Maths of the Day

$$\int_0^{\frac{\pi}{4}} \int_0^{\frac{\pi}{4}} \arctan(\cos(x)\cot(y))\sec^3(x)\tan^2(y)\sec^2(y)\,dxdy = \frac{1}{3}$$