$$\int \cot^5 x \ dx = -\frac{1}{4}\csc^4 x + \csc^2 x + \ln|\sin x| + C$$