

A Generalization

The numerators form a
sequence A330905

$$\frac{1}{\pi^{4k+3}} \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^{4k+3} \sinh(n\pi)}$$