Homework 3

- Submit your solutions electronically on the course Gradescope site as PDF files. If you plan to typeset your solutions, please use the ETEX solution template on the course web site. If you must submit scanned handwritten solutions, please use a black pen on blank white paper and a high-quality scanner app (or an actual scanner, not just a phone camera). We will mark difficult to read solutions as incorrect and move on.
- Every homework problem must be done *individually*. Each problem needs to be submitted to Gradescope before 6AM of the due data which can be found on the course website: https://ecealgo.com/su24/homeworks.html.
- For nearly every problem, we have covered all the requisite knowledge required to complete a homework assignment prior to the "assigned" date. This means that there is no reason not to begin a homework assignment as soon as it is assigned. Starting a problem the night before it is due a recipe for failure.

 Policies to 	keep in	mind —
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- You may use any source at your disposal—paper, electronic, or human—but you *must* cite *every* source that you use, and you *must* write everything yourself in your own words. See the academic integrity policies on the course web site for more details.
- Being able to clearly and concisely explain your solution is a part of the grade you will receive. Before submitting a solution ask yourself, if you were reading the solution without having seen it before, would you be able to understand it within two minutes? If not, you need to edit. Images and flow-charts are very useful for concisely explain difficult concepts.

See the course web site (https://ecealgo.com/su24/) for more information.

If you have any questions about these policies, please don't hesitate to ask in class, in office hours, or on Piazza.

1. **Cyclic paths of hell.** A Hamiltonian cycle in a graph is a cycle that visits every vertex exactly once. A Hamiltonian path in a graph is a path that visits every vertex exactly once, but it need not be a cycle (the last vertex in the path may not be adjacent to the first vertex in the path.)

Consider the following three problems:

- *Directed Hamiltonian Cycle* problem: checks whether a Hamiltonian cycle exists in a *directed* graph,
- *Undirected Hamiltonian Cycle* problem: checks whether a Hamiltonian cycle exists in an *undirected* graph.
- *Undirected Hamiltonian Path* problem: checks whether a Hamiltonian path exists in an *undirected* graph.
- a Give a polynomial time reduction from the *directed* Hamiltonian cycle problem to the *undirected* Hamiltonian cycle problem.
- b Give a polynomial time reduction from the *undirected* Hamiltonian Cycle to *directed* Hamiltonian cycle.
- c Give a polynomial-time reduction from undirected Hamiltonian *Path* to undirected Hamiltonian *Cycle*.
- 2. Pls No Yapping. Just Circle Em'.
 - 1. **True/False:** If *L* is an NP-complete language and $L \in P$, then P = NP.
 - 2. **True/False:** There exists a polynomial-time reduction from every problem in NP to every problem in P.
 - 3. True/False: If a problem is both NP-hard and co-NP-hard, then it must be in NP.
 - 4. **True/False:** If there is a polynomial-time reduction from problem A to problem B and B is in NP, then A must also be in NP.
 - 5. **True/False:** If a problem is solvable in polynomial space, then it is also solvable in polynomial time.
- 3. Cooking Levin so hard he won't even be able to SAT Special 4SAT is a version of 4SAT in which each literal appears at most once in Φ . We write a solver for Special 4SAT as follows:

For each literal q in Φ :

- Flip a fair coin
- If heads, assign q = True
- If tails, assign q = False

In terms of m, what is the expected number of clauses satisfied? Write the most efficient solver for Special4SAT.