Statistical inference with weights and survey design variables

A practical guide using UKDS datasets

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Introduction

This note aims at setting out guidelines for population inference using weights and survey design variables with UKDS social surveys. It focuses on providing users with practical procedures for safe estimation and only discuss the theoretical underpinnings of survey design, sampling or estimation with weighted survey data where it is necessary. The content is based on technical documents by data producers such as the Office for National Statistics as well as the relevant statistical literature. Examples are currently drawn from the Labour Force Survey, the Family Expenditure Survey and the British Social Attitudes Survey and will be gradually be expanded. A list of key references and online tutorials is provided in the bibliography.

Social surveys are data collection exercises that produce datasets enabling researchers and analysts to learn about the characteristics of human populations and societies. This is achieved by way of conducting statistical inference, the process through which unknown quantities (sometimes called parameters) of such 'large' populations are estimated with the help of samples that are drawn from them. Estimation of population parameters traditionally consist in computing two pieces of information: a measure of a value of interest also known as point estimate, such as a mean or a median, together with an indication of its degree of uncertainty or precision (as standard error). Alternatively, one could also decide to represent likely values of population estimates explicitly as a range of values or interval.

It has been demonstrated that when certain conditions are met, such as when samples are randomly drawn and sample size is large enough, surveys and the parameter estimates inferred from them are representative of the corresponding population (Lohr 2019 - 2010). Robust, unbiased estimates are estimates that are not only *representative* – they reflect the characteristic of interest in the population, but also *precise* enough for the inference to be meaningful. Unfortunately, in part as a result of design decisions, in part – and increasingly so – due to non response, raw, ie uncorrected, population estimates from real-world social surveys present some degree of bias.

It is usually considered that in order to produce robust population estimates from potentially biased samples, including as much of the survey design information as possible along-side(non response and sampling) weights is required. Conversely, estimates computed without weights or accounting for survey design will at best present some degree of bias or even might be altogether unreliable. Computing weighted estimates and accounting for survey design require specific procedures that are not usually very well documented as the relevant statistical techniques are more complex and overlooked in introductory textbooks, and their practical implementation in statistical software may not always be clear. It is therefore necessary to add some clarity to this situation and provide adequate guidelines in order for users of UKDS data to properly implement robust estimation strategies that are adapted to their needs, which is the purpose of this document.

1. Basics of Survey Design

At the core of survey design are the strategies adopted in order to collect samples. Sample units can either be selected randomly, an approach also known as probability sampling, or not - for example when internet users are taking part to an online poll. Random sampling is usually preferred as it minimises the risk of obtaining non representative or biased samples - for example where certain groups of the population are under represented or altogether excluded. Statistical textbooks usually consider that simple random sampling - simply drawing population members at random - is the best way to obtain a random sample and avoid bias. This is however difficult to achieve in practice with real life social surveys. Simple random sampling requires a sampling frame ie ideally a list of all members of the population of interest. In countries without a national register - a database of all residents - such a list does not exist and needs to be approximated by other means which may be costly to achieve. Simple random sampling can also not be optimal when groups within the population are known to have different probability to take part to surveys.

In practice designing surveys entails striking a balance between maximising representativeness as well as sample size (for greater precision of the results) while keeping costs down. For these reasons, large scale social surveys tend to produce random samples via other means than simple random sampling. Techniques are employed for example, to ensure each country of the UK is correctly represented which may might involve taking separate samples for England, Scotland, Wales and Northern Ireland and that certain sub-groups, for example the ethnic minorities, are adequately represented..

Two common survey design techniques employed are *clustering* and *stratification*.

1.1 Clustering

Clustering usually goes hand in hand with multistage sampling, that is drawing sample units in several stages rather than all at once. It consists in dividing the population into groups that are as internally heterogeneous as possible - one could think of them as 'mini populations', some of which are then randomly selected while others are left out.

The UK context In Great-Britain, the closest that comes to a population register that can be used as a sampling frame is a list of addresses kept by Royal Mail, also know as the Postcode Address File (PAF). For Northern Ireland the most commonly used is the Land and Property Services Agency's (LPSA). As a list of addresses however, the PAF cannot be used to draw a simple random sample of either households or individuals as the number of dwellings, households and individuals at each address in not indicated.

The nature of the PAF address structure easily enables geographical clustering in UK surveys. Addresses, or 'delivery points' cluster into larger units, for example the post code M13 9PL is embedded within the the M13 'post code district' and the M13 9 'postcode sector'. Survey designs often use either postcode sectors or districts as Primary Sampling Units (PSUs). This may be used for instance in order to reduce fieldwork costs and time.

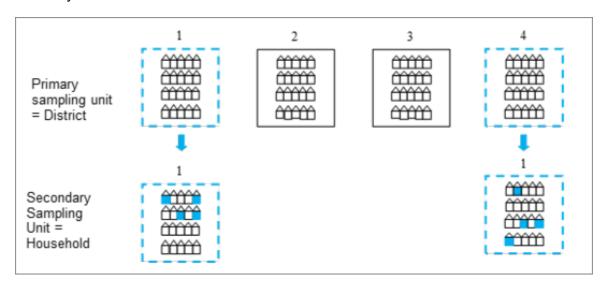


Figure 1: Clustering in two stage sampling

Figure 1 provides a simplified illustration of clustering with four districts as Primary Sampling Units (PSUs). The dotted lines indicate that districts 1 and 4 have been selected to be in the sample. A second stage of sampling follows where within the two sampled districts samples of households are taken. As a result, of this design we obtain a sample of households but these households are clustered within a sample of districts.

Subsequently drawing of either further clusters or final sample members take place within the already selected clusters. These higher level clusters, ie those at which the first random draw happened as known as Primary Sampling Units (PSUs). In large scale surveys the PSUs are often geographical areas.

Household level clustering

A lesser discussed aspect of clustering arise if all individuals at a sampled household are selected. Imagine we are estimating the proportion of individuals who are born outside the UK from a population of 100 people who live in 50 households. We would expect people who are born outside the UK to be more likely to live together than if they were scattered

randomly across all households. Instead we will find them 'clustered' within households, with some households being wholly overseas born, some mixed and most wholly UK born.

e.g.

```
Household 1: 1 UK born individuals
Household 2: 3 UK born
Household 3: 2 Overseas born
Household 4: 6 UK born
Household 5: 1 Overseas born, 1 UK born
Household 6: 2 UK born
Household 7: 1 UK born
Household 8: 1 UK born
Household 9: 5 Overseas born
Household 10: 3 UK born
```

And so on...

This means that if we are selecting only one in ten of the households for our sample we might expect the sample to be less accurate in predicting the proportion of our population who were born outside the UK than if we had sampled individuals at random.

More generally, using clustering comes at the cost of making the sampling coarser in the sense that we are shrinking the size of the population from which it is going to be drawn reducing its diversity - which in turn makes the estimates produced from the resulting data less precise. We will cme back to this in the next section.

1.2 Stratification

In stratified sampling, the population is divided into groups, or strata, and a sample of units is selected from each. Stratified sampling ensures the sample includes a certain proportion of units from the selected groups that may have been missed otherwise. By contrast with clustering strata are constructed so as to maximise their internal homogeneity.

Figure 2 provides a simplified example where the population is divided into four strata: North, South, East and West. Within each strata five sampling units (represented by houses) are selected.

Common stratification characteristics used in UK surveys are geographical (e.g. Government Office Regions); socio-economic (e.g. proportion of people in the area in certain occupations; car ownership) or demographic (e.g. proportion of people who are pensioners, population density). Such information is usually obtained from Census data.

It is considered that overall stratification by improving the representativeness of potentially less represented or harder to reach groups increases the precision of surveys.

##1.3 Proportional vs non proportional stratification In simple random sample each element drawn from the sampling frame have an equal selection probability, therefore the sampling

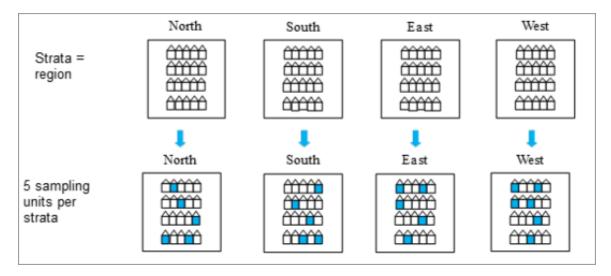


Figure 2: An example of stratified sampling

fraction is n/N with n the sample size and N the population size. This can either be achieved by directly selecting sample units at random or by choosing a random start and an interval.

In the context of stratified sampling *proportionate stratification* refers to case where the same sampling fraction is used for elements within all stratum: ie n_h/N_h . We can see this in Figure 2 as the same proportion of units is selected for all strata with a sampling fraction of 1/4.

It is sometimes necessary to use *disproportionate stratification* where the sampling fraction varies across strata. This method is used to increase the numbers of a specific group in the population and is useful when a sub-population of interest is numerically small, like less populated areas or ethnic minority groups. In such a case, $n_h/N_h>n_{h+1}/N_{h+1}$: the sampling fraction in stratum h is larger ie we are proportionally drwing more units in that stratum relative to its size, than in stratum h+1. For example the British Election Study 2010 respondents from an ethnic minority background were over-sampled as too little was known about ethnic minority voting behaviour. Disproportionate stratification will mean some groups are over-represented in the sample.

2 Design-based inference from social surveys

As we have just seen, collecting data about people at random is not necessarily straight-forward to achieve. There is no such thing as a sampling frame - a list of all UK residents to pick from - and even if there were one, some people would be less likely to take part to survey than others. As a result most UK social surveys rely on sampling techniques such as multi-stage clustering and stratification, alongside sampling proportional to size in order to strike a compromise between tackling non response, unequal probability of selection,

improving the representativeness of hard to reach groups while keeping fieldwork costs down.

Conducting inference consist in estimating parameters - quantities of interests from surveys, whether point estimates such as means or median and/or measures of their degree of precision such as confidence intervals or standard errors. Both are potentially affected by the sample design that was implemented during data collection, and need to be adapted accordingly. It is generally accepted that by increasing the sampling fraction for groups, stratification improves the precision of estimates, whereas by in effect removing part of the population from the sample, clustering will negatively impact precision. Since most survey use a combination of both, the impact of survey design will depend on the quantity and the subgroups of the population estimated, if any. Furthermore using weights to reflect non-response or unequal probability of selection also affect the precision of estimations - often negatively - and this should ideally be also taken into account when computing estimates.

Traditional textbooks or introductory courses tend to leave out this aspect, which may give a false impression of simplicity to users. There are traditionally two main ways to produce population estimates from surveys while accounting for sample design: either by directly using methods that correct estimates for the characteristics of the sample - also known a design-based estimation - or by modelling the effect of sample design - the model-based approach. Both have advantages and downsides, but for now we will only focus on the design based approach as it tends to be more straightforward to use.

2.1 Survey design variables

Weights are a special type of numeric variables included in survey datasets, whose value tends to be the inverse of the relative 'importance' of sampled observations. They are designed to prevent estimates from being biased, that is reflecting a value that is not representative of the population. They are usually made of at least two components:

- a design component that accounts for issues of unequal probability of selection of sample members resulting from survey design;
- a *non-response* component, correcting for (known) lower propensity to take part to surveys among certain categories of respondents.

Rather confusingly, these components are sometimes labelled 'weights' in their own right, even if in practice they are most of the time merged into a single variable.

Survey weights may also be rescaled in order to inflate sample counts to population totals thus becoming *grossing weights* which enable estimating populations size. In that sense the numerical values of the weights attached to observations are an indication of the number of units these observation 'represent' in the population.

Computation of weights rely on calibration algorithms that optimise the conditional distribution of the weighting variables given the sample size (for example the conditional distribution

of people by age, gender and economic status) with a view to strike a balance between minimising standard errors and maximising representativeness.

Survey design variables typically consist of identifiers for the strata and/or clusters used when the sample was drawn, especially the Primary Sampling Units (PSU) used during the sampling process. Used in conjunction with weights, they enable researchers to produce more accurate estimates.

2.2 Design factors and Design effects (DEFF)

Whereas most surveys curated by UKDS include weights, survey design variables are not always provided by data producers often due to data protection concerns. This leaves users with having to rely on alternative solutions to reduce estimation bias. Design factors (Deff) and/or Design effect (DEFTS) may provide a solution for such scenarios. Design effects/factors are two versions of similar coefficients which provide an indication of the extent to which the standard error of a given estimate departs from what it would have been under simple random sampling (Kish 1995). They can therefore be used to broadly assess how sample design affect the precision of a particular set of estimates as well as enabling users to manually correct standard errors and confidence intervals produced under the assumption of simple random sampling. Examples of Design effect for major surveys

3. The practice of inference: things to keep in mind

The variability (and therefore the degree of precision with which they can be estimated) of point estimates is contingent on survey weights and survey design. Although therefore the optimum approach to estimating population parameters from surveys relies on using both weights and survey design variables, it is not always possible to go down that path. In practice, trade-offs have to be made depending on several factors. Let us briefly consider them.

3.1 Data availability

Most UKDS datasets are available under *End User License (EUL)*. This presents the advantage of enabling large numbers of users to access data with a minimal level of formalities to go through but comes at the significant cost that survey design variables are often not included by the data producer, due to concerns about the risk of personal information disclosure. There are notable exceptions, such as for example the British Social Attitudes survey which does include survey design variables in some of its releases.

For a number of key studies such as the Labour Force Survey or the Family Resources Survey, users may apply for access to a version of the data that includes survey design information via the (virtual) SecureLab or at the UKDS Safe Room. Application for access to these facilities can be a lengthy process, and not practically feasible for all researchers,

in particular those outside academia or large organisations. More information is available on the UKDS website. There are also a large number of studies for which such controlled access is not available. The consequence is that in a significant number of cases, there will inevitably be limitations to the level of precision of the estimates most will be able to produce.

3.2 Sensitivity of the analysis

Not all analyses necessarily require the highest degree of precision. Reflecting on the stakes of their intended analysis will help users decide how important it is to strive to use the most robust estimation technique available or instead to settle for one that is 'good enough'. Typical usages of survey data could be seen as lying on a continuum ranging from 'playing with the data' to producing numbers that will be subject to public scrutiny, or that will be used in policymaking. The latter require such a degree of precision – for example when publishing official population estimates or writing a research article, other less so – for instance when exploring data or preparing examples for teaching. In the former cases, users may simply need to get a rough idea of a population estimate or the interval within which it may lie.

3.3 Complexity of the analysis

What an analysis actually entails will help determine whether accessing survey design variables is crucial or not. Estimation involving small numbers of observations will be more at risk of providing incorrect estimates if survey design variables are not taken into account. Similarly, interest for specific subgroups of the population (also known as domains) rather than the population as a whole will involve more complex estimation techniques as domain estimation needs to account for the distribution of weights in the whole population, not just for the subgroup of interest.

These analytical scenarios could be seen as lying on a continuum ranging from producing simple univariate descriptive estimates for the population as a whole to complex estimation of small groups characteristics and/or multivariate analysis. The former is conceptually and practically more straightforward than the latter. In some cases the estimates of interest may already have been published by the data producer using the adequate estimation techniques and the full information available. Data producers may also have published *design factors* ie numbers allowing to adjust the precision of estimates produced without survey design variables. Examples of such design factors for the Labour Force Survey and the Family Resources Surveys are provided below.

3.4 Software issues

Most statistical analysis software include commands specifically designed to analyse survey data: such is the case of the R *Survey* package, the SPSS *Complex Survey* add-on and Stata's *svy:* set of commands. However, because weighting can be used in other contexts

than inference from surveys, most statistical software also have options for directly weighting estimation commands "on the fly" outside of procedures accounting for survey design. This can lead some users to solely rely on weighted commands without explicitly declaring the survey design in their analysis which potentially raises issues:

- Whereas weighted commands will most of the time compute the correct point estimates, they will also silently produce biased estimates of their precision (standard errors or confidence intervals), based on the incorrect assumption that the sample was collect via simple random sampling. Depending on the survey design, this will lead to underor over- estimation of standard errors and confidence intervals, and could affect the validity of statistical tests, in particular if small groups within the population are involved.
- In addition, there are specific cases where estimation of standard errors and confidence intervals will be not just biased but wholly incorrect: the standard (ie command-based) weighting procedure of SPSS ans SAS relies on population rather than sample totals to compute them, which results in unrealistic values.
- Software such as Stata does not allow users to directly compute confidence interval
 or use sampling weights outside of survey commands. This may lead users to rely on
 'quick and dirty' tricks that will help them quickly produce weighted point estimates,
 with incorrect standard errors.

3.5 What are we in fact estimating?

Users can prioritise producing weighted point estimates over estimating their precision and the factors that influence it - chiefly survey design variables. It can be tempting indeed to consider that the goal of statistical inference mainly consists in producing 'representative' point estimates of a quantity of interest such as the 'mean weight of adult males', the 'median poverty rate', or the value of some regression coefficient in a multivariate study with estimates of their precision a secondary consideration, or a qualifier of the point estimate.

This is potentially risky. Point estimates can be at the same time representative *and* imprecise, and therefore carry little practical meaning. It could also be argued that focusing too narrowly on single value population estimates implicitly entertains the idea that such unique, 'true' value exist. As these in fact constantly vary, different surveys will return inevitably different estimates.

Instead, conceiving from the start these two aspects as a single reality – a range of plausible values we think a parameter of interest can take in the population, with a certain degree of confidence – could help alleviate such a risk and most importantly provide a more accurate reflection of the reality we seek to describe. Striving to produce confidence intervals whenever it makes sense to do so will help the notion that precision and therefore inevitably survey design are key to robust estimation.

4. Statistical inference from survey data in practice

Ultimately there should be a flowchart here or in the next section

This section provides practical recommendations for robust inference taking into account the factors highlighted in Section 3. In general, four strategies are available when conducting population inference from survey data. They are listed below by order of recommendation by the UK Data Service:

- 1. Estimation accounting for weights and survey design using survey-specific commands
- 2. Estimation accounting for weights only using survey-specific commands
- 3. Estimation using weighted standard commands
- 4. (Unweighted estimation)
- Strategy 1, using weights alongside survey design variables when conducting statistical
 inference is the statistically most robust way to compute population estimates with
 survey data and should be prioritised by users whenever possible. In real life research
 however, this option is not always available. Accessing survey design variables can
 prove challenging as they are not always provided by data producers or may require
 applying for a special version of the data, which may prove time consuming.
- In the absence of survey design information, Strategy 2 should be considered the second best option. The value of point estimates are likely to be identical to those produced under Strategy 1, but the confidence intervals/standard errors will be biased ie too narrow or wide depending on the survey design, which should be explicitly mentioned alongside the results. Information from the data documentation should provide information about how results may be affected. Using survey-specific estimation commands even in the absence of survey design variables is a recommended option over simply applying weights to standard commands, as it will avoid getting incorrect estimates (SAS and SPSS), is the only option available for computation with survey weights or obtaining confidence intervals (Stata), or coherent survey data analysis (R). In addition, it might be possible to correct 'by hand' biased standard errors or confidence interval using data producer-provided design factors.
- It can be understandable that when survey design variables are not available some users privilege *Strategy 3* which tend to focus on producing weighted estimates using standard commands and give little consideration to the methodological implication of this approach. Whereas point estimates are likely to be identical to those produced under Strategy 1 and 2, SAS and SPSS users are likely to produce incorrect confidence intervals/standard errors. R and Stata users might get standard errors and confidence intervals that are close to those produced using Strategy 2, but there is not guarantee that this will be the case. Overall UKDS only recommend following this strategy in case of low sensitivity analysis.
- As population estimates produced without weights or survey design variables will almost certainly be unreliable Strategy 4 should be discouraged except when data usage is purely descriptive. For example when teaching non-inferential (ie descriptive) statistical techniques.

4.1 Medium to high sensitivity analysis: workflow

Most of the time survey researchers or data analysts are required to produce a confidence interval or provide an indication of the degree of precision of their point estimate, usually with standard errors, whose correct estimation depends on the amount of information held about the survey design.

- 1. **If survey design variables are available** a typical workflow could involve (see examples in Section 5):
- Finding out about the survey design and identify the relevant weights and survey design variables in the data documentation;
- Declaring the survey design using software-specific commands
- Producing the estimates of interest, using survey design specific estimation commands available
- Documenting the confidence interval for the estimate of interest or alternatively the point estimates *and* its standard error.
- If required, provide a brief discussion of the possible source of bias of the results (specifically under/over estimation of the uncertainty of the estimates)
- 2. If the survey design variables are not included in the EUL version of the data but are available under controlled access: perform a cost vs benefits analysis of applying for controlled access for instance via the UKDS SecureLab, a process that can take some time. Information about how to apply for Secure Lab Access is available on the UKDS website.
- 3. If the survey design variables such as strata, cluster, or primary sampling unit are not available an alternative workflow could consist in:
 - If the user is interested in overall population characteristics, checking whether the
 estimates of interest may already have been published by the data producer, in which
 case they may be directly cited instead of computed from data.
- Finding out about the survey design in the data documentation and identify the weights variable ;
- Declaring the survey design as simple random sampling using software-specific commands
- Producing the estimates of interest, using survey design specific estimation commands available
- Checking whether the data producer has published design factors that could be used
 to remedy to biased confidence intervals/ standards errors computed without survey
 design variables (for example design factors computed for the same population at
 another point in time). A design factor is a number by which to multiply standard
 errors estimated under the assumption of simple random sampling, that will adjust it
 for survey design characteristics.

- Documenting the resulting confidence interval for the estimate of interest or alternatively the point estimates *and* its standard error.
- If no design factors are available for the estimates of interest, an explicit mention of the likely nature and cause of bias is good practice ie under estimation in case of cluster sampling, over estimation in case of stratified sample, usually available from the survey documentation. The wider the initial confidence interval (ie computed under SRS assumptions) the larger the likely bias. Or from another perspective, the smaller the (sub)sample, the larger the likely bias. In cases of conducting significance testing with small subsample or groups, it would be a good practice to only consider test outcomes significant at P<.01 or p<.001.</p>
- 4. Computing SDI estimates for subpopulations (also known as 'domains') rather than for the population as a whole requires extra precautions. This is the case for example when we are interested in the mean age by employment status, or some other categories, or alternatively, in analyses restricted to a subset of the population (for example only those in employment). The key differences is that when computing domain estimates we are in fact producing estimates about a group of the population whose size we also need to estimate. This requires ensuring that the whole distribution of weights in the sample is taken into account, not just the weights values for the groups we are interested in. Failure to do so might result in computing incorrect point estimates and standard errors/confidence intervals. SDI commands in statistical software are designed to tackle this potential issue.

4.2 Lower sensitivity analysis

The UKDS does not recommend using command-specific or casual weighting for inferential analysis, but there are circumstances where this will be the only option available to users. There are also cases when users are not interested in knowing about the uncertainty of their estimates (ie their confidence interval, standard errors of point estimates, or conduct statistical testing), for example because they are simply learning or teaching basic statistical concepts or how to use software.

In such cases, it can be acceptable to compute point estimates by applying weights to commands that accepts them, without using survey design specific functions. Most of these will provide the correct point estimate. By default however, some statistical software will also provide an estimate of standard errors or confidence intervals, which is likely to be misleading as they 'silently' assume simple random sampling, and in some cases will carry out computation with population (ie grossed) totals, resulting in the incorrect values.

5. R examples

5.1 Inference with survey design variables using R

The R *Survey* package (Lumley 2023) provides a comprehensive set of function for computing point estimates and reliability from survey data. At the same time, R Base does not provide a unified sets of commands or syntax for computing weighted estimates. Implementation of statistical theory may vary between packages, but algorithms are usually described in detail in the package documentation.

Example 1 Estimating the proportion of people interested in politics using the 2017 British Social Attitudes Survey

```
rm(list=ls())
library(dplyr) ### Data manipulation functions
library(haven) ### Importing stata/SPSS files
library(Hmisc) ### Extra statistical functions
library(survey) ### Survey design functions

bsa17<-read_spss("data/UKDA-8450-spss/spss/spss25/bsa2017_for_ukda.sav")
dim(bsa17)</pre>
[1] 3988 580
```

Once this is done we can specify the survey design: using Spoint as Primary Sampling Unit, StratID as strata, and WtFactor as weights. R does this by creating a svydesign object, ie a SDI version of the data, which will be used for subsequent estimation.

```
bsa17.s<-svydesign(ids=~Spoint, strata=~StratID, weights=~WtFactor,data=bsa17)
class(bsa17.s)

[1] "survey.design2" "survey.design"</pre>
```

Mean age and its 95% confidence interval

We can now produce a first set of estimates using this information and compare them with those we would have got without accounting for the survey design. We will compute the average (ie mean) age of respondents in the sample. We will need to use svymean()

```
svymean(~RAgeE,bsa17.s)

mean SE

RAgeE 48.313 0.4236
```

By default <code>svymean()</code> computes the standard error of the mean. We need to embed it within <code>confint()</code> in order to get a confidence interval.

```
confint(svymean(~RAgeE,bsa17.s)) ### Just the confidence interval...

2.5 % 97.5 %

RAgeE 47.48289 49.1433

round(
    c(
        svymean(~RAgeE,bsa17.s),
        confint(svymean(~RAgeE,bsa17.s))
        ),
        1) ### Estimate and CI, rounded

RAgeE
48.3 47.5 49.1
```

Computing a proportion and its 95% confidence interval

We can now similarly compute the distribution of a categorical variable in the population by estimating proportions (or percentages), for instance, the proportion of people who declare that they are interested in politics. This is the <code>Politics</code> variable in the BSA. It has five categories ranging from 1 'A great deal' to 5- 'Not at all'. We could recode 1 and 2 - <code>quite a lot</code> into 'Significantly', but since we are only interested in estimating the confidence intervals, we will select the relevant values 'on the go'.

```
attr(bsa17$Politics,"label")
                          ### Phrasing of the question
[1] "How much interest do you have in politics?"
 attr(bsa17$Politics,"labels")
                           ### Value labels
... a great deal,
               -2
                                 -1
                                some,
                                          not very much,
        quite a lot,
     or, none at all?
                           Don`t know
                                                Refusal
                                  8
```

```
table(as factor(bsa17$Politics)) ### Sample distribution
```

Note: Changes in a data frame are not automatically transferred into svydesign objects used for inferences. We therefore need to recreate it each time we create or recode a variable.

```
round(100*prop.table(svytable(~(Politics==1 | Politics==2),bsa17.s)),1)

Politics == 1 | Politics == 2

FALSE TRUE
57 43
```

Let us now compute the confidence intervals for these proportions. Traditional statistical software compute these without giving us an idea of the underlying computations going on. Doing this in R requires more coding, but also a better understanding of what is actually estimated.

Confidence intervals for proportions of categorical variables are usually computed as a sequence of binomial/dichotomic estimations – ie one for each category. In R this needs to be specified explicitly via the $\mathtt{svyciprop}()$ and $\mathtt{I}()$ functions. The former actually computes the proportion and its confidence interval (by default 95%), whereas the latter allows us to define the category we are focusing on.

Computing domain estimates

Computing domain estimates, that is estimates for subgroups adds a layer of complexity to the above example. They key point is that as weights were designed using the whole of the sample, computing estimates, in particular confidence intervals or standard errors for part of the sample, therefore using a fraction of these weights may affect the estimates. Instad it is recommended to use commands that take into account the entire distribution of the weights.

In R, the command that does this is svyby()

For instance, if we would like to compute the mean age of BSA respondents by Government Office Regions, we need to specify:

- The outcome variable whose estimate we want to compute: ie RAgeE
- The grouping variable(s) GOR ID
- The estimate function we are going to use here: svymean, the same as we used before
- And the type of type of variance estimation we would like to see displayed ie standard errors or confidence interval

```
round(
    svyby(~RAgeE,by=~as_factor(GOR_ID),svymean,design=bsa17.s,vartype = "ci")[-1]
,1)
```

```
RAgeE ci l ci u
                      46.1 43.6 48.6
A North East
B North West
                       49.6 47.3 52.0
D Yorkshire and The Humber 48.0 45.2 50.8
E East Midlands
                      48.6 45.9 51.3
F West Midlands
                       48.1 45.0 51.2
G East of England
                      49.0 46.0 52.0
H London
                       45.0 43.0 46.9
J South East
                       48.0 45.1 50.8
K South West
                      53.4 51.5 55.2
L Wales
                       49.1 45.1 53.1
                       47.3 44.7 50.0
M Scotland
```

Note: we used [-1] from the object created by svyby() in order to remove a column with alphanumeric values (the region names), so that we could round the results without getting an error.

Our inference seem to suggest that the population in London is among the youngest in the country, and that those in the South West are among the oldest – their respective 95% confidence intervals do not overlap. We should not feel so confident about differences between London and the South East for example, as the CIs partially overlap.

We can follow a similar approach with proportions: we just need to specify the category of the variable we are interested in as an outcome, for instance respondents who are significantly interested in politics, and replace symmetry by syyciprop.

```
round(
        100*
         svyby(~I(Politics==1 | Politics==2),
              by=~as_factor(GOR_ID),
              svyciprop,
              design=bsa17.s,
              vartype = "ci")[-1],
              1)
                           I(Politics == 1 | Politics == 2) ci l ci u
A North East
                                                        33.4 26.6 40.9
                                                        41.9 36.1 48.0
B North West
D Yorkshire and The Humber
                                                        35.6 29.1 42.6
E East Midlands
                                                        36.9 32.9 41.1
F West Midlands
                                                        36.3 31.5 41.5
G East of England
                                                        47.2 41.4 53.1
                                                        54.2 47.2 61.1
H London
                                                        44.6 38.7 50.8
J South East
K South West
                                                        46.5 39.4 53.8
L Wales
                                                        38.6 27.7 50.7
```

5.2 Inference without survey design variables using R

Example: count and proportion of the regional population of the UK using the LFS with End User License (EUL)

42.7 36.0 49.8

The EUL version of the LFS does not include sample design variables, just two weight variables:

pwt22 for estimation with the whole sample

M Scotland

 piwt22 for estimation using respondents currently in employment (typically used for earnings estimation)

```
lfs<-droplevels(read_dta("/home/piet/Dropbox/work/UKDS/DSP/DSP-core-inference/data/UKDA-
8999-stata/lfsp_aj22_eul_pwt22.dta")%>%select(PWT22,PIWT22,URESMC))
names(lfs)<-tolower(names(lfs))
lfs$uresmc.f<-droplevels(as_factor(lfs$uresmc))
lfs.s<-svydesign(ids=~1,weights=~pwt22,data=lfs)
knitr::kable(confint(svytotal(~uresmc.f,lfs.s)))</pre>
```

See here for the Labour for Survey and for the family resource survey - For the FRS: https://assets.publishing.service.gov.uk/government/uploads/system/uploads/attachment_data/file/972808/Ch1_Methodology_and_Standard_Errors.xlsx - For the LFS: https://www.ons.gov.uk/methodology/methodologicalpublications/generalmethodology/onsworkingpaperseries/onsmethodologyworkingpaperseriesno9guidetocalculatingstandarderrorsforonssocialsurveys#annex-a-labour-force-survey-standard-errors-january-tomarch-2015-united-kingdom

6. SPSS Examples

At the time of writing this document (September 2023) Standard editions of SPSS did not include support for estimation with survey design variables, and only limited use of sampling weights. When using grossing weights – ie weight that have been designed to enable computing population totals from sample data – as is the case for instance with the Labour Force and Family Resources surveys, measures of dispersion and standard errors will not be adequately computed. It is therefore not recommended to attempt using the base version of SPSS with survey data beyond estimating point estimates. Significance testing, and standard errors will not reflect the correct values. Users willing to use SPSS with survey data will need to acquire the Premium Edition or the Complex Samples add-on of the software.

7 Stata examples

Stata provides comprehensive support for computing estimates from survey data. Users may either opt to add sampling weights to the standard estimation commands, or use survey-specific commands. The latter is recommended when knowledge of estimate precision is required. Stata provides a conceptual distinction between four types of weights:

- frequency weights (fweight),
- analytical weights (aweight),
- importance weights (iweight) and
- probability weights (pweight).

These differences impact on the way standard errors are computed during estimation. In most cases, social survey weights from UKDS datasets should be treated as probability weights. A number of of basic estimation commands, such as *summarise* do not allow using probability weights. This is an explicit features of Stata, meant to nudge users of survey data to prioritise the survey commands rather than 'casual' weighting.

Using standalone weight specification (ie not using survey design functions). In Stata it consists in the weighting variable being specified between square brackets. Stata defines four kind of weights:

Only probability weights (abbreviated as p_W in most Stata commands) should be used with survey data. However, Stata does not allow using them with its main commands, for the

reason highlighted above ie in order for users not overlook survey design issues in their data. Therefore, one has to specify instead the wrong frequency weights (fw) if one does not wish to use the survey design functions.

(TBC)

8. Appendix: Study-specific weighting and sample design information

8.1 British Social Attitudes Survey

The BSA is a three stage stratified random survey, with postcode sectors, addresses and individuals as the units selected at each stage. Primary sampling units were furthermore stratified according to geographies (sub regions), population density, and proportion of owner-occupiers. Sampling rate was proportional to the size of postcode sectors (ie number of addresses). Some issues of the BSA such as the 2017 include survey design information. The 2017 issue included information about Primary Smapling Units (Spoint), strata (StratID). Weights are called WtFactor.

8.2 Labour Force Survey

The LFS is a geographically stratified random survey. For the main part Primary sampling units are addresses within postcode sectors, drawn from the Small Users Postcode Address File (PAF). The small users PAF is limited to addresses which receive, fewer than 50 items of post per day. In a small number of cases a second stage sampling occurs where several households exist at a given address. A clustering effect is also present to the extent that units of observations are individuals withing households, and that some groups are clustered within these, typically ethnicity. LFS weights: - PWTxx - person level sampling weight; enables inferring population counts - IWTxx - Person-level sampling weight for income analysis (ie subsample of people in paid work) - PHHWTxx - Household-level sampling weight (for household-level analysis)

8.3 Family Resources Survey

The FRS is a stratified clustered random survey, with survey design differing slightly between countries of the UK. In great Britain, Primary sampling units are postcode sectors, drawn from the Small Users Postcode Address File (PAF). The small users PAF is limited to addresses which receive, fewer than 50 items of post per day. Before being selected, PSUs are stratified according to geography, proportion of household reference persons from higher social classes in the area, proportion of economically active respondents in the area, and proportion of economically active men who ware unemployed. In Northern Ireland, the sample is a systematic random sample of addresses.

9. References

- Blair, Johnny. 2014. *Designing Surveys : A Guide to Decisions and Procedures.* 3rd edition / Johnny Blair, Ronald F. Czaja, Edward A. Blair. Los Angeles: SAGE.
- DWP. 2014. "Uncertainty in Family Resources Survey-Based Analysis. Guidance on Estimating Uncertainty in Family Resources Survey-Based Analysis." Edited by Department for Work and Pensions. 2014. https://www.gov.uk/government/publications/uncertainty-in-family-resources-survey-based-analysis.
- IBM Support. 2020. "Inconsistency in the Output When Using Weighting Procedure. IBM Support Document Number 419449." 2020. https://www.ibm.com/support/pages/inconsistency-output-when-using-weighting-procedure.
- Kish, Leslie. 1995. Survey Sampling. Wiley Classics Library. New York: Wiley.
- Lohr, Sharon L. 2019 2010. *Sampling: Design and Analysis*. Second edition. Texts in Statistical Science. Boca Raton, FL: CRC Press.
- Lumley, Thomas. 2023. "Survey: Analysis of Complex Survey Samples."
- ONS. 2022. "Family Resources Survey, 2020/21 Methodology and Standard Error Tables." Edited by Office for National Statistics. 2022. https://assets.publishing.service.gov.uk/government/uploads/system/uploads/attachment_data/file/1065513/Ch1_Methodology_and Standard Errors.ods.
- P, Curran. 2016. "Complex Survey Designs and Weighting Using Stata: Part 1-3." 2016. https://www.youtube.com/watch?v=oOpJdC_oeKY.
- UKDS. 2018. "Data Skills Modules: Applying Weights to Survey Data." Edited by UK Data Service. 2018. https://www.youtube.com/watch?v=Tlad5 WP8g.
- ——. 2019. "Weights in Social Surveys: An Introduction:" Edited by UK Data Service. 2019. https://www.youtube.com/watch?v=Vllr4olp3N4&t=39s.
- Wallrich, Lukas. 2019. "Week 7 Using Survey Weights in r." Edited by Goldsmiths Core Quantitative Methods Series. 2019. https://www.youtube.com/watch?v=brxx81U6N1o.