Water Bottle Rocket Design Contest Calculation Exercises



Elementary School Division $3^{rd} - 5^{th}$ Grade



1. The Skywalker team constructed a water bottle rocket and used the materials hidden in the word search below. Help your team figure out the list by finding the words.

J	S	G	J	Α	V	В	Τ	Χ	Н	Μ	D	Α	M
V	0	L	F	E	Χ	E	Н	Τ	Α	S	0	V	L
W	D	J	L	Τ	Τ	Χ	E	Y	С	Р	U	В	С
Α	Α	S	V	E	Α	V	R	Ι	G	Η	Τ	0	G
Α	Q	С	J	K	Η	R	S	Μ	J	Η	R	Χ	Y
M	Ν	Ι	U	С	В	S	В	F	Τ	R	Α	С	K
0	D	Ε	N	0	0	Ν	G	Χ	U	В	L	0	L
Χ	Ν	Ρ	Α	R	Τ	Y	Μ	G	M	0	U	Χ	F
G	L	R	S	Z	Т	Т	Α	Р	Ε	Α	G	Ι	J
Τ	D	Y	N	M	L	Τ	L	Ε	Ε	F	N	Y	Ε
0	D	L	I	Т	Ε	R	K	U	U	L	Α	S	Р
U	G	F	Z	D	Т	Ν	J	С	Χ	Т	I	M	D
I	Ν	G	G	Y	С	S	Т	Ε	0	С	R	N	K
Τ	V	U	R	M	Q	R	J	M	0	Ε	Τ	M	0
Q	K	Χ	K	V	V	D	0	S	Α	Ε	Χ	S	С
	V W A A W O X G T O U I T	V O W D A A A Q W N O D X N G L T D O D U G I N T V	V O L W D J A A S A Q C W N I O D E X N P G L R T D Y O D L U G F I N G I V U	V O L F W D J L A A S V A Q C J W N I U O D E N A A S A F D Y N O D L I D F Z D T T <td>V O L F E W D J L T A A S V E A Q C J K W N I U C O D E N O X N P A R Y N W W Y N W W Y Y X Y Y Y X Y Y Y X Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y</td> <td>V O L F E X W D J L T T A A S V E A A Q C J K H W D E N O O A D A R T C D Y N W L D D I I T E D D I I T E D D I I I I D D I I I I D D I I I I D D I I I I D I I I I I D I I I I I D I I I I I D I I I I I</td> <td>V O L F E X E W D J L T T X A A S V E A V A Q C J K H R W D E N O O N W D E N D D N W D D D D D D D W D</td> <td>V O L F E X E H W D J T T X E A A S V E A V R A Q C J K H R S W N I</td> <td>V O L F E X E H T W D J L T T X E Y A A S V E A V R I A A S V E A V R I W A C B S B F W A D C D A C X W A D D D D X D D W A D</td> <td>V O L F E X E H T A W D J L T T X E Y C A A S V E A V R I G A A S V E A V R I G W A B B S B F T W A B B S B F T W A B B S B F T W A B B S B F T W A B B B B F T D W A B</td> <td>V O L F E X E H T A S W D J T T X E Y C P A A S V E A V R I G H A A S I</td> <td>V O L F E X E H T A S O W D J L T T X E Y C P U A A S V E A V R I G H T A A S I</td> <td>W D J T T X E Y C P U B A A S V E A V R I G H T O A Q C J K H R S M J H R X W N I U C B S B F T R A C W N I</td>	V O L F E W D J L T A A S V E A Q C J K W N I U C O D E N O X N P A R Y N W W Y N W W Y Y X Y Y Y X Y Y Y X Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y Y	V O L F E X W D J L T T A A S V E A A Q C J K H W D E N O O A D A R T C D Y N W L D D I I T E D D I I T E D D I I I I D D I I I I D D I I I I D D I I I I D I I I I I D I I I I I D I I I I I D I I I I I	V O L F E X E W D J L T T X A A S V E A V A Q C J K H R W D E N O O N W D E N D D N W D D D D D D D W D	V O L F E X E H W D J T T X E A A S V E A V R A Q C J K H R S W N I	V O L F E X E H T W D J L T T X E Y A A S V E A V R I A A S V E A V R I W A C B S B F W A D C D A C X W A D D D D X D D W A D	V O L F E X E H T A W D J L T T X E Y C A A S V E A V R I G A A S V E A V R I G W A B B S B F T W A B B S B F T W A B B S B F T W A B B S B F T W A B B B B F T D W A B	V O L F E X E H T A S W D J T T X E Y C P A A S V E A V R I G H A A S I	V O L F E X E H T A S O W D J L T T X E Y C P U A A S V E A V R I G H T A A S I	W D J T T X E Y C P U B A A S V E A V R I G H T O A Q C J K H R S M J H R X W N I U C B S B F T R A C W N I

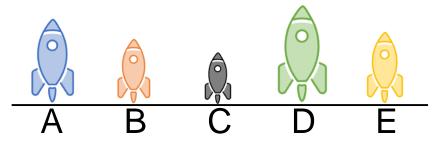
Word List

BOARD	
BOTTLE	
BOX	
CORRUGATED	
EGGSHELLS	
FIN	

HAT LITER PARTY RIGHT ROCKET SCISSORS SODA TAPE TRIANGULAR TWO



Use the data table below to answer questions 2 and 3.



Rocket	Weight (kg)	Height (cm)
А	100	125
В	25	65
С	15	25
D	125	100
E	80	85

2. List the five rockets from lightest to heaviest. Use the data in the table above.

Rocket (Letter)			
Weight (kg)			

3. List the five rockets above from tallest to shortest. Use the data in the table above.

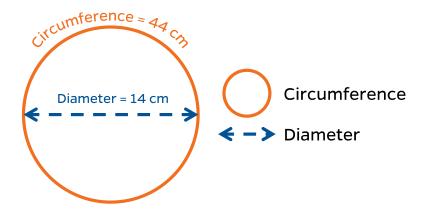
Rocket (Letter)			
Height (cm)			



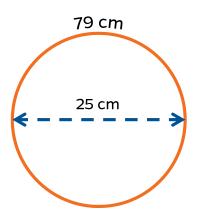
Question 4 Example:

The **distance around a circle** is known as the **circumference**. The **diameter** is the **distance across the circle**, which goes through the circle's center.

The example below shows the circle circumference is **44 cm**, and the diameter is **14 cm**.



4. What is the circumference and diameter of the circle below?



Circumference = ____ cm

Diameter = ____ cm



Question 5 Example:

The equation for the circumference of a circle is:

$$C = \pi \times D$$

C is the circumference of a circle.

 π is the Greek symbol pi and is constant equal to $22/7 \approx 3.14$

D is the diameter of the circle.

Example A:

A circle has a diameter of 5 cm. What is the circumference of the circle?

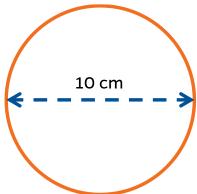
$$C = \pi \times D$$

$$C = \pi \times (5 cm)$$

$$C = (3.14 \times 5 cm)$$

$$C = 16 cm$$

5. What is the circumference and diameter of the circle below? (Use 3.14 for the value of π)



Diameter = ____ cm

Circumference = ____ cm



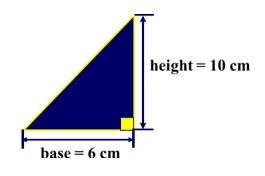
Question 6 Examples:

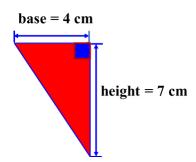
A **triangle** is a shape that has three sides and three angles that add up to **180 degrees**. A **right triangle** is a type of triangle that has one angle that is **90 degrees**. The fins on the water bottle rockets are made of triangles. These fins help keep the rocket on track and stop it from spinning in the air.

Below are two right triangles with the bases and heights labeled. Notice that the height is the "up and down" measurement and that the base is the "across" measurement.

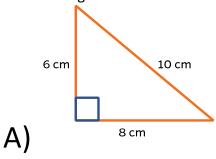
Example 1: The height of the triangle below is **10 cm**, and the base is **6 cm**.

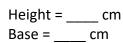
Example 2: The base of the triangle is <u>4 cm</u>, and the height of the triangle is <u>7 cm</u>.

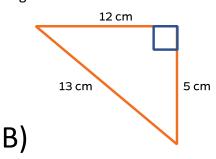




6. What are the heights and the bases of the right triangular fins below?









Question 7 Examples:

The perimeter of a figure is the total distance around a shape; in other words, it is the sum of the lengths of the sides of a shape.

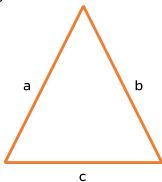
The equation for the perimeter of a triangle is the following:

$$P = a + b + c$$

a = side length

b = side length

c = side length

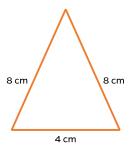


Example A: What is the perimeter of the triangle?

$$P = a + b + c$$

$$P = 8 \text{ cm} + 8 \text{ cm} + 4 \text{ cm}$$

 $P = 20 \text{ cm}$

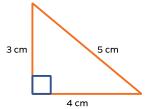


Example B: What is the perimeter of the right triangle?

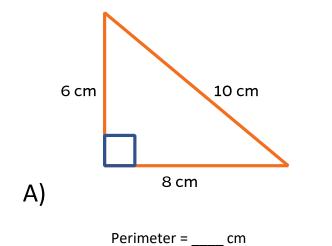
$$P = a + b + c$$

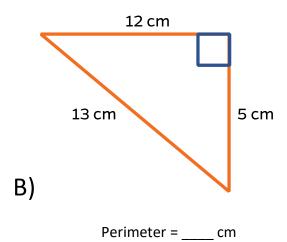
$$P = 3 cm + 5 cm + 4 cm$$

 $P = 12 cm$



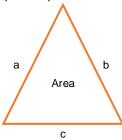
7. What are the perimeters of the two right triangle fins below?



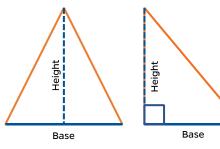


Question 8 Examples:

The **area** of a shape is the space within or enclosed by the perimeter of a shape. The area of a triangle is the space between sides a, b, and c, shaded blue in the triangle below.



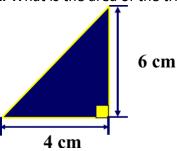
We can calculate the area of a triangle using this formula:

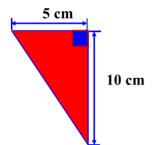


Area (A) =
$$\frac{1}{2}$$
 b × h

b = base of the triangleh = height of the triangle

Example A: What is the area of the triangle fin?

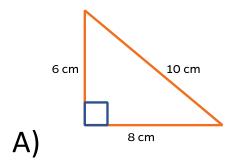


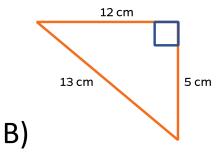


Area (A) =
$$\frac{1}{2}$$
 b × h
A = ½ (4 cm) X 6 cm
A = 12 cm²

Area (A) =
$$\frac{1}{2}$$
 b × h
A = ½ (5 cm) X 10 cm
A = 25 cm²

8. Calculate the area for each of the fins below and compare.







Question 9 Examples:

MEAN

The mean is the average value of the number set, or the "central" value of the number set ("How to Find the Mean," 2020).

How to Find the Mean. (n.d.). Retrieved November 21, 2020, from https://www.mathsisfun.com/mean.html

To find the **mean** of set of numbers, follow these steps:

- A. Add up all the values (the numbers) in the number set to find the **sum** or **total** of the number set.
- B. **Count** the number of **values** in the number set.
- C. Divide the sum (or total) calculated in Step A by the number of values counted in Step B to calculate the **mean**.

Example A: What is the mean of this number set? 9, 13, 1, 15, 8, 4, 6

Step A: Find the sum of the number set. Sum = 9 + 13 + 1 + 15 + 8 + 4 + 6

Sum = 56

Step B: Count the number of values in the number set. Number of Values = 7

Step C: Divide the Sum by the Number of Values. Mean = 56/7 Mean = 8

MEDIAN

The median is the middle number of a set of numbers ("How to Find the Median Value," 2020). How to Find the Median. (n.d.). Retrieved November 21, 2020, from https://www.mathsisfun.com/median.html

To find the **median** follow these steps:

- A. Rearrange the numbers in the number set to be in numerical order from least to greatest
- B. Find the number that is in the middle of the number set. Do this by crossing off 1 number from each end until you get to the middle of the number set.
 - a. If you have a number set with an even number of numbers, complete Step B until you get to the last 2 numbers in the middle. Calculate the B of the two middle numbers to find the median.

Example A: What is the median of this number set? 9, 13, 1, 15, 8, 4, 6

Step A: Rearrange from lowest to highest: 1, 4, 6, 8, 9, 13, 15

Step B: Cross off numbers from each end to find the middle: 1, 4, 6, 8, 9, 13, 15

Median = 8

Example B: What is the median of this number set? 21, 9, 13, 1, 15, 8, 4, 6 Step A: Rearrange from lowest to highest: 1, 4, 6, 8, 9, 13, 15, 21

Step B: Cross off numbers from each end to find the middle: 1, 4, 6, 8, 9, 13, 15, 21

Step B(a): Find the mean between the two middle numbers: Median = $\frac{8+9}{2} = \frac{17}{2} = 8.5$



MODE

The mode is the number that appears most often(frequent) in the number set ("How to Find the Mode or Modal Value," 2020). A number set having two modes is called "bimodal," and a number set having more than two modes is called "multimodal."

How to Find the Mode. (n.d.). Retrieved November 21, 2020, from https://www.mathsisfun.com/mode.html

To find the **mode** follow these steps:

A. Put the numbers in numerical order from least to greatest.

B. Count the number of times each number appears in the number set.

C. The number that appears the most is the **mode**.

Example A: What is the mode of the number set? 9, 15, 13, 1, 15, 8, 4, 15, 8 Step A: Rearrange from lowest to highest: 1, 4, 8, 8, 9, 13, 15, 15, 15

Step B: Count the number of times each number appears:

1 Time: 1, 4, 9, 13 2 Times: 8 3 Times: 15

Step C: Number repeated the most is the mode: Mode = 15

Example 2: What is the mode of the number set? 1, 9, 15, 13, 1, 15, 8, 4, 15, 1

Step A: Rearrange from lowest to highest: 1, 1, 1, 4, 8, 9, 13, 15, 15

Step B: Count the number of times each number appears:

1 Time: 4, 8, 9, 13 3 Times: 1, 15

Step C: Number repeated the most is the mode: Modes = 1 & 15

RANGE

The range is the difference between the lowest and highest values ("The Range (Statistics)," 2020).

The Range (Statistics). (n.d.). Retrieved November 21, 2020, from https://www.mathsisfun.com/data/range.html

To find the **range** follow these steps:

- A. Put the numbers in numerical order from least to greatest.
- B. Subtract the smallest number in the number set from the largest number in the data set.

Example A: What is the range of this number set? 9, 13, 1, 15, 8, 4, 15 Step A: Rearrange from lowest to highest: 1, 4, 8, 9, 13, 15, 15

Step B: Subtract the smallest number from the largest: Range = 15 - 1

Range = 14



9. The hangtime is the amount of time the water bottle rocket stays in the air before landing. The hangtimes of five water bottle rockets are listed below.

Rocket	Hangtime (seconds)
А	7
В	5
С	9
D	5
E	11

Determine the following using the data in the chart above. Reference the previous examples for help.

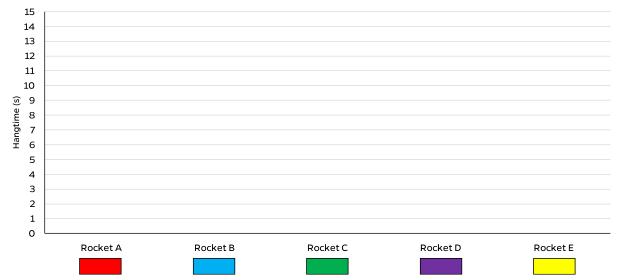
- a) Longest hangtime = ____ seconds, Rocket ____
- b) Shortest hangtime = _____ seconds, Rocket _____
- c) Mean hangtime = ____ seconds, Rocket ____
- d) Median hangtime = ____ seconds, Rocket ____
- e) Mode hangtime = _____ seconds, Rocket _____
- f) Range of hangtimes = ____ seconds



10. Construct a bar graph to illustrate hangtimes in problem 9 with the space provided for each water bottle rocket using the same colors below the name of each Rocket.

Rocket	Hangtime (seconds)		
А	7		
В	5		
С	9		
D	5		
E	11		

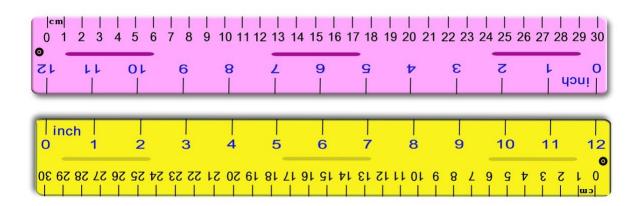
Water Bottle Rocket Hangtime





11. Examine the rulers below. Note that one side measures centimeters, part of the metric system, and the other side measures in inches, part of the imperial system commonly used in the United States.

It is important to know how to take measurements using both systems and how to convert measurements between them.



How many centimeters are in an inch? (Between which centimeter values does 1 inch lie?)

____ cm to ____ cm

How many inches are in 10 centimeters? (Between which inch values does 10 cm lie?)

____ in. to ____ in.



12. Examine the below the volumes in ounces and liters with the different containers

How many ounces are in 1 liter?

____ ounces = 1 liter



Question 13 & 14 Examples

The average weight of a fully assembled space shuttle is 4,500,000 pounds. What is the average weight of a space shuttle in kilograms?

https://www.nasa.gov/centers/johnson/pdf/167751main FS SpaceShuttle508c.pdf



This Photo by Unknown Author is licensed under CC BY

$$1 lb = 0.45 kg$$

Let's convert pounds to kilograms.

4,500,000 Jbs. X
$$\frac{0.45 \text{ kg}}{1 \text{ Jbs.}}$$
 = 2,025,000 kg

13. How much do you weigh in pounds (lbs)? (Write an estimate if you are not sure)

lbs

14. How much do you weight in kilograms (kg)? 1 pound = 0.45 kg

____ kg







