- 1. Suppose we are given both an undirected graph *G* with weighted edges and a minimum spanning tree *T* of *G*.
 - (a) Describe an efficient algorithm to update the minimum spanning tree when the weight of one edge $e \in T$ is decreased.
 - (b) Describe an efficient algorithm to update the minimum spanning tree when the weight of one edge $e \notin T$ is increased.
 - (c) Describe an efficient algorithm to update the minimum spanning tree when the weight of one edge $e \in T$ is increased.
 - (d) Describe an efficient algorithm to update the minimum spanning tree when the weight of one edge $e \notin T$ is decreased.

In all cases, the input to your algorithm is the edge e and its new weight; your algorithms should modify T so that it is still a minimum spanning tree. Of course, we could just recompute the minimum spanning tree from scratch in $O(|E| + |V| \log |V|)$ time, but you can do better.

2. Let G = (V, E) be an undirected graph where each edge has a weight from the set $\{1, 10, 25\}$. Describe a *linear-time* algorithm to find an MST of G.