Description Logics

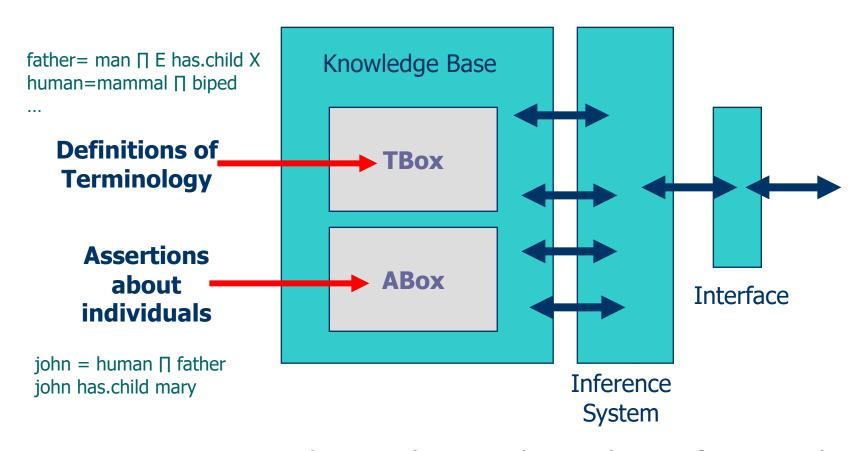
What Are Description Logics?

- A family of logic based KR formalisms
 - Descendants of semantic networks and KL-ONE
 - Describe domain in terms of concepts (classes), roles (relationships) and individuals
- Distinguished by:
 - Formal semantics (typically <u>model theoretic</u>) based on a <u>decidable</u> fragments of FOL
 - Provision of inference services
 - Sound and complete decision procedures for key problems
 - Implemented systems (highly optimized)
- Formal basis for OWL (DL profile)

DL Paradigm

- <u>Description Logic</u> characterized by a set of constructors that allow one to build complex descriptions or terms out of concepts and roles from atomic ones
 - Concepts: classes interpreted as sets of objects,
 - Roles: relations interpreted as binary relations on objects
- Set of axioms for asserting facts about concepts, roles and individuals

Typical Architecture



Division into TBox and ABox has no logical significance, but is made for conceptual and implementation convenience

DL defines a family of languages

- The expressiveness of a description logic is determined by the operators that it uses
 - Adding or removing operators (e.g., \neg , \cup) increases or decreases the kinds of statements expressible
 - Higher expressiveness usually means higher reasoning complexity
- AL or Attributive Language is the base and includes just a few operators
- Other DLs are described by the additional operators they include

AL: Attributive Language

Constructor	Syntax	Example
atomic concept	С	Human
atomic negation	~ C	~ Human
atomic role	R	hasChild
conjunction	$C \wedge D$	Human ∧ Male
value restriction	R.C	Human ∃ hasChild.Blond
existential rest. (lim)	∃ R	Human ∃ hasChild
Top (univ. conc.)	T	T
bottom (null conc)	上	上

for concepts C and D and role R

ALC

ALC is the smallest DL that is propositionally closed (i.e., includes full negation and disjunction) and include booleans (and, or, not) and restrictions on role values

constructor	Syntax	Example
atomic concept	C	Human
negation	~ C	~ (Human V Ape)
atomic role	R	hasChild
conjunction	C ^ D	Human ^ Male
disjunction	CVD	Nice V Rich
value restrict.	∃ R.C	Human ∃ hasChild.Blond
existential restrict.	∃ R.C	Human ∃ hasChild.Male
Top (univ. conc.)	T	Т
bottom (null conc)	\perp	\perp

Examples of ALC concepts

- Person ∧ ∀hasChild.Male (everybody whose children are all male)
- Person ∧ ∀hasChild.Male ∧∃hasChild.T (everybody who has a child and whose children are all male)
- Living_being ∧ ¬Human_being (all living beings that are not human beings)
- Student ∧ ¬∃interestedIn.Mathematics (all students not interested in mathematics)
- Student ∧ ∀drinks.tea (all students who only drink tea)
- ∃hasChild.Male V ∀hasChild.⊥ (everybody who has a son or no child)

Other Constructors

The general DL model has additional constructors...

Constructor	Syntax	Example
Number restriction	>= n R	>= 7 hasChild
	<= n R	<= 1 hasmother
Inverse role	R-	haschild-
Transitive role	R*	hasChild*
Role composition	$R \circ R$	hasParent o hasBrother
Qualified # restric.	>= n R.C	>= 2 hasChild.Female
Singleton concepts	{ <name>}</name>	{Italy}

Special names and combinations

See http://en.wikipedia.org/wiki/Description_logic

- S = ALC + transitive properties
- H = role hierarchy, e.g., rdfs:subPropertyOf
- O = nominals, e.g., values constrained by enumerated classes, as in owl:oneOf and owl:hasValue
- I = inverse properties
- N = cardinality restrictions (owl:cardinality, maxCardonality)
- (D) = use of datatypes properties
- R = complex role axioms (e.g. (ir)reflexivity, disjointedness)
- Q = Qualified cardinality (e.g., at least two female children)
- → OWL-DL is SHOIN(D)
- → OWL 2 is SROIQ^(D)

Note: R->H and Q->N



Concept constructors:

Notes:

Complexity of reasoning in Description Logics

Note: the information here is (always) incomplete and <u>updated</u> often

Base description logic: Attributive Language with $\mathcal C$ omplements



Role constructors:



trans reg

𝔻 - functionality ² : (≤1 R) 𝔻 - (unqualified) number restrictions: (≥n R), (≤n R) ā		.C), (≤n R.C) -of")	☐ I - role inverse: R^- ☐ Ω - role intersection $\frac{3}{2}$: $R \cap S$ ☐ U - role union: $R \cup S$ ☐ U - role complement: U - U - role complement: U - U - role composition): U - U - role chain (composition): U - U - reflexive-transitive closure U - U - role concept identity: U - U		
TBox (concept axioms): • empty TBox • acyclic TBox (A ≡ C, A is a concept name; no cycles) • general TBox (C ⊆ D, for arbitrary concepts C and D)			RBox (role axioms): $S - \text{role transitivity: } Tr(R)$ $H - \text{role hierarchy: } R \subseteq S$ $R - \text{complex role inclusions: } R \circ S \subseteq R, R \circ S \subseteq S$ $S - \text{some additional features (check it to see)}$		
You have selected a Description Logic: ALC					
		Complexity of re	asoning problems ^Z		
Reasoning problem	Complexity ⁸	Comments and references			
Concept satisfiability	PSpace-complete	Hardness for ALC: see [80]. Upper bound for ALCQ: see [12, Theorem 4.6].			
ABox consistency	PSpace-complete	Hardness follows from that for concept satisfiability. Upper bound for ALCQO: see [17, Appendix A].			
	Important properties of the description logic				
	2	Important properties	or the description regic		
Finite model property	Yes		ne multi-modal logic \mathbf{K}_m (cf. [77]), for which the finite model property can be		
	Yes Yes	ALC is a notational variant of the found in [4, Sect. 2.3].			

1. The letters Q, I, and Q are customary written in various orders, e.g., ALCOJO, but SHOJO, Here we do not reflect this tradition, but rather use a uniform naming scheme.

OWL as a DL

- OWL-DL is SHOIN^(D)
- We can think of OWL as having three kinds of statements
- Ways to specify classes
 - the intersection of humans and males
- Ways to state axioms about those classes
 - Humans are a subclass of apes
- Ways to talk about individuals
 - John is a human, a male, and has a child Mary

Subsumption: $D \subseteq C$?

- Concept C subsumes D iff on every <u>interpretation</u> I
 I(D) ⊆ I(C)
- This means the same as $\forall (x)(D(x) \rightarrow C(x))$ for complex statements D & C
- Determining whether one concept logically contains another is called the subsumption problem.
- Subsumption is undecidable for reasonably expressive languages
 - e.g.; for FOL: does one FOL sentence imply another
- and non-polynomial for fairly restricted ones

Other reasoning problems

These problems can be reduced to subsumption (for languages with negation) and to the satisfiability problem

- Concept satisfiability is C (necessarily) empty?
- Instance Checking Father(john)?
- **Equivalence** CreatureWithHeart ≡ CreatureWithKidney
- Disjointness
 C □ D
- **Retrieval** Father(X)? X = {john, robert}
- **Realization** X(john)? X = {Father}

Definitions

- A definition is a description of a concept or a relationship
- It is used to assign a meaning to a term
- In description logics, definitions use a specialized logical language
- Description logics are able to do limited reasoning about concepts defined in their logic
- One important inference is classification (computation of subsumption)

Necessary vs. Sufficient

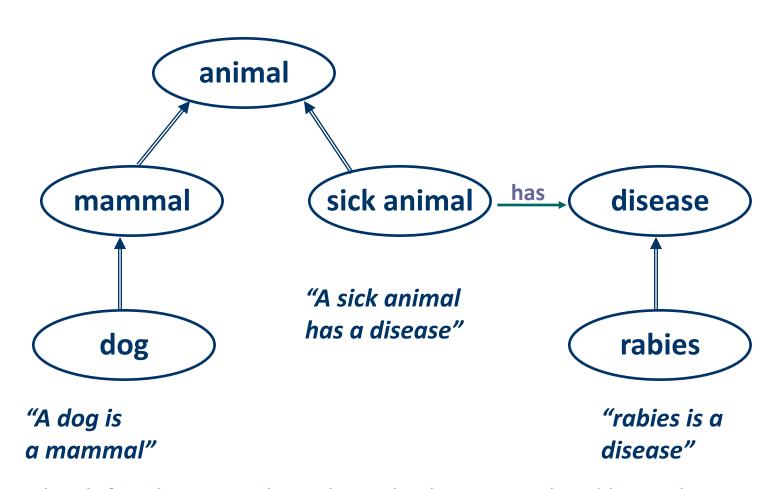
- Necessary properties of an object are common to all objects of that type
 - Being a man is a necessary condition for being a father
- Sufficient properties allow one to identify an object as belonging to a type and need not be common to all members of the type
 - Speeding is a sufficient reason for being stopped by the police
- Definitions typically specify both necessary and sufficient properties

Subsumption

- Meaning of Subsumption
 - A more general concept or description **subsumes** a more specific one. Members of a subsumed concept are necessarily members of a subsuming concept
- Example: Animal subsumes Person; (aka IS-A, rdfs:subClassOf)
- Two ways to formalize meaning of subsumption
 - Using logic: satisfying a subsumed concept implies that the subsuming concept is satisfied also
 - E.g., if john is a person, he is also an animal
 - Using set theory: instances of subsumed concept are necessarily a subset of subsuming concept's instances

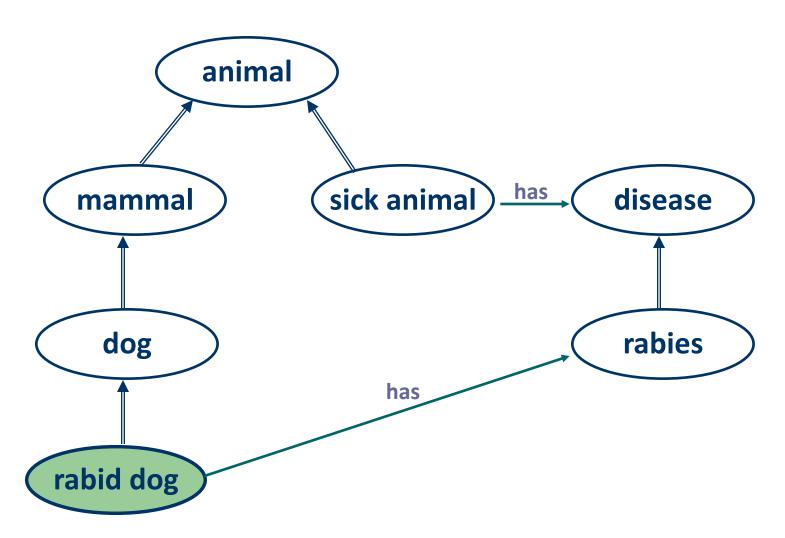
E.g., the set of all persons is a subset of all animals

How Does Classification Work?



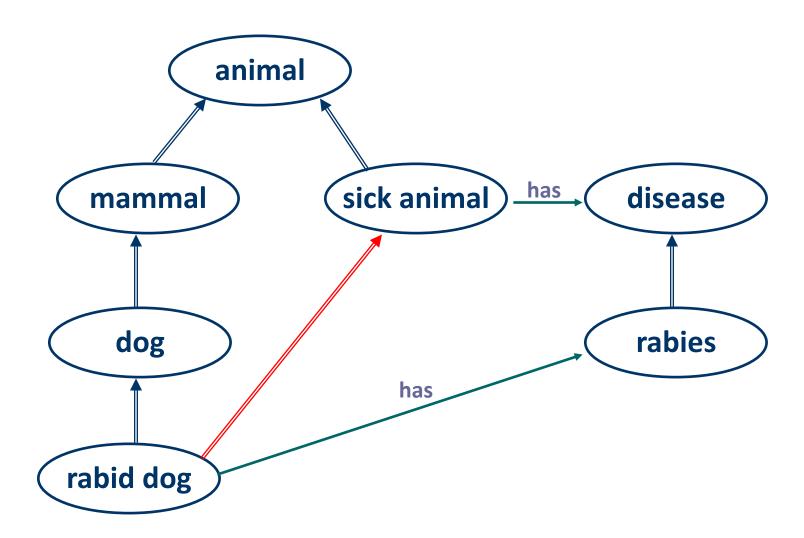
A sick animal is **defined** as something that is both an animal and has at least one thing that is a kind of a disease

Defining a "rabid dog"



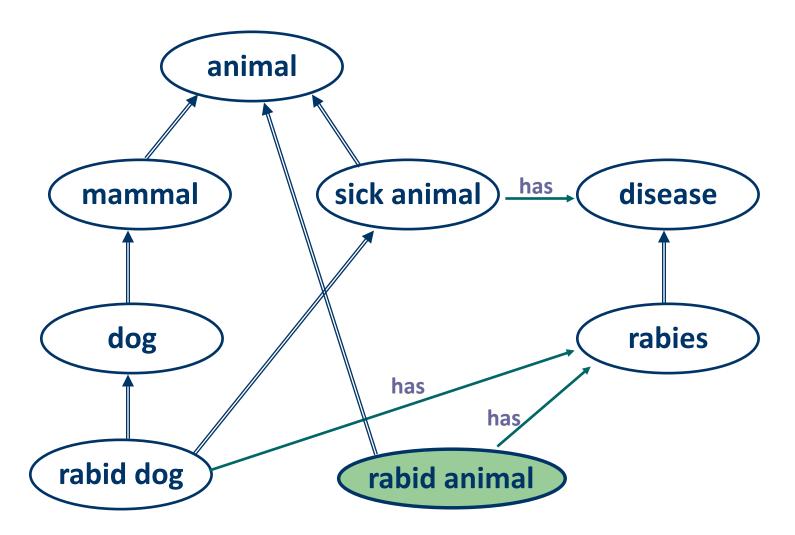
A rabid dog is **defined** as something that is both a dog and has at least one thing that is a kind of a rabies

Classification as a "sick animal"



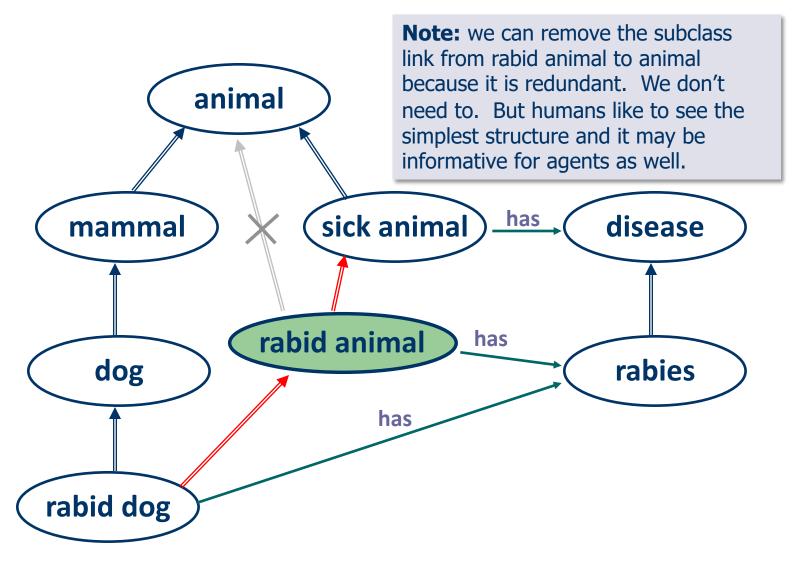
We can easily prove that s rabid dog is a kind of sick animal

Defining "rabid animal"



A rabid animal is **defined** as something that is both an animal and has at least one thing that is a kind of a rabies

DL reasoners places concepts in hierarchy



We can easily prove that s rabid dog is a kind of rabid animal

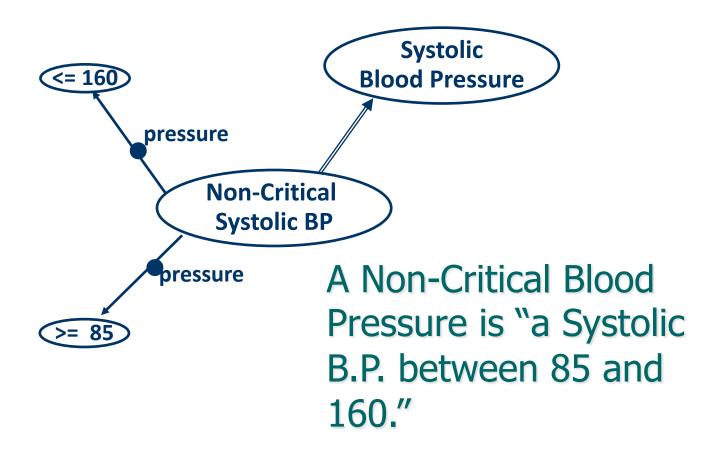
Primitive versus Structured (Defined)

- Description logics reason with definitions
 - They prefer to have complete descriptions
 - A complete definition includes both necessary conditions and sufficient conditions
- Often impractical or impossible, especially with natural kinds
- A "primitive" definition is an incomplete one
 - Limits amount of classification that can be done automatically
- Example:
 - Primitive: a Person
 - Defined: Parent = Person with at least one child

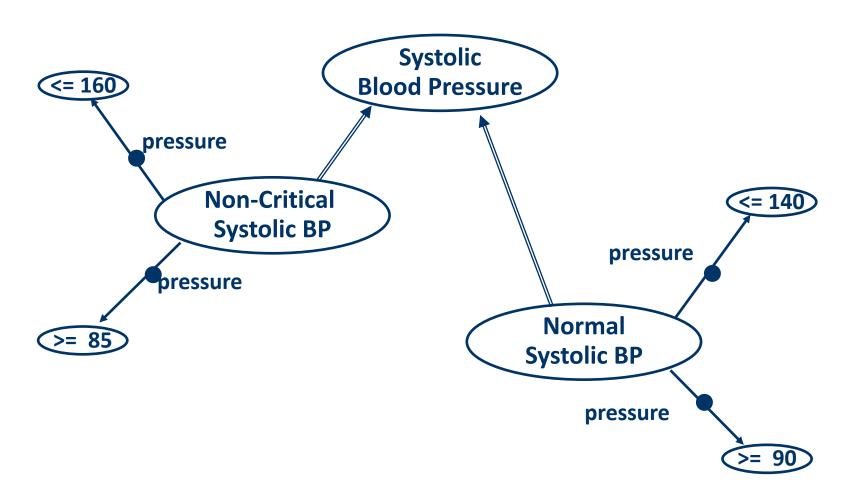
Classification is very useful

- Classification is a powerful kind of reasoning that is very useful
- Many expert systems can be usefully thought of as doing "heuristic classification"
- Logical classification over structured descriptions and individuals is also quite useful
- But... can classification ever deduce something about an individual other than what classes it belongs to?
- And what does *that* tell us?

Example: Blood Pressure

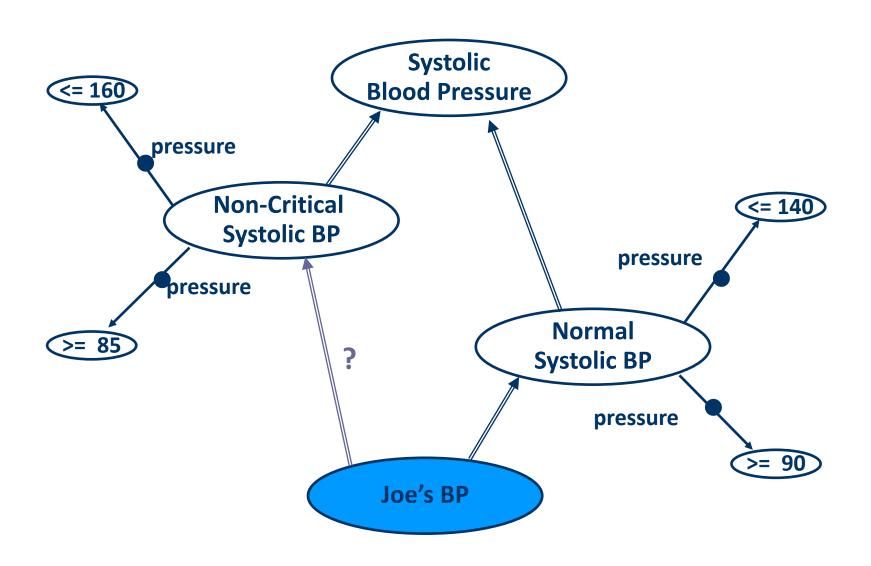


Example: Blood Pressure

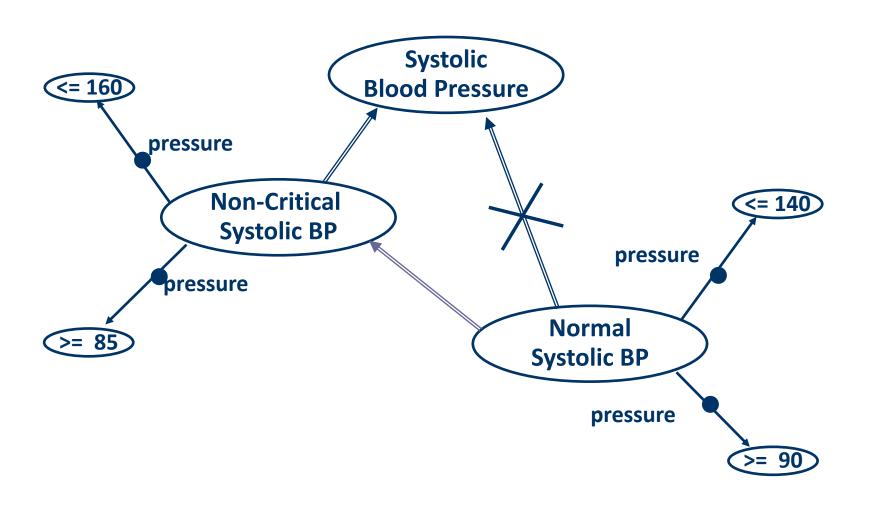


Normal Systolic B.P. is "a Systolic B.P. between 90 and 140.

If Joe's BP is Normal is it also Non-Critical?



Concept Classification Infers Normal BP is Subsumed by Non-Critical BP



With Classified Concepts the Answer is Easy to Compute

