

Ranking Models

Structural Models

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The ranking problem



Simplifying assumptions

Query terms occur independently of one another

- [information retrieval] = [information + retrieval]

All query term occurrences worth the same

- information (title) = information (anchor text) = ...
- retrieval (title) = retrieval (anchor text) = ...

Structural models

Exploiting query structure

- Term dependence models

Exploiting document structure

- Field-based models

Exploiting query structure

Term independence widely assumed

- Make modeling simpler
- Make estimation tractable

Key limitation

- Assumption does not hold in practice
- $P(\text{retrieval} \mid \text{information}) \neq P(\text{retrieval})$

Term dependence models

Full dependence model

- $P(t_1 \dots t_k) = P(t_1)P(t_2|t_1) \dots P(t_k|t_1 \dots t_{k-1})$
- Infeasible in practice (expensive and unreliable)

Tunable dependence (e.g., bigram model)

- $P(t_1 \dots t_k) = P(t_1)P(t_2|t_1) \dots P(t_k|t_{k-1})$
- Considers only dependences wrt previous terms

Term dependence models

Different dependence types

- [hubble telescope achievements]

Short-range dependences

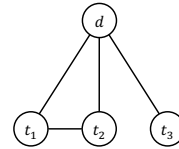
- hubble-telescope, telescope-achievements

Long-range dependences

- hubble-achievements, achievements-hubble

Markov Random Field (MRF) model

Undirected graphical model representing the joint probability $P(q, d)$ over $q = t_1 \dots t_k$ and d



Markov Random Field (MRF) model

Undirected graphical model representing the joint probability $P(q, d)$ over $q = t_1 \dots t_k$ and d

$$P(q, d) = \frac{1}{Z_\Lambda} \prod_{c \in \mathcal{C}(G)} \psi(c; \Lambda)$$

where

- $c \in \mathcal{C}(G)$ is a clique on G
- $\psi(c; \Lambda)$ is a potential function over c

Dependence types

Full independence (FI)

- All terms are independent

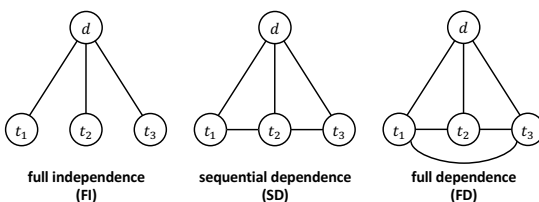
Sequential dependence (SD)

- Terms dependent on neighbor terms

Full dependence (FD)

- Terms dependent on all other terms

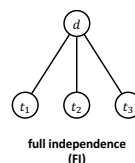
Dependence types



Potential functions

Linear models defined over cliques

$$\psi(c; \Lambda) \propto \lambda_x f_x(c_x)$$



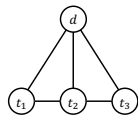
$$c_1 \in \{\{t_1, d\}, \{t_2, d\}, \{t_3, d\}\}$$

full independence (FI)

Potential functions

Linear models defined over cliques

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sequential dependence
(SD)

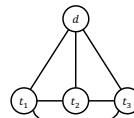
$$c_1 \in \{\{t_1, d\}, \{t_2, d\}, \{t_3, d\}\}$$

$$c_2 \in \{\{t_1, t_2, d\}, \{t_2, t_3, d\}\}$$

Potential functions

Linear models defined over cliques

$$\circ \psi(c; \Lambda) \propto \lambda_x f_x(c_x)$$



full dependence
(FD)

$$c_1 \in \{\{t_1, d\}, \{t_2, d\}, \{t_3, d\}\}$$

$$c_2 \in \{\{t_1, t_2, d\}, \{t_2, t_3, d\}, \{t_1, t_2, t_3, d\}\}$$

$$c_3 \in \{\{t_1, t_3, d\}\}$$

Potential functions

Linear models defined over cliques

$$\circ \psi(c; \Lambda) \propto \lambda_x f_x(c_x)$$

Different measures of compatibility

$$\circ f_1(c_1) \equiv P(t_i | d)$$

$$\circ f_2(c_2) \equiv P(\langle t_i, t_{i+1} \rangle_w | d)$$

$$\circ f_3(c_3) \equiv P(\langle t_i, t_{k \neq i} \rangle_w | d)$$

Markov Random Field (MRF) model

$$f(q, d) = P(d | q)$$

$$= P(q, d) / P(q)$$

$$\propto P(q, d)$$

$$= \frac{1}{Z_\Lambda} \prod_{c \in \mathcal{C}(G)} \psi(c; \Lambda)$$

$$\propto \sum_{c \in \mathcal{C}(G)} \log \lambda_x f_x(c_x)$$

Markov Random Field (MRF) model

$$\begin{aligned} f(q, d) = & \lambda_1 \sum_{t_i} \log P(t_i | d) \\ & + \lambda_2 \sum_{t_i} \sum_{t_k = i+1} \log P(\langle t_i, t_k \rangle_w | d) \\ & + \lambda_3 \sum_{t_i} \sum_{t_k \neq i} \log P(\langle t_i, t_k \rangle_w | d) \end{aligned}$$

Proximity matches

How to estimate $P(\langle t_i, t_k \rangle_w | d)$?

◦ Must compute proximity matches

Counting pairs of words within a window of size w

◦ Efficiently computed with positional indexes

What's wrong with per-field scores?

Ranking with fields

Scores across fields are incompatible

- Summing saturated (non-linear) tf over fields may inflate the overall document score
- Sparse background statistics for some fields (e.g., title) may lead to a poor estimation of idf
- Document length semantics varies across fields (e.g., a long anchor text should not be penalized)

Ranking with fields

Rather than combining per-field scores

$$f(q, d) = \sum_{t \in q} \sum_{a \in d} w_a g(\text{tf}_{t,a})$$

Combine per-field frequencies

$$f(q, d) = \sum_{t \in q} g\left(\sum_{a \in d} w_a \text{tf}_{t,a}\right)$$

Cross-field statistics

Calculate weighted variants of statistics

- $\tilde{\text{tf}}_{t,d} = \sum_{a \in d} w_a \text{tf}_{t,a}$
- $\tilde{\text{dl}}_d = \sum_{a \in d} w_a \text{dl}_a$

Example: BM25F

BM25 [Robertson and Walker, 1994]

$$\circ f(q, d) = \sum_{t \in q} \text{tf}_{t,q} \frac{(k_1+1)\text{tf}_{t,d}}{\text{tf}_{t,d} + k_1 \left((1-b) + b \frac{\text{dl}_d}{\text{avdl}} \right)} \log \frac{n+1}{n_t}$$

Example: BM25F

BM25F [Robertson and Zaragoza, 2004]

$$\circ f(q, d) = \sum_{t \in q} \text{tf}_{t,q} \frac{(k_1+1)\tilde{\text{tf}}_{t,d}}{\tilde{\text{tf}}_{t,d} + k_1 \left((1-b) + b \frac{\tilde{\text{dl}}_d}{\text{avdl}} \right)} \log \frac{n+1}{n_t}$$

Empirically, field-specific document length normalization (i.e., b_a) has shown benefits

Summary

Structural properties of queries and documents can help improve ranking effectiveness

Term dependence models

- Both short- and long-range dependences

Field-based models

- Field-adjusted term-document statistics

References

[Search Engines: Information Retrieval in Practice](#), Ch. 11

Croft et al., 2009

[Dependence language model for information retrieval](#)

Gao et al., SIGIR 2004

[A Markov random field model for term dependencies](#)

Metzler and Croft, SIGIR 2005

References

[Modeling higher-order term dependencies in information retrieval using query hypergraphs](#)

Bendersky and Croft, SIGIR 2012

[A comparison of retrieval models using term dependencies](#)

Huston and Croft, CIKM 2014

References

[Introduction to Information Retrieval](#), Ch. 6

Manning et al., 2008

[Simple BM25 extension to multiple weighted fields](#)

Robertson et al., CIKM 2004

[Parameterized fielded term dependence models for ad-hoc entity retrieval from knowledge graph](#)

Nikolaev et al., SIGIR 2016



Coming next...

Quality Models

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