

I)

Show how 32-bit addresses are divided into tag, index, and offset given the following cache descriptions:

- 1) 8KB, byte addressable, 4-way set associative cache with 4 byte blocks
- 2) 16KB, byte addressable, 8-way set associative cache with 2 byte blocks.
- 3) 32 KB fully associative cache with 128 byte blocks

1)

```
addressable (K_byte): 8
way : 4
blocks : 4
line 9      offset 2   tag 21
```

2)

```
addressable (K_byte): 16
way : 8
blocks : 2
line 10     offset 1   tag 21
```

3)

```
addressable (K_byte): 32
blocks : 128
line 8
offset 7
tag 25
```

II)

Consider a 2-way set associative cache with 64 blocks and a block size of 16 bytes. To which set number does byte address 1200 map?

Block address memory = $1200/16 = 75$

Block address cache = $75 \bmod(64) = 11$

III)

4) A computer system uses 16-bit memory addresses. It has a 2K-byte cache organized as a 2-way set-associative cache that uses the LRU replacement algorithm with 64 bytes per cache block. Assume that the size of each memory word is 1 byte.

(a) Calculate the number of bits in each of the Tag, Block, and Word fields of the memory address.

64 bytes = 2(6) bytes = 2(6) words

Word 6

2K-byte = 2(11) bytes

$2(11)/2(6) = 2(5)$

Block 5

$16 - 6 - 5 = 5$

Tag 5

(b) When a program is executed, the processor reads data sequentially from the following word addresses: 128, 144, 2176, 2180, 128, 2176. All the above addresses are shown in decimal values. Assume that the cache is initially empty. For each of the above addresses, indicate whether the cache access will result in a hit or a miss.

$(128)_{10} = (0000000010000000)_2$

Tag = 00000, Block = 00010, Word = 000000 miss

Block1 0010 - 000000

$(144)_{10} = (0000000010010000)_2$

Tag = 00000, Block = 00010, Word = 010000 hit

$(2176)_{10} = (0000100010000000)_2$

Tag = 00001, Block = 00010, Word = 000000 miss

Block2 00001 - 000000

$(2180)_{10} = (0000100010000100)_2$

Tag = 00001, Block = 00010, Word = 000100 hit

$(128)_{10} = (0000000010000000)_2$

Tag = 00000, Block = 00010, Word = 000000 hit

$(2176)_{10} = (0000100010000000)_2$

Tag = 00001, Block = 00010, Word = 000000 hit

