Figures Mathematical Techniques For Engineers
Complex Analysis

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October 9, 2025

2.1.1 Continuity Definition

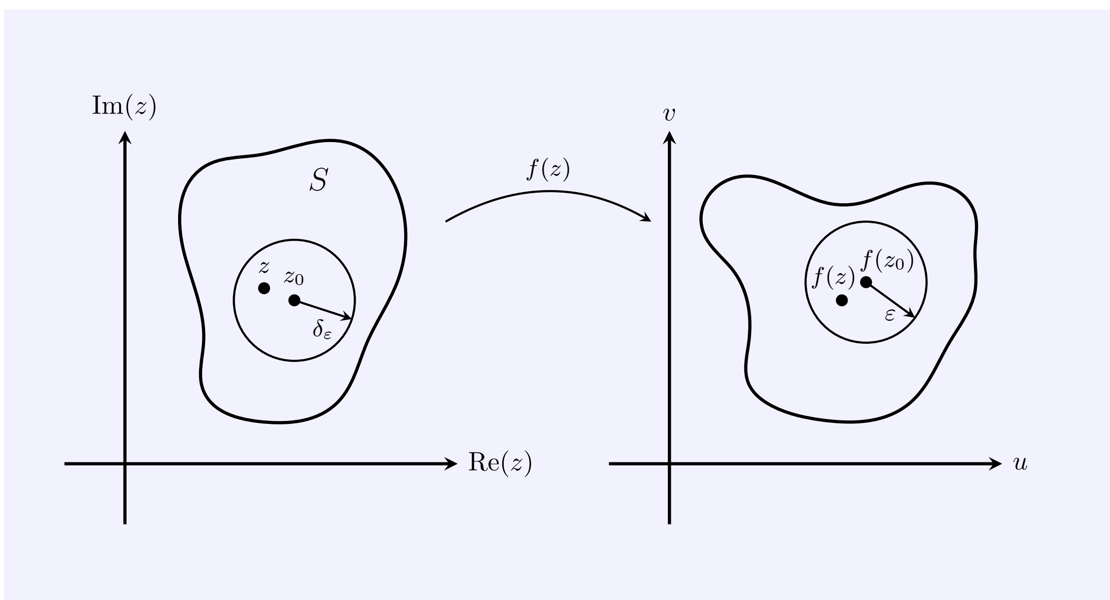

Figure 1: The function f is continuous in z_0 if $(\forall \varepsilon > 0)(\exists \delta_\varepsilon > 0)(\forall z \in S)(|z - z_0| < \delta_\varepsilon \Longrightarrow |f(z) - f(z_0)| < \varepsilon)$.

2.4 Geometrical Interpretation Of The Complex Derivative

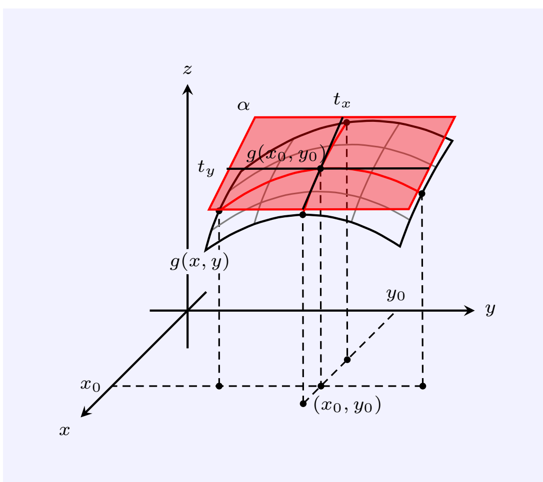

Figure 2: In every point $g(x_0, y_0)$ of a surface $g(x, y)$, a tangent plane can be drawn (red). The tangent lines t_x, t_y are oriented according to the x- and y-axis, respectively. They have a slope which corresponds to the partial derivatives $\frac{\partial}{\partial x}$ and $\frac{\partial}{\partial y}$, respectively.

3.2.12 Symmetry of points

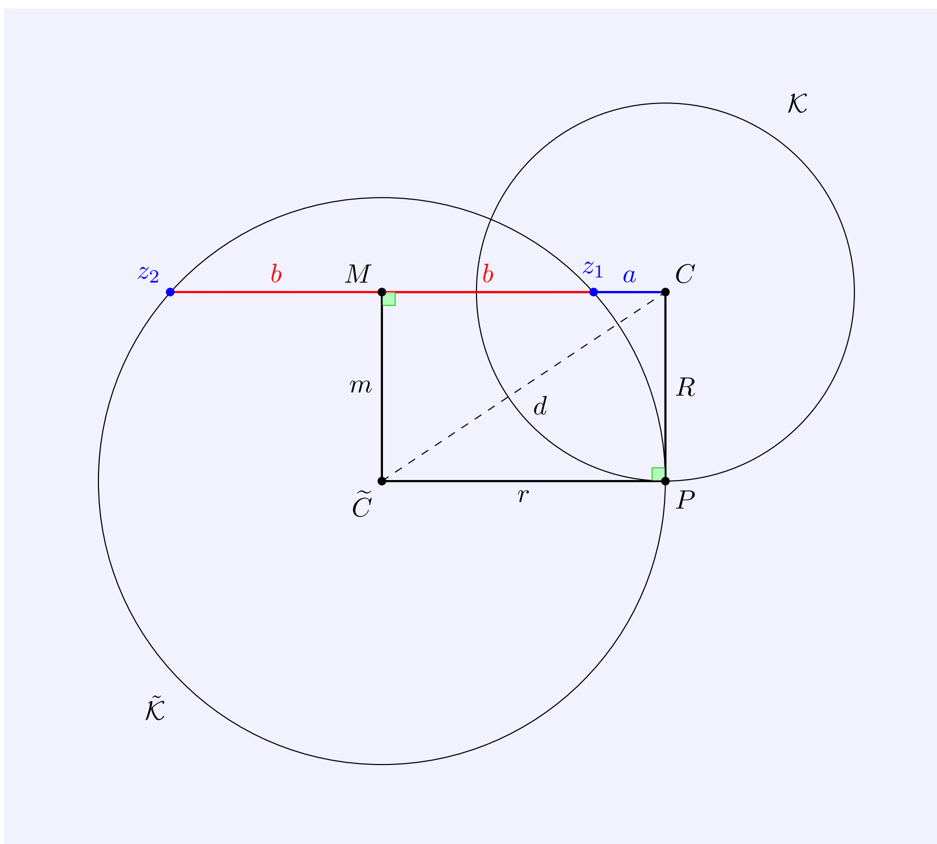

Figure 3: The points z_1 and z_2 are symmetrical with respect to the circle $\mathcal{K} = S(C, R)$.

3.5.1 Exponential function periodicity

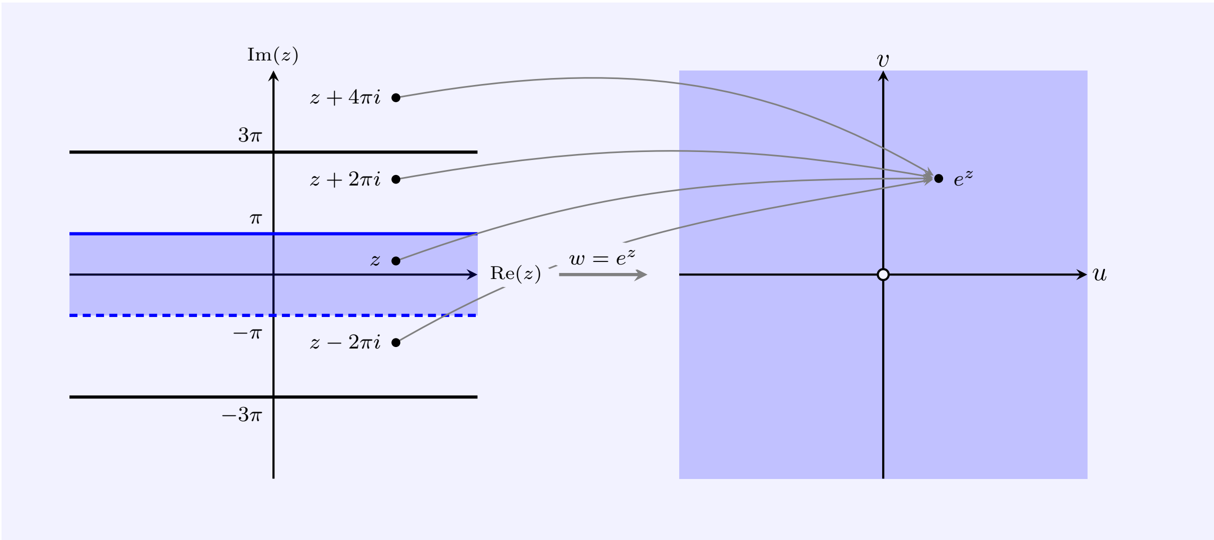

Figure 4:

3.5.2 Exponential function image vertical lines

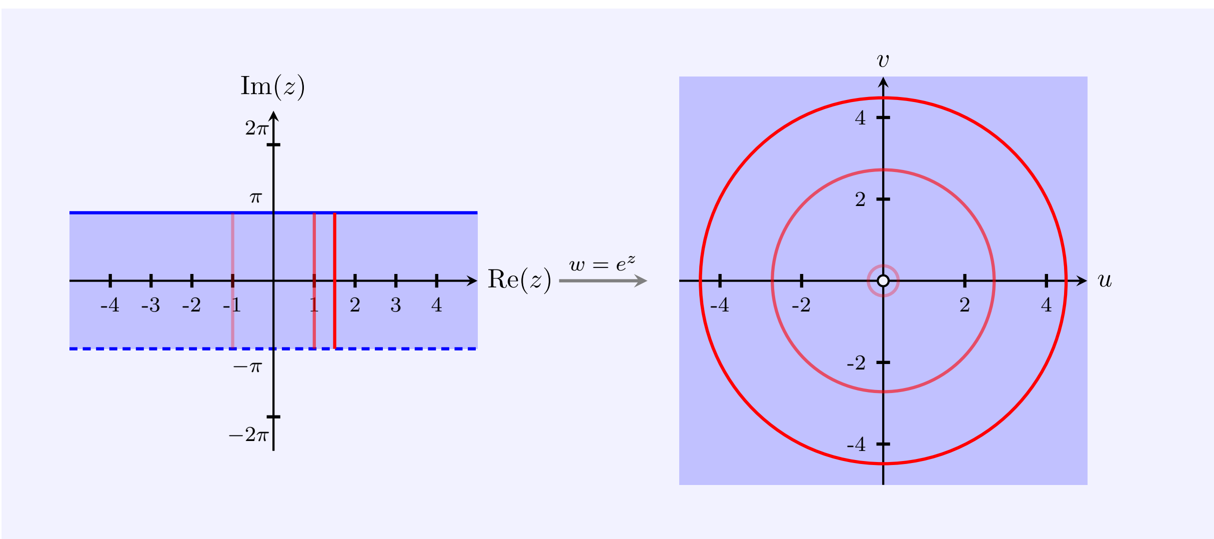

Figure 5:

3.5.3 Exponential function image horizontal lines

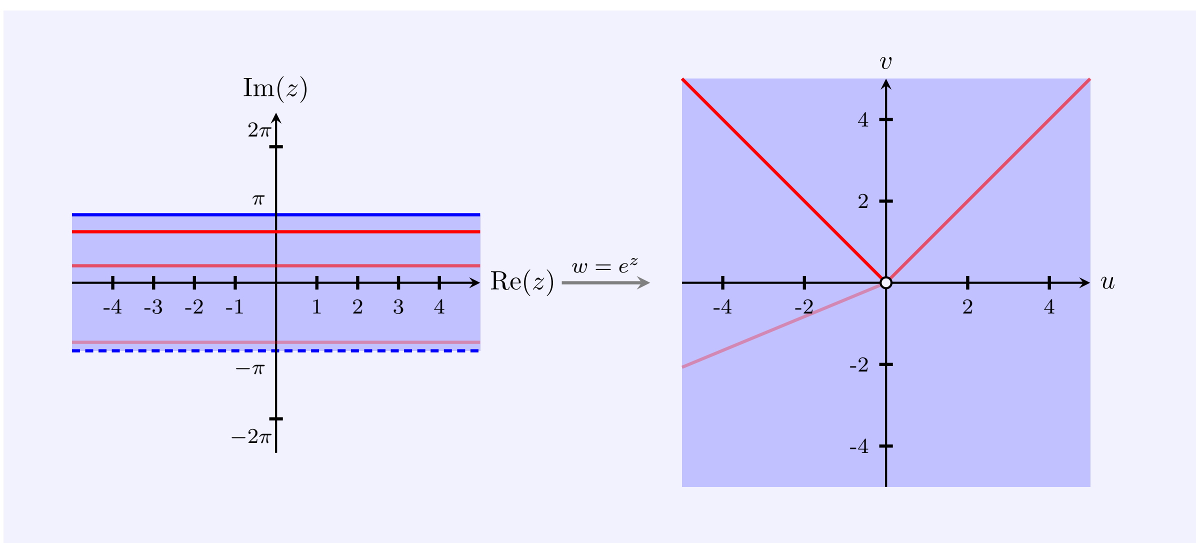

Figure 6:

3.8.4 Exercise

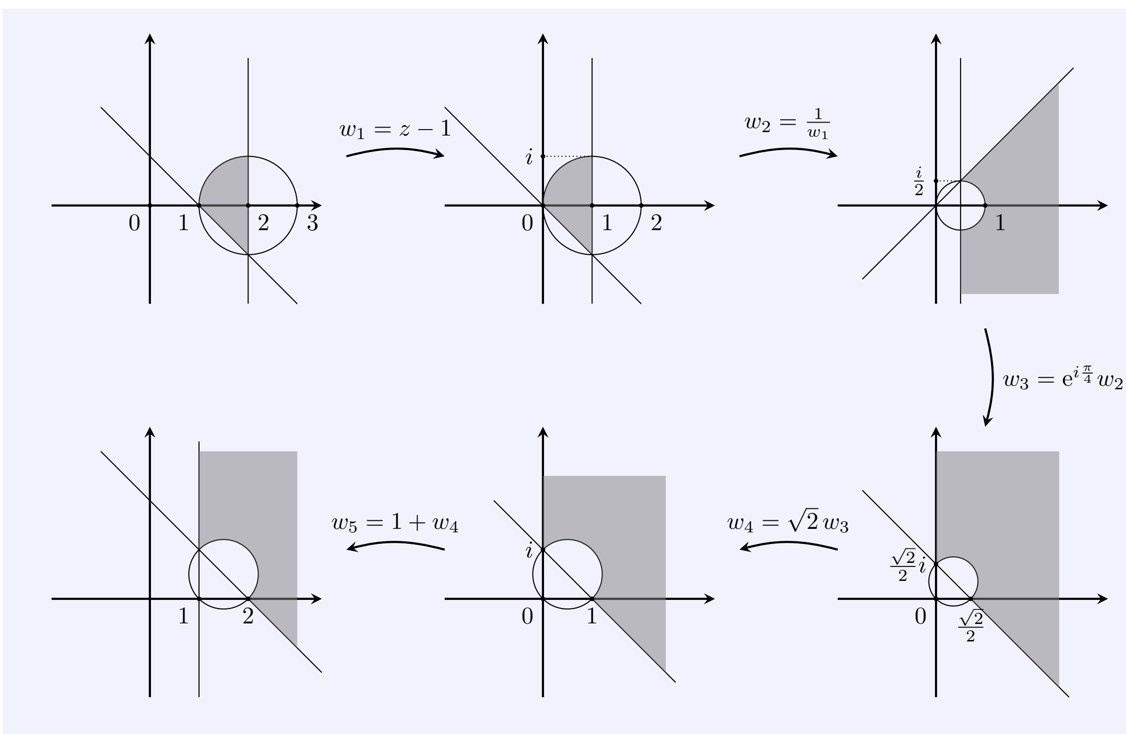

Figure 7: Image of domain $\mathcal{D} = \{z \in \mathbb{C} | \mathrm{Re}(z) + \mathrm{Im}(z) \geq 1,\ |z-2| \leq 1,\ \mathrm{Re}(z) \leq 2\}$ through the function $f(z) = \frac{z+i}{z-i}$.

5.1.1

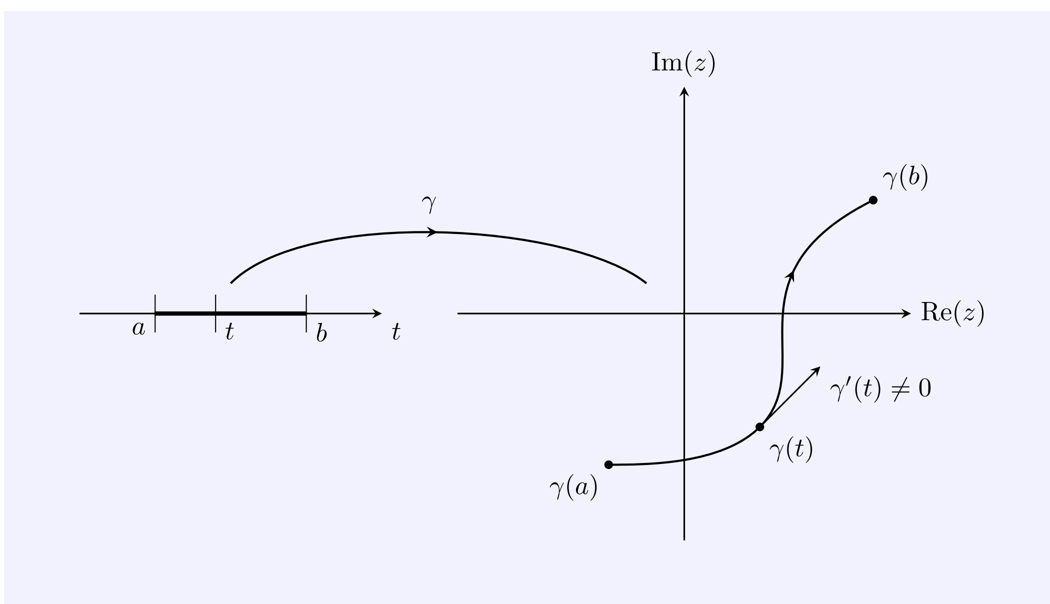
$\mathrm{Im}(z)$
$\gamma(b)$
γ
$\mathrm{Re}(z)$
a
t
b
t
$\gamma'(t) \neq 0$
$\gamma(t)$
$\gamma(a)$

Figure 8:

5.2.3

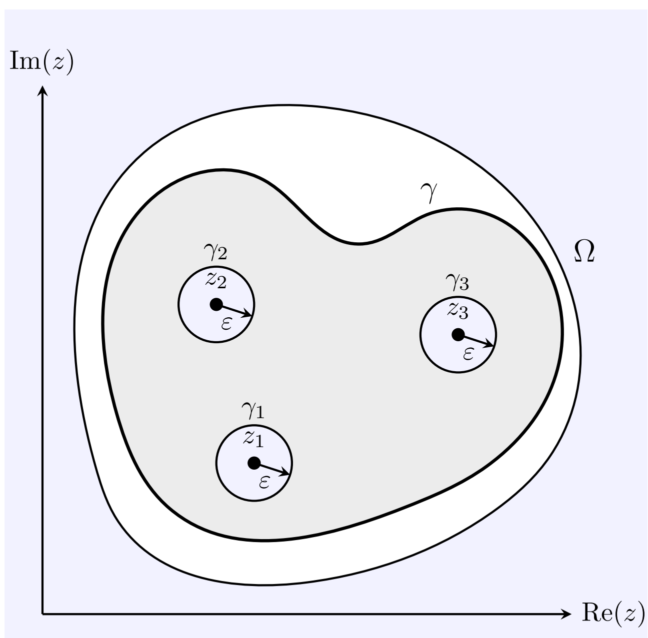
Im(z)
Re(z)
γ
Ω
γ_2
z_2
ε
γ_3
z_3
ε
γ_1
z_1
ε

Figure 9:

5.3 Cauchy integral formulas and consequences

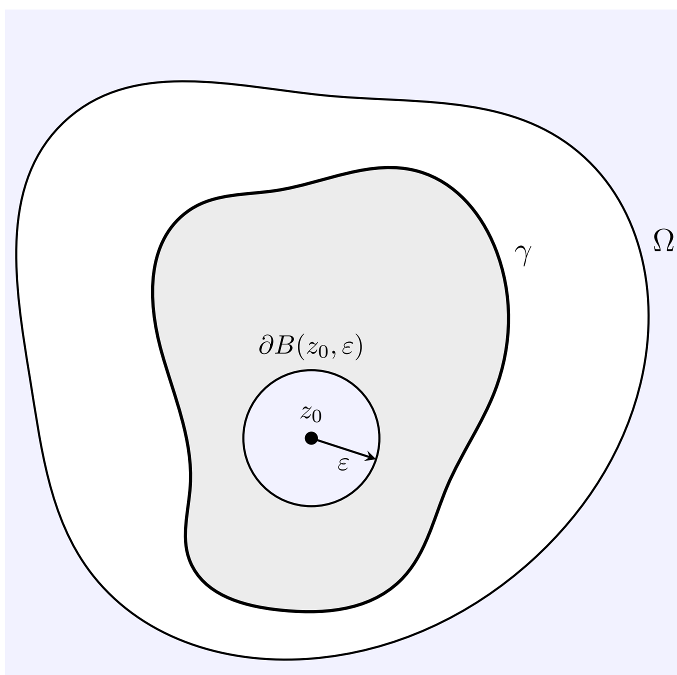

Figure 10:

5.4.4

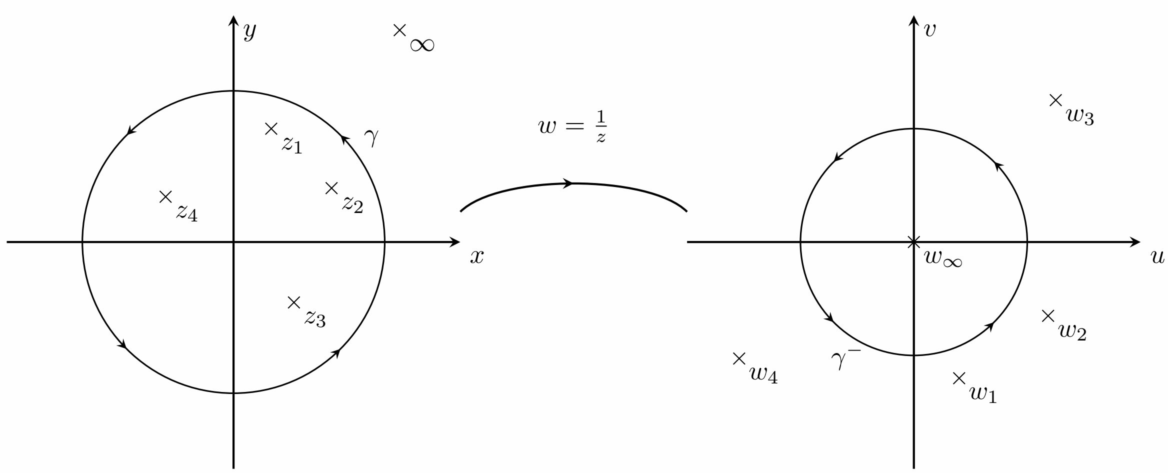

Figure 11:

5.5.2 Uniqueness of holomorphic functions

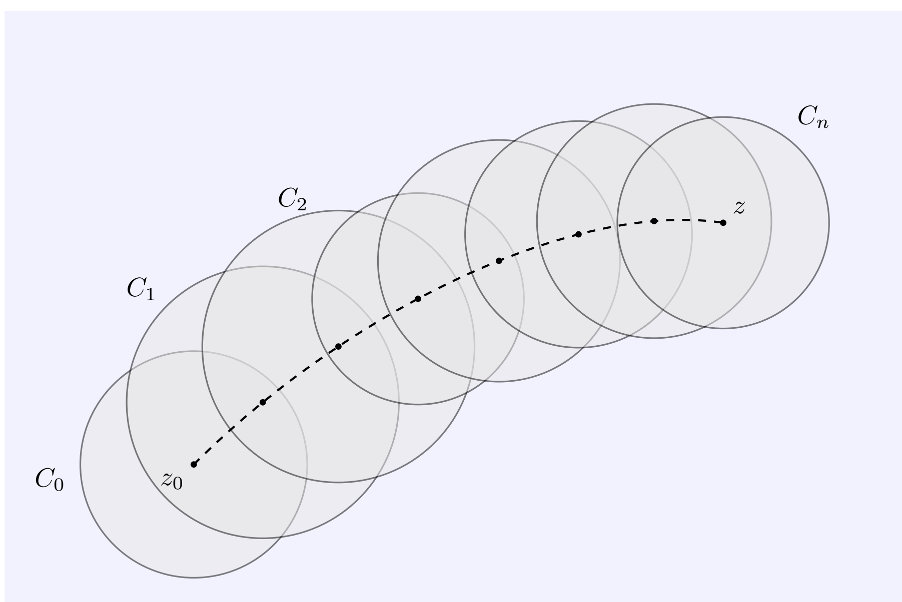

Figure 12: Let f be holomorphic in the space $\Omega \subseteq \mathbb{C}$. If $z_0 \in \Omega$ is an accumulation point of zeros of f, then $f \equiv 0$ over the entire space Ω.

5.6.2

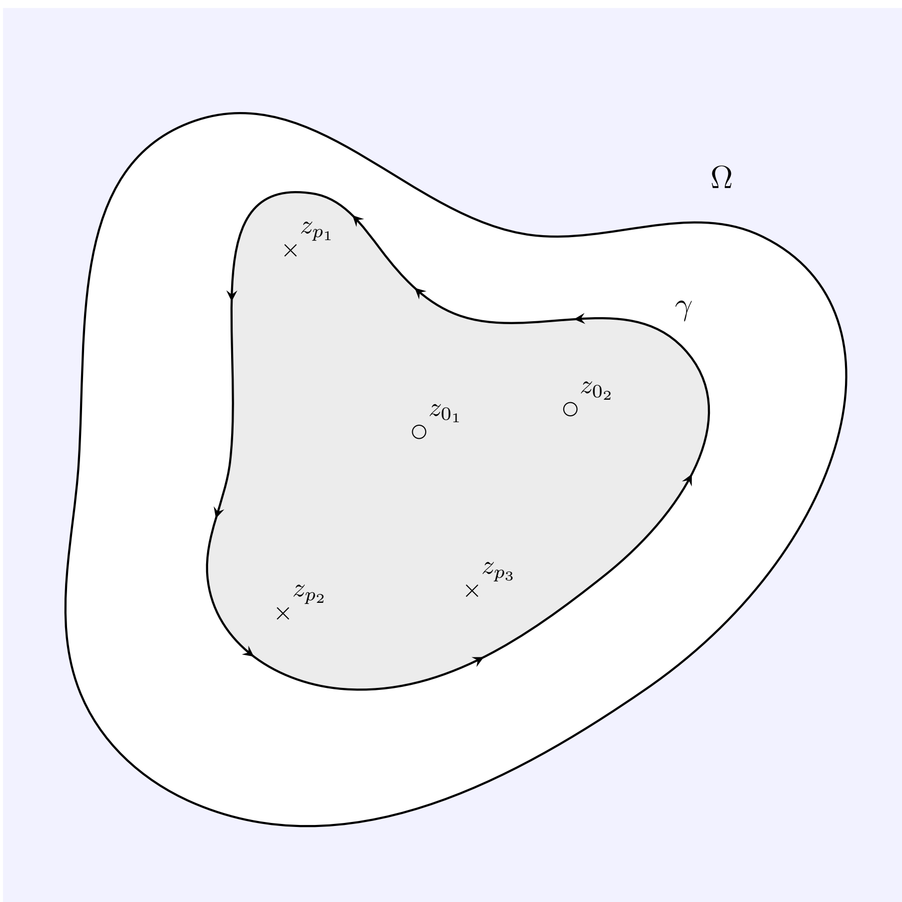

Figure 13:

5.6.3 Argument Principle

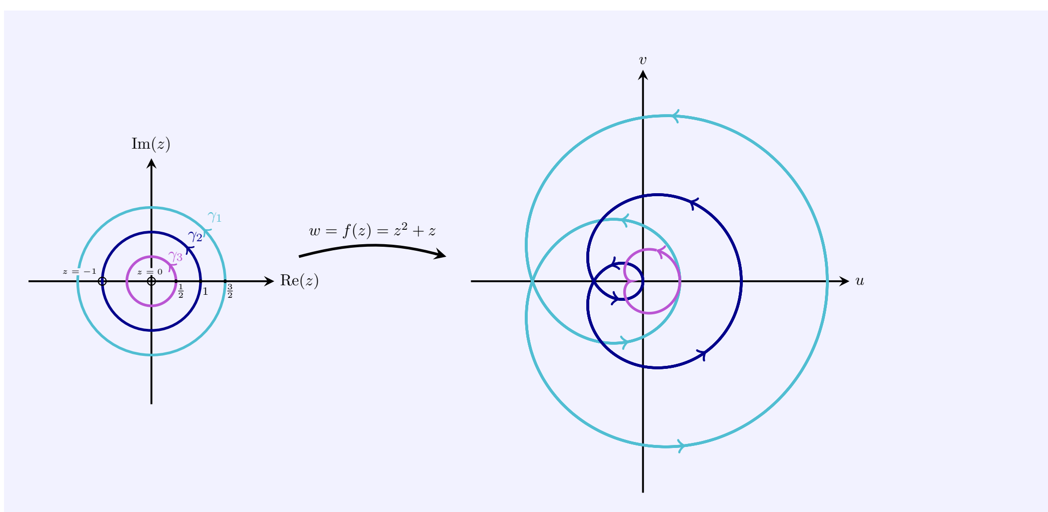

Figure 14: Illustration of the argument principle for $f(z) = z^2 + z$. The images of the circles $\gamma_1, \gamma_2, \gamma_3$ under f show how many times each curve winds around the origin, corresponding to the number of zeros of f inside each circle.

5.6.3 Rouches theorem

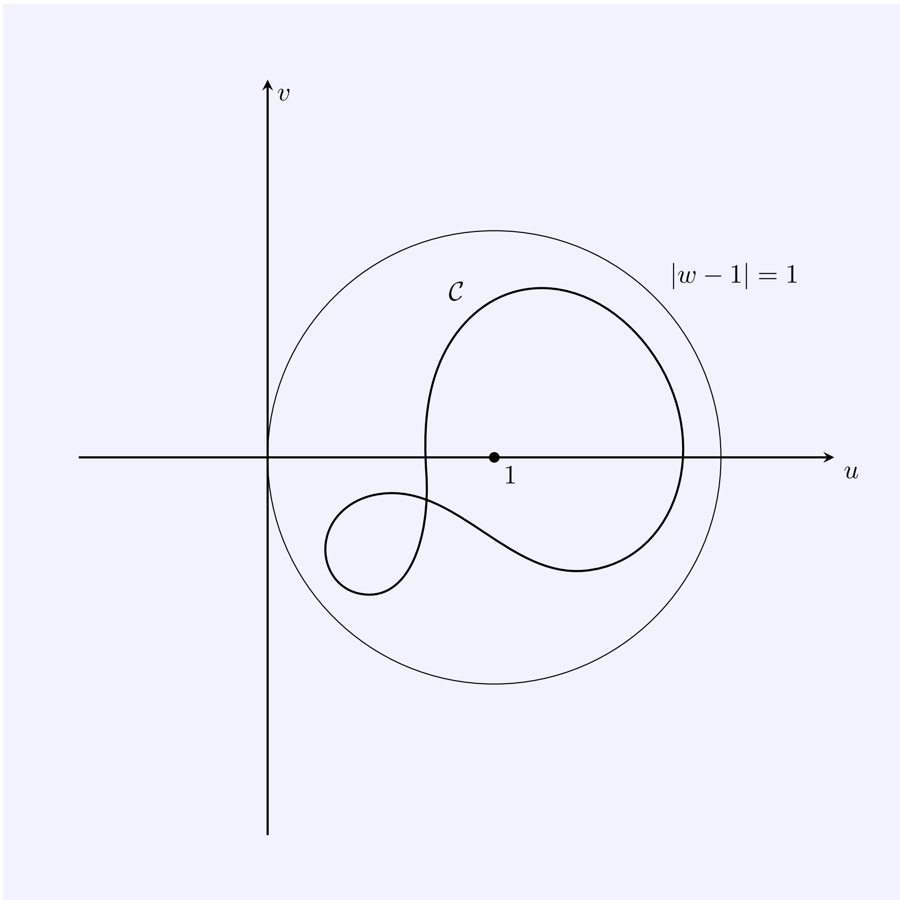

Figure 15: