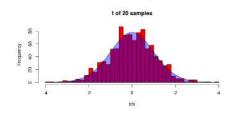


How's the $t$ test work? The central limit theorem.	
In words: The number of $standard\ errors\ that\ the\ sample\ mean\ is\ away\ from\ the\ true\ mean\ has\ a\ t\ distribution.$	
2.4	
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- ullet ... with n-2 degrees of freedom.
- "standard error" =  $s/\sqrt{n}$  = SD of the sample mean



For instance, the probability that the sample mean is within 2 standard errors of the true mean is approximately

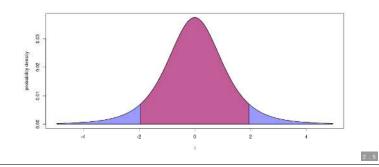
2 . 4

2 . 5

$$\int_{-2}^2 \frac{\Gamma\big(\frac{n-1}{2}\big)}{\sqrt{(n-2)\pi}\Gamma\big(\frac{n-2}{2}\big)} \bigg(1+\frac{x^2}{n-2}\bigg)^{-\frac{n-1}{2}} dx.$$

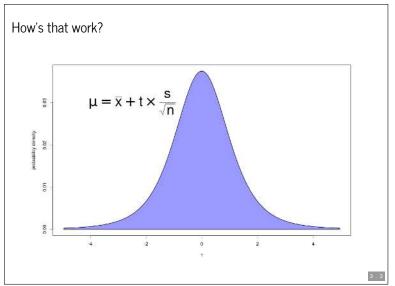
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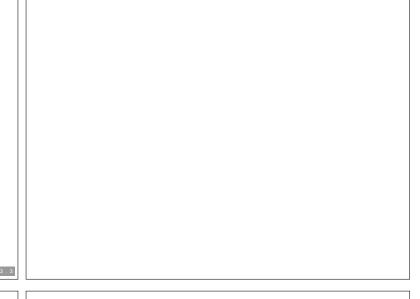
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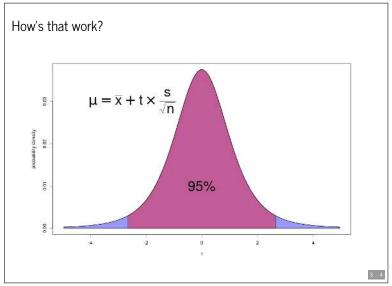


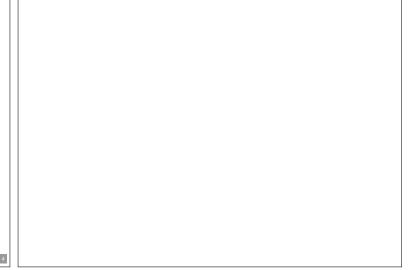
Intuition 1. Simulate a dataset of 20 random draws from a Normal distribution with mean 0, and do a $t$ test of the hypothesis that $\mu=0$ .	
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Intuition  1. Simulate a dataset of 20 random draws from a Normal distribution with mean 0, and do a $t$ test of the hypothesis that $\mu=0$ .  2. Do that 1,000 times, and make a histogram of the resulting $p$ -values. What proportion are less than 0.05?  3. Change mean of the simulated values to 1, and do the same.	

Confidence intervals	
A 95% confidence interval for an estimate is constructed so that no matter what the true values, 95% of the the confidence intervals you construct will overlap the truth.	
1000	
A 95% confidence interval for an estimate is constructed so that no matter what the true values, 95% of the the confidence intervals you construct will overlap the truth. In other words, if we collect 100 independent samples from a population with true mean $\mu$ , and 95% construct confidence intervals for the mean from each, then about 95 of these should overlap $\mu$ .	
3.2	









# Check this.

if we collect 100 independent samples from a population with true mean  $\mu$ , and construct 95% confidence intervals from each, then about 95 of these should overlap  $\mu$ .

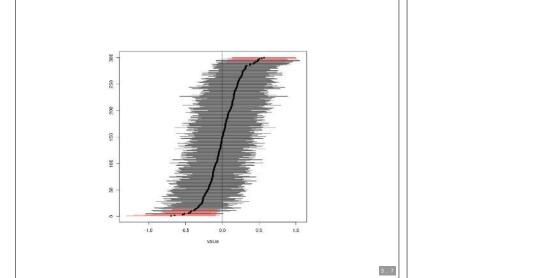
Let's take independent samples of size n=20 from a Normal distribution with  $\mu=0.$  Example:

```
n <- 20; mu <- 0
t.test(rnorm(n, mean=mu))$conf.int
## [1] -0.4019083 0.5862080
## attr(,"conf.level")
## [1] 0.95
```

3 . 5



3 . 8



## What's that 95% mean?

Suppose we survey 100 random UO students and find that 10 had been to a party recently and so get a 95% confidence interval of 4%-16% for the percentage of UO students who have been to a party recently.

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3.8	
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Power analysis	

Statistical power is how good our statistics can find things out.	
42	
Statistical power is how good our statistics can find things out. Formally: the probability of identifying a true effect.	
Statistical power is how good our statistics can find things out.  Formally: the probability of identifying a true effect.  Example: Suppose two snail species' speeds differ by 3cm/h. What's the chance our experiment will identify the difference?	

### A prospective study

Suppose that we're going to do a survey of room prices of an AirBnB competitor. How do our power and accuracy depend on sample size? Supposing that prices roughly match AirBnB's: mean  $\mu=\$120$  and SD  $\sigma=\$98$ , estimate:

- 1. The size of the difference between the mean price of a random sample of size n and the (true) mean price.
- 2. The probability that a sample of size n rooms has a sample mean within \$10 of the (true) mean price.

## Group exercise

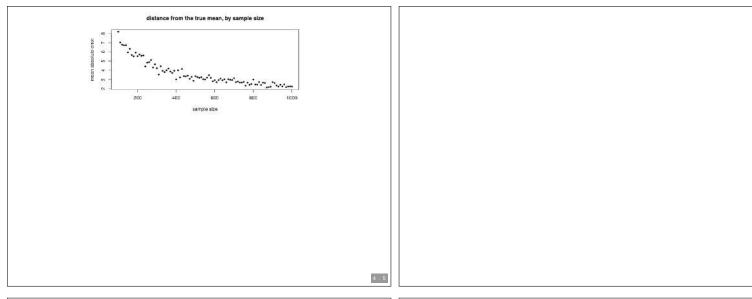
Answer those questions *empirically*: by taking random samples from the price column of the airbnb data, make two plots:

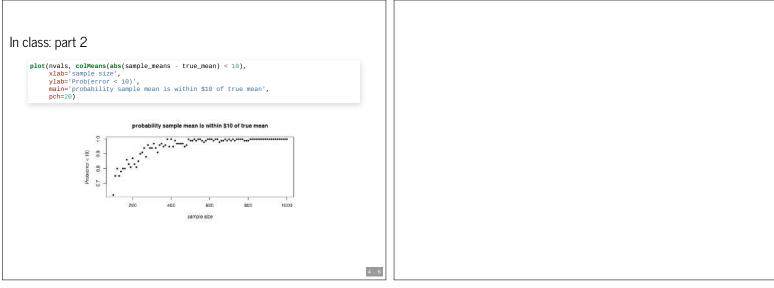
4 . 3

4.4

- 1. Expected difference between the mean price of a random sample of n Portland AirBnB rooms and the (true) mean price of *all* rooms, as a function of n.
- 2. Probability that a sample of size n of Portland AirBnB rooms has a sample mean within \$10 of the (true) mean price of *all* rooms, as a function of n.

#### In class: part 1





/ reveal, is plugins