Типовой расчет

Функции f(x) задана в виде таблицы - известны значения $f(x_j)$ в 26 равноотстоящих точках x_j (узлах сетки с постоянным шагом h) на отрезке [a,b]: $a=x_0 < x_1 < x_2 < ... < x_{25} = b$.

Требуется аппроксимировать функцию на заданном отрезке средствами пакета Mathematica:

- выбрать и применить соответствующую встроенную функцию пакета;
- записать уравнение полученной аппроксимирующей функции;
- вывести график аппроксимирующей функции на отрезке [a-h,b+h] и значения исходной функции в узлах.

Задание 1. Постройте интерполяционный многочлен степени n=25 для функции f(x), выведите его график и оцените его поведение на отрезке.

Постройте многочлены меньшей степени на отрезке, используя не все узлы сетки:

- используете значения функции в нечетных узлах (n=12);
- используете значения функции в каждом 3- узле (n=8);
- используете значения функции в каждом 5- узле (n=5).

Сравните результаты и сделайте выводы о зависимость погрешности интерполирования от числа узлов.

Задание 2. Постройте сплайн, аппроксимирующий функцию f(x) по значениям в узлах, выведите его график и сравните его с графиком интерполяционного многочлена степени, построенного по тем же узлам.

Задание 3. Постройте для функции f(x) многочлены наилучшего среднеквадратичного приближения $P_n^*(x)$ степени n=1,2. Вычислите для каждого многочлена сумму квадратов отклонения в узлах, сравните их значения и сделайте выводы. Выведите графики узлов и многочленов $P_n^*(x)$, аппроксимирующих функцию.

Задание 4. Вычислите для таблично заданной функции определенный интеграл $\int_{a}^{b} f(x) dx$ следующими методами:

- методами левых, правых и средних прямоугольников;
- методом трапеций;

Примените для вычисления интеграла функцию Integrate[.....] пакета Mathematica, воспользовавшись одной из аппроксимирующих функций.

Сравните полученные приближенные значения интеграла и сделайте выводы о точности результата.

Варианты заданий

1	2	3
(0.3 -1.10525)	/ -1.3 4.82322 \	(-0.5 0.535916)
0.348 -1.07996	-1.228 3.33765	-0.42 0.485126
0.396 -1.1225	-1.156 2.70397	-0.34 0.437118
0.444 -1.05986	-1.084 1.98662	-0.26 0.371678
0.492 -1.06783	-1.012 1.66705	-0.18 0.301733
0.54 -0.978257	-0.94 1.24847	-0.1 0.207338
0.588 -0.955469	-0.868 1.05544	-0.02 0.073557
0.636 -0.846209	-0.796 0.788668	0.06 0.155576
0.684 -0.794931	-0.724 0.659343	0.14 0.283913
0.732 -0.671395	-0.652 0.482783	0.22 0.390199
0.78 -0.593028	-0.58 0.391398	0.3 0.497748
0.828 -0.459459	-0.508 0.274337	0.38 0.592501
0.876 -0.354877		0.46 0.69812
0.924 -0.214726	-0.436 0.209228	0.54 0.789936
0.972 - 0.0844691	-0.364 0.134515	
1.02 0.0593841	-0.292 0.0904061	0.62 0.898493
1.02 0.0393841	-0.22 0.0477204	0.7 0.990582
1.116 0.360097	-0.148 0.0227273	0.78 1.10445
1.164 0.540909	-0.076 0.00561353	0.86 1.19854
	-0.004 0.0000164801	0.94 1.31926
1.212 0.685119 1.26 0.891074	0.068 0.00449221	1.02 1.4165
	0.14 0.0203209	1.1 1.54526
1.308 1.03252	0.212 0.0442608	1.18 1.64652
1.356 1.26364	0.284 0.0853837	1.26 1.78436
1.404 1.40065	0.356 0.128405	1.34 1.89036
1.452 1.65703	0.428 0.201112	1.42 2.03825
1.5 1.7881	0.5 0.264957	1.5 2.14963
4	5	6
(-0.5 0.419945)	(-1.2 0.397688)	(-0.5 1.6313)
-0.5 0.419945 -0.412 0.395988	-1.2 0.397688 -1.112 0.40388	-0.5 1.6313 -0.412 1.47756
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402	(-1.2 0.397688)	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691 1.084 0.417327
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871 0.996 0.574811	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531 0.384 1.469	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871 0.996 0.574811 1.084 0.632645	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531 0.384 1.469 0.472 1.55989	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691 1.084 0.417327
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871 0.996 0.574811 1.084 0.632645 1.172 0.67142	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531 0.384 1.469 0.472 1.55989 0.56 1.71796	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691 1.084 0.417327 1.172 0.393931
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871 0.996 0.574811 1.084 0.632645 1.172 0.67142 1.26 0.743887	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531 0.384 1.469 0.472 1.55989 0.56 1.71796 0.648 1.81039	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691 1.084 0.417327 1.172 0.393931 1.26 0.389793
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871 0.996 0.574811 1.084 0.632645 1.172 0.67142 1.26 0.743887 1.348 0.793733	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531 0.384 1.469 0.472 1.55989 0.56 1.71796 0.648 1.81039 0.736 1.9764	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691 1.084 0.417327 1.172 0.393931 1.26 0.389793 1.348 0.373315
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871 0.996 0.574811 1.084 0.632645 1.172 0.67142 1.26 0.743887 1.348 0.793733 1.436 0.882993	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531 0.384 1.469 0.472 1.55989 0.56 1.71796 0.648 1.81039 0.736 1.9764 0.824 2.06229	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691 1.084 0.417327 1.172 0.393931 1.26 0.389793 1.348 0.373315 1.436 0.374944
-0.5 0.419945 -0.412 0.395988 -0.324 0.391402 -0.236 0.374437 -0.148 0.375642 -0.06 0.364857 0.028 0.371704 0.116 0.366656 0.204 0.379343 0.292 0.379948 0.38 0.399032 0.468 0.405545 0.556 0.43196 0.644 0.444969 0.732 0.480039 0.82 0.500438 0.908 0.545871 0.996 0.574811 1.084 0.632645 1.172 0.67142 1.26 0.743887 1.348 0.793733 1.436 0.882993 1.524 0.944755	-1.2 0.397688 -1.112 0.40388 -1.024 0.429882 -0.936 0.442532 -0.848 0.47711 -0.76 0.497096 -0.672 0.541939 -0.584 0.570401 -0.496 0.627532 -0.408 0.665761 -0.32 0.737406 -0.232 0.786648 -0.144 0.874982 -0.056 0.936111 0.032 1.04284 0.12 1.1159 0.208 1.24167 0.296 1.32531 0.384 1.469 0.472 1.55989 0.56 1.71796 0.648 1.81039 0.736 1.9764	-0.5 1.6313 -0.412 1.47756 -0.324 1.38862 -0.236 1.25078 -0.148 1.17048 -0.06 1.05118 0.028 0.982116 0.116 0.8818 0.204 0.824781 0.292 0.742362 0.38 0.697 0.468 0.630556 0.556 0.595805 0.644 0.543107 0.732 0.517675 0.82 0.476544 0.908 0.459175 0.996 0.427691 1.084 0.417327 1.172 0.393931 1.26 0.389793 1.348 0.373315 1.436 0.374944 1.524 0.3646

7	8	9
(0.5 1.25066)	(0.5 0.443179)	(0.5 2.02)
0.552 1.29388	0.56 0.469718	0.56 1.76786
0.604 1.38282	0.62 0.509651	0.62 1.62903
0.656 1.41156	0.68 0.523462	0.68 1.45588
0.708 1.49275	0.74 0.551931	0.74 1.36486
0.76 1.51117	0.8 0.551792	0.8 1.2375
0.812 1.58776	0.86 0.566707	0.86 1.17442
0.864 1.59938	0.92 0.551781	0.92 1.07609
0.916 1.6742	0.98 0.551341	0.98 1.03061
0.968 1.68197	1.04 0.521204	1.04 0.951923
1.02 1.75758	1.1 0.503945 1.16 0.458602	1.1 0.918182
1.072 1.76405 1.124 1.84283	1.22 0.42344	1.16 0.853448
1.176 1.85019	1.28 0.363326	1.22 0.827869
1.228 1.93443	1.34 0.309594	1.28 0.773438 1.34 0.753731
1.28 1.94466	1.4 0.235574	1.4 0.707143
1.332 2.03664	1.46 0.163046	1.46 0.691781
1.384 2.0516	1.52 0.0764054	1.52 0.651316
1.436 2.15368	1.58 -0.014687	1.58 0.639241
1.488 2.17516	1.64 -0.112269	1.64 0.603659
1.54 2.28988	1.7 -0.221226	1.7 0.594118
1.592 2.31975	1.76 -0.327705	1.76 0.5625
1.644 2.44992	1.82 -0.45336	1.82 0.554945
1.696 2.49015	1.88 -0.566363	1.88 0.526596
1.748 2.63894	1.94 -0.707094	1.94 0.520619
1.8 2.69173	\ 20.823971)	2. 0.495
10	11	12
(1. 1.01)	(0.5 8.19358)	0.1 0.46648
1.04 0.915311	0.54 7.07926	0.156 0.53563
1.08 0.865912	0.58 6.43005	0.212 0.599255
1.12 0.789222	0.62 5.65999	0.268 0.641507
1.16 0.750595	0.66 5.22464	0.324 0.690263
1.2 0.6875	0.7 4.6644	0.38 0.720694
1.24 0.656868	0.74 4.35966	0.436 0.76207
1.28 0.604248	0.78 3.93554	0.492 0.785497
1.32 0.57966	0.82 3.71504	0.548 0.822419
1.36 0.535251	0.86 3.38366	0.604 0.841076
1.4 0.515306	0.9 3.21991	0.66 0.875012
1.44 0.477431	0.94 2.95423	0.716 0.890145
1.48 0.461103	0.98 2.83008	0.772 0.921945
1.52 0.428497	1.02 2.61247	0.828 0.934329
1.56 0.415023	1.06 2.51677	0.884 0.964532
1.6 0.386719	1.1 2.33529	0.94 0.974688
1.64 0.375521	1.14 2.26054	0.996 1.00366
1.68 0.350765	1.18 2.10686	1.052 1.01196
	1.22 2.04784	1.108 1.03995
1.72 0.341401	1.26 1.91597	1.164 1.04666
1.76 0.319602	1.3 1.86899	
1.8 0.311728	1.34 1.75452	1.22 1.07387
1.84 0.292415	1.38 1.71689	1.276 1.07921
1.88 0.285763	1.42 1.61652	1.332 1.10578
1.92 0.268555	1.46 1.58626	1.388 1.10991
1.96 0.262911	1.5 1.49745	1.444 1.13594
(2. 0.2475)		1.5 1.13899

13	14	15
(-0.5 -0.696613)	(-0.2 0.343705)	(-0.2 0.0398739)
-0.42 -0.542004	-0.124 0.247422	-0.124 0.0151449
-0.34 -0.417593	-0.048 0.132737	-0.048 0.00232526
-0.26 -0.2996	0.028 0.0917477	0.028 0.000775957
-0.18 -0.199443	0.104 0.222257	0.104 0.010885
-0.1 -0.104834	0.18 0.317204	0.18 0.0317362
-0.02 -0.0203037	0.256 0.405191	0.256 0.0647997
0.06 0.0579776	0.332 0.47707	0.332 0.105358
0.14 0.131683	0.408 0.552849	0.408 0.159633
0.22 0.197857	0.484 0.613366	0.484 0.215989
0.3 0.263676	0.56 0.682797	0.56 0.288732
0.38 0.320473	0.636 0.735859	0.636 0.356672
0.46 0.380329	0.712 0.801345	0.712 0.444944
0.54 0.429624	0.788 0.848869	0.788 0.520637
0.62 0.484838	0.864 0.911679	0.864 0.621813
0.7 0.527975	0.94 0.954791	0.94 0.702119
0.78 0.579496	1.016 1.01569	1.016 0.814088
0.86 0.617474	1.092 1.05513	1.092 0.89659
0.94 0.666001	1.168 1.11462	1.168 1.01775
1.02 0.699582	1.244 1.1509	1.244 1.10065
1.1 0.745647	1.32 1.20934	1.32 1.22983
1.18 0.775428	1.396 1.24283	1.396 1.31182
1.26 0.819442	1.472 1.30048	1.472 1.44816
1.34 0.8459	1.548 1.33149	1.548 1.52829
1.42 0.888186	1.624 1.38853	1.624 1.67119
1.5 0.911709	1.7 1.41728	1.7 1.74876