

**Ranking Models** 

# **Language Models**

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## The ranking problem



### Ranking models recap

Boolean model

- o Boolean query
- Set-based retrieval (no actual ranking)

Vector space models

- Query and documents as vectors
- o Similarity-based ranking

## Probabilistic ranking models

Probabilistic relevance models

- Query and documents as random variables
- Ranking based on probability of relevance

$$f(q,d) = P(R|d,q)$$

## Language modeling approach

Key intuition

- $\circ$  Users who try to think of a good query, think of words that are likely to appear in relevant documents
- A document is a good match to a query if it uses the same underlying *language* as the query

# Statistical language model

A probability distribution over word sequences

- ∘ P("Today is Wednesday") ≈ 0.001
- ∘ *P*("Today Wednesday is") ≈ 0.000000000001
- ∘ P("The eigenvalue is positive") ≈ 0.00001

Can also be regarded as a probabilistic mechanism for "generating" text, thus also called a "generative" model

## Types of language models

Full dependence model

- $\circ P(w_1 ... w_k) = P(w_1)P(w_2|w_1) ... P(w_k|w_1 ... w_{k-1})$ Infeasible in practice
- Expensive computation
- Weak estimates (data sparsity)

## Types of language models

Tunable dependence via n-grams

- ∘ 3-gram ("trigram")
- $P(w_1 \dots w_k) = P(w_1)P(w_2|w_1) \dots P(w_k|w_{k-2}, w_{k-1})$
- o 2-gram ("bigram")
- $P(w_1 \dots w_k) = P(w_1)P(w_2|w_1) \dots P(w_k|w_{k-1})$
- ∘ 1-gram ("unigram")
- $P(w_1 \dots w_k) = P(w_1) P(w_2) \dots P(w_k)$

### **Unigram language model**

The simplest language model

o A one-state probabilistic finite automaton



```
STOP
       0.20
```

- P("frog said that toad likes frog STOP")
- = 0.01 · 0.03 · 0.04 · 0.01 · 0.02 · 0.01 · 0.02
- = 0.000000000048

# **Example text generation**





## **Evaluation of language models**

Direct evaluation criterion

 $\circ$  Goodness of fit: data likelihood, perplexity, cross entropy, Kullback-Leibler divergence

Indirect evaluation criterion

• Task-dependent: we hope more "reasonable" LMs would achieve better task performance

### **Applications of language models**

Language modeling offers a principled way to quantify the uncertainties associated with natural language

## Speech recognition

o Given that we see "John" and "feels", how likely will we see "happy" as opposed to "habit" next?

## **Applications of language models**

Language modeling offers a principled way to quantify the uncertainties associated with natural language

#### **Text categorization**

Given that we see "baseball" three times and "game" once in an article, how likely is it about "sports"?

## Applications of language models

Language modeling offers a principled way to quantify the uncertainties associated with natural language

#### **Document ranking**

• Given that a user is interested in sports news, how likely would he or she use "baseball" in a query?

### Language models for ranking

$$f(q,d) = P(R|d,q)$$
 PRP  
 $\propto P(q,d|R)$  Bayes' rule  
 $\approx P(q,d)$ 

Relevance assumed implicitly!

# Query likelihood model

$$f(q,d) \approx P(q,d)$$
  
=  $P(q|d)P(d)$  Bayes' rule

Two core components  $\circ P(q|d)$ : query likelihood  $\circ P(d)$ : document prior

# Computing P(d)

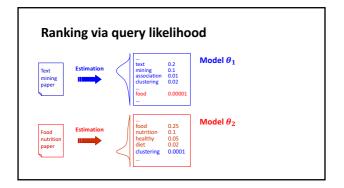
Uninformative (uniform) prior

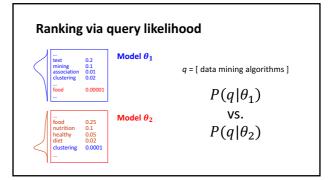
- $\circ P(d) = 1/n$ , for n documents in the corpus Informative prior
- ∘ Authoritativeness (e.g., PageRank)
- o Accessibility (e.g., URL length)
- o Readability (e.g., avg. sentence length)

# Computing P(q|d)

Generative process

 $\circ$  Intuitively, the probability that a user who likes document d (modeled by  $\theta_d)$  will pose query q





# Computing P(q|d)

Under a unigram (term independence) assumption

$$\begin{split} P(q|\theta_d) &= \prod_{t \in q} P(t|\theta_d)^{\mathrm{tf}_{t,q}} \\ &\propto \sum_{t \in q} \mathrm{tf}_{t,q} \log P(t|\theta_d) \end{split}$$

How to estimate  $P(t|\theta_d)$ ?

# Maximum likelihood estimation (MLE)

Simply count observed occurrences

$$\circ P_{\text{MLE}}(t|\theta_d) = \frac{\text{tf}_{t,d}}{|d|}$$

Problems

- $\circ$  Observed terms will be scored too optimistically
- Unobserved terms will receive zero probability

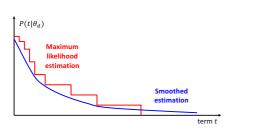
# **Smoothing probabilities**

Smooth probabilities in language models

- $\circ$  Discount the probability of seen words
- o Give some probability mass to unseen words

The probability of a non-occurring term should be close to its probability of occurrence in the corpus  ${\cal C}$ 

## **Smoothing probabilities**



## **Smoothing probabilities**

General form

 $\circ P(t|\theta_d) = (1 - \alpha) P_{\mathsf{MLE}}(t|\theta_d) + \alpha P_{\mathsf{MLE}}(t|\theta_C)$ 

Smoothing controlled through parameter  $\alpha$ 

 $\circ$  Jelinek-Mercer:  $\alpha = \lambda, 0 < \lambda < 1$ 

## Jelinek-Mercer smoothed model

$$\begin{split} f(q, d) &\propto \prod_{t \in q} P(t | \theta_d)^{\mathsf{tf}_{t,q}} \\ &= \prod_{t \in q} \left( (1 - \lambda) \frac{\mathsf{tf}_{t,d}}{|d|} + \lambda \frac{\mathsf{tf}_{t,C}}{|\mathsf{C}|} \right)^{\mathsf{tf}_{t,q}} \end{split}$$

# Jelinek-Mercer example ( $\lambda = 1/2$ )

q: [ michael jackson ]

 $\circ d_1$ : Jackson was a gifted entertainer

 $\circ$   $d_2$ : Michael Jackson anointed himself King of Pop

$$P(q|\theta_1) = \left[\frac{0/5 + 1/12}{2}\right] \times \left[\frac{1/5 + 2/12}{2}\right] \approx 0.008$$

$$P(q|\theta_2) = \left[\frac{1/7 + 1/12}{2}\right] \times \left[\frac{1/7 + 2/12}{2}\right] \approx 0.018$$

## Where is tf-idf weighting?

$$\begin{split} f(q, d) &\propto \sum_{t \in q} \mathsf{tf}_{t, q} \log P(t | \theta_d) \\ &= \sum_{t \in q} \mathsf{tf}_{t, q} \log \left( (1 - \lambda) \frac{\mathsf{tf}_{t, d}}{|d|} + \lambda \frac{\mathsf{tf}_{t, C}}{|\mathsf{C}|} \right) \end{split}$$

### Where is tf-idf weighting?

$$f(q, d) \propto \sum_{t \in q} \operatorname{tf}_{t, q} \log \left( \frac{(1 - \lambda) \frac{\operatorname{tf}_{t, d}}{|d|}}{\lambda \frac{\operatorname{tf}_{t, C}}{|C|}} + 1 \right)$$

## Where is tf-idf weighting?

$$f(q,d) \propto \sum_{t \in q} \mathrm{tf}_{t,q} \log \left( \frac{(1-\lambda) \frac{\mathrm{tf}_{t,d}}{|d|}}{\lambda \frac{\mathrm{tf}_{t,C}}{|C|}} + 1 \right)$$

- Proportional to term frequency: tf effect
- o Inv. proportional to collection frequency: idf effect

## How about document length?

General form

 $\circ P(t|\theta_d) = (1 - \alpha) P_{\mathsf{MLE}}(t|\theta_d) + \alpha P_{\mathsf{MLE}}(t|\theta_C)$ 

Smoothing controlled through parameter  $\alpha$ 

 $\circ$  Jelinek-Mercer:  $\alpha = \lambda$ ,  $0 < \lambda < 1$ 

 $\circ \text{ Dirichlet:} \qquad \qquad \alpha = \frac{\mu}{|d| + \mu} \qquad \qquad \frac{|d| \to 0 \ :: \ \alpha \to 1}{|d| \to \infty \ :: \ \alpha \to 0}$ 

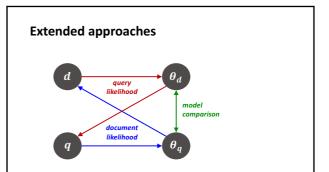
#### How effective are these?

Dirichlet smoothing works the best

o Particularly effective for keyword queries

Length-adjusted smoothing

- Shorter documents get more smoothing
- o Longer documents get less smoothing



# Document likelihood model

$$f(q,d) \approx P(q,d)$$
  
=  $P(d|q)P(q)$  Bayes' rule  
 $\propto P(d|\theta_q)$ 

Problem: queries are short  $\circ$  Poor estimation of  $\theta_q$ 

Solution: improve query model via feedback

### **Model comparison**

Two steps

- $\circ$  Build both  $\theta_q$  and  $\theta_d$
- Measure how much they diverge

Divergence-based ranking

 $\circ f(q,d) = -D(\theta_q||\theta_d)$ 

## **Model comparison**

Kullback-Leibler (KL) divergence ∘ Asymmetric measure [0,∞]

$$\begin{split} f(q, d) &= -D_{\text{KL}}(\theta_q || \theta_d) \\ &= -\sum_t P\Big(t \big| \theta_q\Big) \log \frac{P(t |\theta_q)}{P(t |\theta_d)} \end{split}$$

## **Summary**

Principled ranking approach

Statistical foundations (better parameter setting)

Effectiveness through smoothing

Add key ranking components (idf, document length)

Flexible and extendable

 $\circ$  Relevance feedback, priors, other tasks

#### References

<u>Introduction to Information Retrieval</u>, Ch. 12 Manning et al., 2008

<u>Search Engines: Information Retrieval in Practice</u>, Ch. 7 Croft et al., 2009

Statistical Language Models for Information Retrieval

Zhai, FnTIR 2008

#### References

<u>A language modeling approach to information retrieval</u> Ponte and Croft, SIGIR 1998

A study of smoothing methods for language models applied to information retrieval

Zhai and Lafferty, SIGIR 2001

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Coming next...

# **Information-theoretic Models**

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