

Direct-mapped cache.

I)

Show how 32-bit addresses are divided into tag, index, and offset given the following cache descriptions:

a) 32KB, byte addressable, 8-way set associative cache with 4 byte blocks

b) 16KB, byte addressable, direct mapped cache with 8 byte blocks

$$16\text{KB} = 2^4 * 2^{10} = 2^{14} \text{ Byte}$$

$$\text{lines} = 2^{14} / 2^3 = 2^{11} \rightarrow 11 \text{ bits}$$

$$\text{offset} = 2^3 \rightarrow 3 \text{ bits}$$

$$\text{tag} = 32 - 11 - 3 = 18 \text{ bits}$$

c) 64KB fully associative cache with 64 byte blocks

$$64\text{KB} = 2^6 * 2^{10} = 2^{16}$$

$$\text{Offset} = 2^6 \rightarrow 6 \text{ bits}$$

$$\text{Tag} = 32 - 6 = 26 \text{ bits}$$

II)

Consider a direct-mapped cache with 64 blocks and a block size of 16 bytes. To what block number does byte address 1200 map? (7 ppt)

1200 byte address

$$\text{Block address memory} = 1200 / 16 = 75$$

$$\text{Block address cache} = 75 \bmod(64) = 11$$

III)

Assume a computer has 32 bit addresses. Each block stores 16 words. A direct-mapped cache has 256 blocks. In which block (line) of the cache would we look for each of the following addresses? Addresses are given in hexadecimal for convenience.

a. 1A2BC012

0001 1010 0010 1011 1100 **0000 0001** 0010

0001 1010 0010 1011 1100 -tag

01 \rightarrow 1 block

0010 \rightarrow word

b. FFFF00FF

1111 1111 1111 1111 0000 **0000 1111** 1111

1111 1111 1111 1111 0000 \rightarrow tag

0F \rightarrow 15 \rightarrow block

1111 \rightarrow word

c. 12345678

0001 0010 0011 0100 0101 **0110 0111** 1000

0001 0010 0011 0100 0101 \rightarrow tag

67--→103→block

1000→word

d. C109D532

1100 0001 0000 1001 1101 **0101 0011** 0010

1100 0001 0000 1001 1101→ teg

53 -→83→block

0010→word

IV)

A computer system uses 16-bit memory addresses. It has a 2K-byte cache organized in a direct-mapped manner with 64 bytes per cache block. Assume that the size of each memory word is 1 byte.

(a) Calculate the number of bits in each of the Tag, Block, and Word fields of the memory address.

Word=(64) $2^6 \rightarrow 6$

2K = $2 * 2^{10} = 2^{11}$ (total size)

Line = $2^{11} / 2^6 = 2^5$

Tag = $16 - 5 - 6 = 5$

(b) When a program is executed, the processor reads data sequentially from the following word addresses: 128, 144, 2176, 2180, 128, 2176. All the above addresses are shown in decimal values. Assume that the cache is initially empty. For each of the above addresses, indicate whether the cache access will result in a hit or a miss.

Address = (128)₁₀ = (00000-tag00010-block 000000-word)₂

Tag field for cache block 00010 is set to 00000

144=0000 0 -tag 000 10-block 01 0000word -hit

2176

Address = (2176)₁₀ = (0000100010000000)₂

Tag = 00001, Block = 00010, Word = 000000

ag field for cache block 00010 is set to 00001-miss

2180

Address = (2176)₁₀ = (0000100010000000)₂

Tag = 00001, Block = 00010, Word = 000000

Tag field for cache block 00010 is set to 00001-hit

Address = (128)₁₀ = (00000-tag00010-block 000000-word)₂

Tag field for cache block 00010 is set to 00000-miss

Tag = 00001, Block = 00010, Word = 000000

ag field for cache block 00010 is set to 00001-miss

$$2/6=0.33$$