


Matrix Multiplication

Matrix Multiplication

$$\begin{bmatrix} a_{00} & a_{01} \\ a_{10} & a_{11} \end{bmatrix} * \begin{bmatrix} b_{00} & b_{01} \\ b_{10} & b_{11} \end{bmatrix}$$

$$c_{00} = a_{00} * b_{00} + a_{10} * b_{01}$$

$$c_{10} = a_{10} * b_{00} + a_{11} * b_{10}$$

For matrix size L :

c_{mn}

$$= a_{m0} * b_{0n} + a_{m1} * b_{1n} + \dots + a_{mL-1} * b_{L-1n}$$

$$\begin{bmatrix} a_{00} & a_{01} \\ a_{10} & a_{11} \end{bmatrix} * \begin{bmatrix} b_{00} & b_{01} \\ b_{10} & b_{11} \end{bmatrix}$$

Matrix Multiplication

- For $L \times L$ matrix to multiply using naïve multiplication it would require:
 - L^3 multiplications and $L^2 \cdot (L-1)$ Additions
 - *Many algorithms are used to minimize and reduce the computation needed for matrices.*

Assignment

- Write UC/Arduino Code that implements Matrix Multiplication
- Tracking your instructions and UC datasheet try to predict how many cycles will the program take
- Make the code modular to allow the ability of increasing matrix size later on
- Optimize your code for least time to compute as possible.
- The winner of best implementation will have a CCs gift card ;)

Strassen Algorithm (One way to accelerate Matrix Multiplication)

$$M1 = (A00 + A11)(B00 + B11)$$

$$M2 = (A10 + A11) * B00$$

$$M3 = A00 * (B01 - B11)$$

$$M4 = A11 * (B10 + B00)$$

$$M5 = (A00 + A01) * B11$$

$$M6 = (A10 - A00)(B00 + B01)$$

$$M7 = (A01 - A11)(B10 + B11)$$

$$C00 = M1 + M4 - M5 + M7$$

$$C01 = M3 + M5$$

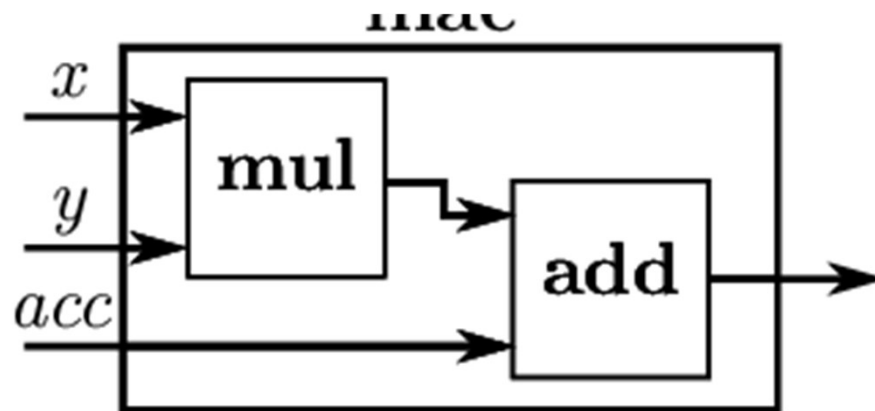
$$C10 = M2 + M4$$

$$C11 = M1 - M2 + M3 + M6$$



Speed $\propto O(L^{2.8})$

Verilog Assignment



- Design Multiply Accumulate block whose block diagram looks like the following.
- Each parameter is an 8-bit Block

Verilog Assignment

- Test pattern
 - A = 1; B = 10
 - A = 1; B = 100
 - A = 1; B = 255
 - A = 5; B = 10
 - A = 5; B = 100
 - A = 5; B = 255
 - A = 100; B = 100
 - A = 100; B = 255
 - A = 255; B = 255