

Fall 2022

INTRODUCTION TO COMPUTER VISION

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<https://vita-group.github.io/>

Many slides here were adapted from CMU 16-385 Computer Vision

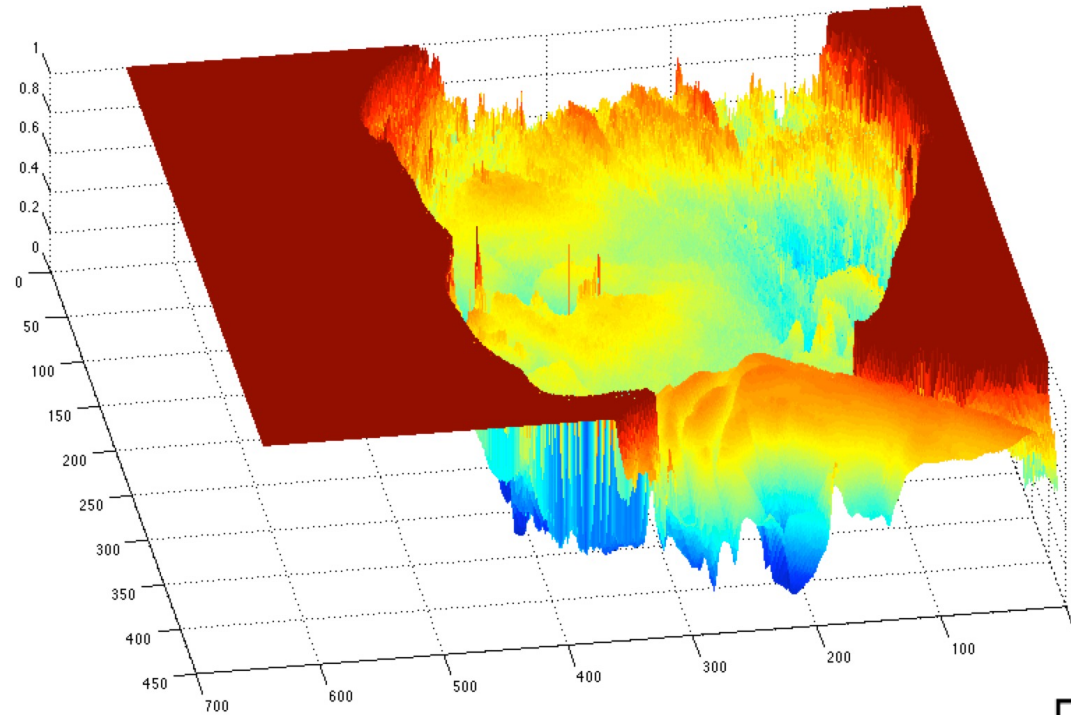
What is an image?

$$f(\mathbf{x})$$



grayscale image

What is the range of the image function f ?



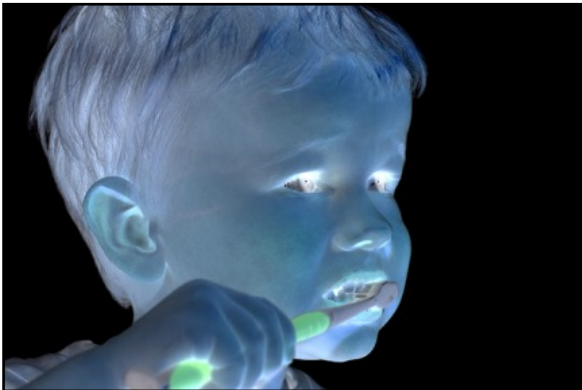
domain $\mathbf{x} = \begin{bmatrix} x \\ y \end{bmatrix}$

A (grayscale) image is a 2D function.

What types of image transformations can we do?



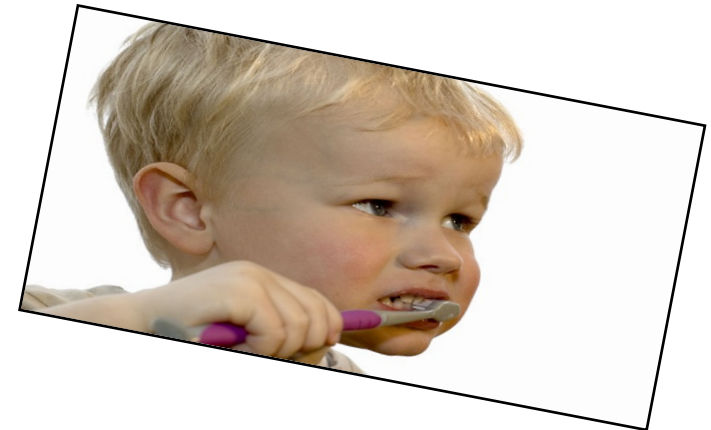
Filtering



changes pixel *values*



Warping



changes pixel *locations*

What types of image transformations can we do?

F

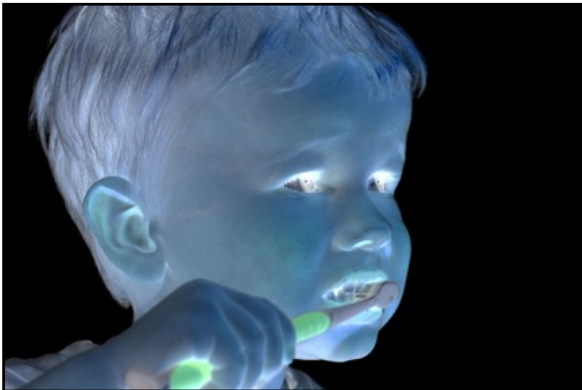


Filtering



$$G(\mathbf{x}) = h\{F(\mathbf{x})\}$$

G



changes *range* of image function

F

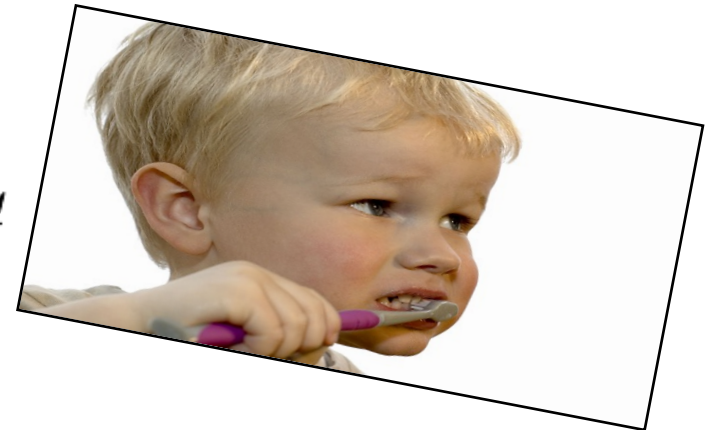


Warping



$$G(\mathbf{x}) = F(h\{\mathbf{x}\})$$

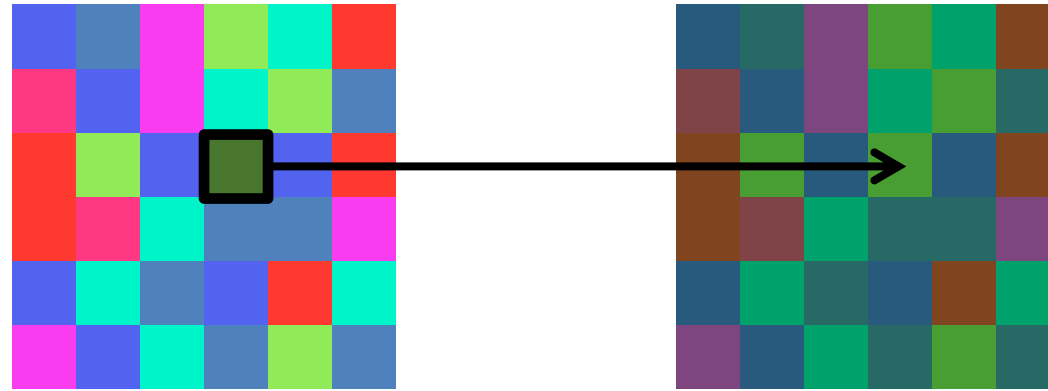
G



changes *domain* of image function

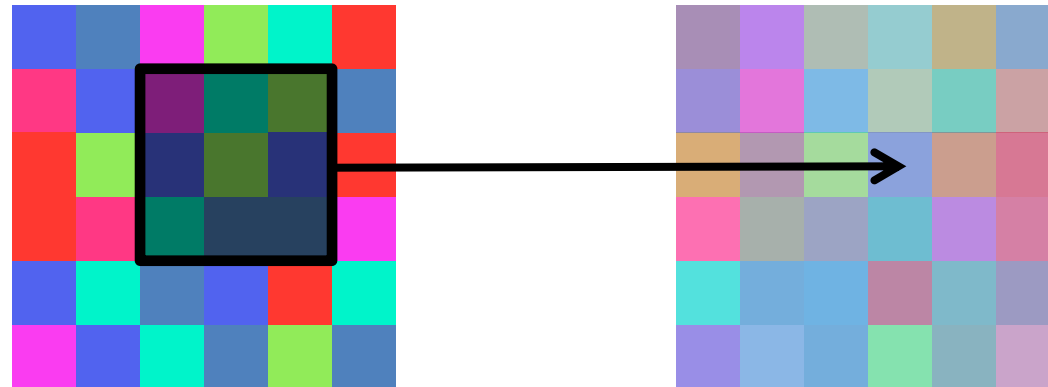
What types of image filtering can we do?

Point Operation



point processing

Neighborhood Operation



“filtering”

Examples of point processing

original



darken



lower contrast



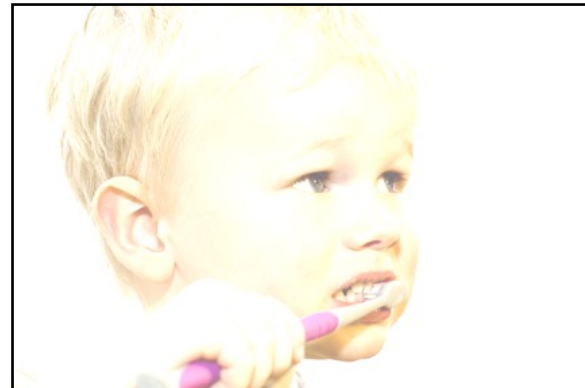
non-linear raise contrast



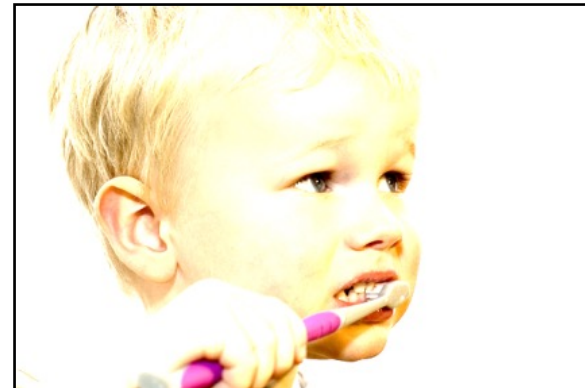
invert



lighten



raise contrast



non-linear lower contrast



How would you
implement these?

Examples of point processing

original



darken



lower contrast

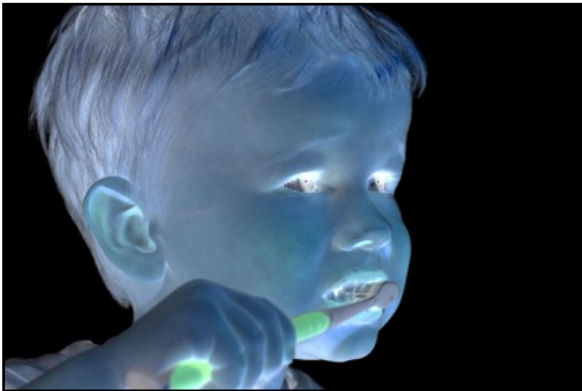


non-linear raise contrast

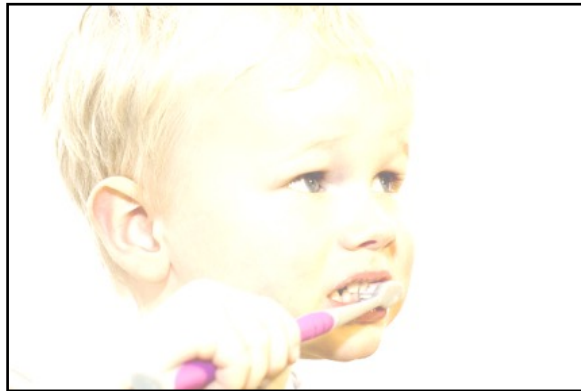


x

invert



lighten



raise contrast



non-linear lower contrast



How would you
implement these?

Examples of point processing

original



$$x$$

darken



$$x - 128$$

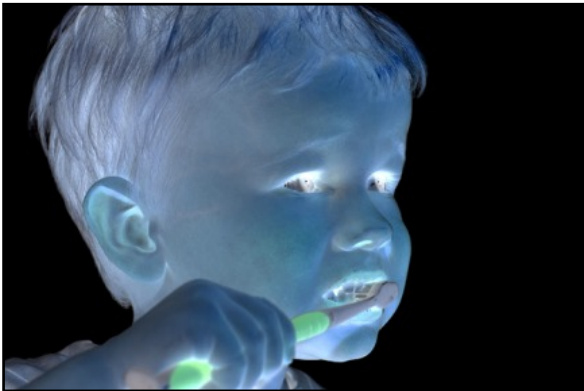
lower contrast



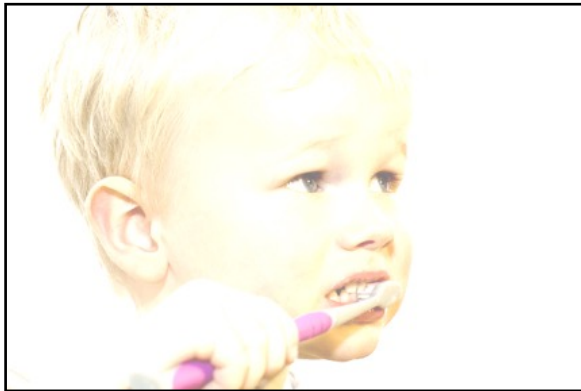
non-linear raise contrast



invert



lighten



raise contrast



non-linear lower contrast



How would you
implement these?

Examples of point processing

original



$$x$$

darken



$$x - 128$$

lower contrast

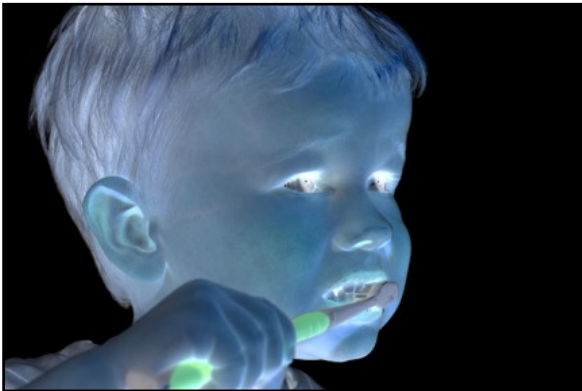


$$\frac{x}{2}$$

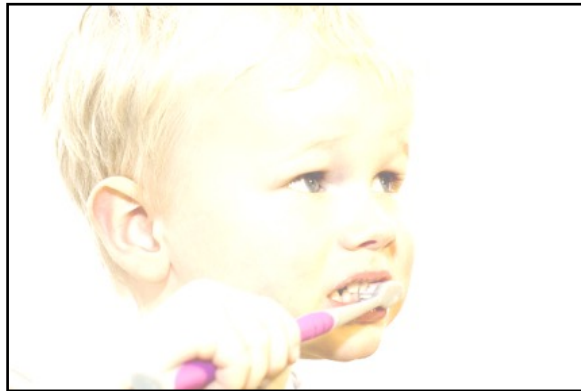
non-linear raise contrast



invert



lighten



raise contrast



non-linear lower contrast



How would you
implement these?

Examples of point processing

original



$$x$$

darken



$$x - 128$$

lower contrast



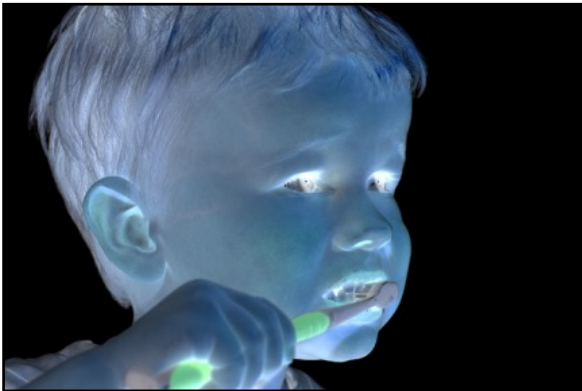
$$\frac{x}{2}$$

non-linear raise contrast



$$\left(\frac{x}{255} \right)^{1/3} \times 255$$

invert



lighten



raise contrast



non-linear lower contrast



How would you
implement these?

Examples of point processing

original



$$x$$

darken



$$x - 128$$

lower contrast



$$\frac{x}{2}$$

non-linear raise contrast



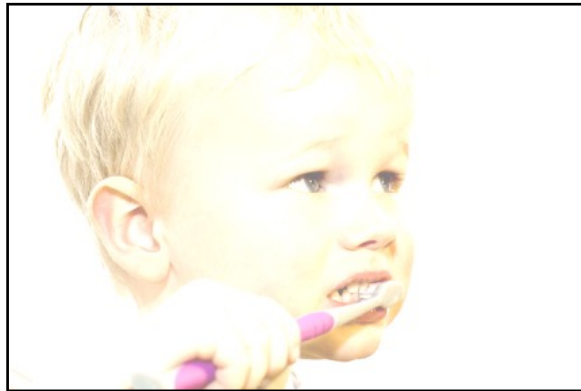
$$\left(\frac{x}{255}\right)^{1/3} \times 255$$

invert



$$255 - x$$

lighten



raise contrast



non-linear lower contrast



How would you
implement these?

Examples of point processing

original



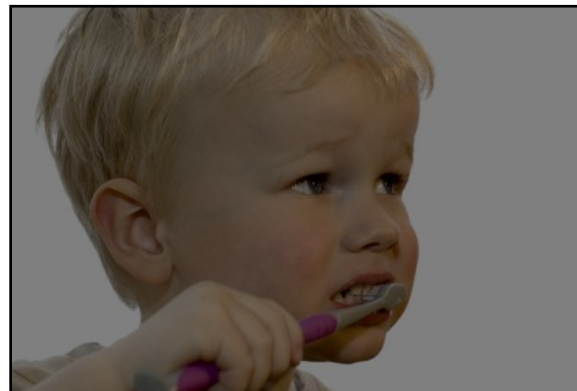
$$x$$

darken



$$x - 128$$

lower contrast



$$\frac{x}{2}$$

non-linear raise contrast



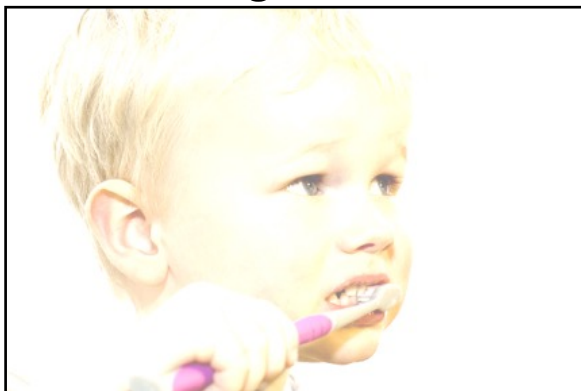
$$\left(\frac{x}{255}\right)^{1/3} \times 255$$

invert



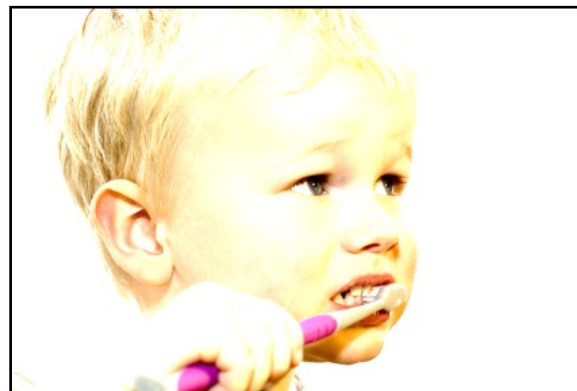
$$255 - x$$

lighten



$$x + 128$$

raise contrast



non-linear lower contrast



How would you
implement these?

Examples of point processing

original



$$x$$

darken



$$x - 128$$

lower contrast



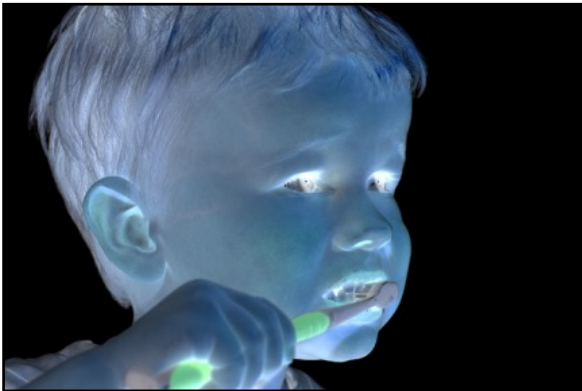
$$\frac{x}{2}$$

non-linear raise contrast



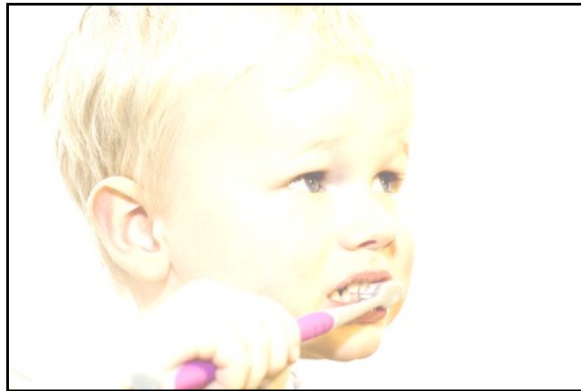
$$\left(\frac{x}{255}\right)^{1/3} \times 255$$

invert



$$255 - x$$

lighten



$$x + 128$$

raise contrast



$$x \times 2$$

non-linear lower contrast



How would you
implement these?

Examples of point processing

original



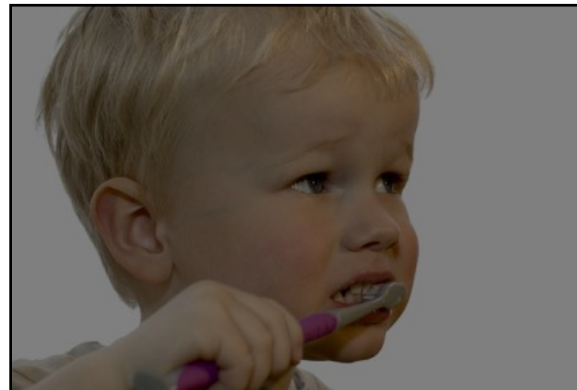
$$x$$

darken



$$x - 128$$

lower contrast



$$\frac{x}{2}$$

non-linear raise contrast



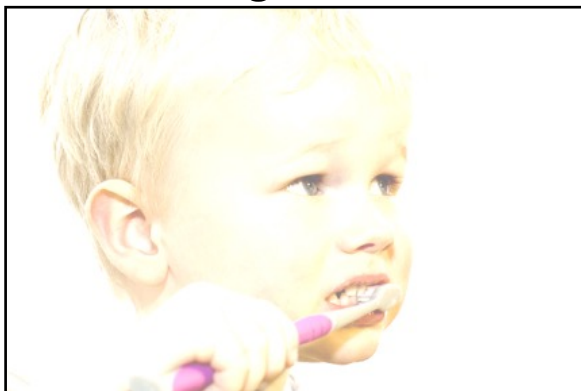
$$\left(\frac{x}{255}\right)^{1/3} \times 255$$

invert



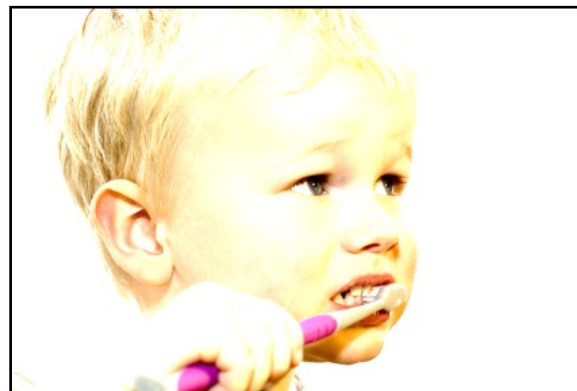
$$255 - x$$

lighten



$$x + 128$$

raise contrast



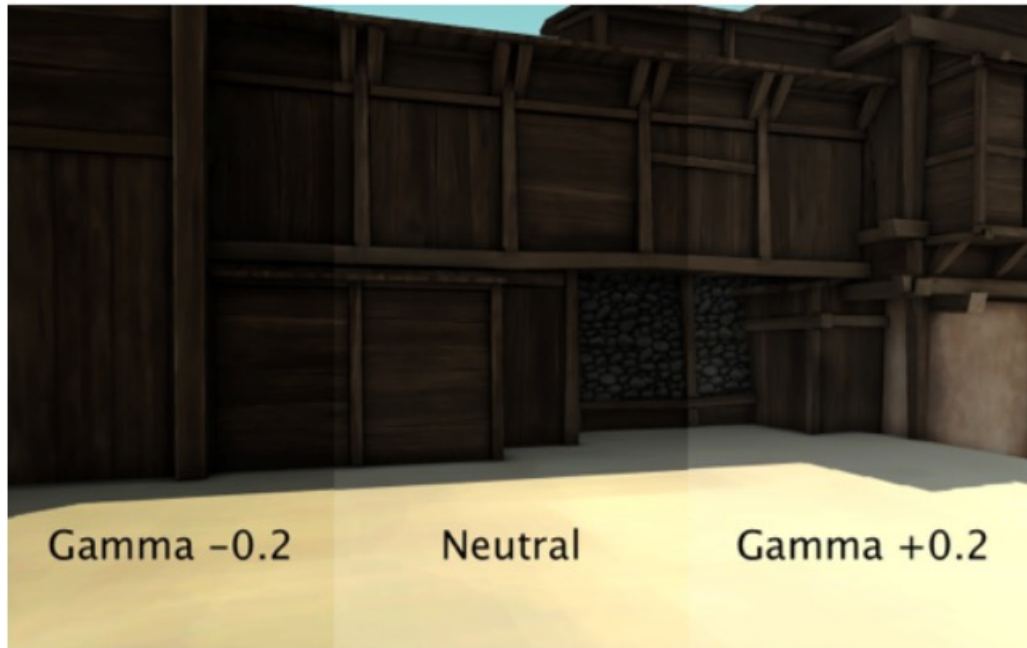
$$x \times 2$$

non-linear lower contrast



$$\left(\frac{x}{255}\right)^2 \times 255$$

Many other types of point processing



Linear shift-invariant image filtering

- Replace each pixel by a *linear* combination of its neighbors (and possibly itself).
- The combination is determined by the filter's *kernel*.
- The same kernel is *shifted* to all pixel locations so that all pixels use the same linear combination of their neighbors.
- **Modern name?** [Convolution](#) (yes, the same guy in convolutional neural network)

Convolution for 1D continuous signals

Definition of filtering as convolution:

$$(f * g)(x) = \int_{-\infty}^{\infty} f(y)g(x - y)dy$$

Diagram illustrating the convolution operation:

- filtered signal**: Points to the result $(f * g)(x)$.
- filter**: Points to $f(y)$.
- input signal**: Points to $g(x - y)$.
- notice the flip**: Points to the minus sign in $x - y$, indicating time reversal.

Convolution for 1D continuous signals

Definition of filtering as convolution:

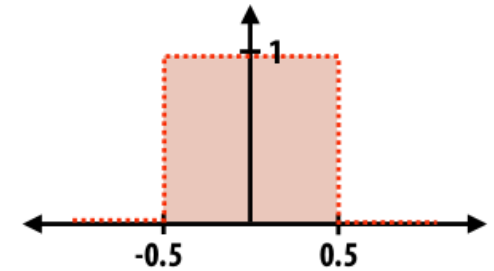
$$(f * g)(x) = \int_{-\infty}^{\infty} f(y)g(x - y)dy$$

filtered signal \nearrow \nwarrow notice the flip \nwarrow filter \nwarrow input signal

Consider the box filter example:

1D continuous
box filter

$$f(x) = \begin{cases} 1 & |x| \leq 0.5 \\ 0 & \text{otherwise} \end{cases}$$







filtering output is a
blurred version of g

$$(f * g)(x) = \int_{-0.5}^{0.5} g(x - y)dy$$

Convolution for 2D discrete signals

Definition of filtering as convolution:

$$(f * g)(x, y) = \sum_{i, j = -\infty}^{\infty} f(i, j) I(x - i, y - j)$$

filtered image   filter  input image  notice the flip

Convolution for 2D discrete signals

Definition of filtering as convolution:

$$(f * g)(x, y) = \sum_{i, j = -\infty}^{\infty} f(i, j) I(x - i, y - j)$$

Diagram illustrating the convolution operation with annotations:

- filtered image (points to $(f * g)(x, y)$)
- filter (points to $f(i, j)$)
- input image (points to $I(x - i, y - j)$)
- notice the flip (points to the minus signs in $x - i$ and $y - j$)

If the filter $f(i, j)$ is non-zero only within $-1 \leq i, j \leq 1$, then

$$(f * g)(x, y) = \sum_{i, j = -1}^1 f(i, j) I(x - i, y - j)$$

The kernel we saw earlier is the 3x3 matrix representation of $f(i, j)$.

Convolution vs correlation

Definition of discrete 2D convolution:

$$(f * g)(x, y) = \sum_{i, j=-\infty}^{\infty} f(i, j) I(x - i, y - j)$$

notice the flip

Definition of discrete 2D correlation:

$$(f * g)(x, y) = \sum_{i, j=-\infty}^{\infty} f(i, j) I(x + i, y + j)$$

notice the lack of a flip

- Most of the time won't matter, because our kernels will be symmetric.
- Will be important when we discuss frequency-domain filtering

Simplest Convolution: the box filter

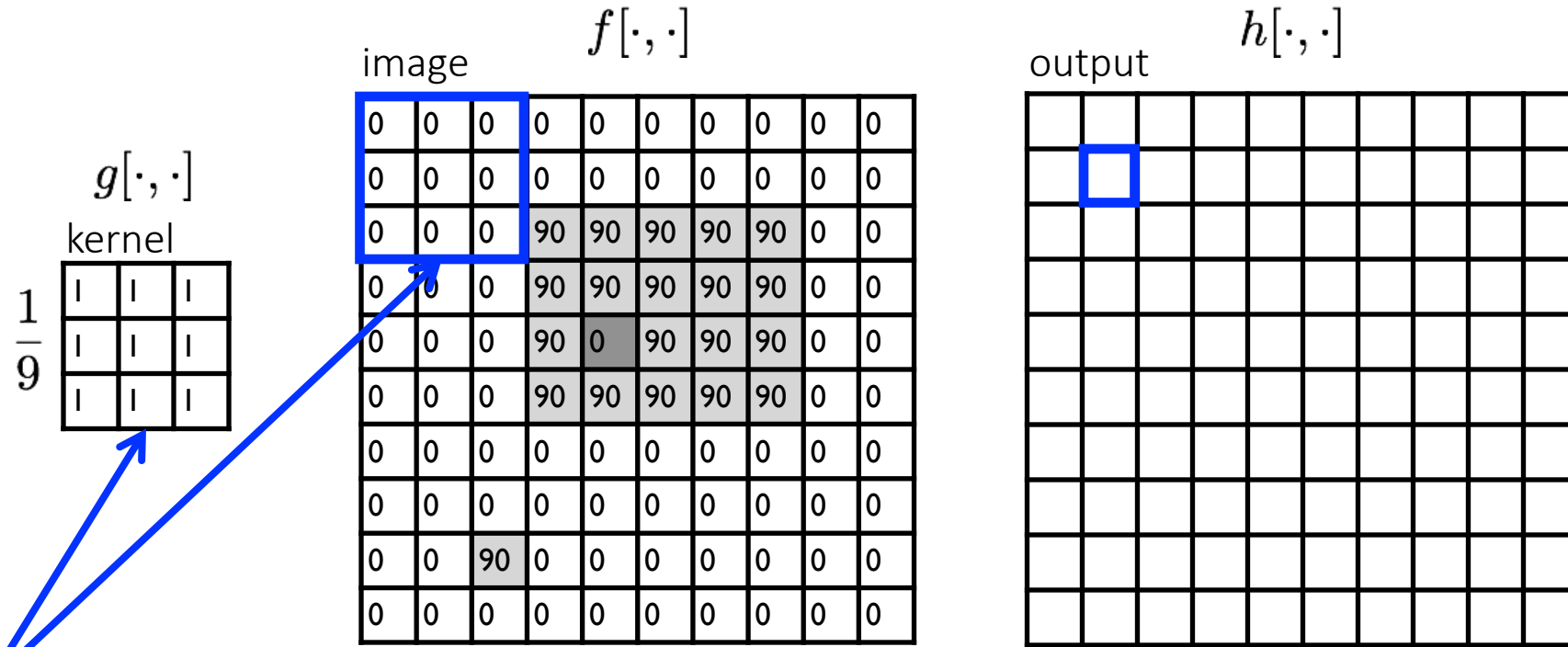
- also known as the 2D rectangular filter
- also known as the square mean filter

$$\text{kernel } g[\cdot, \cdot] = \frac{1}{9} \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

- replaces pixel with local average
- has smoothing (blurring) effect



Let's run the box filter

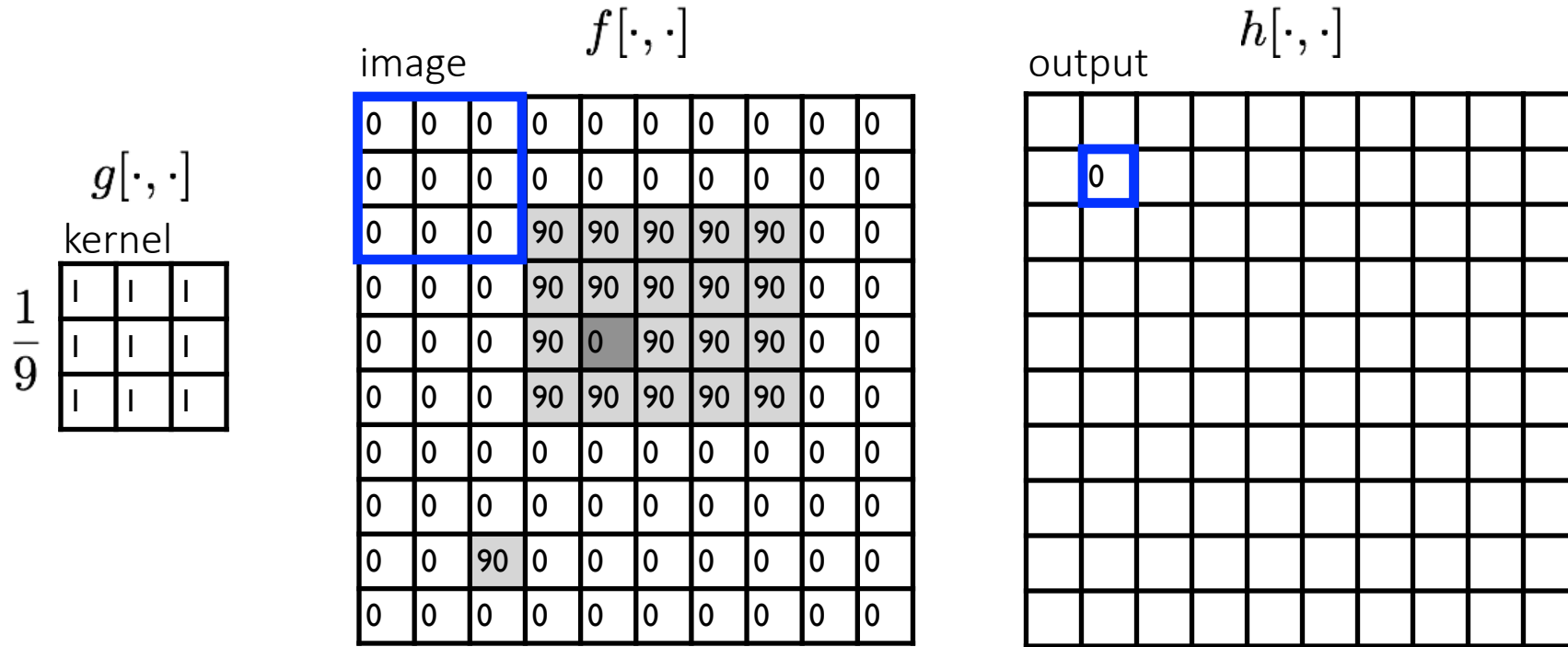


note that we assume that
the kernel coordinates are
centered

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l filter
image (signal)

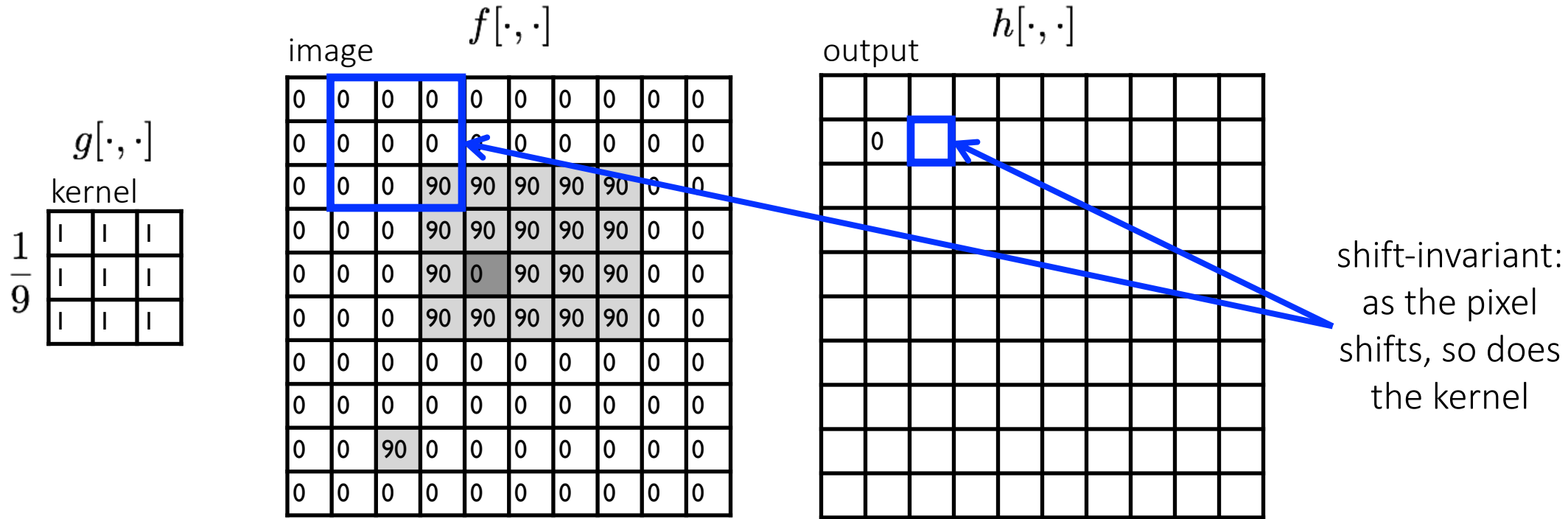
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

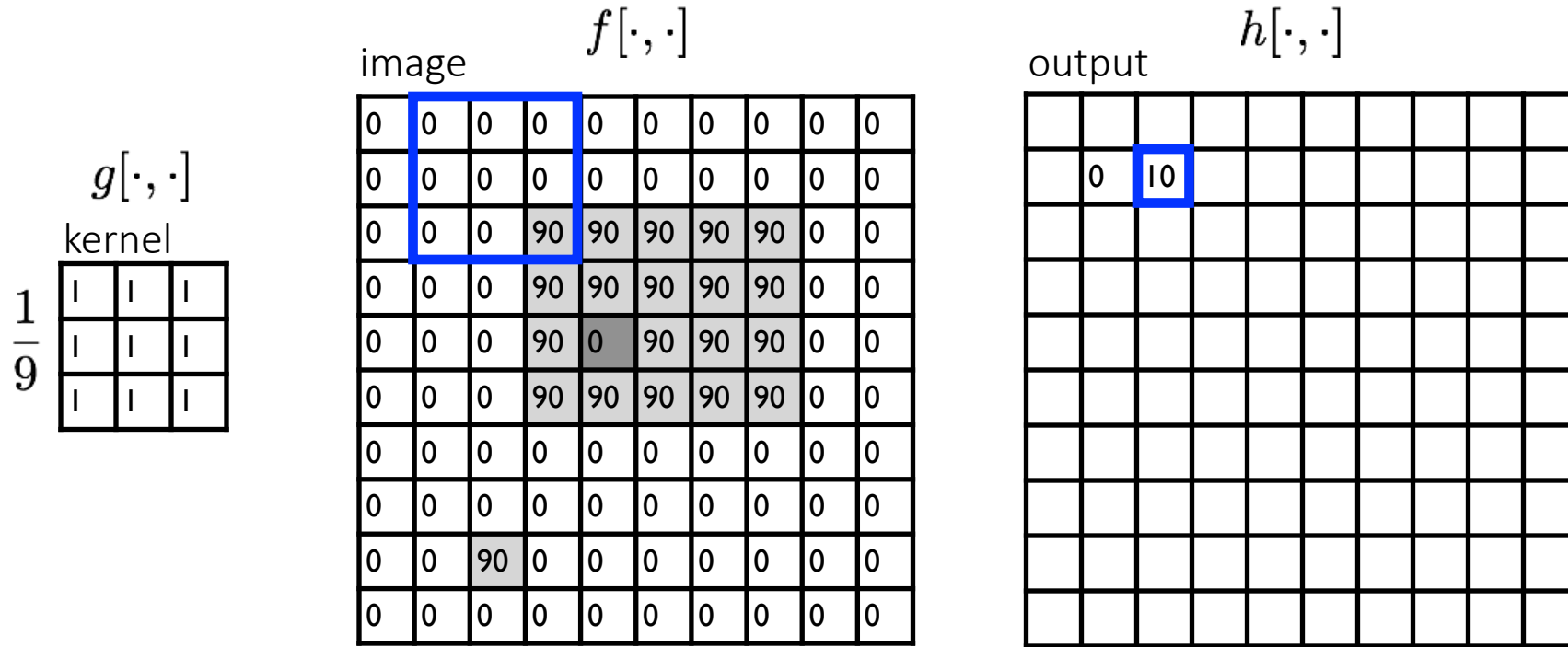
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l
filter
image (signal)

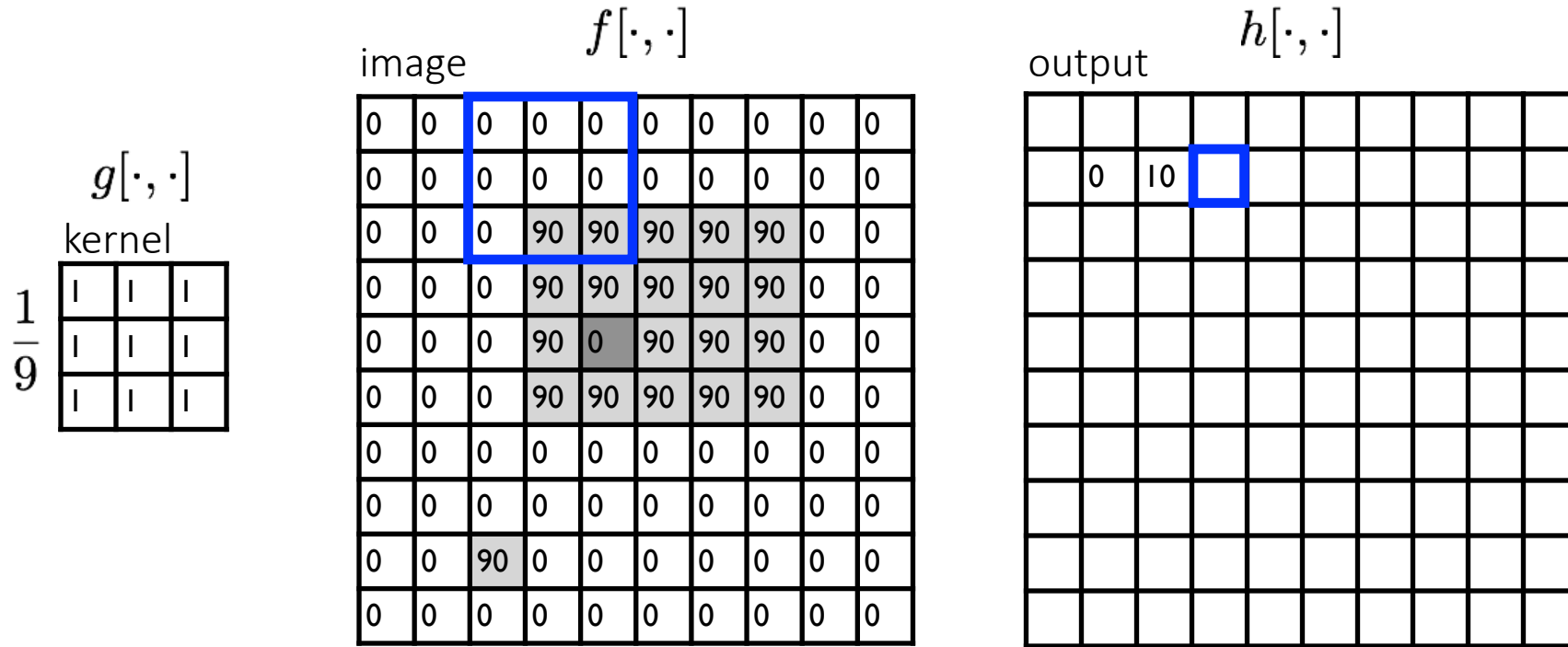
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

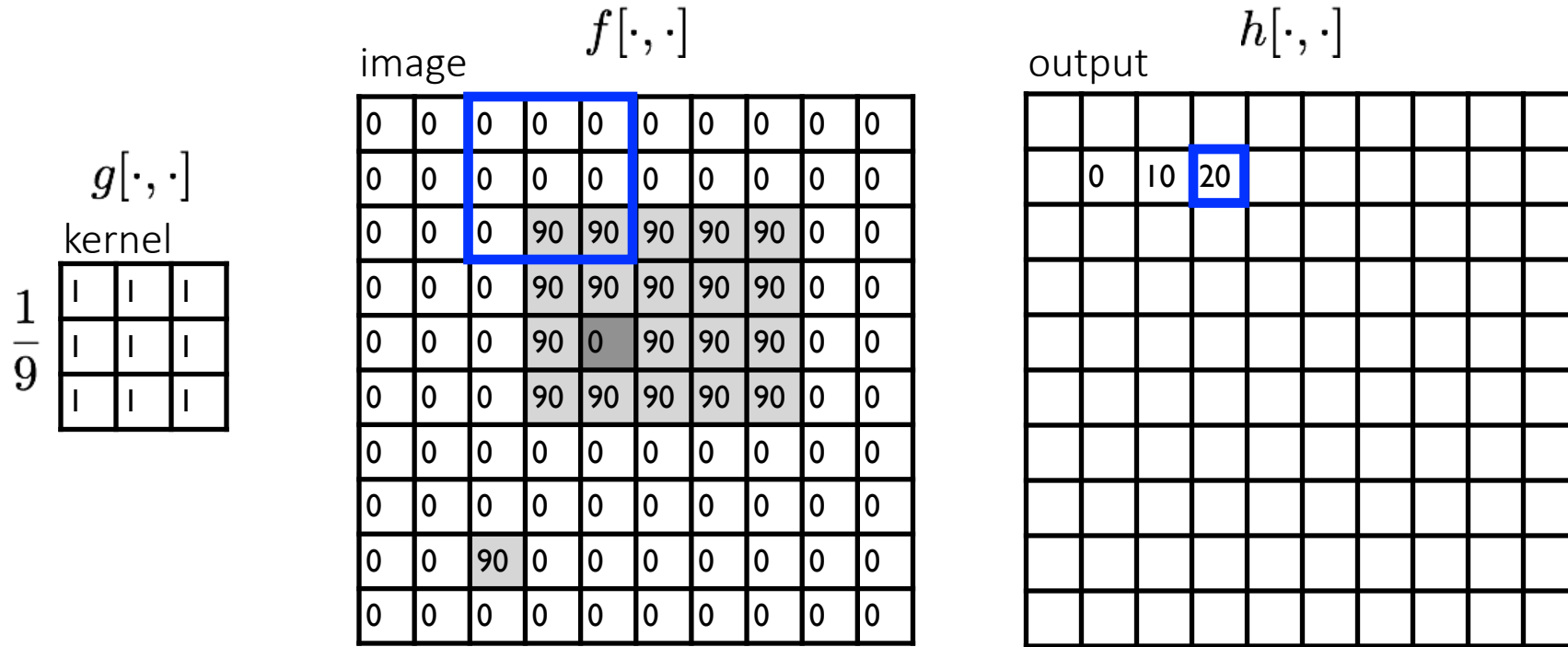
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

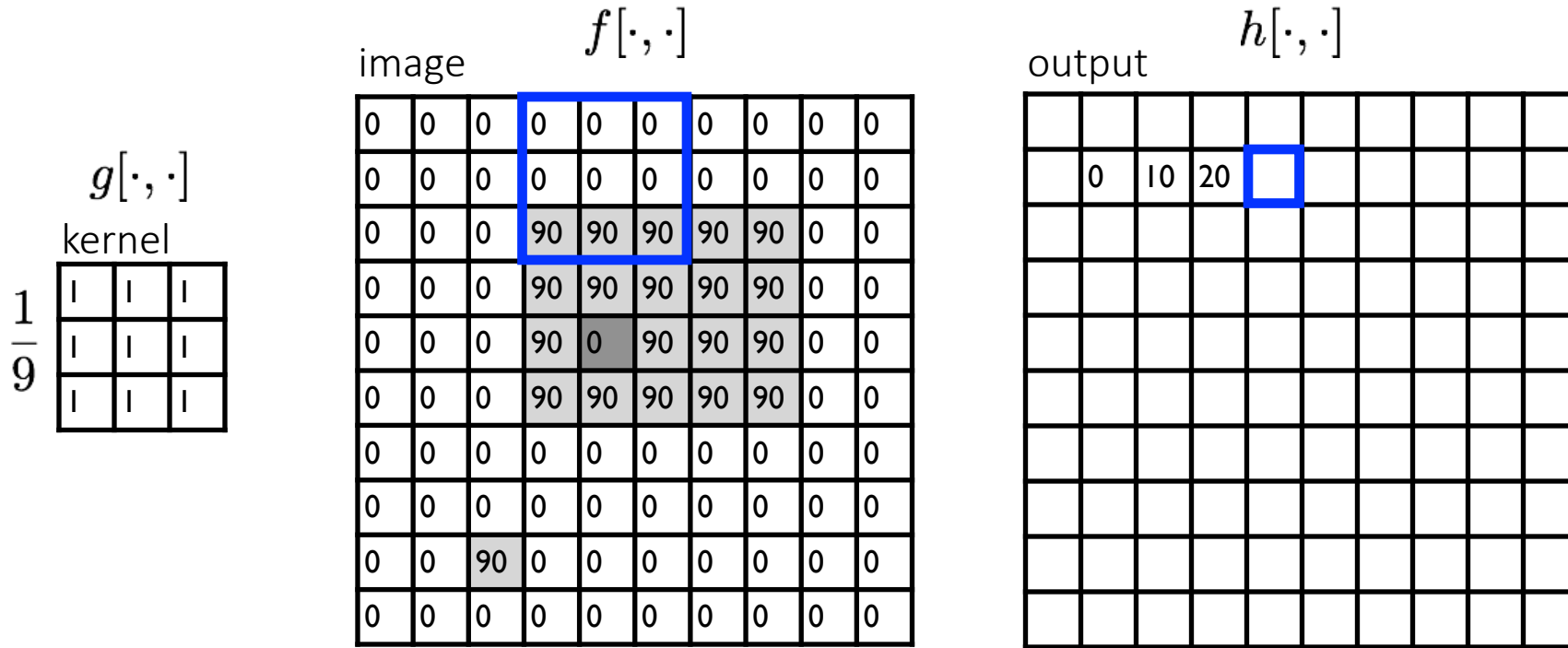
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

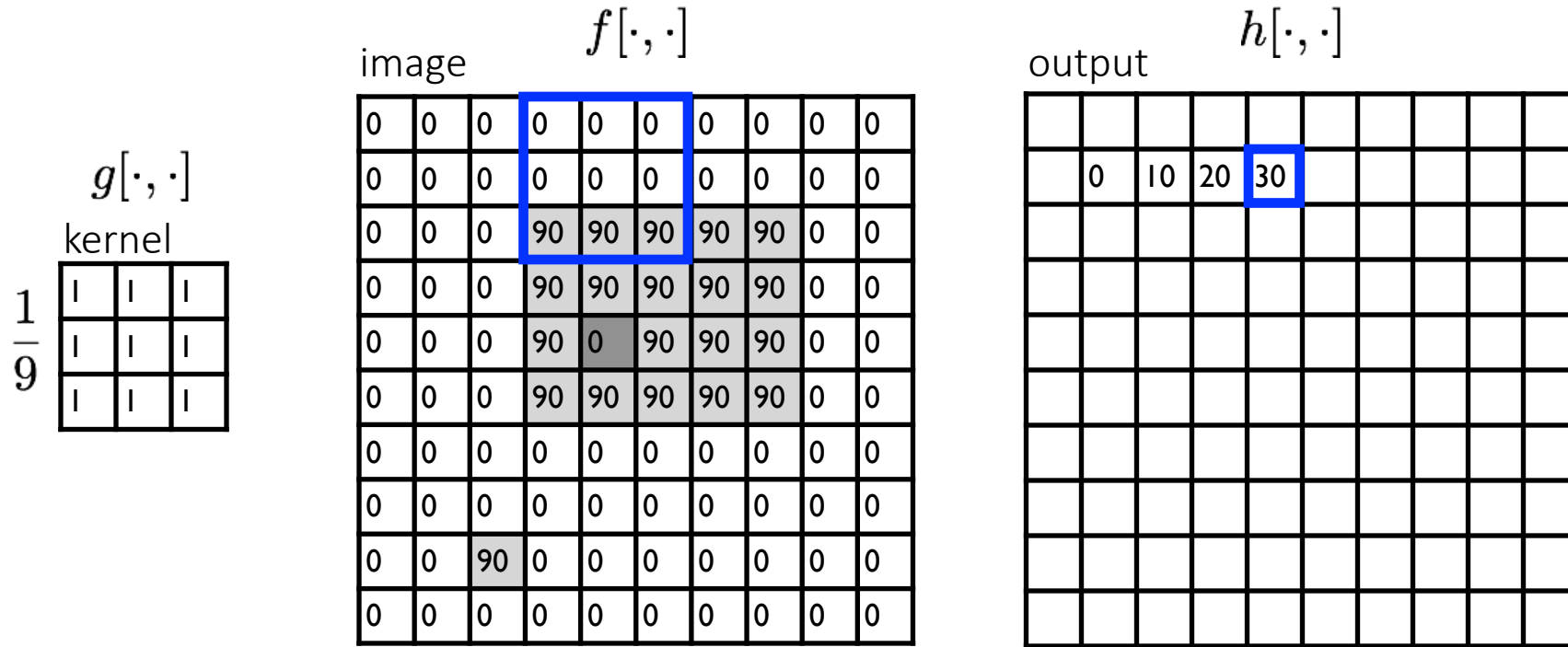
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l
filter
image (signal)

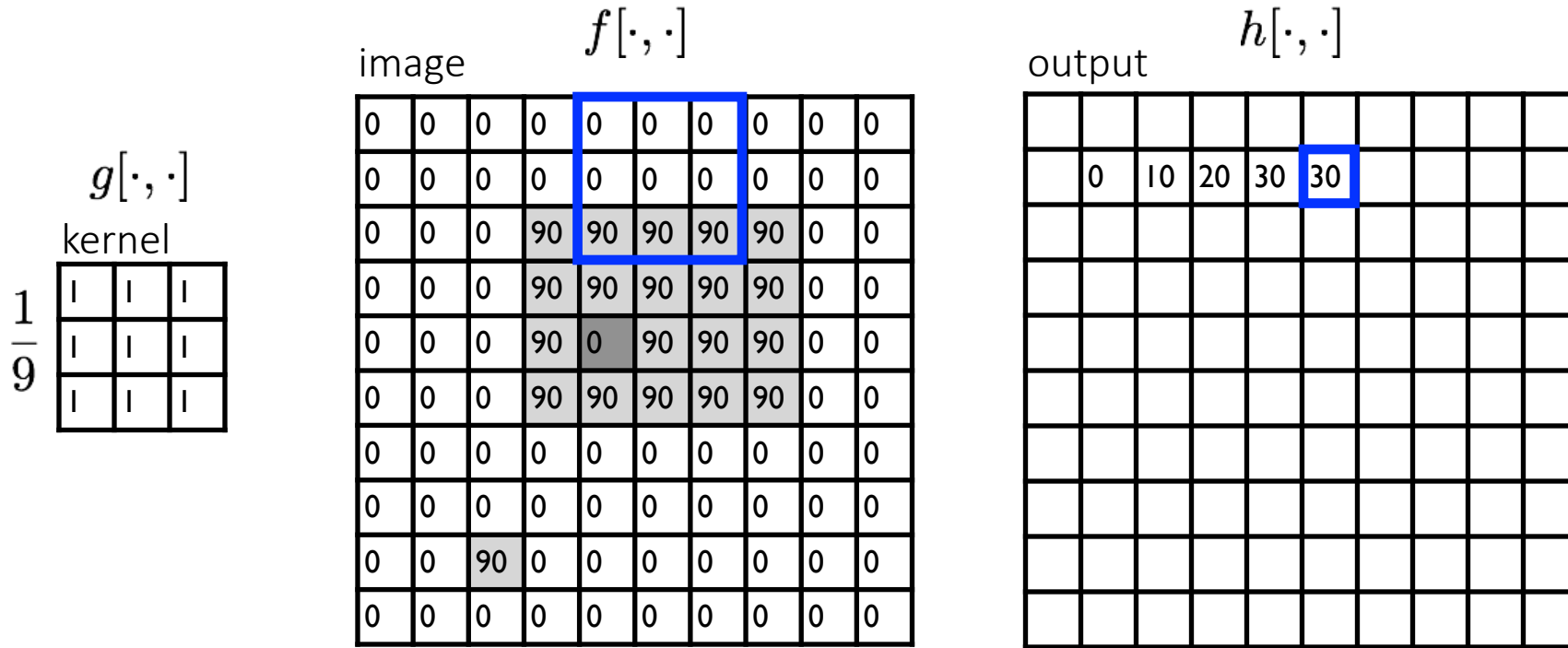
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l
filter
image (signal)

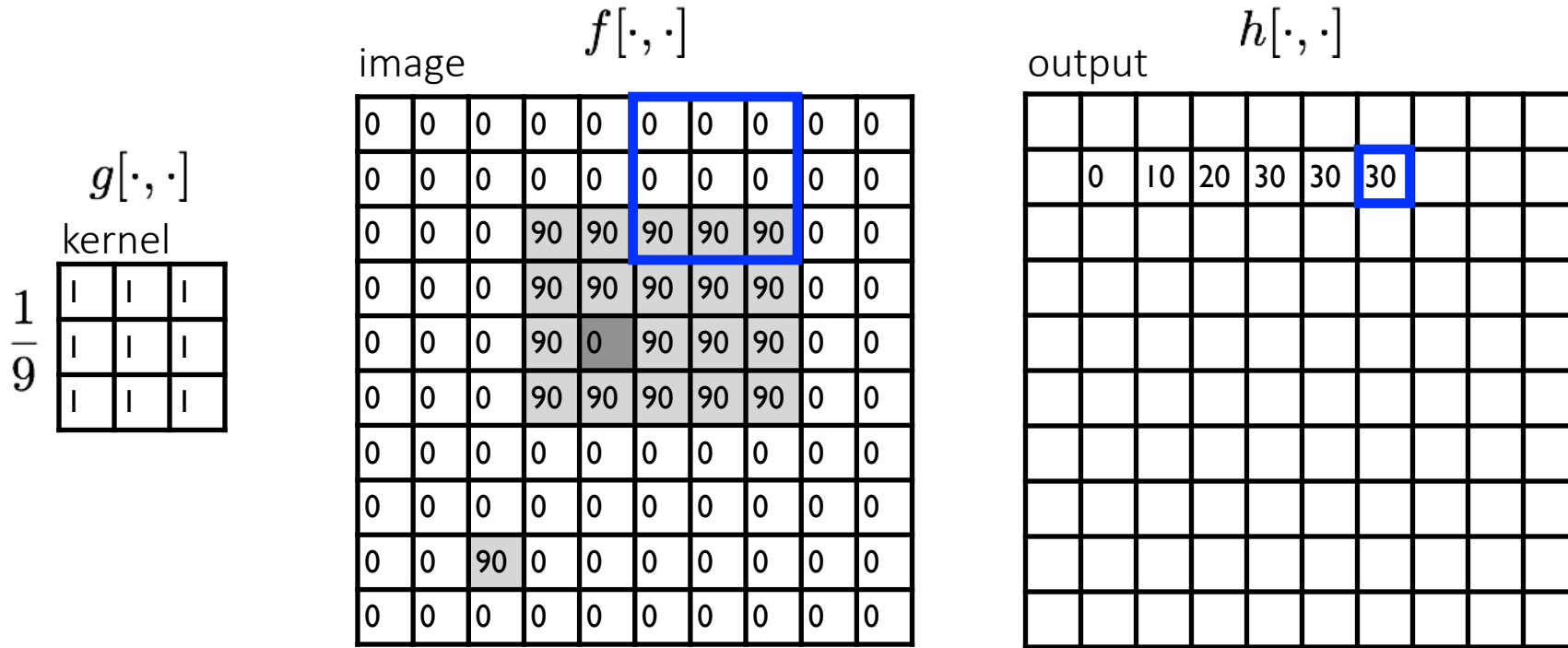
Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

Let's run the box filter

$$\frac{1}{9} g[\cdot, \cdot]$$

1	1	1
1	1	1
1	1	1

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20		

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l
filter
image (signal)

Let's run the box filter

$$\frac{1}{9} g[\cdot, \cdot]$$

1	1	1
1	1	1
1	1	1

kernel

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20	10	

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

Let's run the box filter

$$\frac{1}{9} g[\cdot, \cdot]$$

1	1	1
1	1	1
1	1	1

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20	10	
	0								

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l
filter
image (signal)

Let's run the box filter

$$\frac{1}{9} \begin{matrix} g[\cdot, \cdot] \\ \text{kernel} \\ \begin{bmatrix} | & | & | \\ | & | & | \\ | & | & | \end{bmatrix} \end{matrix}$$

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

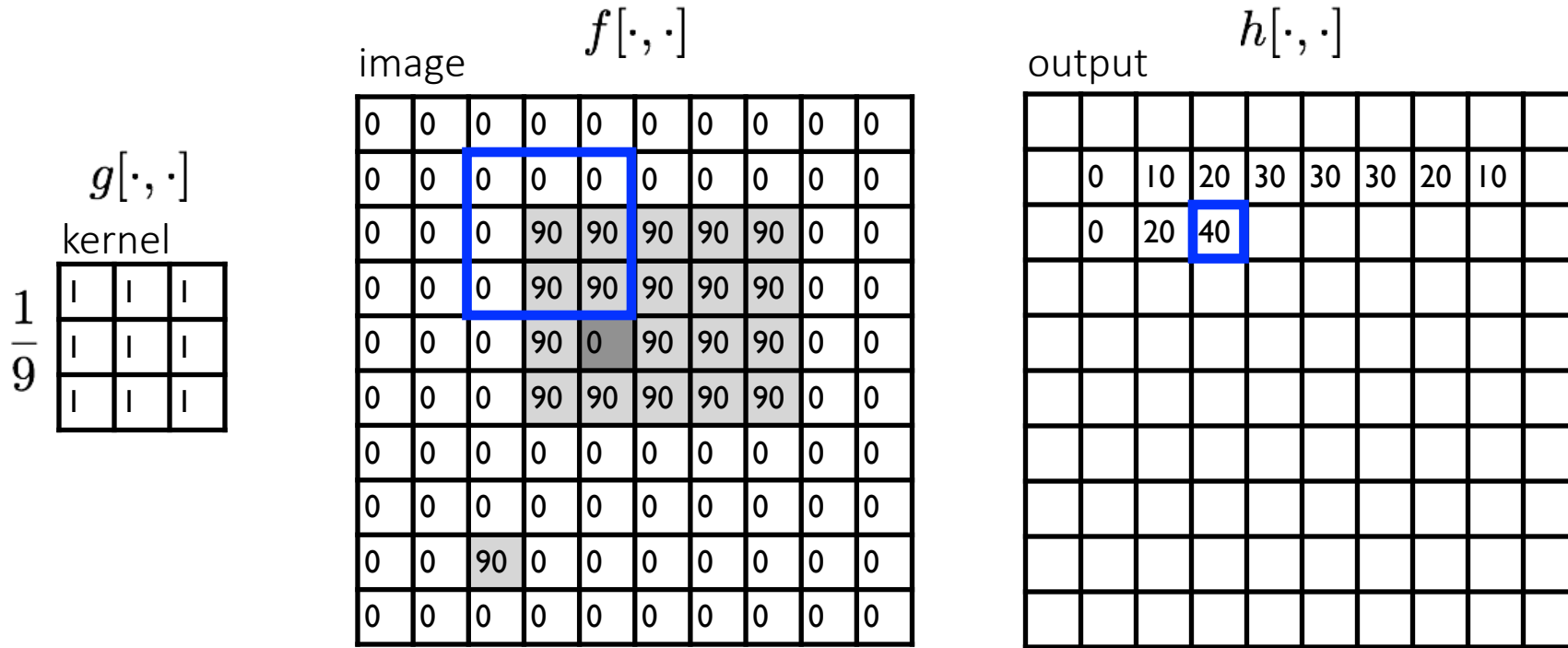
output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20	10	
	0	20							

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l
filter
image (signal)

Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

Let's run the box filter

$$g[\cdot, \cdot]$$

kernel

1	1	1
1	1	1
1	1	1

$\frac{1}{9}$

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

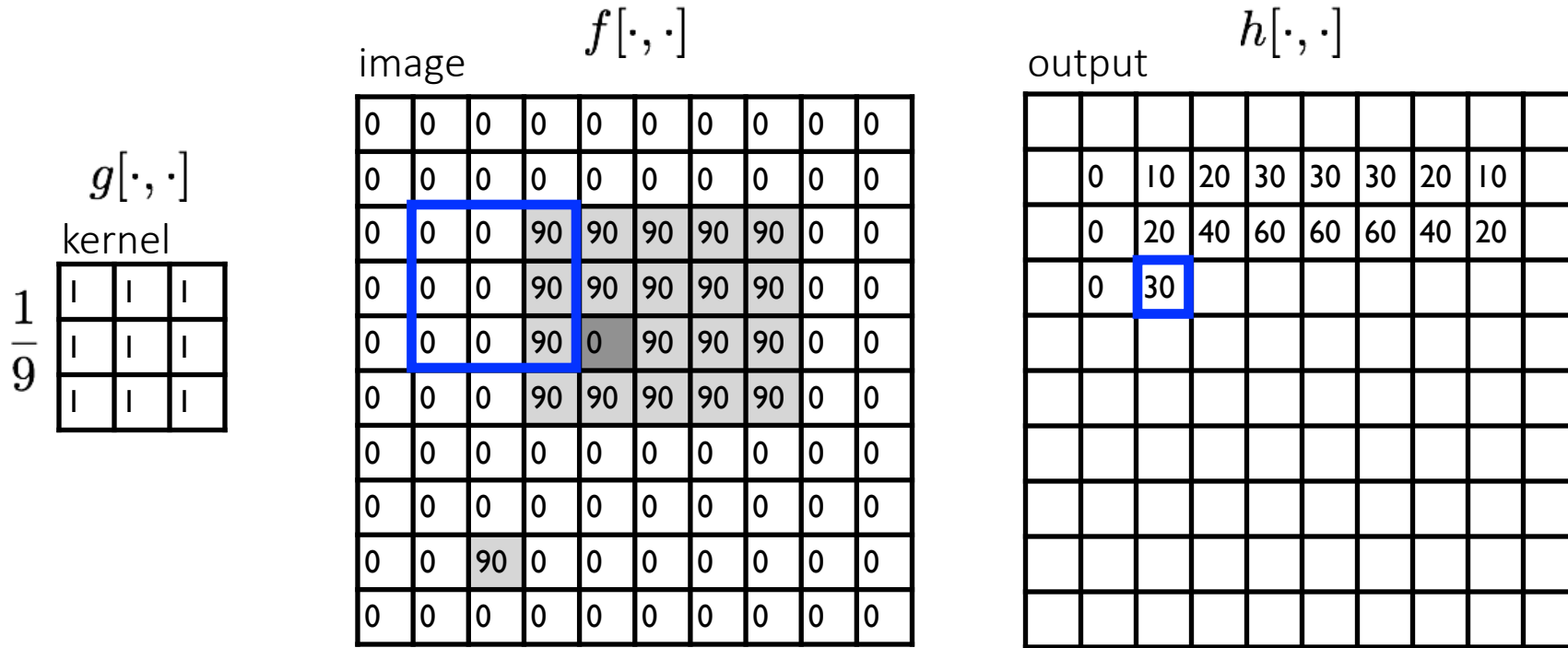
output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20	10	
	0	20	40	60	60	60	40	20	
0									

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

Let's run the box filter



$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

Let's run the box filter

$$\frac{1}{9} \begin{matrix} g[\cdot, \cdot] \\ \text{kernel} \\ \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \end{matrix}$$

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20	10	
	0	20	40	60	60	60	40	20	
	0	30	50	80	80	90	60	30	
	0	30	50	80	80	90	60	30	
	0	20	30	50	50	60	40	20	
	0	10	20	30	30	30	20	10	
	10	10	10	10	0	0	0	0	
	10								

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output
 k, l
filter
image (signal)

Let's run the box filter

$$\frac{1}{9} g[\cdot, \cdot]$$

1	1	1
1	1	1
1	1	1

kernel

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20	10	
	0	20	40	60	60	60	40	20	
	0	30	50	80	80	90	60	30	
	0	30	50	80	80	90	60	30	
	0	20	30	50	50	60	40	20	
	0	10	20	30	30	30	20	10	
	10	10	10	10	0	0	0	0	
	10	10	10	10	0	0	0	0	

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

... and the result is

$$\frac{1}{9} g[\cdot, \cdot]$$

1	1	1
1	1	1
1	1	1

kernel

image $f[\cdot, \cdot]$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

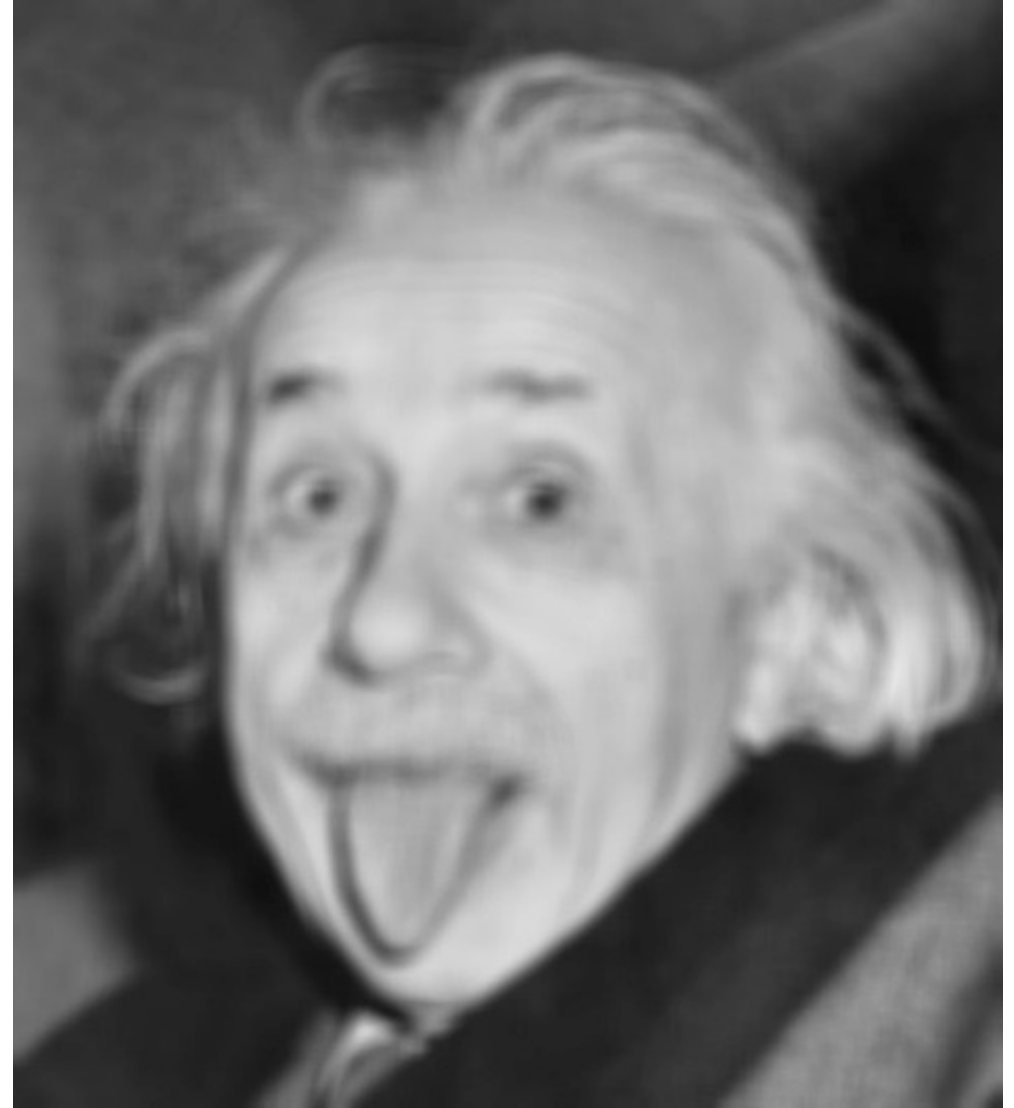
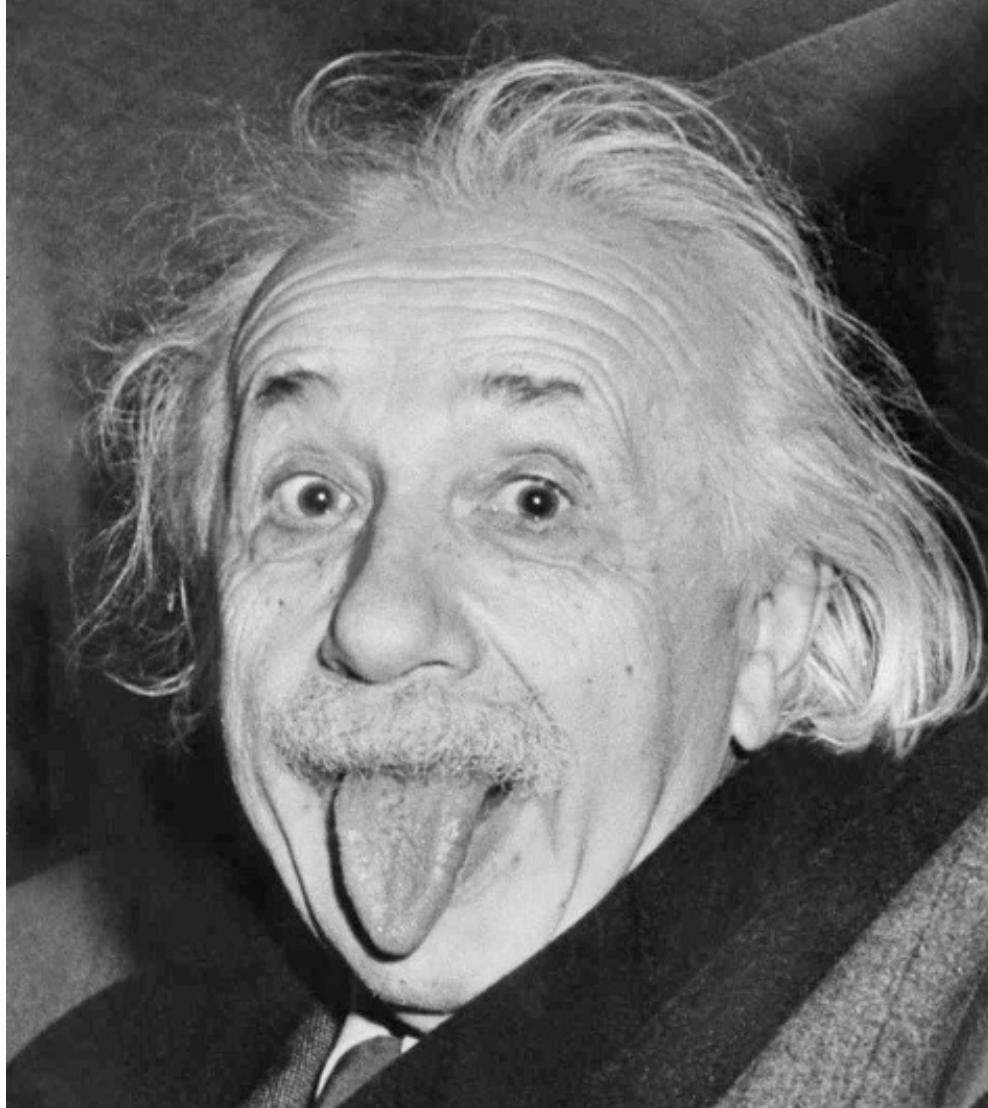
output $h[\cdot, \cdot]$

	0	10	20	30	30	30	20	10	
	0	20	40	60	60	60	40	20	
	0	30	50	80	80	90	60	30	
	0	30	50	80	80	90	60	30	
	0	20	30	50	50	60	40	20	
	0	10	20	30	30	30	20	10	
	10	10	10	10	0	0	0	0	
	10	10	10	10	0	0	0	0	

$$h[m, n] = \sum_{k, l} g[k, l] f[m + k, n + l]$$

output k, l filter image (signal)

Some more realistic examples

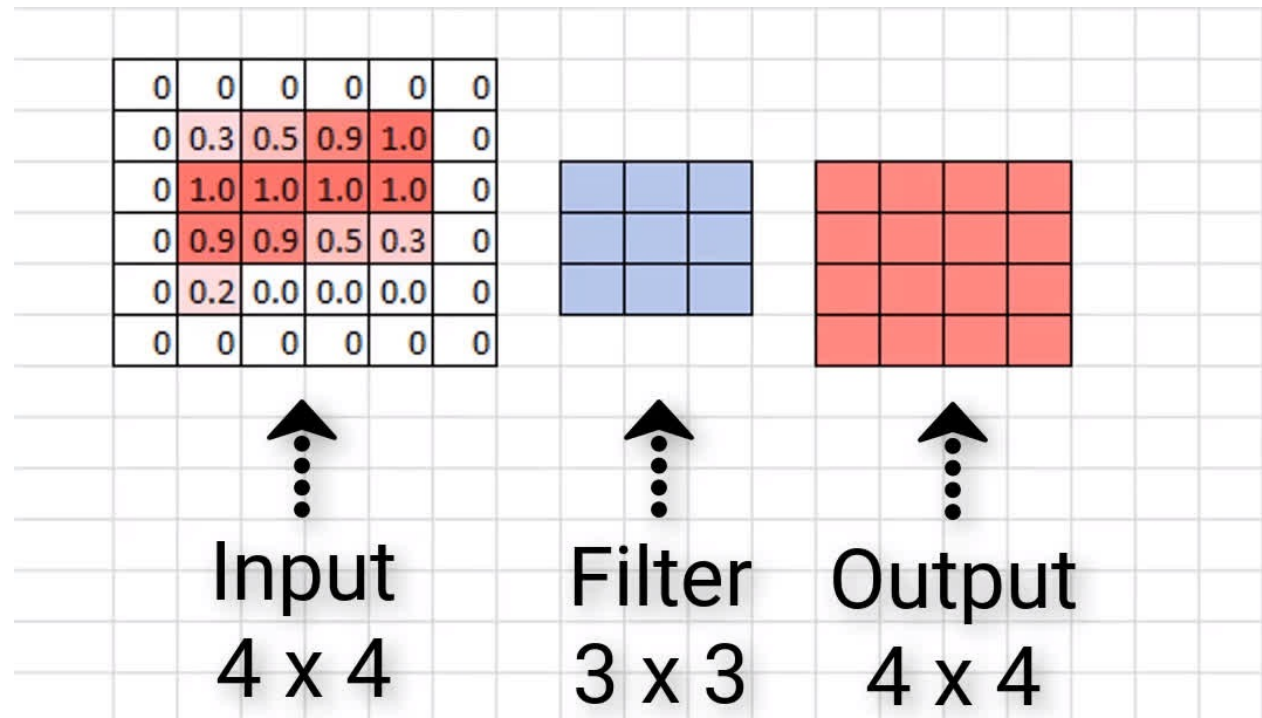


Some more realistic examples



Practical matters: what about near the edge?

- The filter window falls off the edge of the image
- Need to extrapolate!
- Common ways:
 - clip filter (black)
 - wrap around
 - copy edge
 - reflect across edge
 -



Separable filters

A 2D filter is separable if it can be written as the product of a “column” and a “row”.

example:
box filter

1	1	1
1	1	1
1	1	1

=

1
1
1

column

*

1	1	1
---	---	---

row

What is the rank of this filter matrix?

Separable filters

A 2D filter is separable if it can be written as the product of a “column” and a “row”.

example:
box filter

1	1	1
1	1	1
1	1	1

=

1
1
1

column

*

1	1	1
---	---	---

row

Why is this important?

Separable filters

A 2D filter is separable if it can be written as the product of a “column” and a “row”.

example:
box filter

1	1	1
1	1	1
1	1	1

=

1
1
1

column

*

1	1	1
---	---	---

row

2D convolution with a separable filter is equivalent to two 1D convolutions (with the “column” and “row” filters).

Separable filters

A 2D filter is separable if it can be written as the product of a “column” and a “row”.

example:
box filter

1	1	1
1	1	1
1	1	1

=

1
1
1

column

*

1	1	1
---	---	---

row

2D convolution with a separable filter is equivalent to two 1D convolutions (with the “column” and “row” filters).

If the image has $M \times M$ pixels and the filter kernel has size $N \times N$:

- What is the cost of convolution with a non-separable filter?

Separable filters

A 2D filter is separable if it can be written as the product of a “column” and a “row”.

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box filter

1	1	1
1	1	1
1	1	1

=

1
1
1

column

*

1	1	1
---	---	---

row

2D convolution with a separable filter is equivalent to two 1D convolutions (with the “column” and “row” filters).

If the image has $M \times M$ pixels and the filter kernel has size $N \times N$:

- What is the cost of convolution with a non-separable filter? $\longrightarrow M^2 \times N^2$
- What is the cost of convolution with a separable filter?

Separable filters

A 2D filter is separable if it can be written as the product of a “column” and a “row”.

example:
box filter

1	1	1
1	1	1
1	1	1

=

1
1
1

column

*

1	1	1
---	---	---

row

2D convolution with a separable filter is equivalent to two 1D convolutions (with the “column” and “row” filters).

If the image has $M \times M$ pixels and the filter kernel has size $N \times N$:

- What is the cost of convolution with a non-separable filter? $\longrightarrow M^2 \times N^2$
- What is the cost of convolution with a separable filter? $\longrightarrow 2 \times N \times M^2$

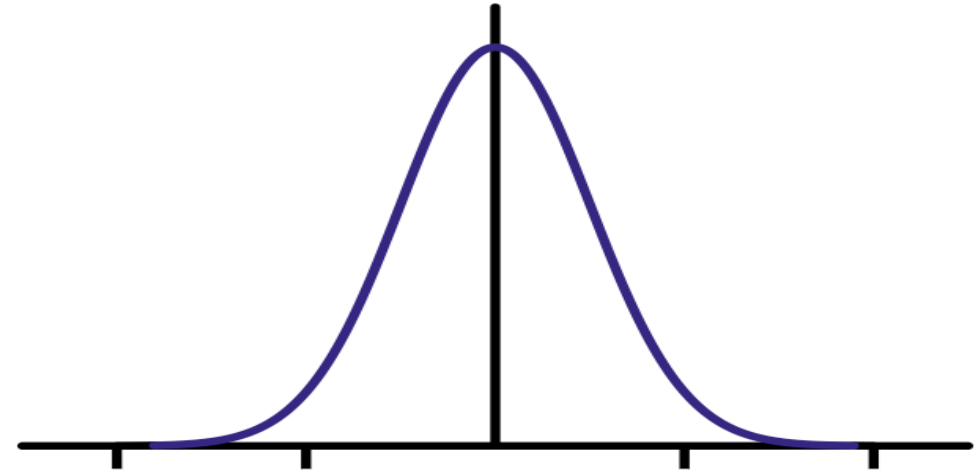
The Gaussian filter

- named (like many other things) after Carl Friedrich Gauss
- kernel values sampled from the 2D Gaussian function:

$$f(i, j) = \frac{1}{2\pi\sigma^2} e^{-\frac{i^2+j^2}{2\sigma^2}}$$

- weight falls off with distance from center pixel
- theoretically infinite, in practice truncated to some maximum distance

Any heuristics for selecting where to truncate?



The Gaussian filter

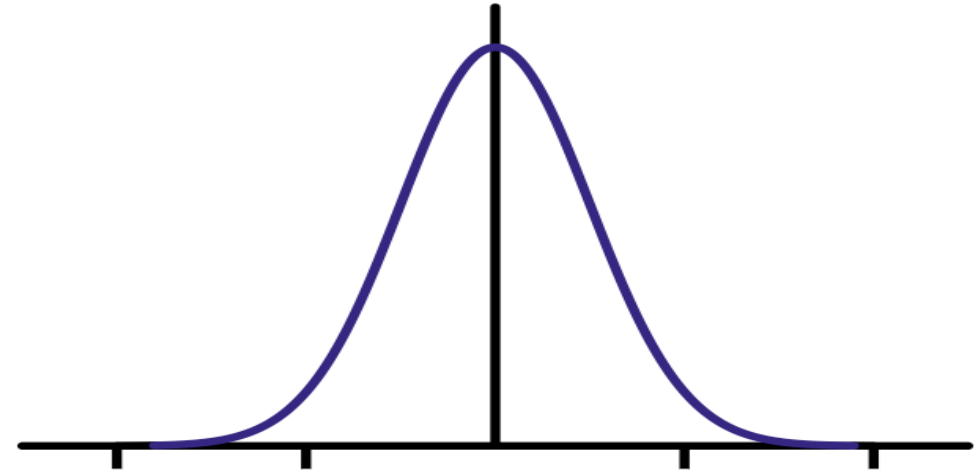
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- weight falls off with distance from center pixel
- theoretically infinite, in practice truncated to some maximum distance

Any heuristics for selecting where to truncate?

- usually at $2-3\sigma$



Is this a separable filter?

kernel $\frac{1}{16}$

1	2	1
2	4	2
1	2	1

The Gaussian filter

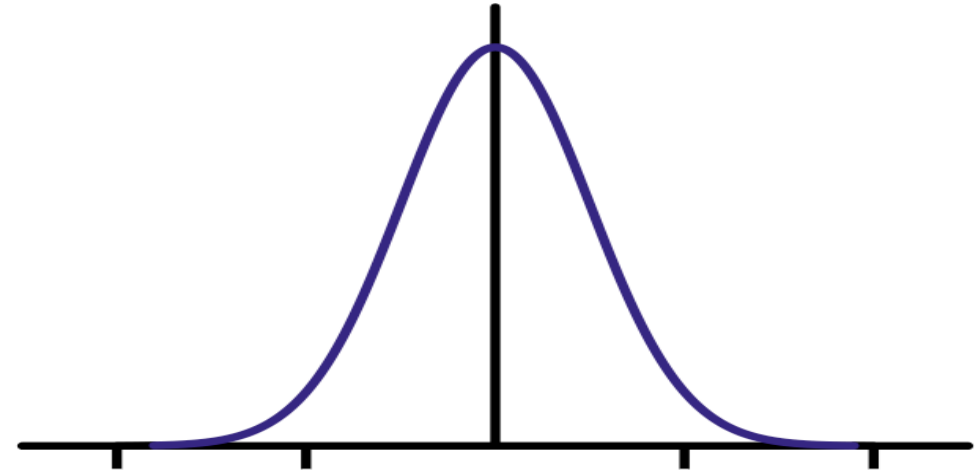
- named (like many other things) after Carl Friedrich Gauss
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Any heuristics for selecting where to truncate?

- usually at $2-3\sigma$

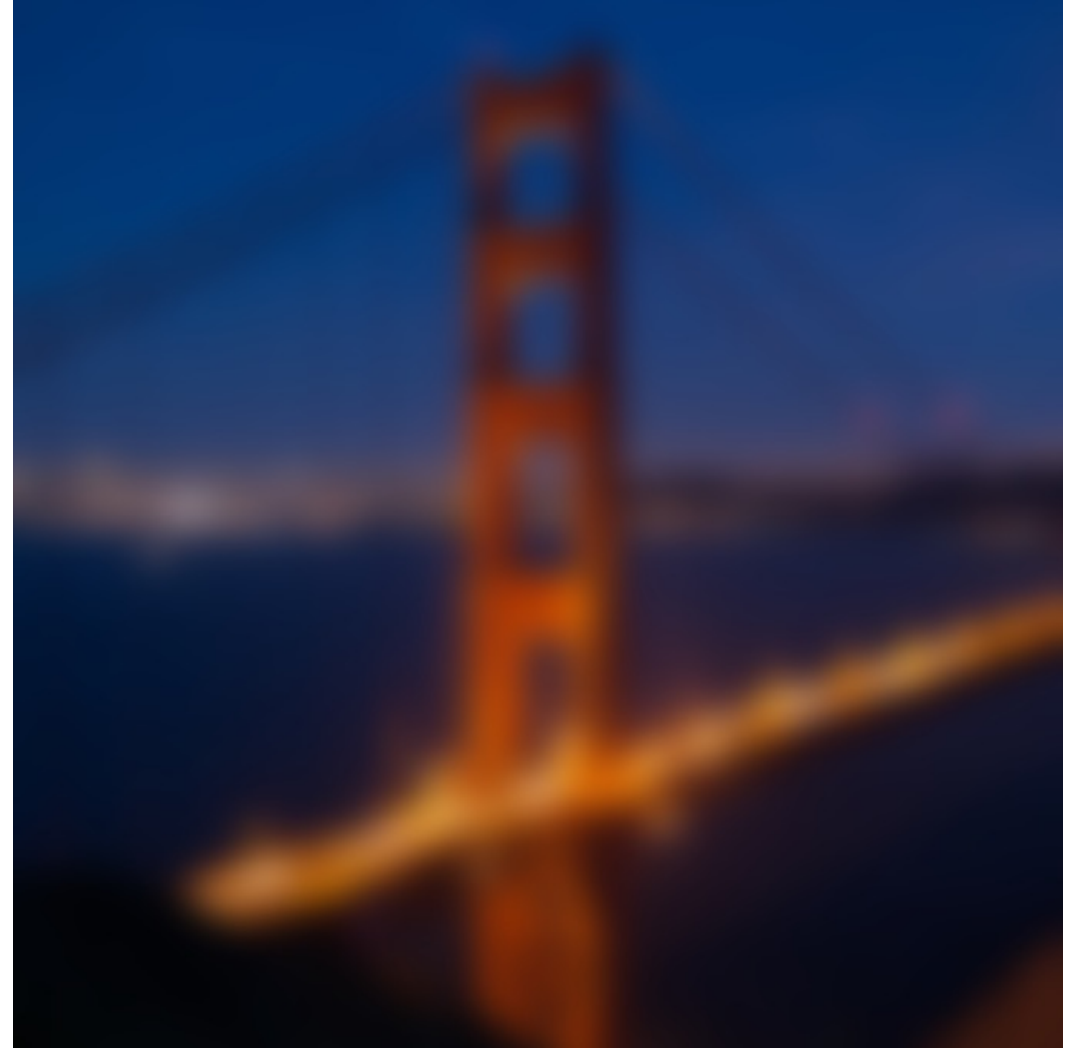


Is this a separable filter? **Yes!**

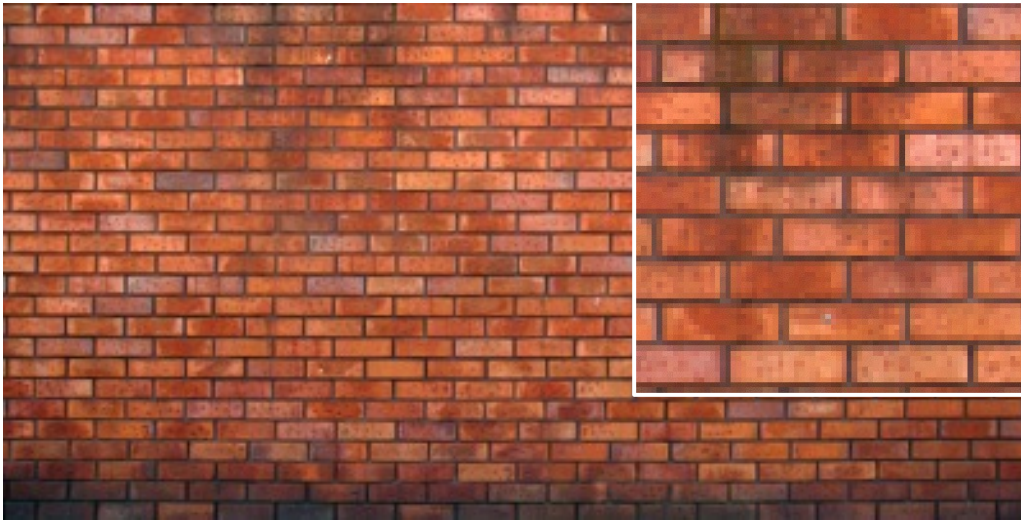
kernel $\frac{1}{16}$

1	2	1
2	4	2
1	2	1

Gaussian filtering example

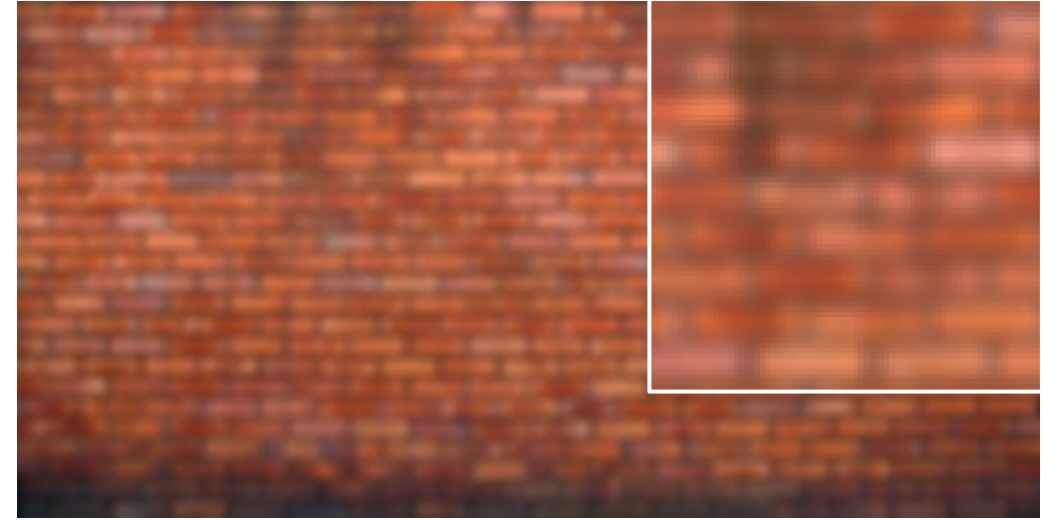


Gaussian vs box filtering



original

Which blur do you like better? Why?



7x7 Gaussian



7x7 box

Other filters

input



filter

0	0	0
0	1	0
0	0	0

output

?

Other filters

input



filter

0	0	0
0	1	0
0	0	0

output



unchanged

Other filters

input



filter

0	0	0
0	1	0
0	0	0

output



unchanged

input



filter

0	0	0
0	0	1
0	0	0

output

?

Other filters

input



filter

0	0	0
0	1	0
0	0	0

output



unchanged

input



filter

0	0	0
0	0	1
0	0	0

output



shift to left
by one

Other filters

input



filter

0	0	0
0	2	0
0	0	0

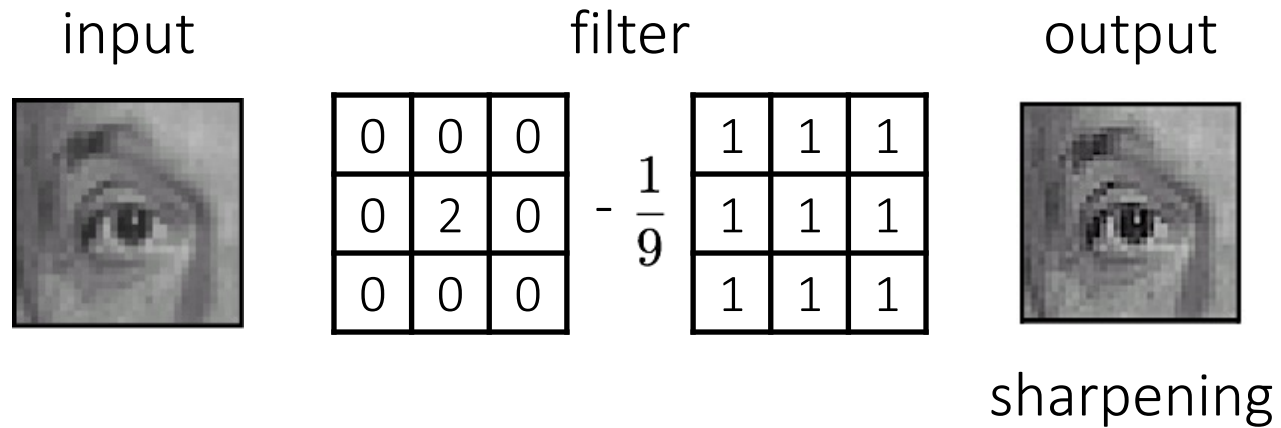
$-\frac{1}{9}$

1	1	1
1	1	1
1	1	1

output

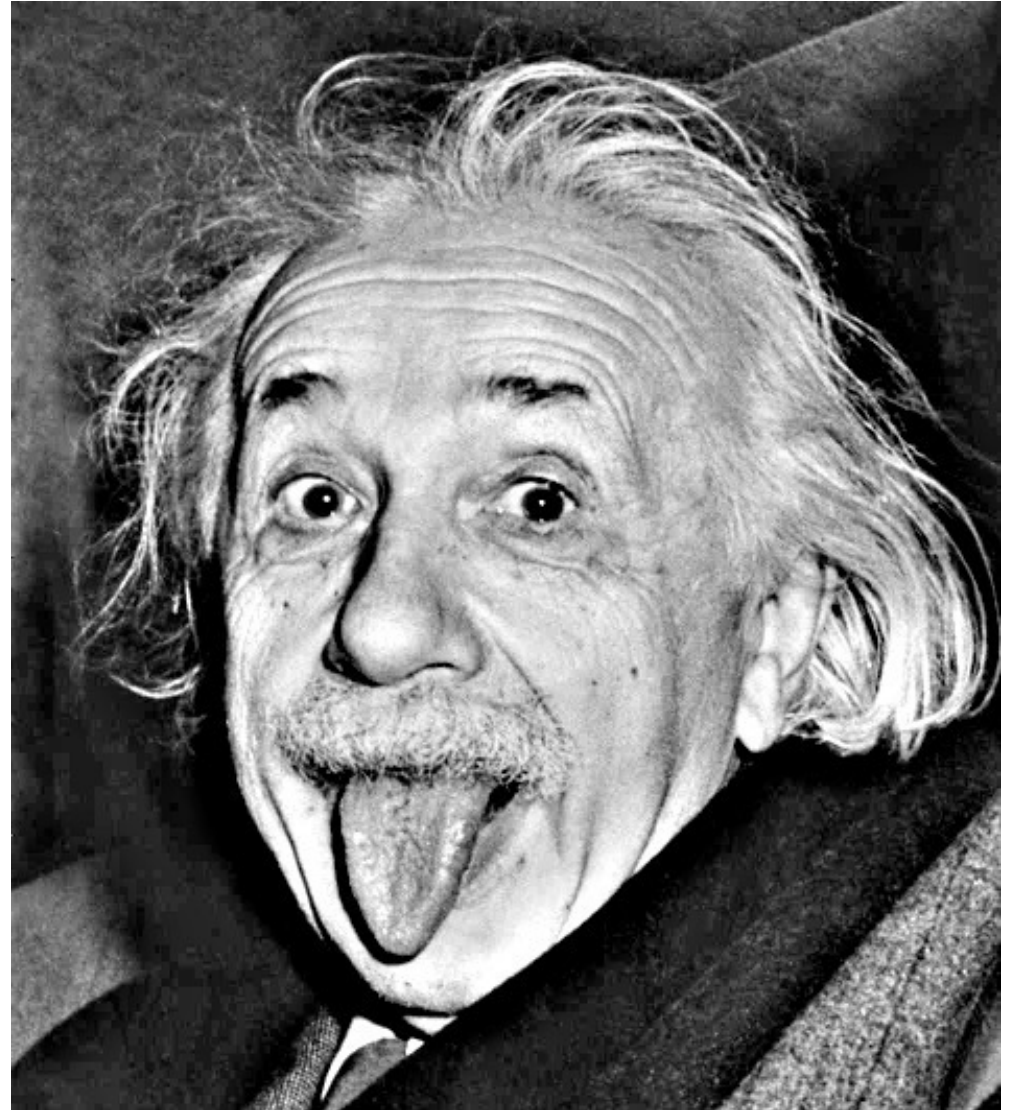
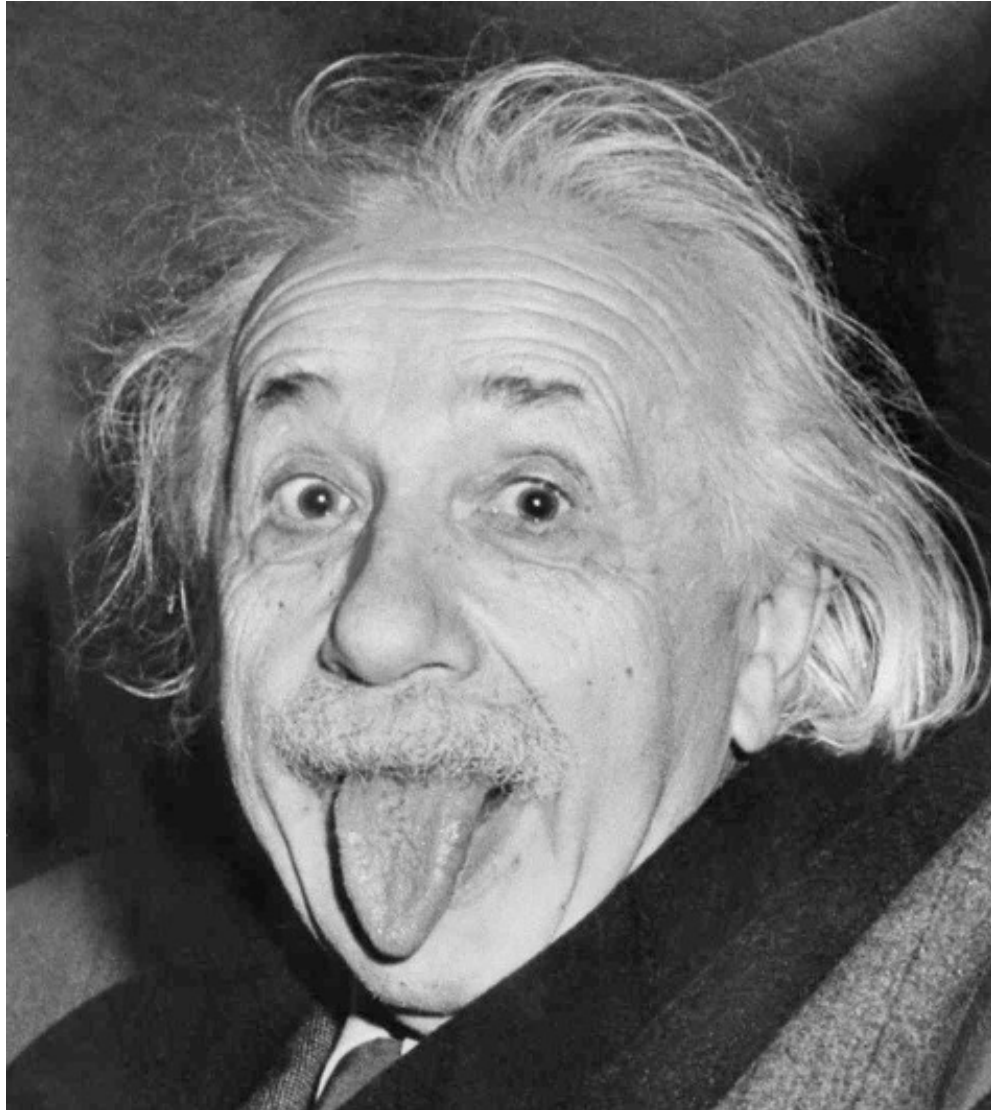
?

Other filters



- do nothing for flat areas
- stress intensity peaks

Sharpening examples



Sharpening examples



Do not overdo it with sharpening



original



sharpened



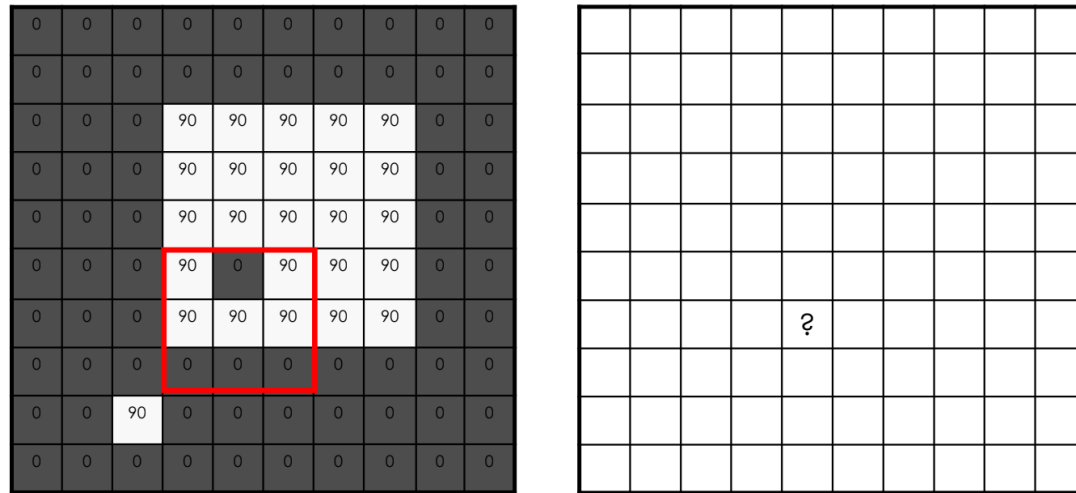
oversharpened

What is wrong in this image?

Not all simple filters are “linear transform”!

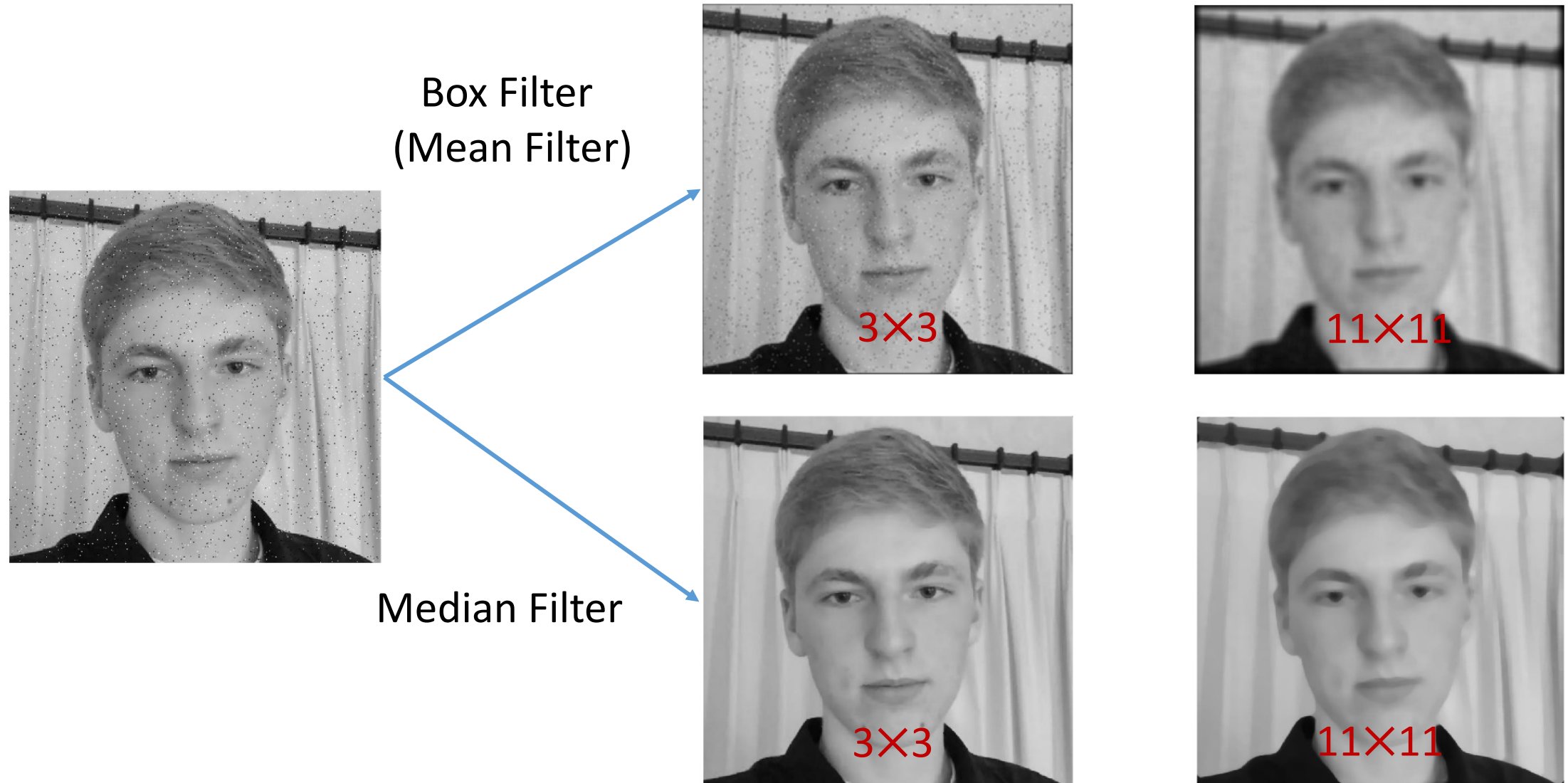
A Simple yet Important Exception: Median Filter

- Operates over a window by selecting the median intensity in the window



- Belong to the class of “**rank**” filter as based on sorting gray levels
 - More example: min, max, range...
 - “Modern name” in deep learning? “Pooling”

Median Filter: When/Why better than Box Filter?



The convolution theorem

The Fourier transform of the convolution of two functions is the product of their Fourier transforms:

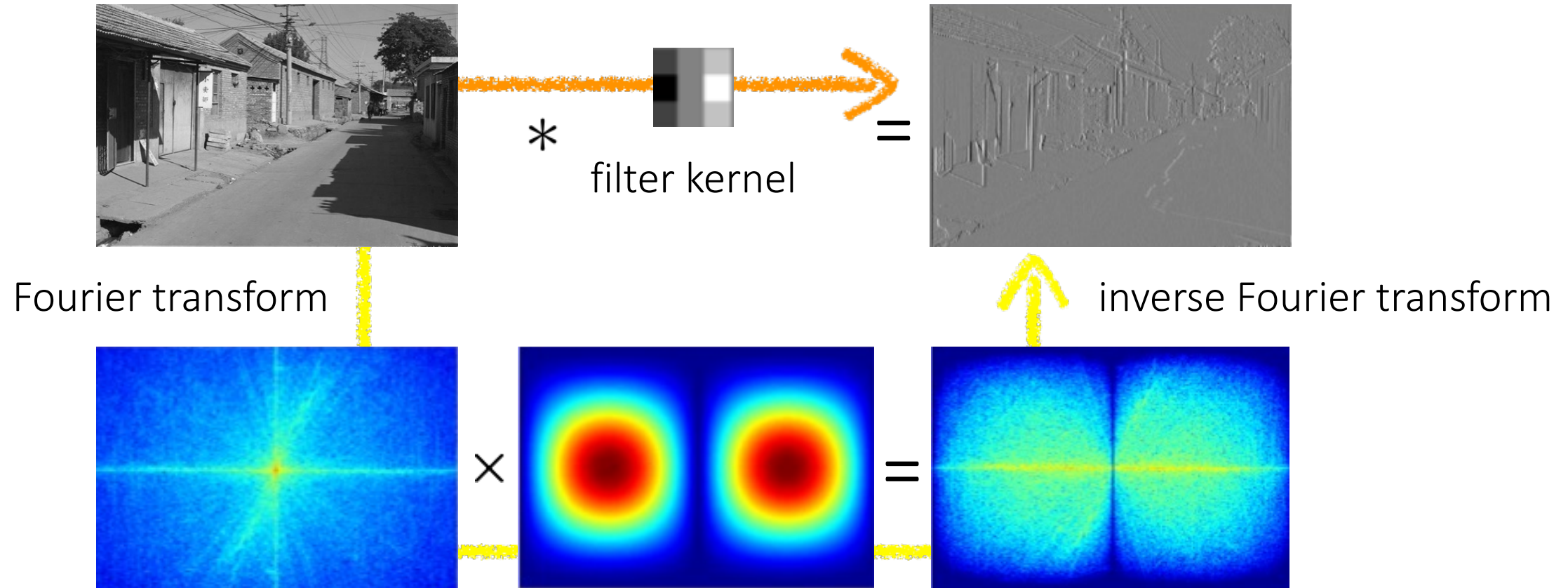
$$\mathcal{F}\{g * h\} = \mathcal{F}\{g\}\mathcal{F}\{h\}$$

The inverse Fourier transform of the product of two Fourier transforms is the convolution of the two inverse Fourier transforms:

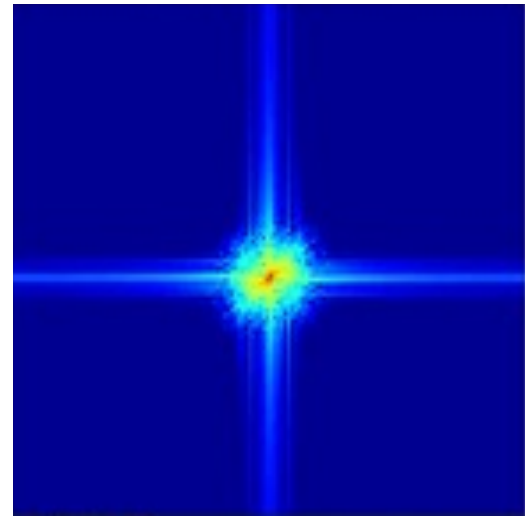
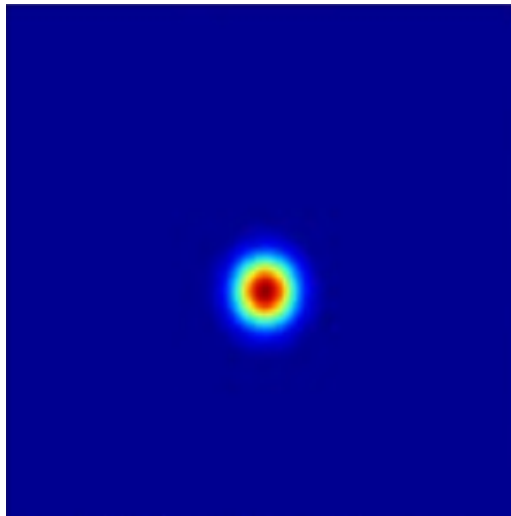
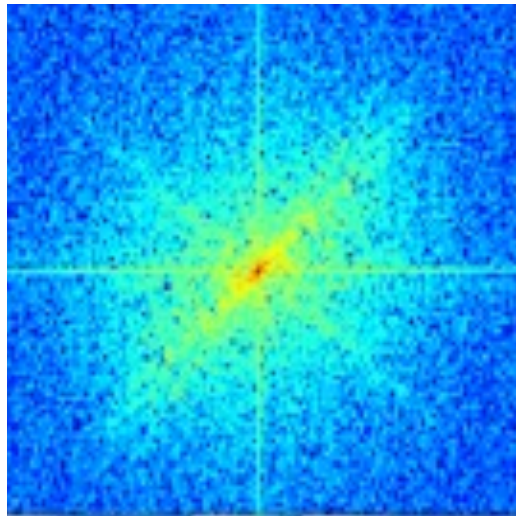
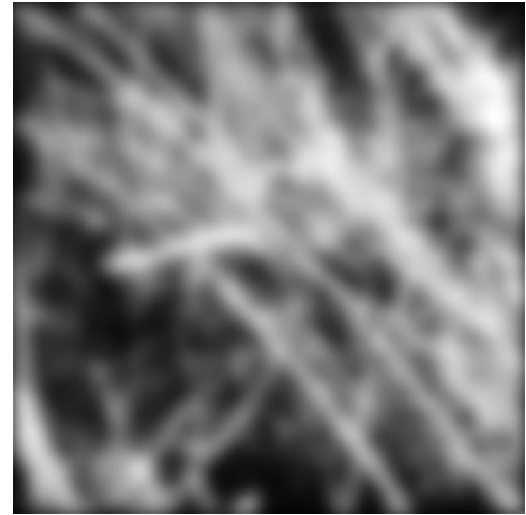
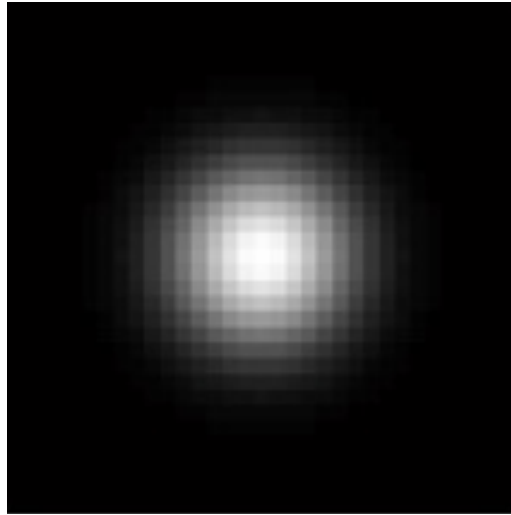
$$\mathcal{F}^{-1}\{gh\} = \mathcal{F}^{-1}\{g\} * \mathcal{F}^{-1}\{h\}$$

Convolution in spatial domain is equivalent to multiplication in frequency domain!

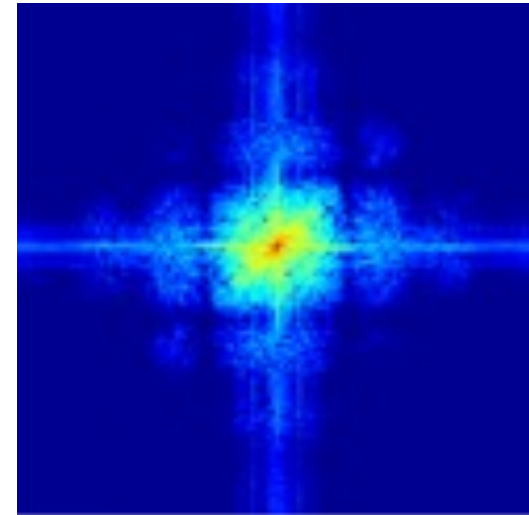
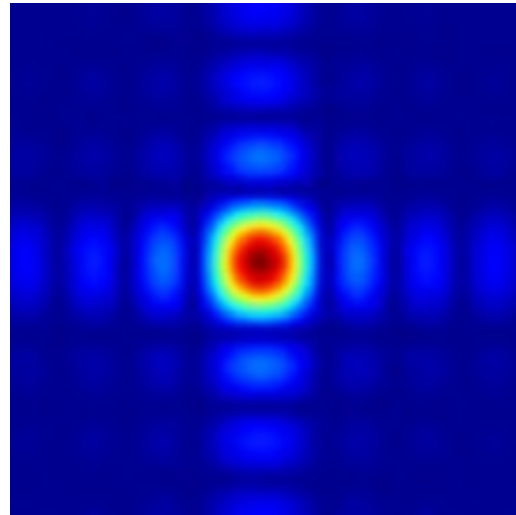
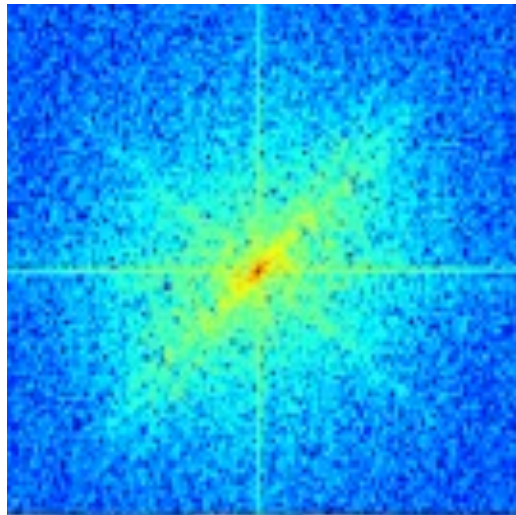
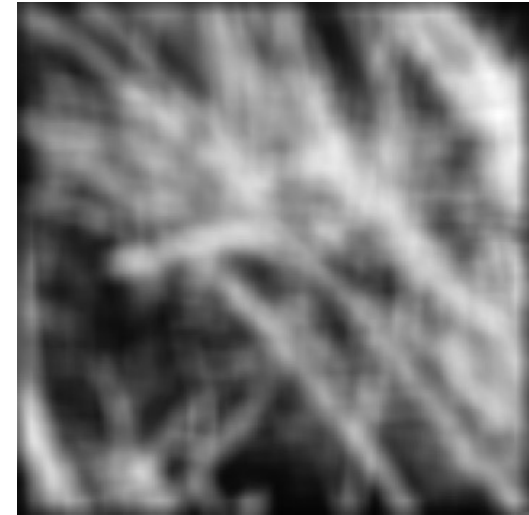
Spatial domain filtering



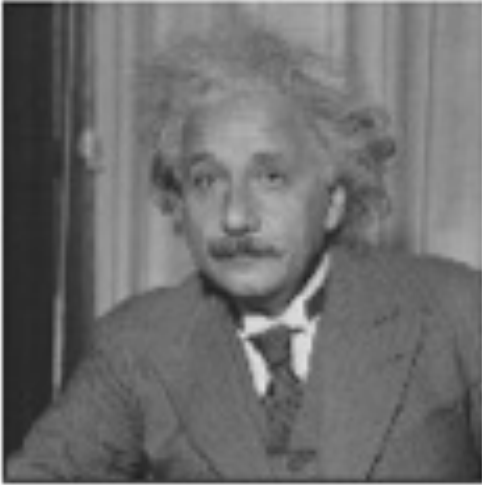
Gaussian blur



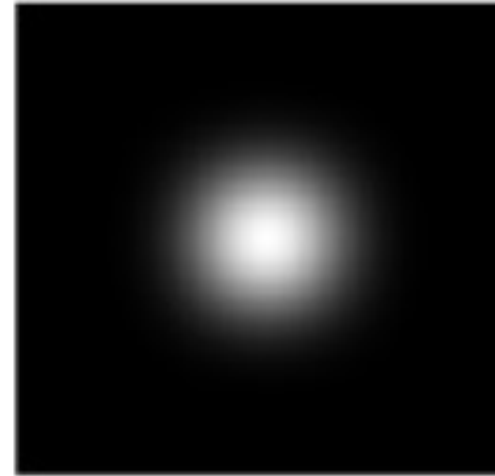
Box blur



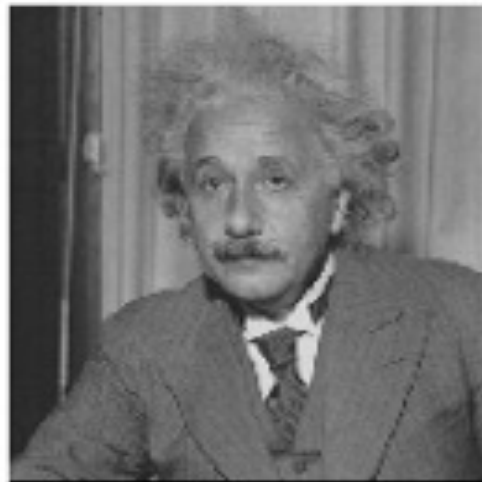
More filtering examples



?



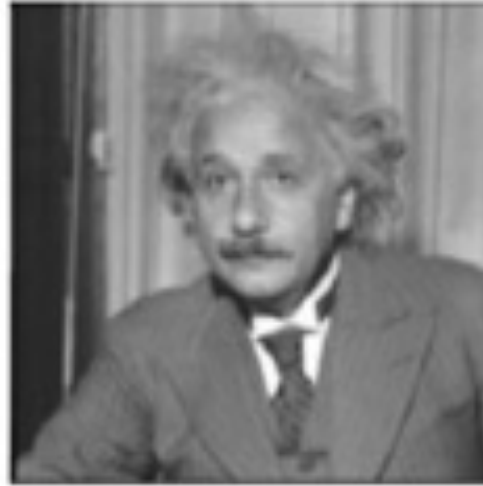
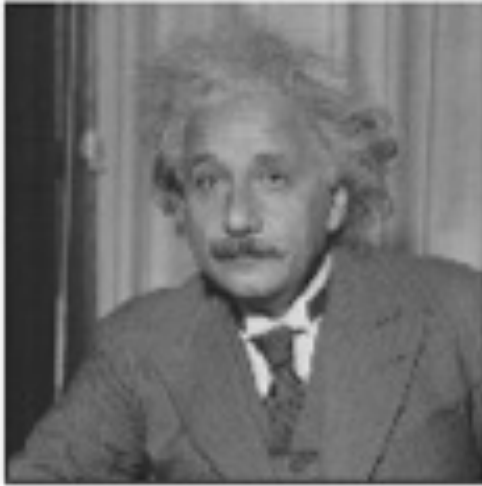
filters shown
in frequency-
domain



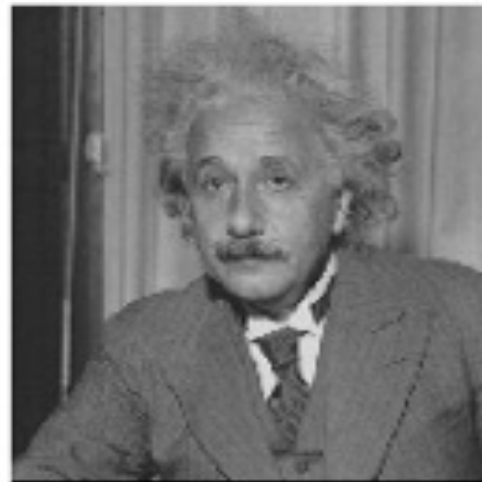
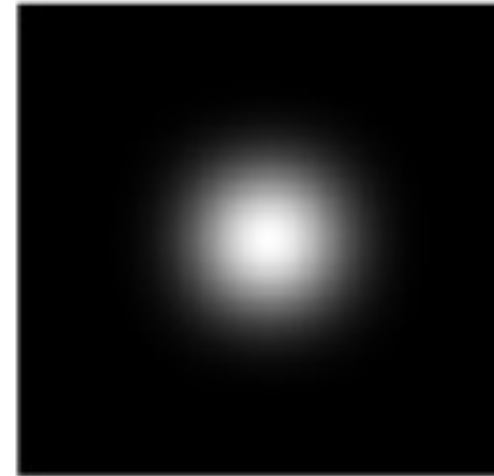
?



More filtering examples



low-pass



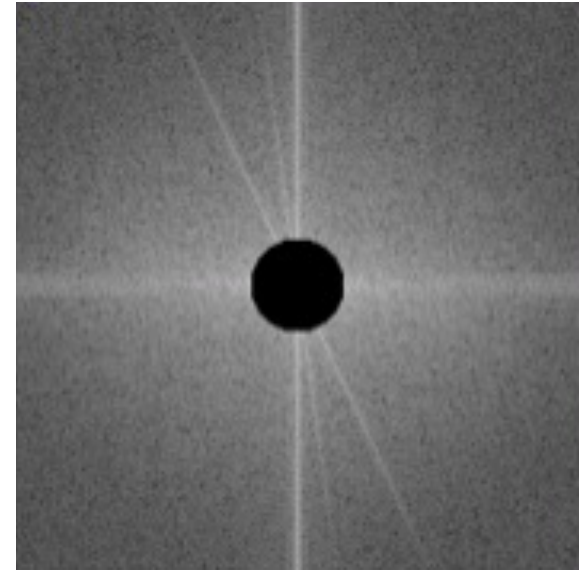
band-pass



filters shown
in frequency-
domain

More filtering examples

high-pass





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