MATH 2710

1.1 - 1.4 Portfolio

Question 1:

- a) What is a finite set?
- b) Give two examples of finite sets.
- c) What is a countably infinite set?
- d) Give two examples of countably infinite sets.
- e) What is an uncountably infinite set?
- f) Give two examples of uncountably infinite sets.

Question 2:

Write the inclusions between N, Z, Q and R, the most important sets of real numbers.

Question 3:

- a). Write the definition of the interval (a, b) and the definition of the interval (a, ∞) .
- b). Give two examples of intervals of each of the above types.

Question 4:

- a). Write the definition of the cartesian product of two sets and give two examples.
- b). Write the definition of the cartesian product of three sets and give two examples.
- c). Write the definition of the cartesian product of n sets and give two examples.

Question 5:

Specify the cardinality of each of the cartesian products in the above examples.

Question 6:

- a). Write the definition of the equality of two sets A and B.
- b). What is the difference between $A \subseteq B$ and $A \subset B$?

Question 7:

- a). What is the definition of the power set of a set A?
- b). Give two examples of sets and write their power sets.

Question 8:

- a). What does the Power Set Theorem state?
- b). Write the cardinalities of the power sets in the examples from Question 7.

Question 9:

- a). What is the definition of $\binom{n}{k}$? Write it in two different ways.
- b). Write the formula for $\binom{n}{k}$ and give two examples that make use of this formula.

Question 10:

- a). What does the Binomial Theorem state?
- b). Write the expansion of $(2+3)^4$ using the Binomial Theorem.