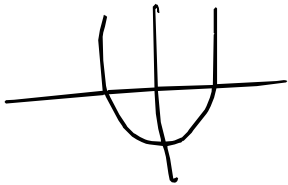
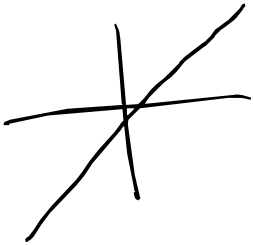
linear

if:

additive: $F(x+y) = F(x) + F(y)$

$$F(ax) = aF(x)$$

if $a \in \mathbb{R}$



higher order polynomials

$x^2, x^3,$

w/ degree > 1

lin eq

$$b = a_1x_1 + a_2x_2 + \dots + a_nx_n$$

a_1, \dots, a_n parameters

x_1, \dots, x_n variables

$$\begin{matrix} b_1 = \\ b_2 \end{matrix} \left. \vphantom{\begin{matrix} b_1 = \\ b_2 \end{matrix}} \right\} \text{linear system}$$

tanks purchased from NATO
allies by Ukraine
 y_i

↓ 1 ... i ... n

$$y_i = 20$$

$x_i = \#$ of visits by country i to UK

$$y_i = \boxed{20} + \boxed{2}x_i$$

$$\hookrightarrow y = \underline{m}x + \underline{b} \rightarrow y = \beta_0 + \beta_1 x$$

$$y = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

SPS: france has 1 visit, 3

germany has 2, 4

$$\left\{ \begin{array}{l} 3 = \beta_0 + \beta_1 \cdot \boxed{1} \\ 4 = \beta_0 + \beta_1 \cdot 2 \end{array} \right.$$

$$4 - 3 = \cancel{\beta_0} - \beta_0 + 2\beta_1 - 1\beta_1$$

$$1 = \beta_1$$

$$3 = \beta_0 + 1 \cdot 1$$

$$\beta_0 = 2$$

Stored as:

Final grades	HW 1	HW 2	HW 3	Final
95	5	10	100	45
30	0	10	13	40
100	100	0	100	100

$$\begin{bmatrix} 95 \\ 30 \\ 100 \end{bmatrix} = \begin{bmatrix} 5 & 10 & 100 & 45 \\ 0 & 10 & 13 & 40 \\ 100 & 0 & 100 & 100 \end{bmatrix} \begin{bmatrix} \text{HW 1} \\ \text{HW 2} \\ \text{HW 3} \\ \text{Final} \end{bmatrix}$$

$$\begin{bmatrix} 4 \\ 3 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} \beta_0 \\ \beta_1 \end{bmatrix}$$

$$4 = \beta_0 + 2\beta_1$$

$$3 = \beta_0 + \beta_1$$

matrices

$m \times n$ matrices have: m rows
 $\downarrow \quad \downarrow$
 $\mathbb{R} \times \mathbb{C}$ n columns

Roman Catholic
 Run & Colours

$$\begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}$$

$$\begin{bmatrix} a_{11} & \dots & a_{1n} \\ \vdots & & \vdots \\ a_{m1} & \dots & a_{mn} \end{bmatrix}$$

1 2 3 ... n

$M \leftarrow C(1, 2, 3), C(1, 4, 5), \text{ rowwise } = T$

$$= \begin{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix} & \begin{bmatrix} 1 \\ 4 \\ 5 \end{bmatrix} \end{bmatrix}$$

$\downarrow \quad \downarrow$
 $C_1 \quad C_2 \quad \dots$

\leftarrow
 $\begin{bmatrix} \vdots \\ \vdots \end{bmatrix}$
 \leftarrow
 $\begin{bmatrix} R_1 \\ R_2 \end{bmatrix}$

$$\vec{C}_i = \begin{bmatrix} a_{1i} \\ \vdots \\ a_{mi} \end{bmatrix}$$

$$\vec{R}_i = [a_{i1} \dots a_{in}]$$

$$R^T = R' = [1 \dots n]$$

$$R = \begin{bmatrix} 1 \\ \vdots \\ n \end{bmatrix}$$

$$\begin{bmatrix} R \\ \vdots \\ R_2 \end{bmatrix} \begin{bmatrix} \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} \\ \begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix} \end{bmatrix}$$

$$\sum \pi [x] = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

$$\begin{bmatrix} 4 \\ 3 \end{bmatrix} = \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} \beta_0 \\ \beta_1 \end{bmatrix}$$

$$= \begin{bmatrix} 1\beta_0 + 2\beta_1 \\ 1\beta_0 + 1\beta_1 \end{bmatrix}$$

$A \cdot \beta$

$$X = \begin{bmatrix} 1 & 1 \\ 1 & 2 \end{bmatrix}$$

$$Y = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$