

**Question 1** What are the eigenvalues of  $A$ ?

$$A = \begin{bmatrix} 2 & 6 \\ 0 & -5 \end{bmatrix}$$

List in order from smallest to largest.  $\lambda_1 = \boxed{-5}$ ,  $\lambda_2 = \boxed{2}$

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**Question 2** What are the eigenvalues of  $A$ ?

$$A = \begin{bmatrix} 1 & 2 & -3 \\ 0 & 2 & 5 \\ 0 & 0 & 1 \end{bmatrix}$$

List in order from smallest to largest.  $\lambda_1 = \boxed{1}$ ,  $\lambda_2 = \boxed{2}$

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**Question 3** What are the eigenvalues of  $A$ ?

$$A = \begin{bmatrix} -1 & 4 & 3 \\ 0 & 5 & -1 \\ 0 & 0 & 8 \end{bmatrix}$$

List in order from smallest to largest.  $\lambda_1 = \boxed{-1}$ ,  $\lambda_2 = \boxed{5}$ ,  $\lambda_3 = \boxed{8}$

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**Question 4** Is  $\lambda = -1$  an eigenvalue of  $A$ ?

$$A = \begin{bmatrix} -1 & 4 \\ 3 & -2 \end{bmatrix}$$

**Multiple Choice:**

- (a) Yes
- (b) No ✓

**Hint:** The eigenvalues of the echelon form of  $A$  are not necessarily the same as the eigenvalues of  $A$ . So row reducing to a triangular matrix and looking at the diagonal is not a valid method here. Instead consider the equation  $(A - \lambda I)\vec{x} = \vec{0}$ .

**Question 5** Which of the following is an eigenvector of  $A$ ?

$$A = \begin{bmatrix} 3 & 0 & -1 \\ 2 & 3 & 1 \\ -3 & 4 & 5 \end{bmatrix}$$

**Multiple Choice:**

- (a)  $\vec{x} = \begin{bmatrix} 2 \\ 4 \\ 1 \end{bmatrix}$
- (b)  $\vec{x} = \begin{bmatrix} 2 \\ 2 \\ -2 \end{bmatrix}$  ✓

**Hint:** A nonzero vector  $\vec{x}$  is an eigenvector of  $A$  if  $A\vec{x}$  is a multiple of  $\vec{x}$ , in other words if  $A\vec{x} = \lambda\vec{x}$  for some  $\lambda$ .

**Question 6** True/False: To find the eigenvalues of  $A$  are the entries in the main diagonal of  $U$  where  $U$  is an echelon form of  $A$ .

**Multiple Choice:**

- (a) True
- (b) False ✓

**Hint:** Question 4 is a counter example.

**Question 7** True/False: The scalar zero is an eigenvalue of  $A$  if and only if  $A$  is not invertible.

**Multiple Choice:**

- (a) True ✓
- (b) False

**Hint:** Zero is an eigenvalue of  $A$  means  $A\vec{x} = 0\vec{x}$  has a nontrivial ( $\vec{x} \neq 0$ ) solution. Use the IMT.