Lay 5.1 Math 2210Q

**Question 1** What are the eigenvalues of A?

$$A = \begin{bmatrix} 2 & 6 \\ 0 & -5 \end{bmatrix}$$

List in order from smallest to largest.  $\lambda_1 = \boxed{-5}$ ,  $\lambda_2 = \boxed{2}$ 

**Question 2** What are the eigenvalues of A?

$$A = \begin{bmatrix} 1 & 2 & -3 \\ 0 & 2 & 5 \\ 0 & 0 & 1 \end{bmatrix}$$

List in order from smallest to largest.  $\lambda_1 = \boxed{1}$ ,  $\lambda_2 = \boxed{2}$ 

**Question 3** What are the eigenvalues of A?

$$A = \begin{bmatrix} -1 & 4 & 3\\ 0 & 5 & -1\\ 0 & 0 & 8 \end{bmatrix}$$

List in order from smallest to largest.  $\lambda_1 = \boxed{-1}$ ,  $\lambda_2 = \boxed{5}$ ,  $\lambda_3 = \boxed{8}$ 

**Question 4** Is  $\lambda = -1$  an eigenvalue of A?

$$A = \begin{bmatrix} -1 & 4 \\ 3 & -2 \end{bmatrix}$$

Multiple Choice:

- (a) Yes
- (b) *No* ✓

**Hint:** The eigenvalues of the echelon form of A are not necessarily the same as the eigenvalues of A. So row reducing to a triangular matrix and looking at the diagonal is not a valid method here. Instead consider the equation  $(A - \lambda I)\vec{x} = \vec{0}$ .

**Question 5** Which of the following is an eigenvector of A?

$$A = \begin{bmatrix} 3 & 0 & -1 \\ 2 & 3 & 1 \\ -3 & 4 & 5 \end{bmatrix}$$

Multiple Choice:

(a) 
$$\vec{x} = \begin{bmatrix} 2\\4\\1 \end{bmatrix}$$

(b) 
$$\vec{x} = \begin{bmatrix} 2 \\ 2 \\ -2 \end{bmatrix} \checkmark$$

**Hint:** A nonzero vector  $\vec{x}$  is an eigenvector of A if  $A\vec{x}$  is a multiple of  $\vec{x}$ , in other words if  $A\vec{x} = \lambda \vec{x}$  for some  $\lambda$ .

**Question 6** True/False: To find the eigenvalues of A are the entries in the main diagonal of U where U is an echelon form of A.

Multiple Choice:

- (a) True
- (b) False ✓

**Hint:** Question 4 is a counter example.

**Question 7** True/False: The scalar zero is an eigenvalue of A if and only if A is not invertible.

Multiple Choice:

- (a) True ✓
- (b) False

**Hint:** Zero is an eigenvalue of A means  $A\vec{x} = 0\vec{x}$  has a nontrivial  $(\vec{x} \neq 0)$  solution. Use the IMT.