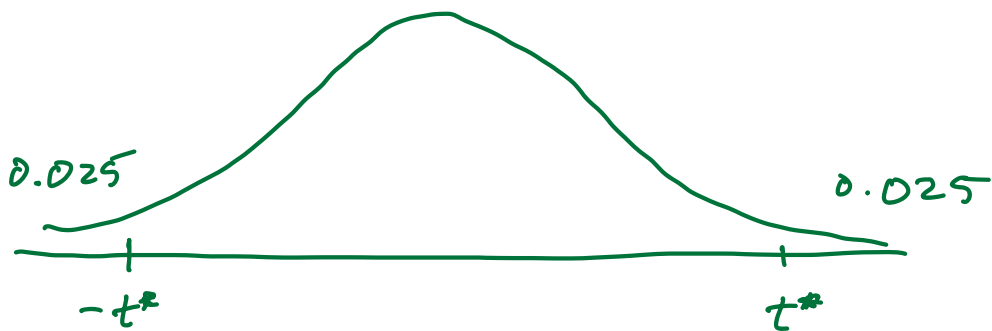


MONDAY OCT 30

- Homework clarifications
- Power
- Multivariate distributions - covariance

Multivariate Normal

Starting Wednesday : OFFICE HRS 12:30 - 1:30 MONDAY
WEDNESDAY
OR BY APT



UNIVARIATE

$$\text{VAR} = E[(x - E x)^2]$$

$$\text{SAMPLE VAR} = \frac{1}{n-1} \sum (x_i - \bar{x})^2$$

$$X = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

$$Y = \begin{bmatrix} y_1 \\ \vdots \\ y_n \end{bmatrix}$$

$$\text{COV}(X, Y) = E[(X - E X)(Y - E Y)]$$

$$\text{SAMPLE COV}(X, Y) = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

$$\underset{k \times 1}{X} = \underset{k \times k}{A} \underset{k \times 1}{Z}$$

$$X_i = \sum_j A_{ij} Z_j$$

$$\begin{aligned} E[X_i] &= \sum_j A_{ij} E[Z_j] \\ &= 0 \end{aligned}$$

$$\text{If } X \text{ is } N(\mu, \Sigma)$$

$\underset{k \times 1}{X} \quad \underset{k \times 1}{\mu}, \quad \underset{k \times k}{\Sigma}$

$$\Sigma_{ij} = \text{cov}(X_i, X_j)$$

$$X = \begin{bmatrix} X_1 \\ X_2 \\ \vdots \\ X_k \end{bmatrix}$$

If Σ is COV MATRIX OF $X = \begin{bmatrix} X_1 \\ \vdots \\ X_k \end{bmatrix}$

$$\underset{n \times 1}{Y} = \underset{n \times k}{A} \underset{k \times 1}{X}$$

$$\underset{n \times n}{\Sigma_Y} = \underset{n \times k}{A} \underset{k \times k}{\Sigma} \underset{k \times n}{A^T}$$