

ECE 374 B ✧ Spring 2024

🌀 Homework 7 🌀

- **Submit your solutions electronically on the course Gradescope site as PDF files.** If you plan to typeset your solutions, please use the \LaTeX solution template on the course web site. If you must submit scanned handwritten solutions, please use a black pen on blank white paper and a high-quality scanner app (or an actual scanner, not just a phone camera).
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👉 Some important course policies 👉

- **You may use any source at your disposal**—paper, electronic, or human—but you *must* cite *every* source that you use, and you *must* write everything yourself in your own words. See the academic integrity policies on the course web site for more details.
 - **Avoid the Three Deadly Sins!** Any homework or exam solution that breaks any of the following rules will be given an *automatic zero*, unless the solution is otherwise perfect. Yes, we really mean it. We're not trying to be scary or petty (Honest!), but we do want to break a few common bad habits that seriously impede mastery of the course material.
 - Always give complete solutions, not just examples.
 - Always declare all your variables, in English. In particular, always describe the specific problem your algorithm is supposed to solve.
 - Never use weak induction.
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See the course web site for more information.

If you have any questions about these policies,
please don't hesitate to ask in class, in office hours, or on Piazza.

1. You are given a list $D[n]$ of n words each of length k over an alphabet Σ in a language you don't know, although you are told that words are sorted in lexicographic order. Using $D[n]$, describe an algorithm to efficiently identify the order of the symbols in Σ . For example, given the alphabet $\Sigma = \{Q, X, Z\}$ and the list $D = \{QQZ, QZZ, XQZ, XQX, XXX\}$, your algorithm should return QZX . You may assume D always contains enough information to completely determine the order of the symbols. (Hint: use a graph structure, where each node represents one letter.)

2. Given a directed-acyclic-graph ($G = (V, E)$) with integer (positive or negative) edge weights:
 - (a) Give an algorithm to find the length of the **shortest** path from a node s to a node t .
 - (b) Give an algorithm to find the length of the **longest** path from a node s to a node t .

3. You are given a **directed-acyclic-graph** $G = (V, E)$ with possibly negative weighted edges:
 - (a) Give an algorithm that finds the length of the shortest path that contains at most k edges between two vertices u and v in $O(k(n + m))$ time.
 - (b) Give an algorithm that finds the length of the shortest path that contains exactly k edges between two vertices u and v in $O(k(n + m))$ time.

Hint: You can solve both problems almost the same way. Modify the graph G and utilize the algorithm from problem 2 part (a).