

CHAPTER 1

Physical Entities (Base quantities)	Fundamental Units SI unit-name (symbol)
length	meter (m)
mass	kilogram (Kg)
time	second (s)
electric current	ampere (A)
temperature	Kelvin (K)
Amount of substance	Mole (mol)
luminous intensity	Candela (cd)

Factor	Prefix ^a	Symbol
10^{24}	yotta-	Y
10^{21}	zetta-	Z
10^{18}	exa-	E
10^{15}	peta-	P
10^{12}	tera-	T
10^9	giga-	G
10^6	mega-	M
10^3	kilo-	k
10^2	hecto-	h
10^1	deka-	da
10^{-1}	deci-	d
10^{-2}	centi-	c
10^{-3}	milli-	m
10^{-6}	micro-	μ
10^{-9}	nano-	n
10^{-12}	pico-	p
10^{-15}	femto-	f
10^{-18}	atto-	a
10^{-21}	zepto-	z
10^{-24}	yocto-	y

Significant Figures (有效數字)

- Meaningful digits

Decimal Place (小數數位)

- The position of a digit to the right of the decimal point in a decimal number

Density (密度)

- $\rho = \frac{m}{v}$

Errors Calculations

- *Absolute Error* = *Measure Error* – *True Value*
- *Relative Error* = $\frac{\text{Absolute Error}}{\text{True Value}}$
- *Percentage Error* = *Relative error* × 100%

Types of Error

1. Human Error
2. Random Error
3. Systematic Error

Precision (精準度)

- Specifies the **repeatability** or **consistency** of successive measurements

Accuracy (準確度)

- Specifies the **deviation** between the **measured and true value**

CHAPTER 2

Distance (距離)

- Total length of path

Displacement (位移)

- Change in position
- $\Delta x = x_2 - x_1$

Average Speed (平均速度)

- $s_{avg} = \frac{\text{Total Distance}}{\Delta t}$

Average Velocity (平均速率)

- $v_{avg} = \frac{\Delta x}{\Delta t}$

Instantaneous Speed (暫態速度)

- Magnitude of instantaneous velocity

Instantaneous Velocity (暫態速率)

- $v = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{dx}{dt}$

Acceleration (加速度)

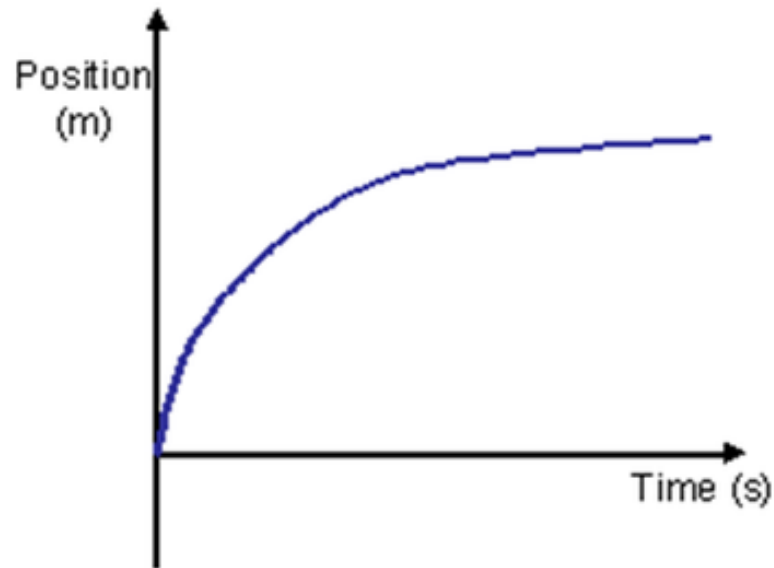
- $a_{avg} = \frac{v_2 - v_1}{t_2 - t_1} = \frac{\Delta v}{\Delta t}$

Instantaneous Acceleration (暫態加速度)

- $a = \frac{dv}{dt}$

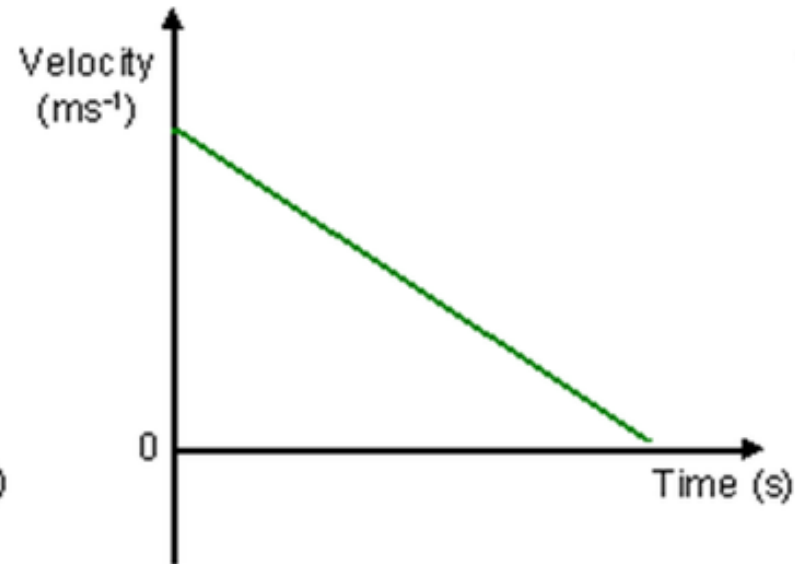
Graphs for a body with positive velocity and negative acceleration

Position -Time Graph



$$\bullet s = \int v dt$$

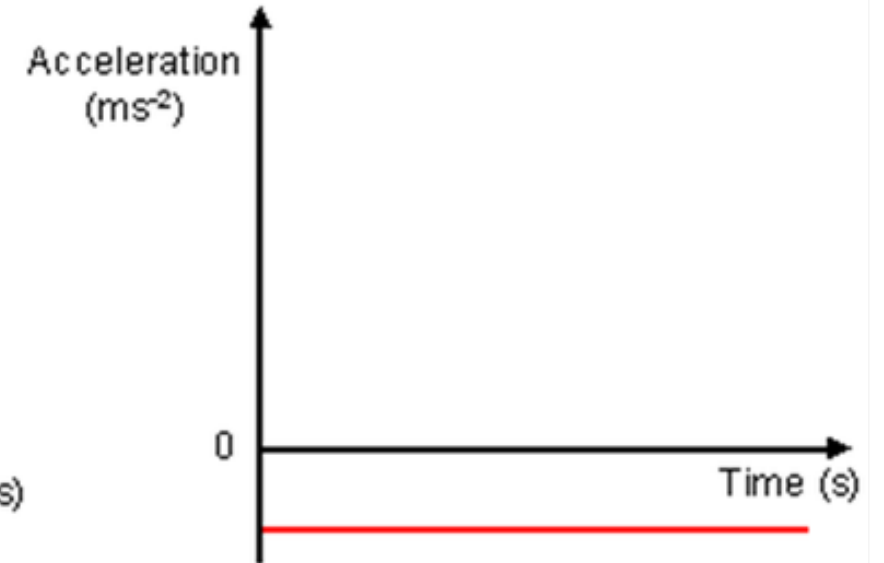
Velocity -Time Graph



$$\bullet v = \int a dt$$

$$\bullet v = \frac{ds}{dt}$$

Acceleration -Time Graph



$$\bullet a = \frac{dv}{dt}$$

Equation Number	Equation	Missing Quantity
→ 2-11	$v = v_0 + at$	$x - x_0$
→ 2-15	$x - x_0 = v_0 \underline{t} + \frac{1}{2} \underline{a} t^2$	v
2-16	$v^2 = v_0^2 + 2a(x - x_0)$	t
2-17	$x - x_0 = \frac{1}{2}(v_0 + v)t$	a
2-18	$x - x_0 = vt - \frac{1}{2}at^2$	v_0

CHAPTER 3

Scalar (標量)

- Have magnitude only

Vector (向量)

- Have both magnitude and direction

Properties of Vector

- $\vec{a} + \vec{b} = \vec{b} + \vec{a}$
- $(\vec{a} + \vec{b}) + \vec{c} = \vec{a} + (\vec{b} + \vec{c})$
- $\vec{a} - \vec{b} = \vec{a} + (-\vec{b})$

Unit-Vector Notations

- $a = a_x \vec{i} + a_y \vec{j}$

Magnitude-Angle Notations

- $a_x = a \cos \theta$

- $a_y = a \sin \theta$

- $a = \sqrt{a_x^2 + a_y^2}$

- $\tan \theta = \frac{a_y}{a_x}$

Unit Vector (單位向量)

- $\hat{A} = \frac{\vec{A}}{|\vec{A}|}$

Scalar Product (標量積)/ Dot Product (點積)

- $\vec{a} \cdot \vec{b} = ab \cos \theta$
- $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z$

Vector Product(向量積)/ Cross Product (叉積)

- $\vec{a} \times \vec{b} = \vec{c}$
- $c = ab \sin \theta$
- $\vec{a} \times \vec{b} = (a_y b_z - b_y a_z) \hat{i} + (a_z b_x - b_z a_x) \hat{j} + (a_x b_y - b_x a_y) \hat{k}$

•**31** **SSM** Suppose a rocket ship in deep space moves with constant acceleration equal to 9.8 m/s^2 , which gives the illusion of normal gravity during the flight. (a) If it starts from rest, how long will it take to acquire a speed one-tenth that of light, which travels at $3.0 \times 10^8 \text{ m/s}$? (b) How far will it travel in so doing?

ANALYZE (a) Given that $a = 9.8 \text{ m/s}^2$, $v_0 = 0$ and $v = 0.1c = 3.0 \times 10^7 \text{ m/s}$, we can solve $v = v_0 + at$ for the time:

$$t = \frac{v - v_0}{a} = \frac{3.0 \times 10^7 \text{ m/s} - 0}{9.8 \text{ m/s}^2} = 3.1 \times 10^6 \text{ s}$$

which is about 1.2 months. So it takes 1.2 months for the rocket to reach a speed of $0.1c$ starting from rest with a constant acceleration of 9.8 m/s^2 .

(b) To calculate the distance traveled during this time interval, we evaluate $x = x_0 + v_0 t + \frac{1}{2} at^2$, with $x_0 = 0$ and $v_0 = 0$. The result is

$$x = \frac{1}{2} (9.8 \text{ m/s}^2) (3.1 \times 10^6 \text{ s})^2 = 4.6 \times 10^{13} \text{ m}.$$

•**33** **SSM** **ILW** A car traveling 56.0 km/h is 24.0 m from a barrier when the driver slams on the brakes. The car hits the barrier 2.00 s later. (a) What is the magnitude of the car's constant acceleration before impact? (b) How fast is the car traveling at impact?

ANALYZE (a) Using Eq. 2-15, we find the acceleration to be

$$a = \frac{2(x - v_0 t)}{t^2} = \frac{2[(24.0 \text{ m}) - (15.55 \text{ m/s})(2.00 \text{ s})]}{(2.00 \text{ s})^2} = -3.56 \text{ m/s}^2,$$

or $|a| = 3.56 \text{ m/s}^2$. The negative sign indicates that the acceleration is opposite to the direction of motion of the car; the car is slowing down.

(b) The speed of the car at the instant of impact is

$$v = v_0 + at = 15.55 \text{ m/s} + (-3.56 \text{ m/s}^2)(2.00 \text{ s}) = 8.43 \text{ m/s}$$

which can also be converted to 30.3 km/h.

••41 **SSM** **ILW** **WWW** Use the definition of scalar product, $\vec{a} \cdot \vec{b} = ab \cos \theta$, and the fact that $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z$ to calculate the angle between the two vectors given by $\vec{a} = 3.0\hat{i} + 3.0\hat{j} + 3.0\hat{k}$ and $\vec{b} = 2.0\hat{i} + 1.0\hat{j} + 3.0\hat{k}$.

ANALYZE Given that $\vec{a} = (3.0)\hat{i} + (3.0)\hat{j} + (3.0)\hat{k}$ and $\vec{b} = (2.0)\hat{i} + (1.0)\hat{j} + (3.0)\hat{k}$, the magnitudes of the vectors are

$$a = |\vec{a}| = \sqrt{a_x^2 + a_y^2 + a_z^2} = \sqrt{(3.0)^2 + (3.0)^2 + (3.0)^2} = 5.20$$

$$b = |\vec{b}| = \sqrt{b_x^2 + b_y^2 + b_z^2} = \sqrt{(2.0)^2 + (1.0)^2 + (3.0)^2} = 3.74.$$

The angle between them is found to be

$$\cos \phi = \frac{(3.0)(2.0) + (3.0)(1.0) + (3.0)(3.0)}{(5.20)(3.74)} = 0.926,$$

or $\phi = 22^\circ$.

53 **SSM** A vector \vec{a} of magnitude 10 units and another vector \vec{b} of magnitude 6.0 units differ in directions by 60° . Find (a) the scalar product of the two vectors and (b) the magnitude of the vector product $\vec{a} \times \vec{b}$.

ANALYZE (a) Given that $a = |\vec{a}| = 10$, $b = |\vec{b}| = 6.0$ and $\phi = 60^\circ$, the scalar (dot) product of \vec{a} and \vec{b} is

$$\vec{a} \cdot \vec{b} = ab \cos \phi = (10)(6.0) \cos 60^\circ = 30.$$

(b) Similarly, the magnitude of the vector (cross) product of the two vectors is

$$|\vec{a} \times \vec{b}| = ab \sin \phi = (10)(6.0) \sin 60^\circ = 52.$$