M-2 Math 2210Q

Question 1 Let  $A = \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix}$  and define  $T : \mathbf{R^2} \to \mathbf{R^2}$  by  $T(\mathbf{x}) = A\mathbf{x}$ . Let  $\mathbf{u} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$  and compute  $T(\mathbf{u})$ .

$$T(\mathbf{u}) = \begin{bmatrix} \boxed{3} \\ \boxed{-1} \end{bmatrix}$$

Question 2 Let  $A = \begin{bmatrix} -1 & 2 \\ 4 & 1 \end{bmatrix}$  and define  $T : \mathbf{R^2} \to \mathbf{R^2}$  by  $T(\mathbf{x}) = A\mathbf{x}$ . Let  $\mathbf{u} = \begin{bmatrix} -3 \\ 1 \end{bmatrix}$  and compute  $T(\mathbf{u})$ .

$$T(\mathbf{u}) = \begin{bmatrix} 5 \\ -11 \end{bmatrix}$$

**Question 3** Let A be a  $7 \times 6$  matrix. What must a and b be in order to define  $T : \mathbf{R}^{\mathbf{a}} \to \mathbf{R}^{\mathbf{b}}$  by  $T(\mathbf{x}) = A\mathbf{x}$ ?

$$a = \boxed{6}$$
  $b = \boxed{7}$ 

**Question 4** Let  $T: \mathbf{R}^3 \to \mathbf{R}$  be a linear transformation. Then

$$T(\mathbf{0}) = \boxed{0}$$