

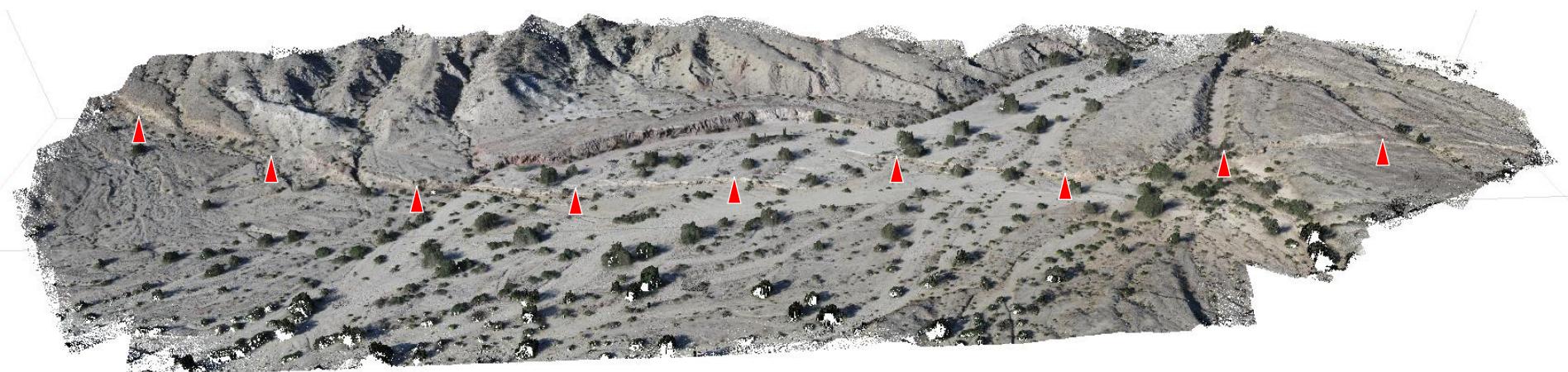
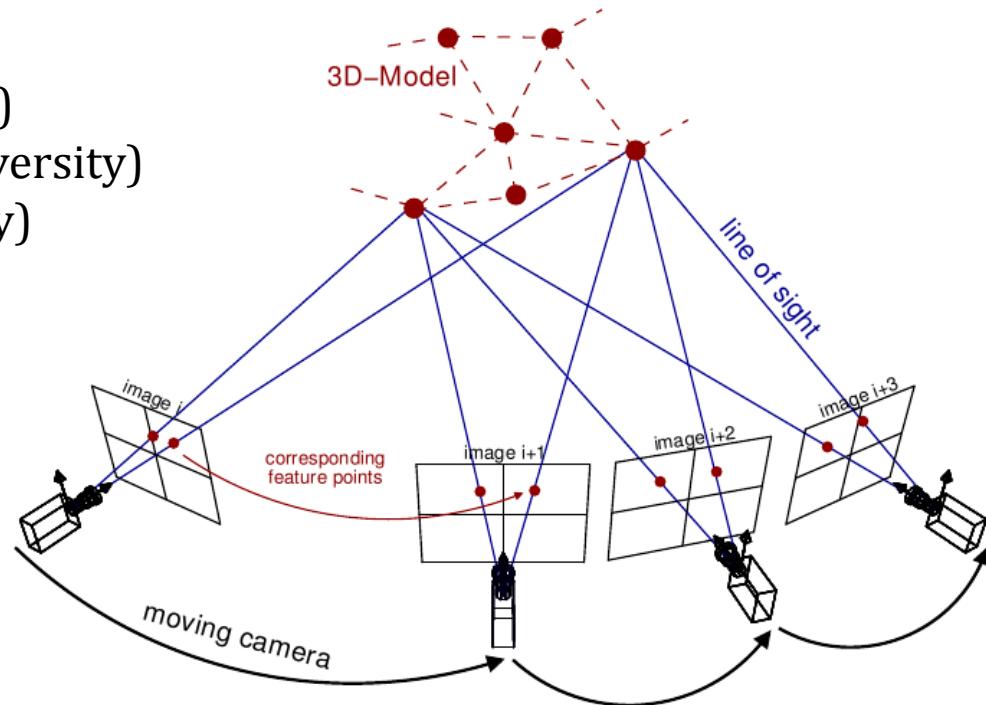
# Introduction to Structure-from-Motion

Edwin Nissen (Colorado School of Mines)

J Ramon Arrowsmith (Arizona State University)

Chris Crosby (UNAVCO/OpenTopography)

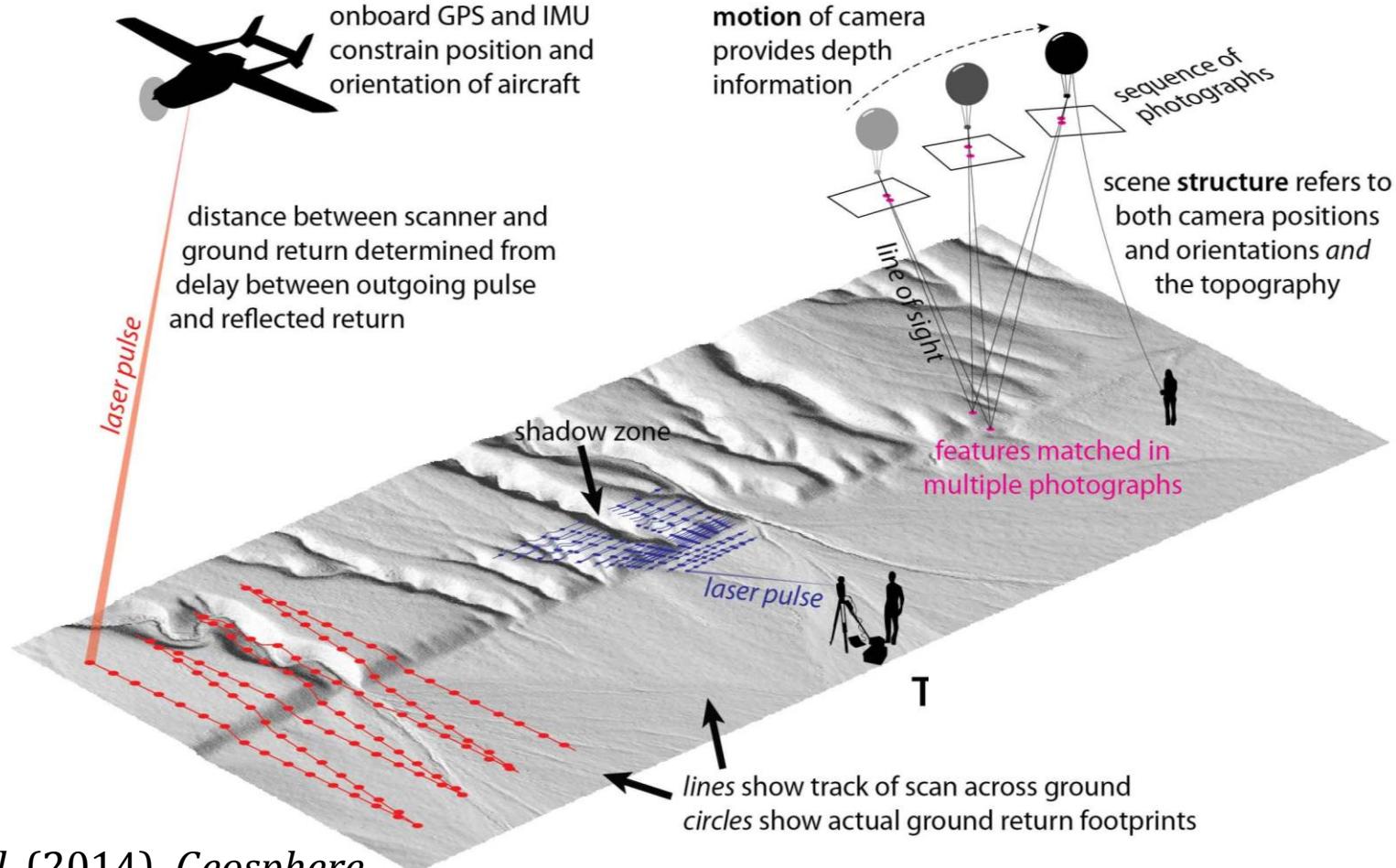
- What is Structure-from-Motion?
- High resolution topography:  
scientific motivations



~500 points/m<sup>2</sup> coloured point cloud along a ~1 km section of the 2010 El Mayor-Cucapah earthquake rupture generated from ~500 photographs captured in 2 hours from a helium blimp

## Lidar (ALS, TLS, MLS)

- Expensive laser equipment required
- Works in densely-vegetated landscapes
- Uses precise time-of-flight measurements but prone to artifacts from GPS and IMU



## Structure-from-Motion

- Requires only a cheap camera
- Coloured points & orthophoto for texture mapping
- Back-solves for camera parameters; warping artifacts are a common problem but easily mitigated

# Where it all started...

## The original idea

*Proc. R. Soc. Lond. B.* **203**, 405–426 (1979)

*Printed in Great Britain*

## The interpretation of structure from motion

BY S. ULLMAN

*Artificial Intelligence Laboratory, Massachusetts Institute of Technology,  
545 Technology Square (Room 808), Cambridge, Massachusetts 02139 U.S.A.*

*(Communicated by S. Brenner, F.R.S. – Received 20 April 1978)*

The interpretation of structure from motion is examined from a computational point of view. The question addressed is how the three dimensional structure and motion of objects can be inferred from the two dimensional transformations of their projected images when no three dimensional information is conveyed by the individual projections.

# Where it all started...

## The algorithm that powers SfM

*Proc. of the International Conference on  
Computer Vision, Corfu (Sept. 1999)*

## Object Recognition from Local Scale-Invariant Features

David G. Lowe

Computer Science Department  
University of British Columbia  
Vancouver, B.C., V6T 1Z4, Canada  
[lowe@cs.ubc.ca](mailto:lowe@cs.ubc.ca)

### Abstract

*An object recognition system has been developed that uses a new class of local image features. The features are invariant to image scaling, translation, and rotation, and partially invariant to illumination changes and affine or 3D projection.*

# Where it all started...

- The **Scale Invariant Feature Transform (SIFT)** (Lowe, 1999) allows corresponding features to be matched even with large variations in scale and viewpoint and under conditions of partial occlusion and changing illumination



# Where it all started...

## First use of the SIFT algorithm to generate large point clouds

Snavely *et al.* (2006). Photo Tourism: Exploring Photo Collections in 3D, *ACM Transactions on Graphics*

Snavely *et al.* (2007). Modeling the World from Internet Photo Collections, *International Journal of Computer Vision*

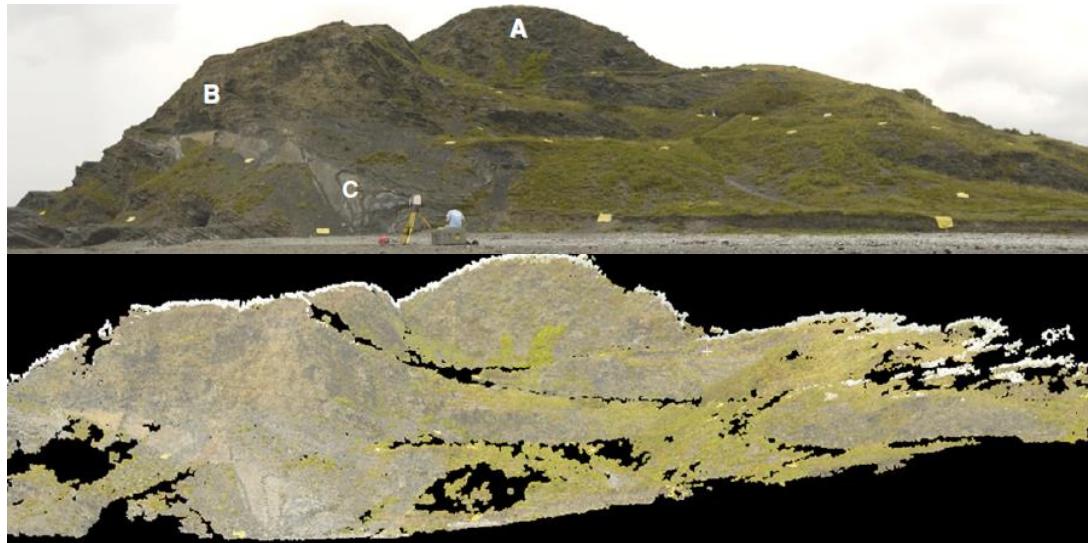


Using photographs from a  
**moving** camera (or cameras)...

... reconstruct the scene **structure** (i.e. the  
geometry of the target *and* the positions,  
orientations & lens parameters of the cameras)

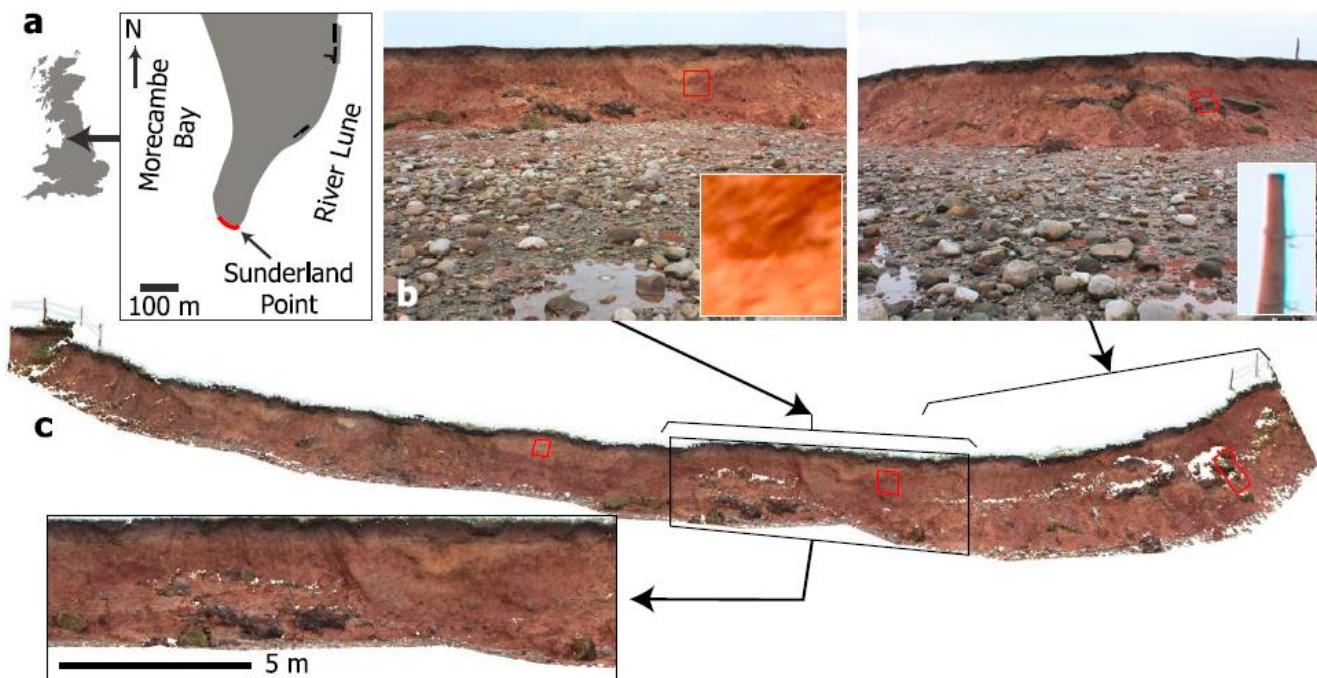
# Where it all started...

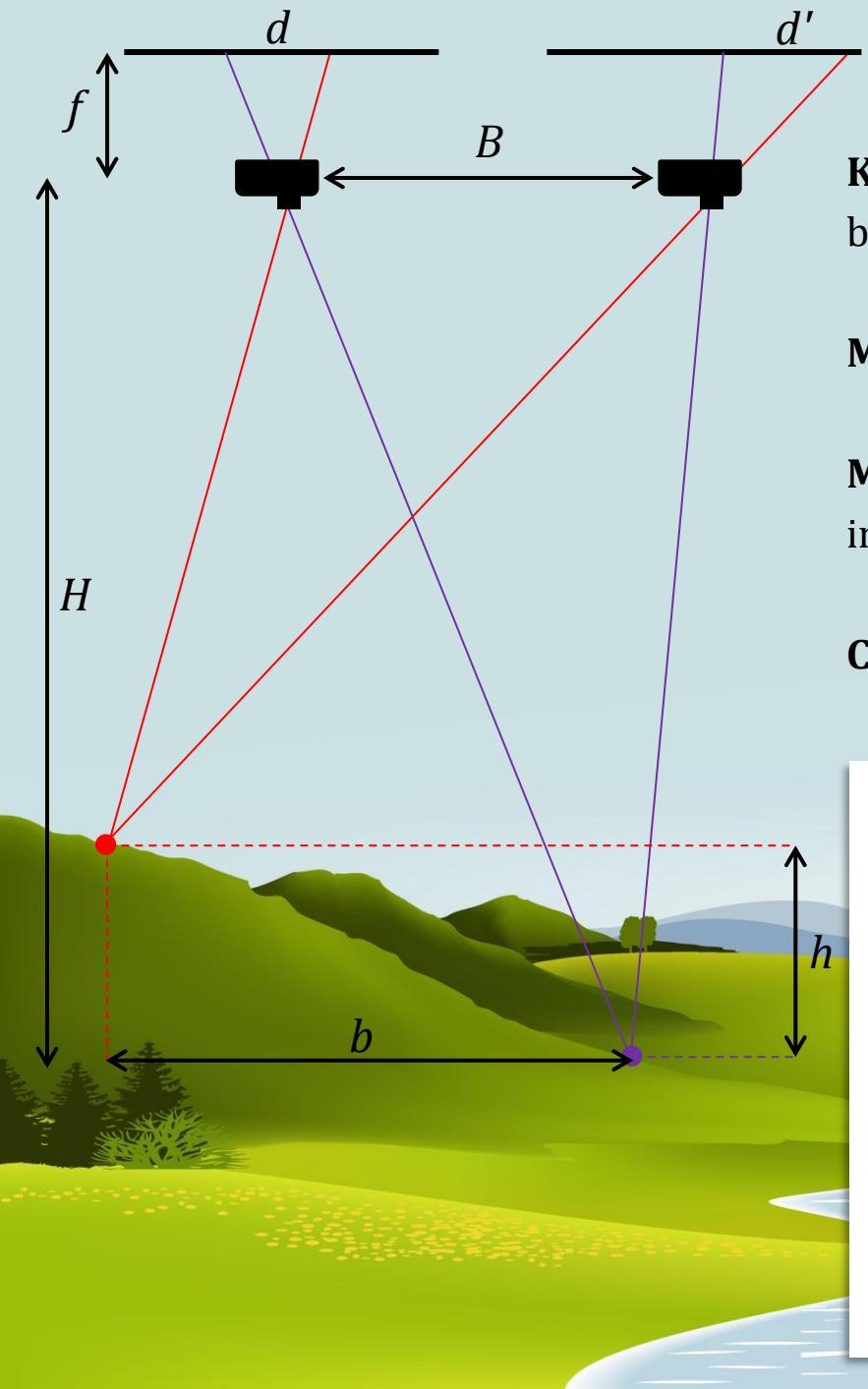
## First geoscience applications



**Left.** Westoby *et al.* (2012). Structure-from-Motion photogrammetry: A low-cost, effective tool for geoscience applications. *Geomorphology*

**Right.** James & Robson (2012). Straightforward reconstruction of 3D surfaces and topography with a camera: Accuracy and geoscience application. *Journal of Geophysical Research*





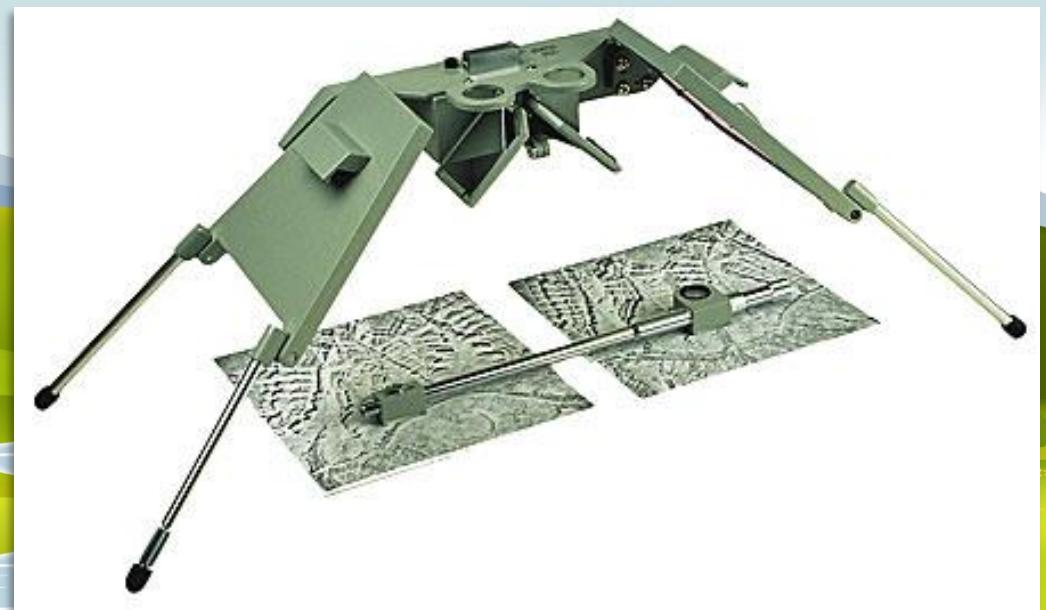
## Traditional stereo-photogrammetry

**Known** camera height  $H$  and focal length  $f$ , and the baseline  $B$  between images

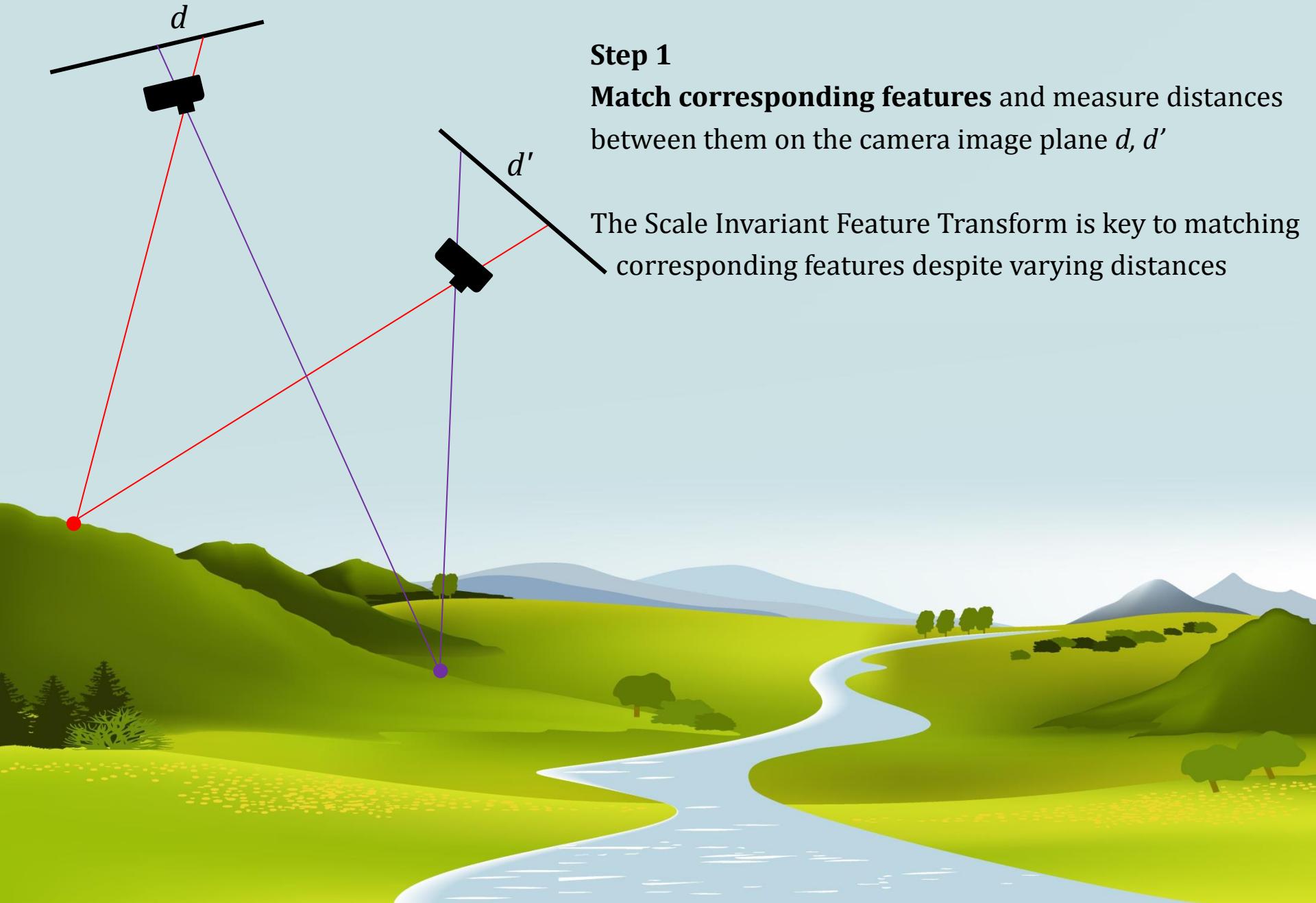
**Match corresponding features**

**Measure** distances between features on the camera image plane  $d, d'$

**Calculate** relative positions of features  $b, h$



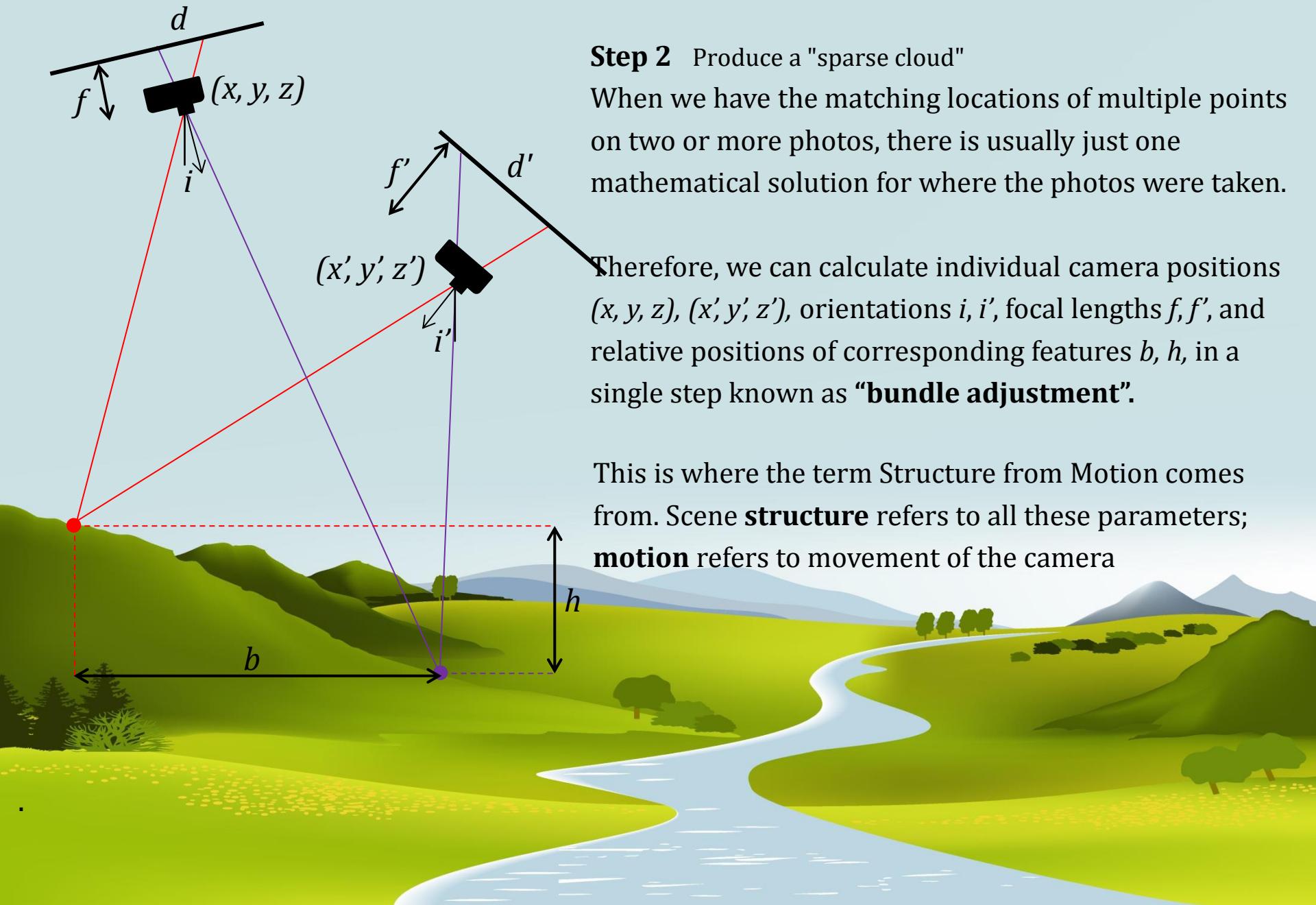
# Structure-from-Motion



- The **Scale Invariant Feature Transform (SIFT)** (Lowe, 1999) allows corresponding features to be matched even with large variations in scale and viewpoint and under conditions of partial occlusion and changing illumination



# Structure-from-Motion



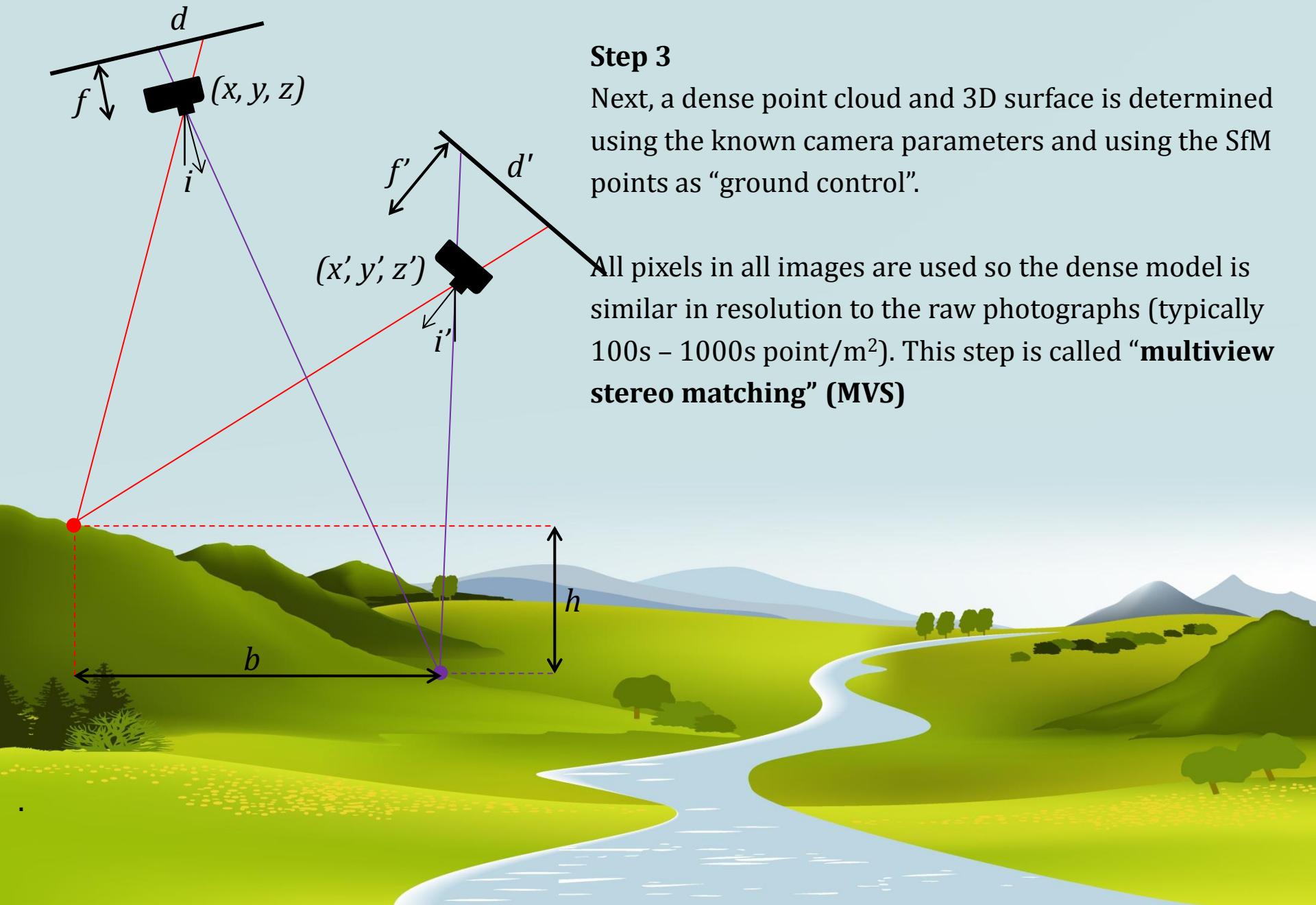
## Step 2 Produce a "sparse cloud"

When we have the matching locations of multiple points on two or more photos, there is usually just one mathematical solution for where the photos were taken.

Therefore, we can calculate individual camera positions  $(x, y, z)$ ,  $(x', y', z')$ , orientations  $i, i'$ , focal lengths  $f, f'$ , and relative positions of corresponding features  $b, h$ , in a single step known as "**bundle adjustment**".

This is where the term Structure from Motion comes from. Scene **structure** refers to all these parameters; **motion** refers to movement of the camera

# Structure-from-Motion

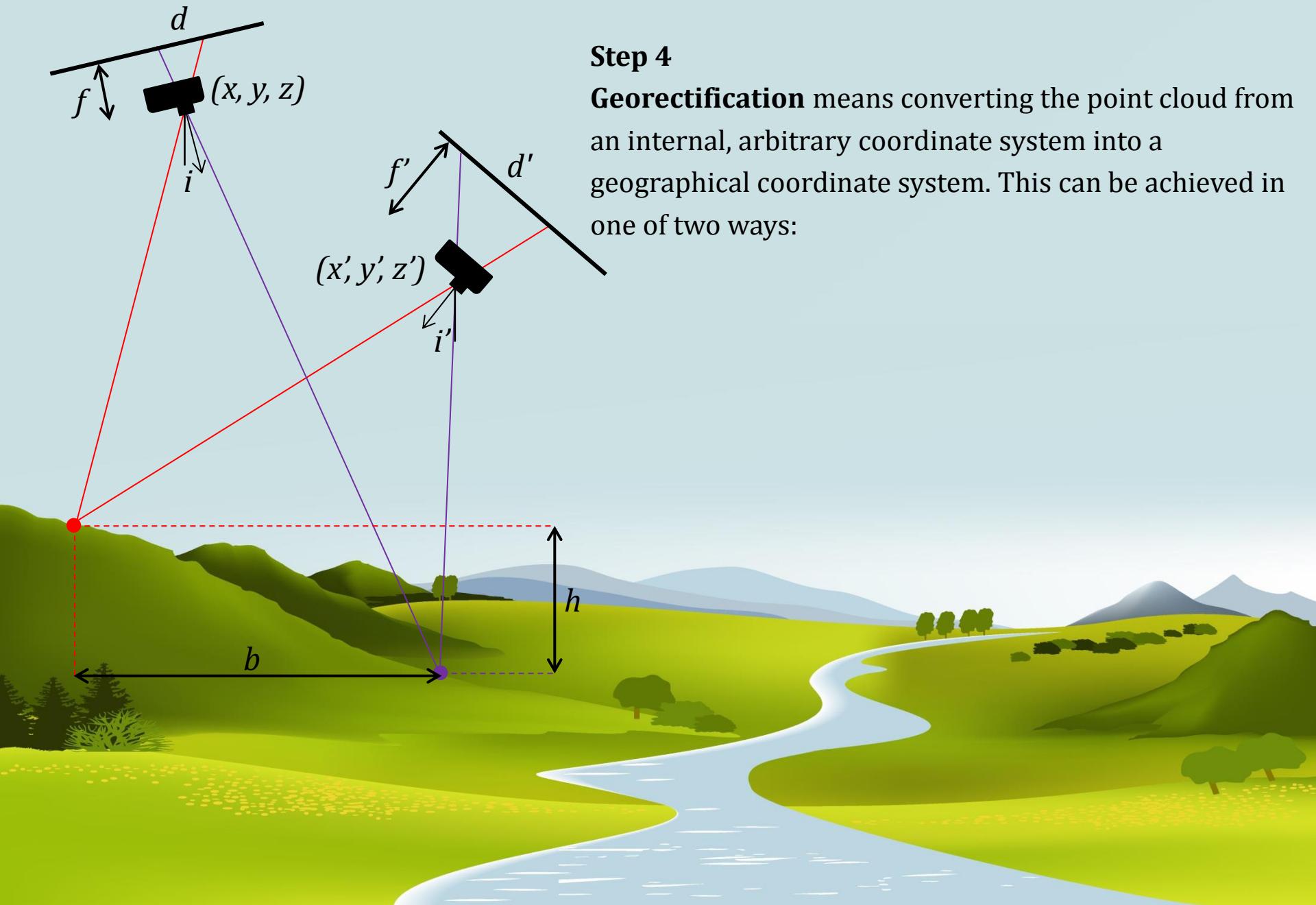


## Step 3

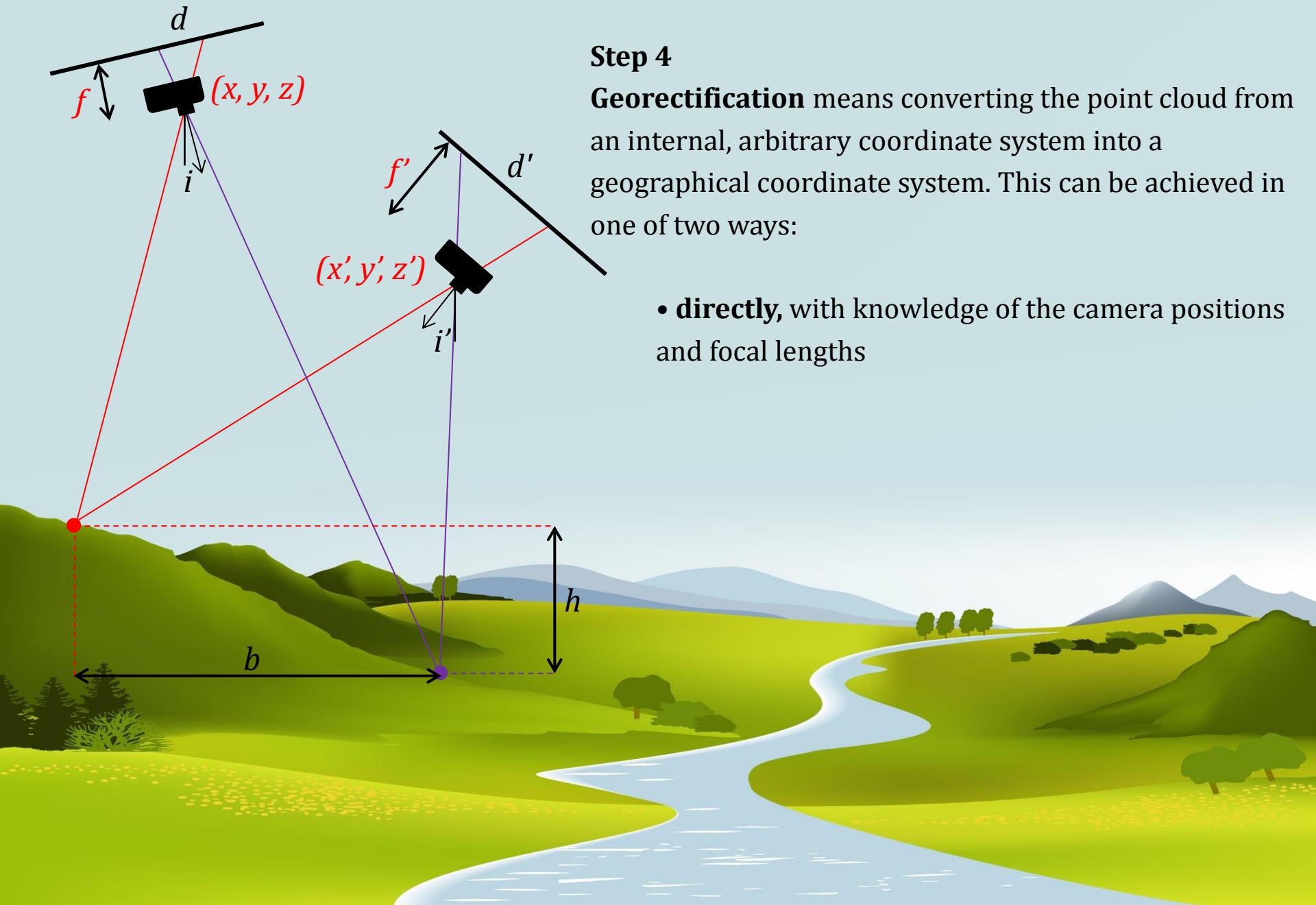
Next, a dense point cloud and 3D surface is determined using the known camera parameters and using the SfM points as “ground control”.

All pixels in all images are used so the dense model is similar in resolution to the raw photographs (typically 100s – 1000s point/m<sup>2</sup>). This step is called “**multiview stereo matching**” (MVS)

# Structure-from-Motion



# Structure-from-Motion

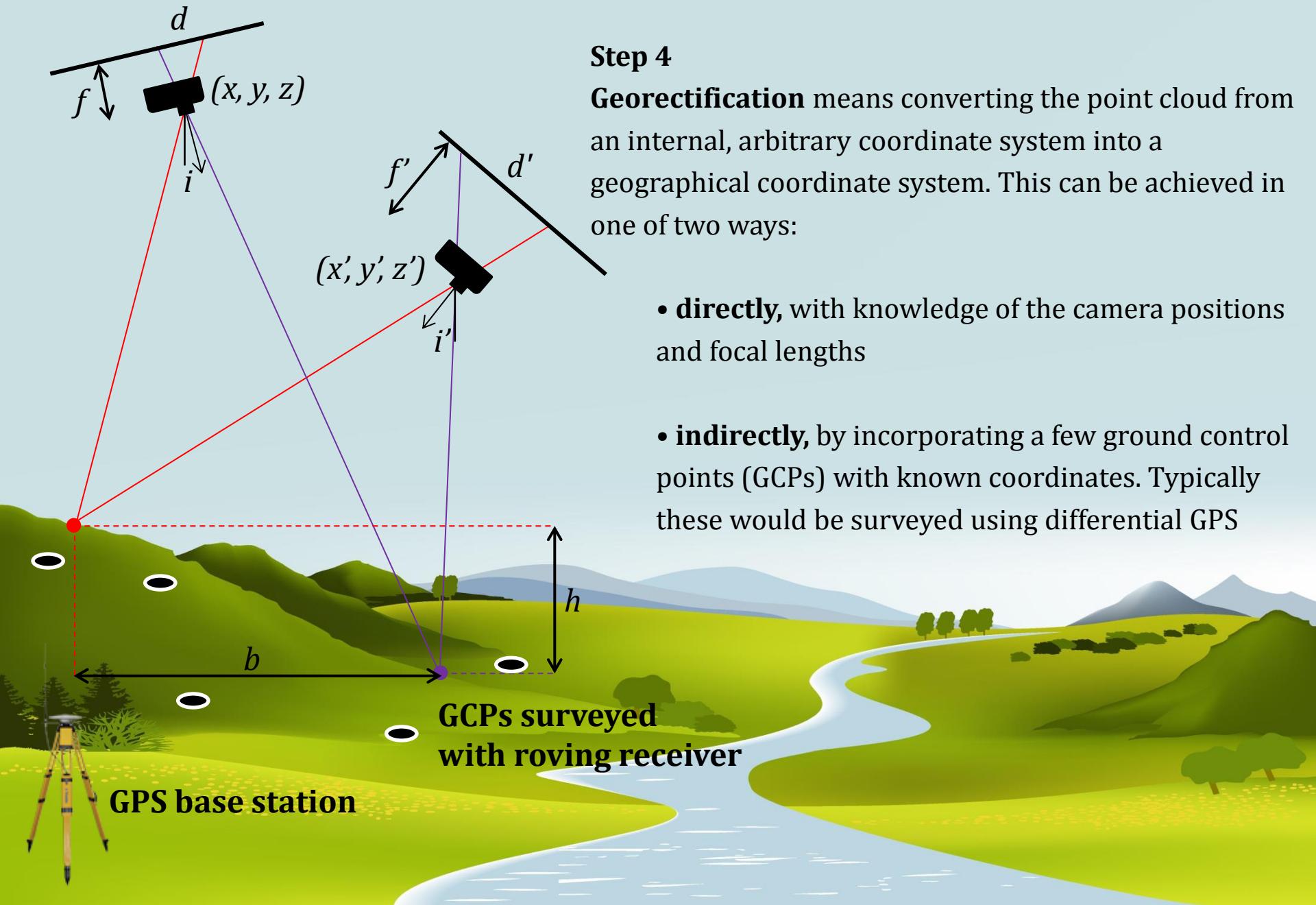


## Step 4

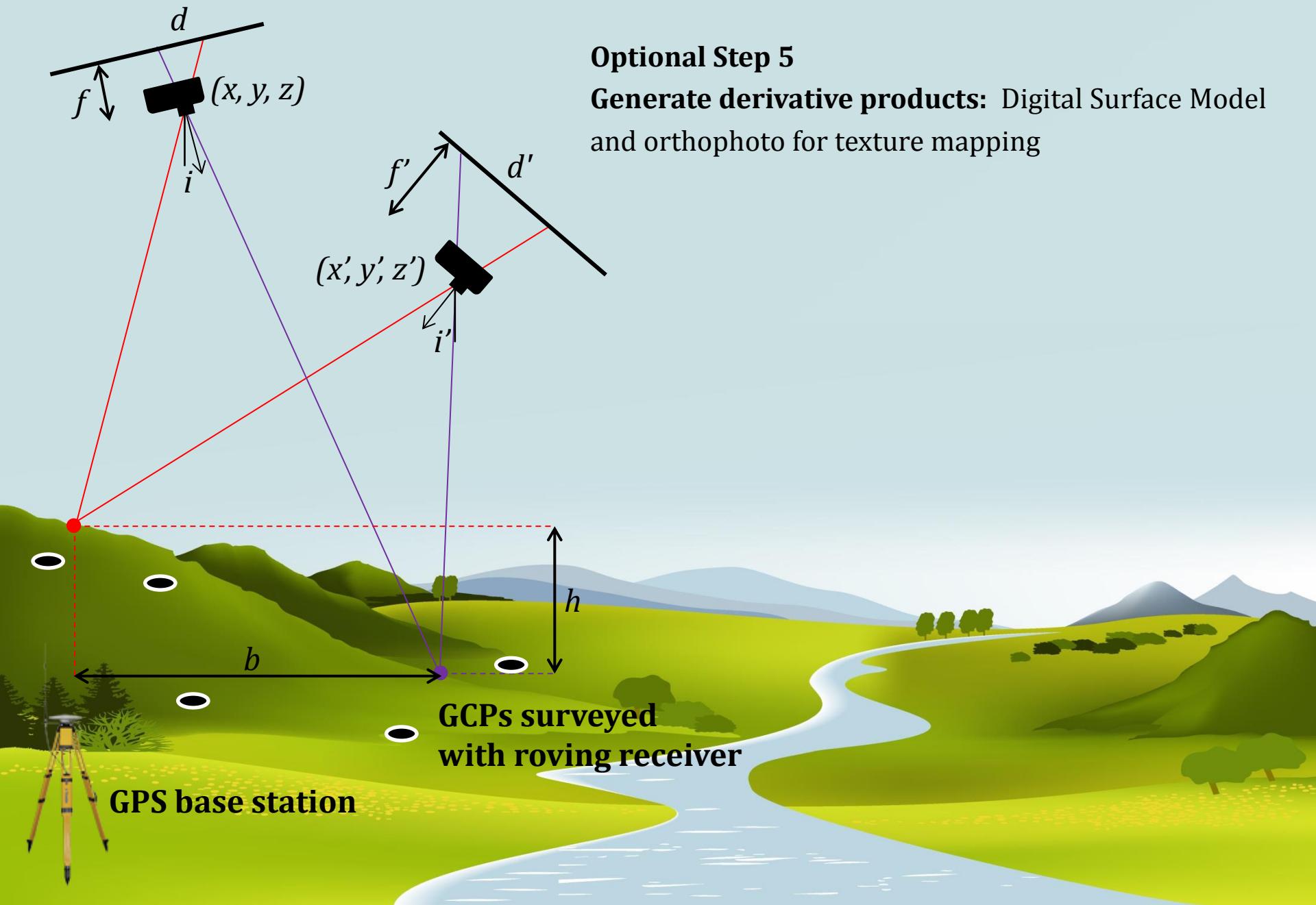
**Georectification** means converting the point cloud from an internal, arbitrary coordinate system into a geographical coordinate system. This can be achieved in one of two ways:

- **directly**, with knowledge of the camera positions and focal lengths

# Structure-from-Motion

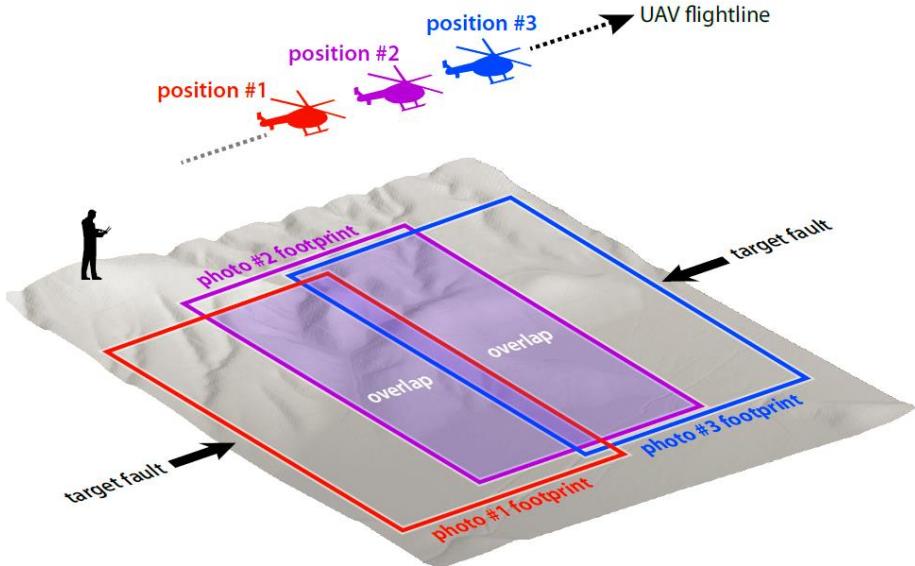


# Structure-from-Motion



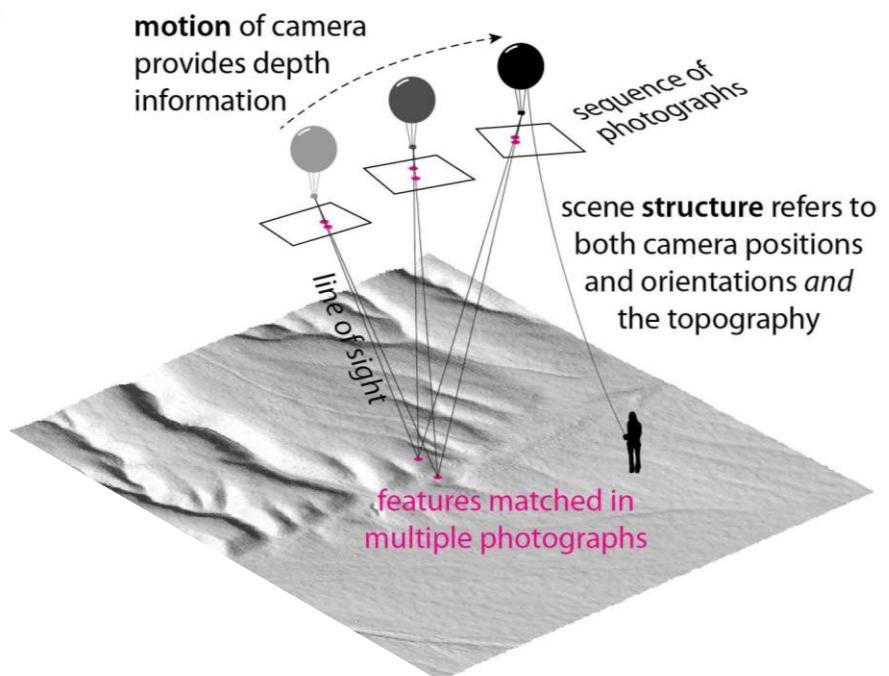
## Traditional stereo-photogrammetry

- Requires a stable platform such as a satellite or aeroplane at a fixed elevation
- Photographs collected at known positions with fixed orientations and incidence angles



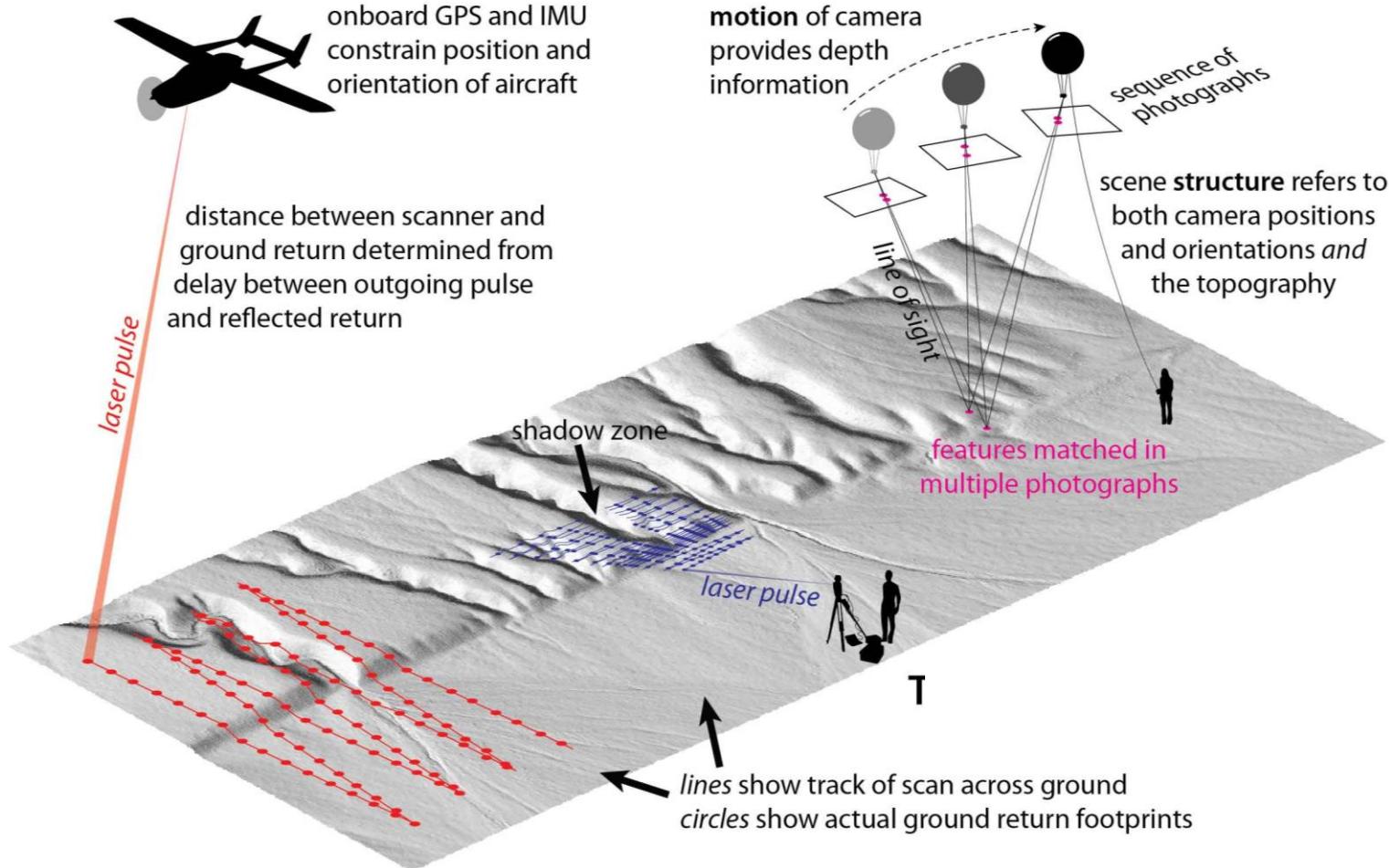
## Structure-from-Motion

- Photos from many angles and distances can be used, with no *a priori* knowledge of locations or pose
- Enables “unstructured” image acquisition from the ground, legacy air-photosets, or unmanned platforms



## Lidar (ALS, TLS, MLS)

- Expensive laser equipment required
- Works in densely-vegetated landscapes
- Uses precise time-of-flight measurements but prone to artifacts from GPS and IMU



## Structure-from-Motion

- Requires only a cheap camera
- Coloured points & orthophoto for texture mapping
- Back-solves for camera parameters; warping artifacts are a common problem but easily mitigated

# SfM & MVS software

**Table 1**  
Examples of open source and commercial software for photo-based 3d reconstruction.

Software	Url (valid on 17 May, 2014)	Notes
<i>Freely available</i>		
Bundler Photogrammetry Package <sup>a,b</sup>	<a href="http://blog.neonascent.net/archives/bundler-photogrammetry-package/">http://blog.neonascent.net/archives/bundler-photogrammetry-package/</a>	Used in <a href="#">James and Robson (2012)</a> . Script-based, no graphical user interface (GUI). Windows OS only.
SFMT toolkit <sup>a,b</sup>	<a href="http://www.visual-experiments.com/demos/sfmtoolkit/">http://www.visual-experiments.com/demos/sfmtoolkit/</a>	Similar software to above.
Python Photogrammetry Toolbox (PPT) <sup>a,b</sup>	<a href="http://code.google.com/p/osm-bundler/">http://code.google.com/p/osm-bundler/</a>	Formerly OSM-bundler. Python-driven GUI and scripts, with a Linux distribution.
VisualSfM <sup>b</sup>	<a href="http://www.cs.washington.edu/homes/ccwu/vsfm/">http://www.cs.washington.edu/homes/ccwu/vsfm/</a>	Advanced GUI with Windows, Linux and Mac. OSX versions. Georeferencing options, but camera model is more restricted than that used in Bundler.
3DF Samantha	<a href="http://www.3dflow.net/technology/samantha-structure-from-motion/">http://www.3dflow.net/technology/samantha-structure-from-motion/</a>	SfM only, but with more advanced camera models than all above ( <a href="#">Farenzena et al., 2009</a> ). Provides output compatible with several dense matching algorithms.
http://opendronemap.org/		
<i>Web sites and services</i>		
Photosynth	<a href="http://photosynth.net/">http://photosynth.net/</a>	Evolved from Bundler. SfM only, no dense reconstruction. Can incorporate a very wide variety of images, but does so at the cost of reconstruction accuracy.
Arc3D	<a href="http://www.arc3d.be/">http://www.arc3d.be/</a>	Vergauwen and Van Gool [2006]
CMP SfM Web service <sup>a</sup>	<a href="http://ptak.felk.cvut.cz/sfmservice/">http://ptak.felk.cvut.cz/sfmservice/</a>	
Autodesk 123D Catch	<a href="http://www.123dapp.com/catch/">http://www.123dapp.com/catch/</a>	Also available as standalone software.
Pix4D	<a href="http://pix4d.com/">http://pix4d.com/</a>	
My3DScanner	<a href="http://www.my3dscanner.com/">http://www.my3dscanner.com/</a>	
<i>Commercial</i>		
PhotoScan	<a href="http://www.agisoft.ru/products/photoscan/">http://www.agisoft.ru/products/photoscan/</a>	Full SfM-MVS-based commercial package.
Acute3D	<a href="http://www.acute3d.com/">http://www.acute3d.com/</a>	
PhotoModeler	<a href="http://www.photomodeler.com/">http://www.photomodeler.com/</a>	Software, originally based on close-range photogrammetry, now also implements SfM.
3DF Zephyr Pro	<a href="http://www.3dflow.net/">http://www.3dflow.net/</a>	Underlying SfM engine is 3DF Samantha

Note: Table modified from <http://www.lancaster.ac.uk/staff/jamesm/research/sfm.htm>.

SfM = Structure from Motion; MVS = Multi-View Stereo.

<sup>a</sup> Uses Bundler (<http://phototour.cs.washington.edu/bundler/>) to compute structure from motion.

<sup>b</sup> Uses PMVS2 (<http://grail.cs.washington.edu/software/pmvs/>) as a dense multi-view matcher.

Bemis *et al.* (2014). Ground-based and UAV-Based photogrammetry: A multi-scale, high resolution mapping tool for structural geology and paleoseismology. *Journal of Structural Geology*

# SfM from Unmanned Aerial Vehicles (UAV)



DJI Phantom 2 quadcopter (~\$1k)



Custom built helicopter (~\$15k)



Autokite (~\$1k, discontinued)



Falcon Unmanned fixed wing (~\$12k)

## SfM from helicopters and multi-rotor UAVs



DJI Phantom 2 quadcopter (~\$1k)



Custom built helicopter (~\$15k)

**Pros** Robust in high wind and can take off and land anywhere. Larger helicopters can carry large SLR camera. Smaller multi-rotors cannot, but are easier to fly.

**Cons** Helicopter needs trained pilot to take-off and land and regular refuelling. Initial costs are high and requires careful maintenance.

Regulations may need to be followed (FAA in the U.S.)

# SfM from fixed wing UAVs

**Pros** Relatively easy to pilot. Can cope in moderate winds. Flight durations are normally longer than copters.

**Cons** Susceptible to damage during landing.

Regulations may need to be followed (FAA in the U.S.)



Autokite (~\$1k, discontinued)

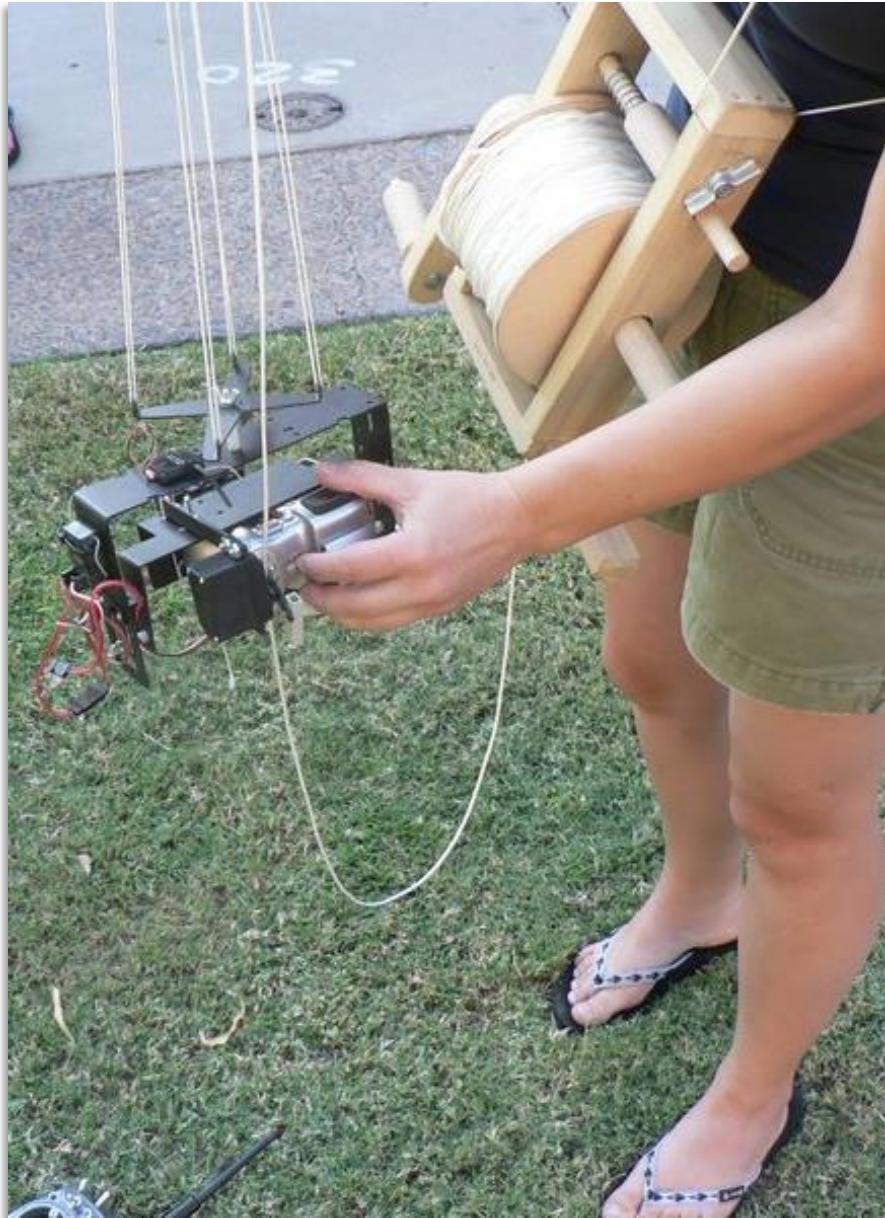


Falcon Unmanned fixed wing (~\$12k)

# SfM from Unmanned Aerial Systems (UAS)



# SfM from Unmanned Aerial Systems (UAS)



**Pros** Easy to drag across target area. Once in the air can remain there. Can carry large SLR cameras. No FAA regulations!

**Cons** Requires helium, which can be expensive (>\$100 per canister), and fiddly picavet. Cannot be automated. Difficult to deploy in windy conditions.

# SfM from Unmanned Aerial Systems (UAS)



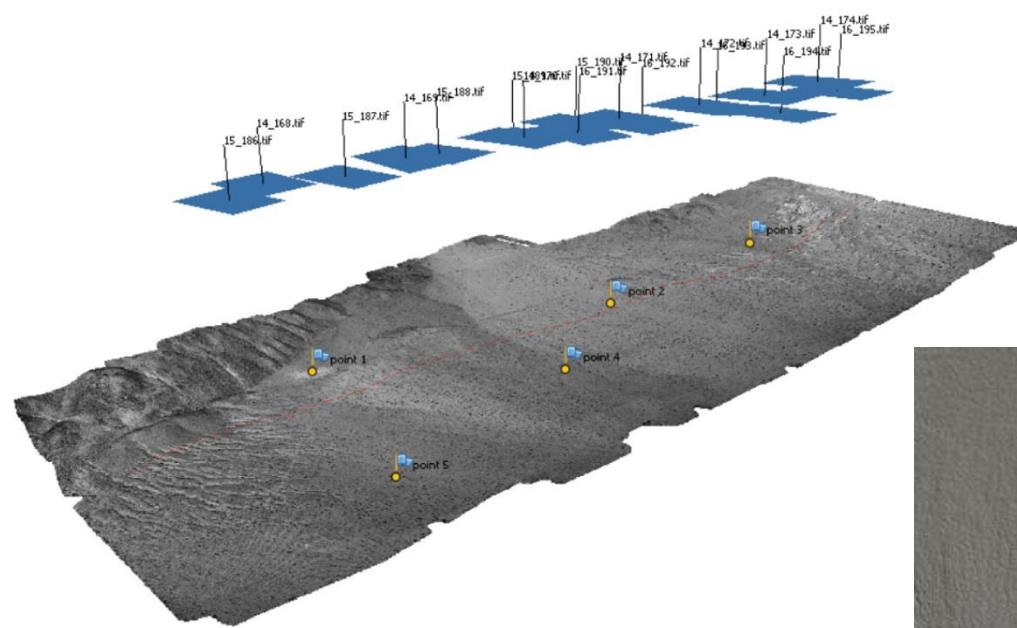
**Pros** Easy to drag across target area. Once in the air can remain there. Robust in high wind. No FAA regulations!

**Cons** Requires helium, which can be expensive (>\$100 per canister). Cannot be automated. Carries small cameras.



# SfM from airplane photos

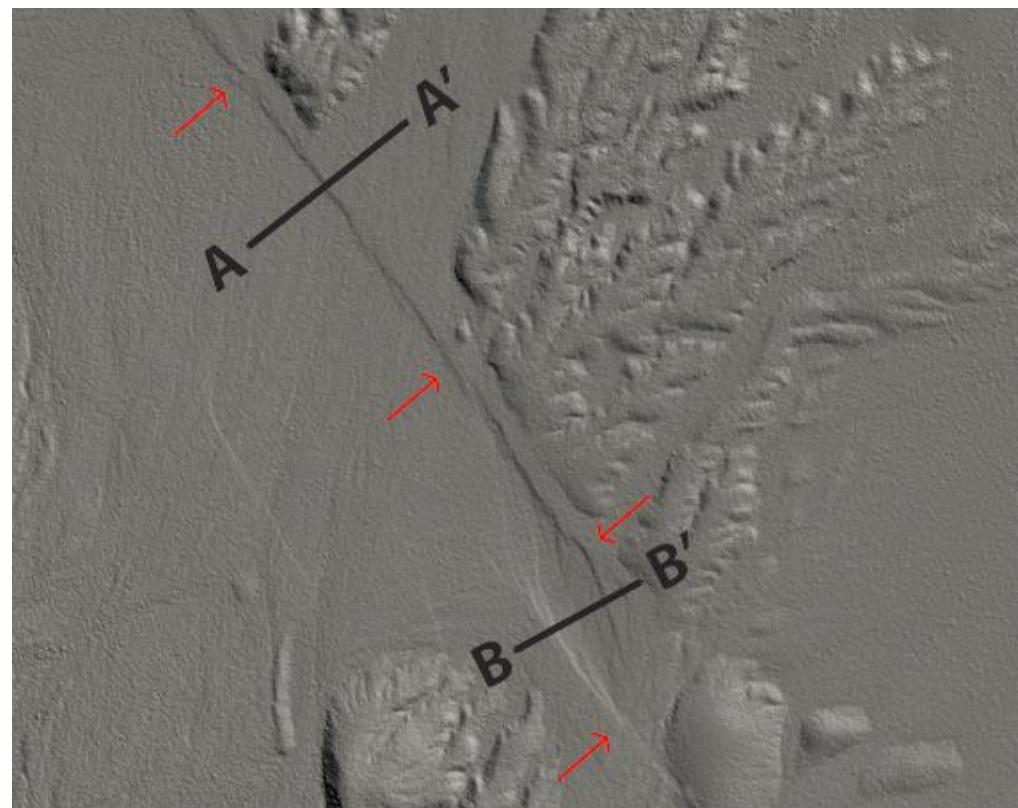
- “Historical topography” and “diachronic geomorphology” possible using legacy air-photos. Requires sufficient photo overlap and georeferencing is a challenge.



**(Left)** A short section of the ~85 km-long USGS aerial survey of the 1992 Landers rupture, California.

**(Right)** Resulting 30 cm-resolution DEM, hillshaded to highlight fine geomorphic features.

Georeferencing was undertaken using modern satellite imagery

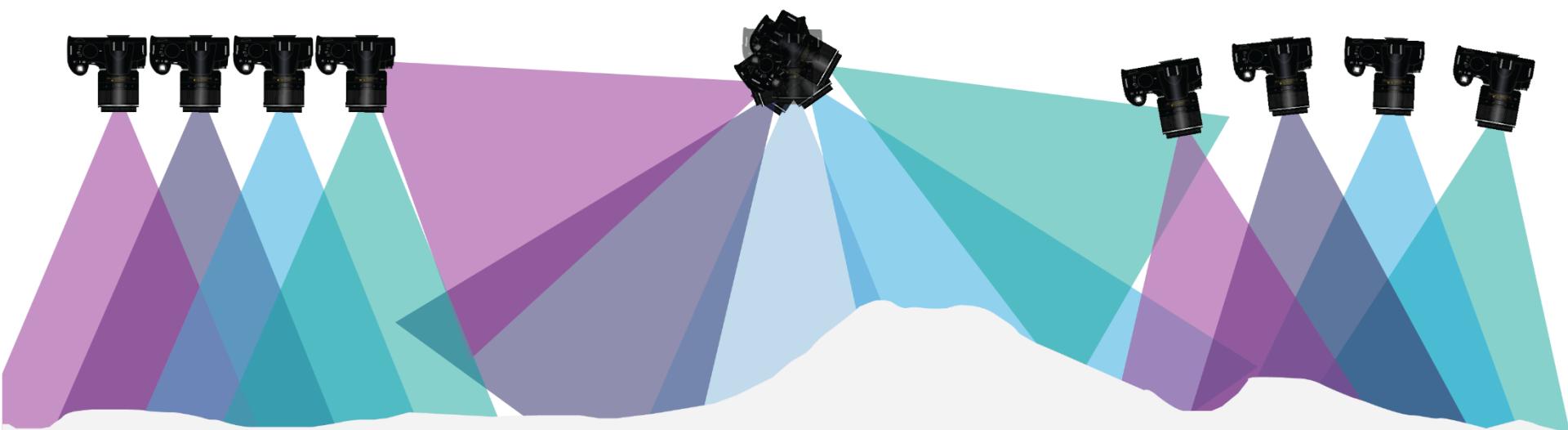


# Acquisition geometry

Nadir

Divergent

Convergent



# Acquisition geometry

Convergent with a range of distances



# Choice of camera



- Most cameras work
- DEM/orthophoto resolution is governed by the ground pixel resolution of the raw photos, so high megapixel cameras are preferable
- Better lenses of SLR cameras mean fewer radial distortions...
- but radial artefacts arising from cheap camera lenses can be mitigated by deploying ground control points
- fish-eye lenses (e.g. GoPro) give rise to largest distortions, but latest software seems to cope
- **time lapse setting** is essential if camera is deployed from drone
- internal or external **GPS tagging** is another useful function, as it enables rough geo-referencing without ground control points

# Camera lens distortions

$f$  = focal length

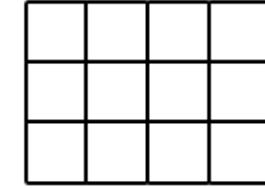
$k_n$  =  $n^{\text{th}}$  radial distortion coefficient

$c_x$  = principal point x coordinate

$p_n$  =  $n^{\text{th}}$  tangential distortion coefficient

$c_y$  = principal point y coordinate

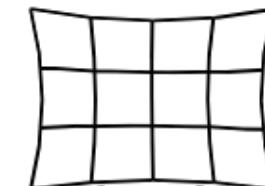
skew coefficient between the x and the y axis.



**No Distortion**



**Barrel Distortion**

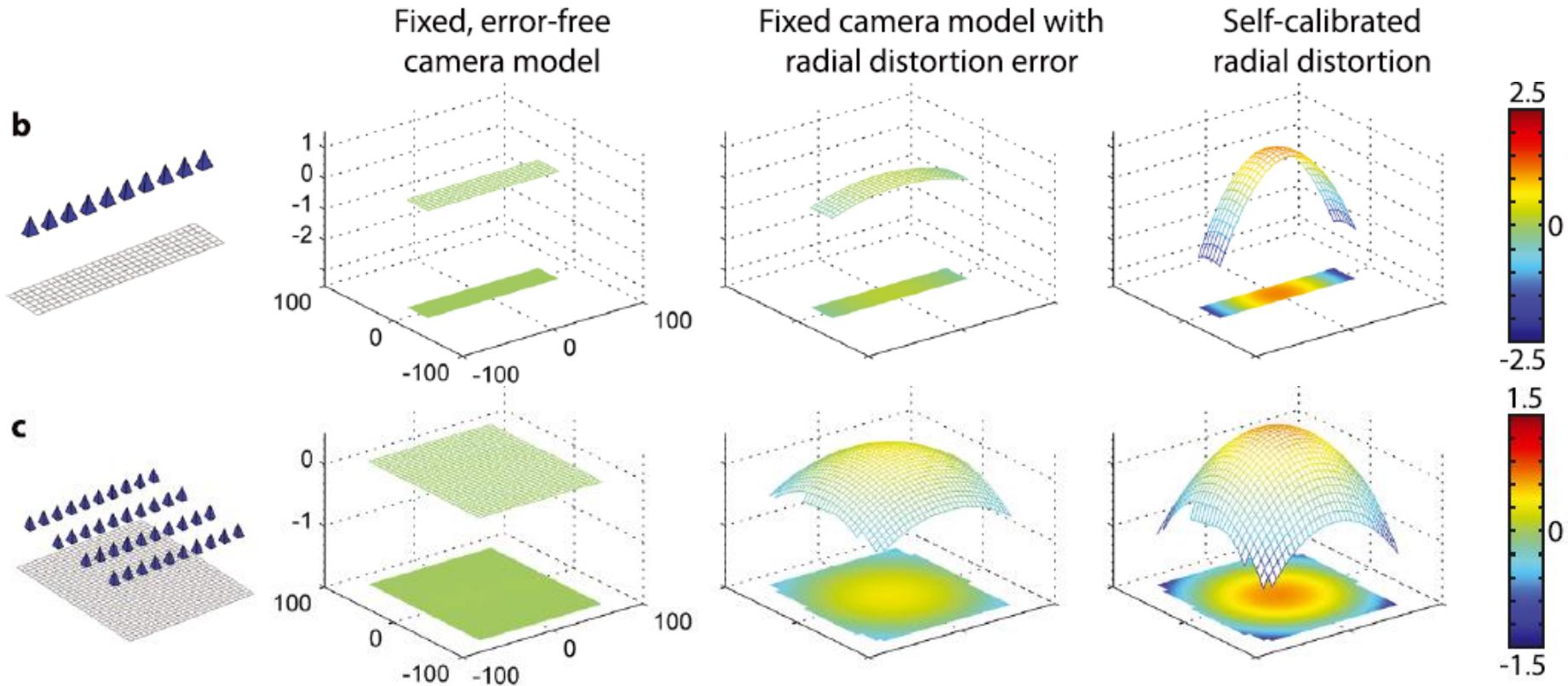


**Pincushion Distortion**

$k_1 < 1$

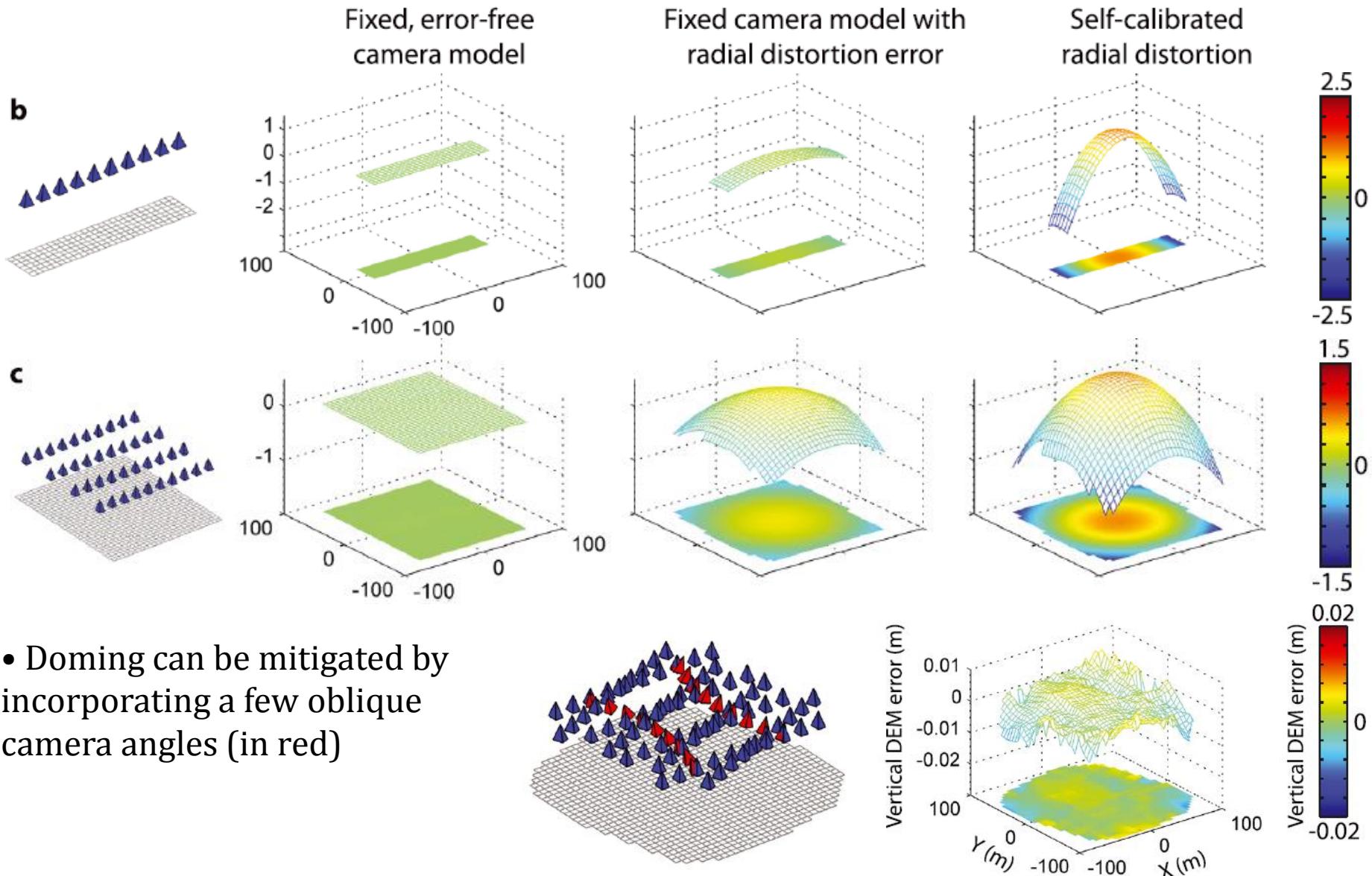
$k_1 > 1$

# Camera lens distortions



- A trade-off between lens radial distortion term and computed surface form can lead to “doming”

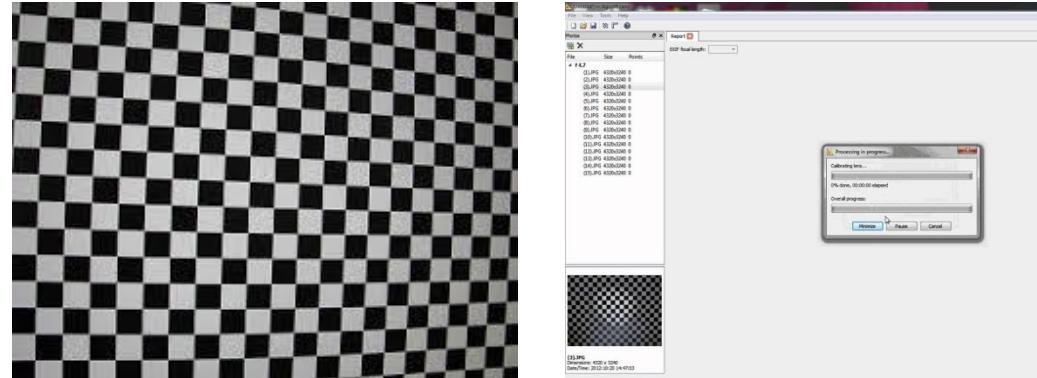
# Camera lens distortions



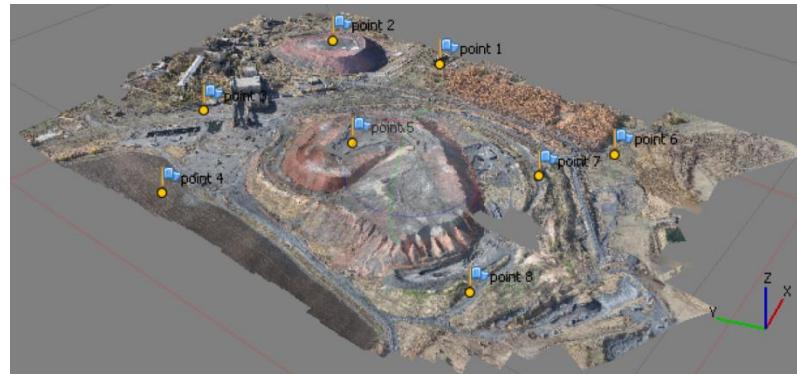
James & Robson (2014), Mitigating systematic error in topographic models derived from UAV and ground-based image networks, *Earth Surface Processes and Landforms*

# Camera lens distortions

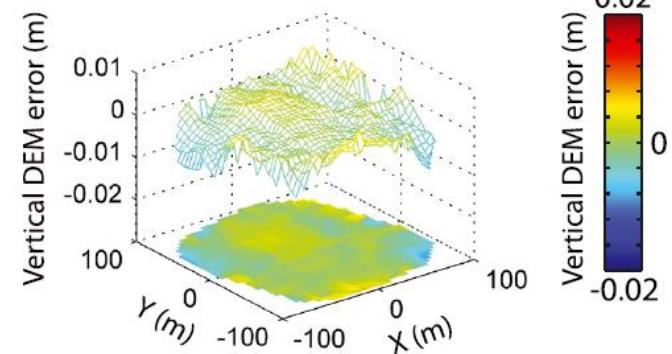
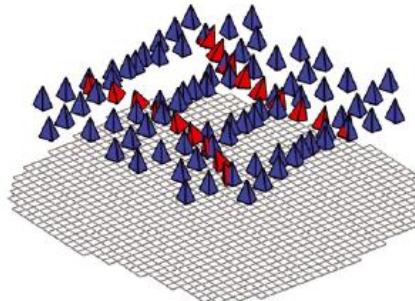
- Doming can be mitigated by calibrating the camera parameters by photographing a calibration target



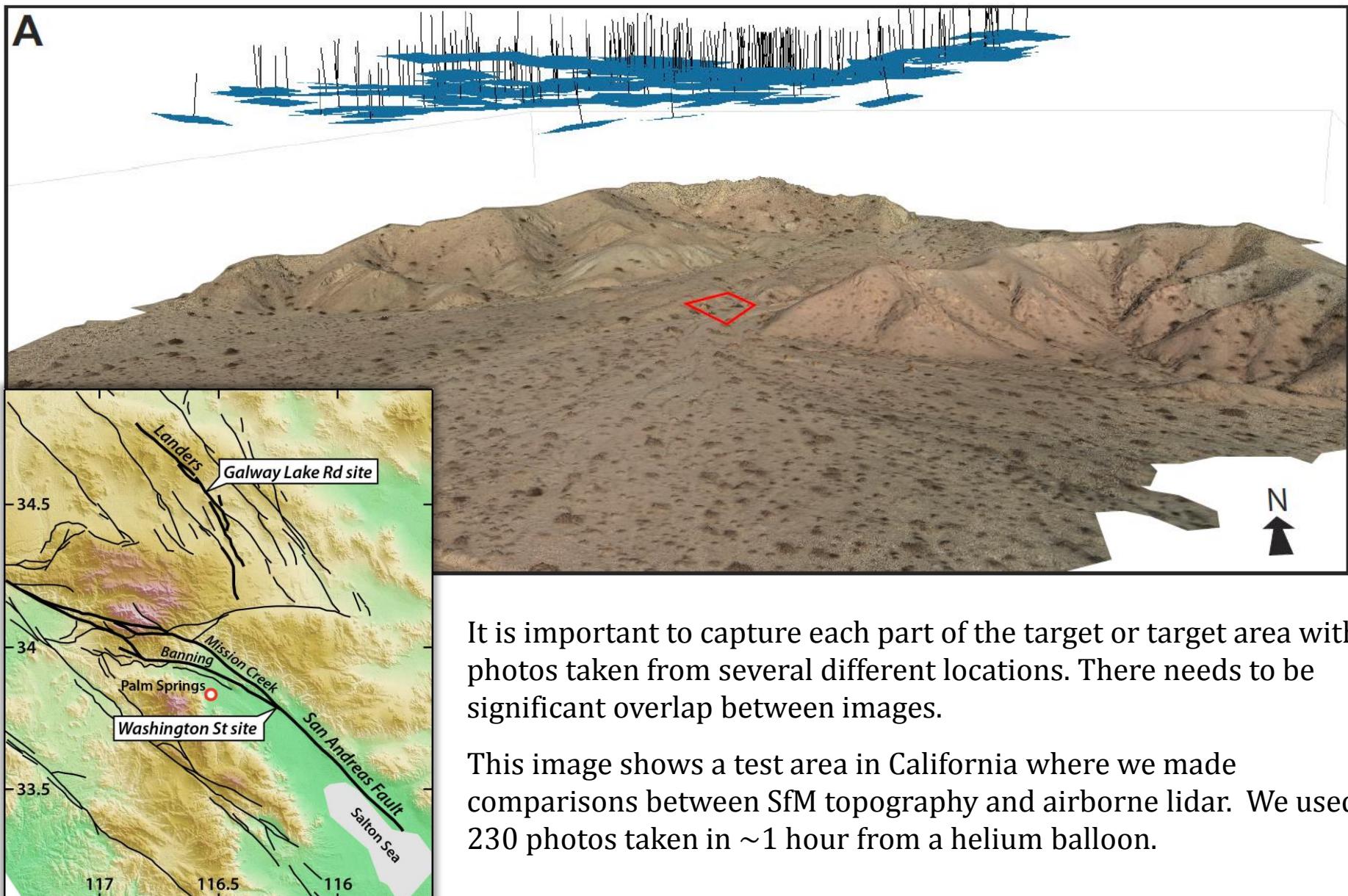
- Doming can be mitigated by georeferencing using ground control points



- Doming can be mitigated by incorporating a few oblique camera angles (in red)



# Resolution and precision of SfM topography



# Resolution and precision of SfM topography

Orthophoto

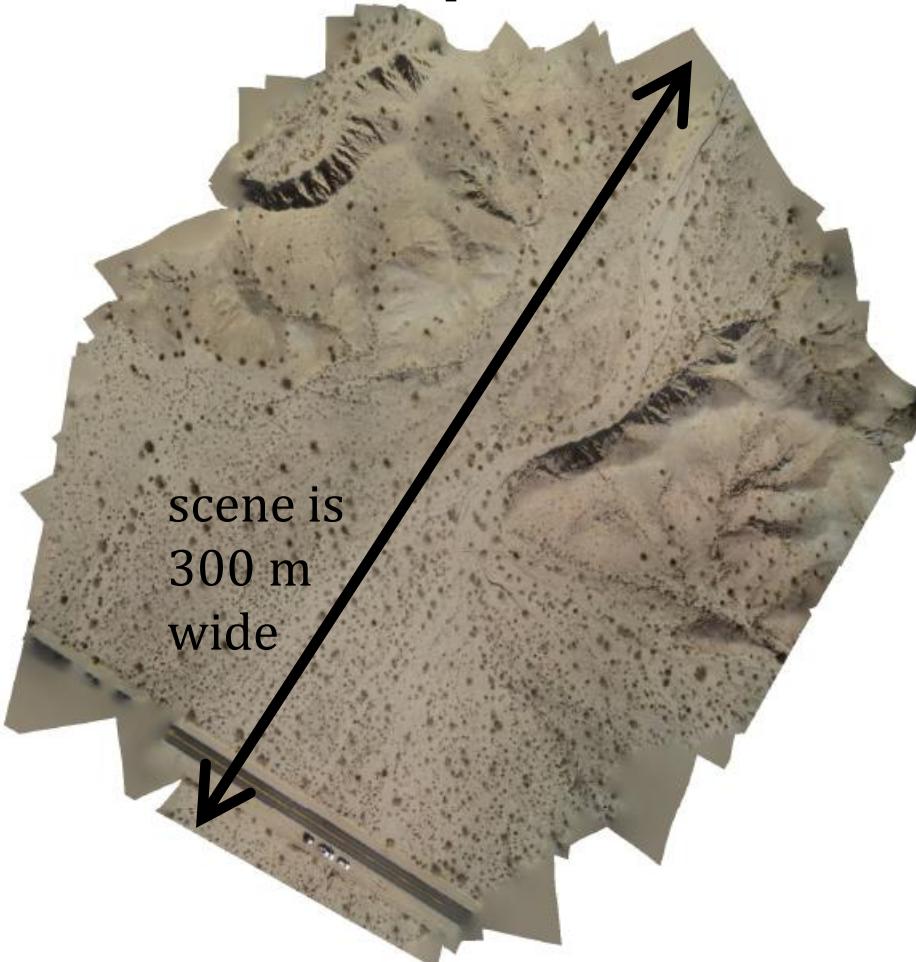


Photo coverage plot

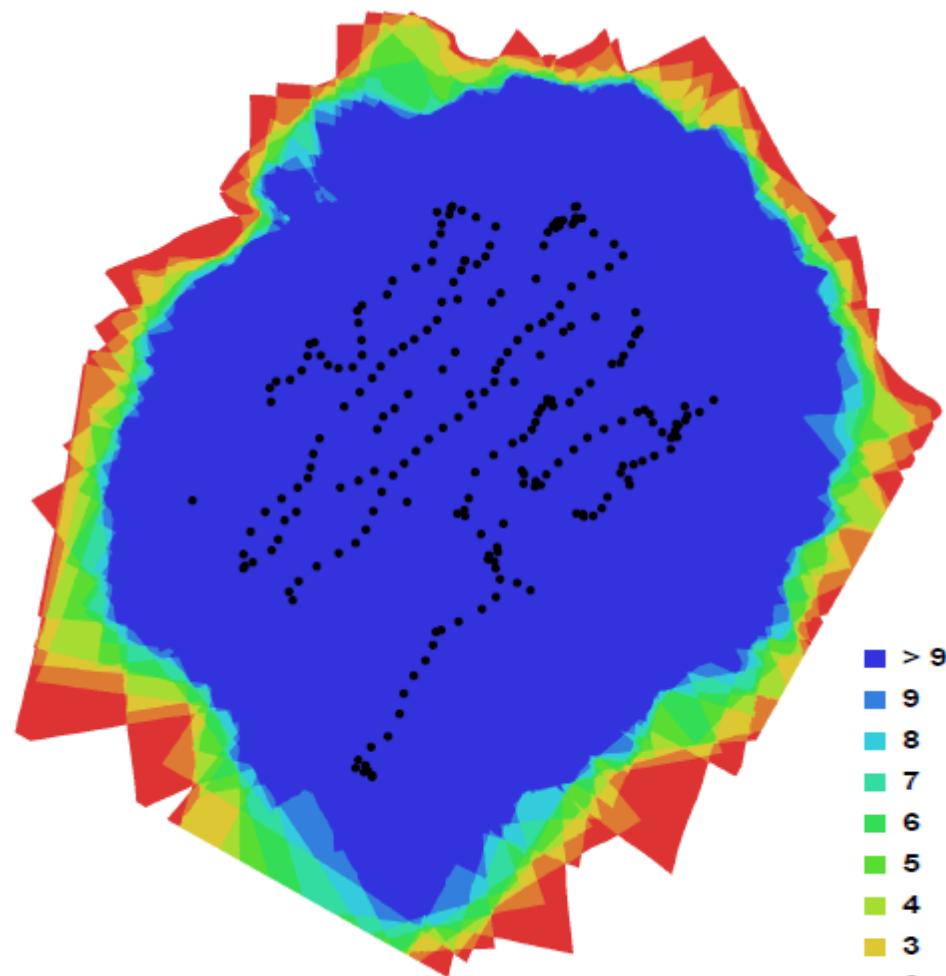
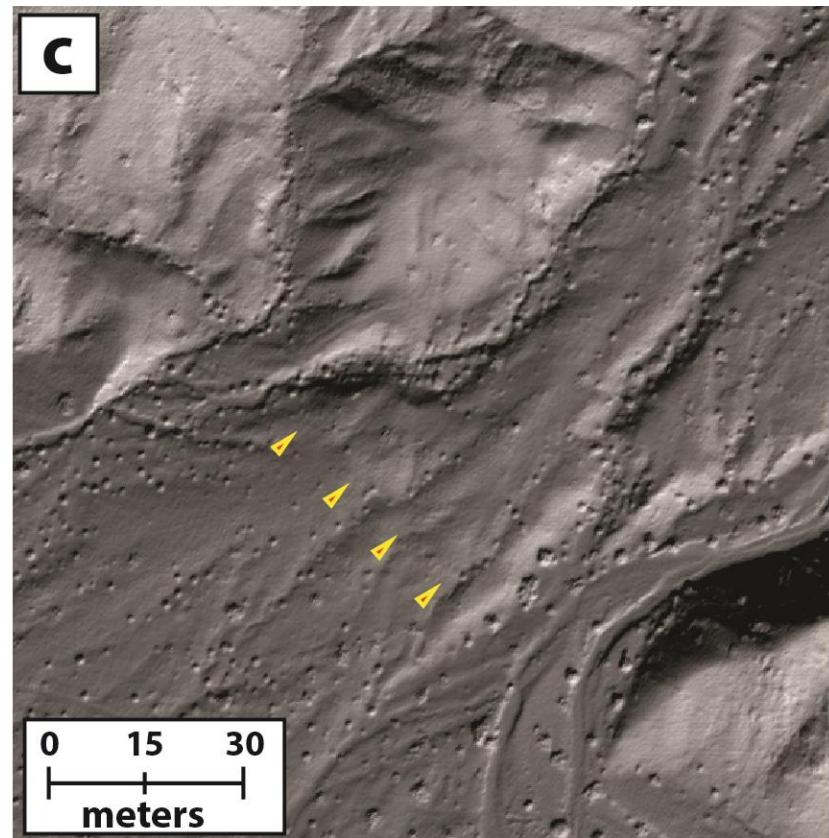
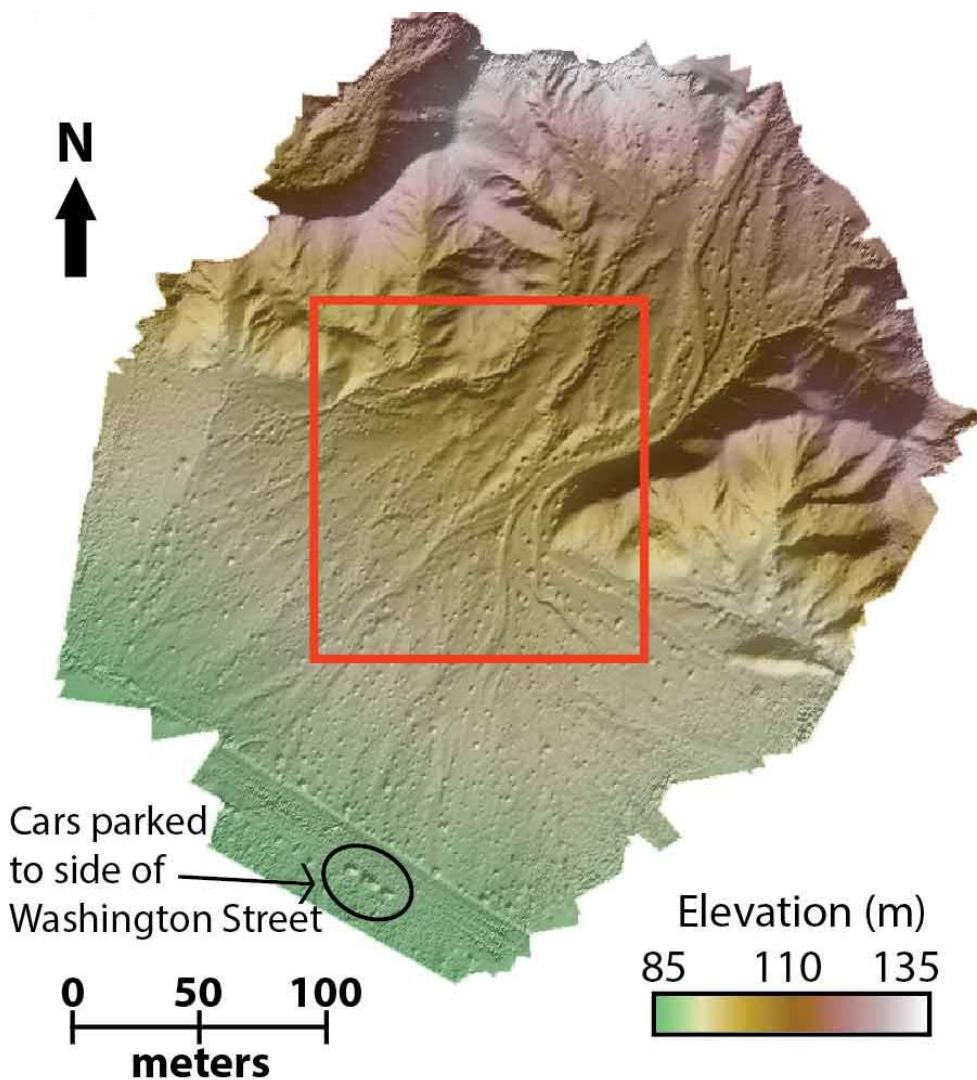


Fig. 1. Camera locations and image overlap.

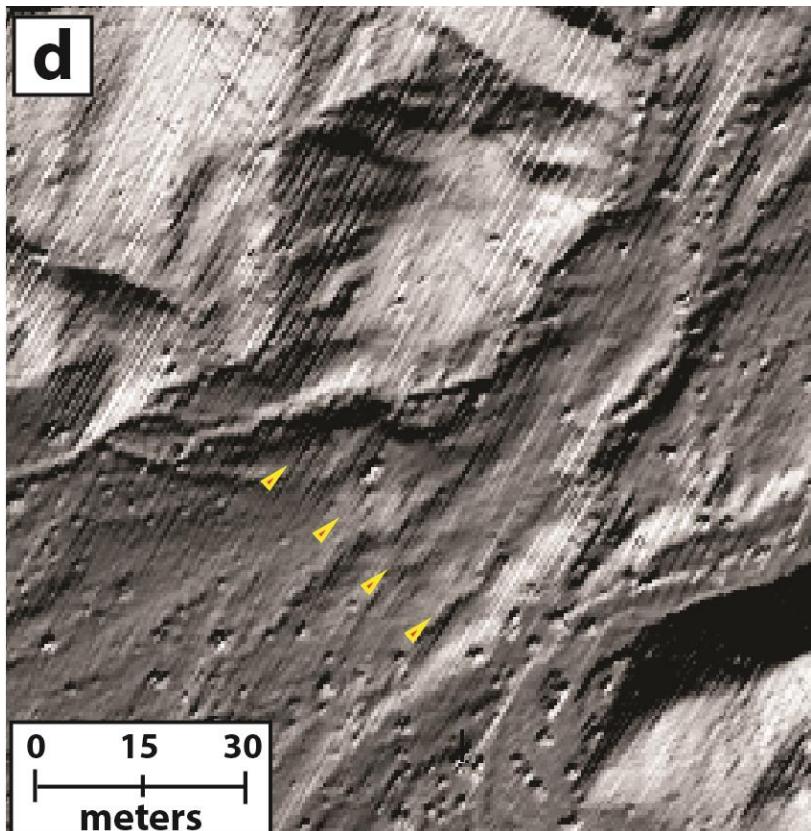
# Resolution and precision of SfM topography



**SfM** ~700 pts/m<sup>2</sup>

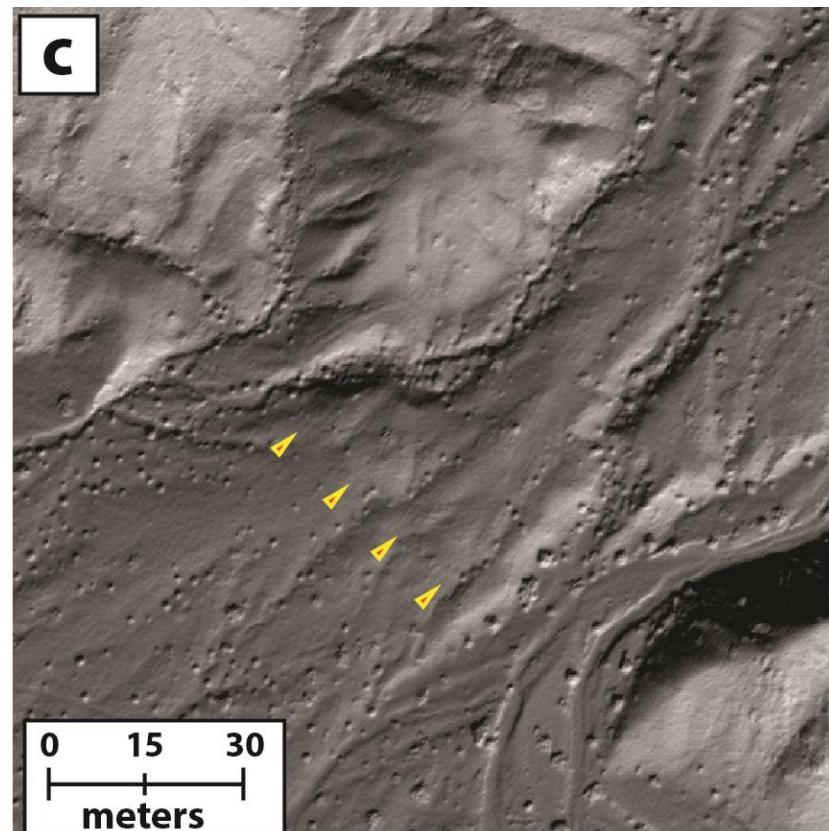
5 cm resolution DEM

# Resolution and precision of SfM topography



**B4 LiDAR** ~4 pts/m<sup>2</sup>

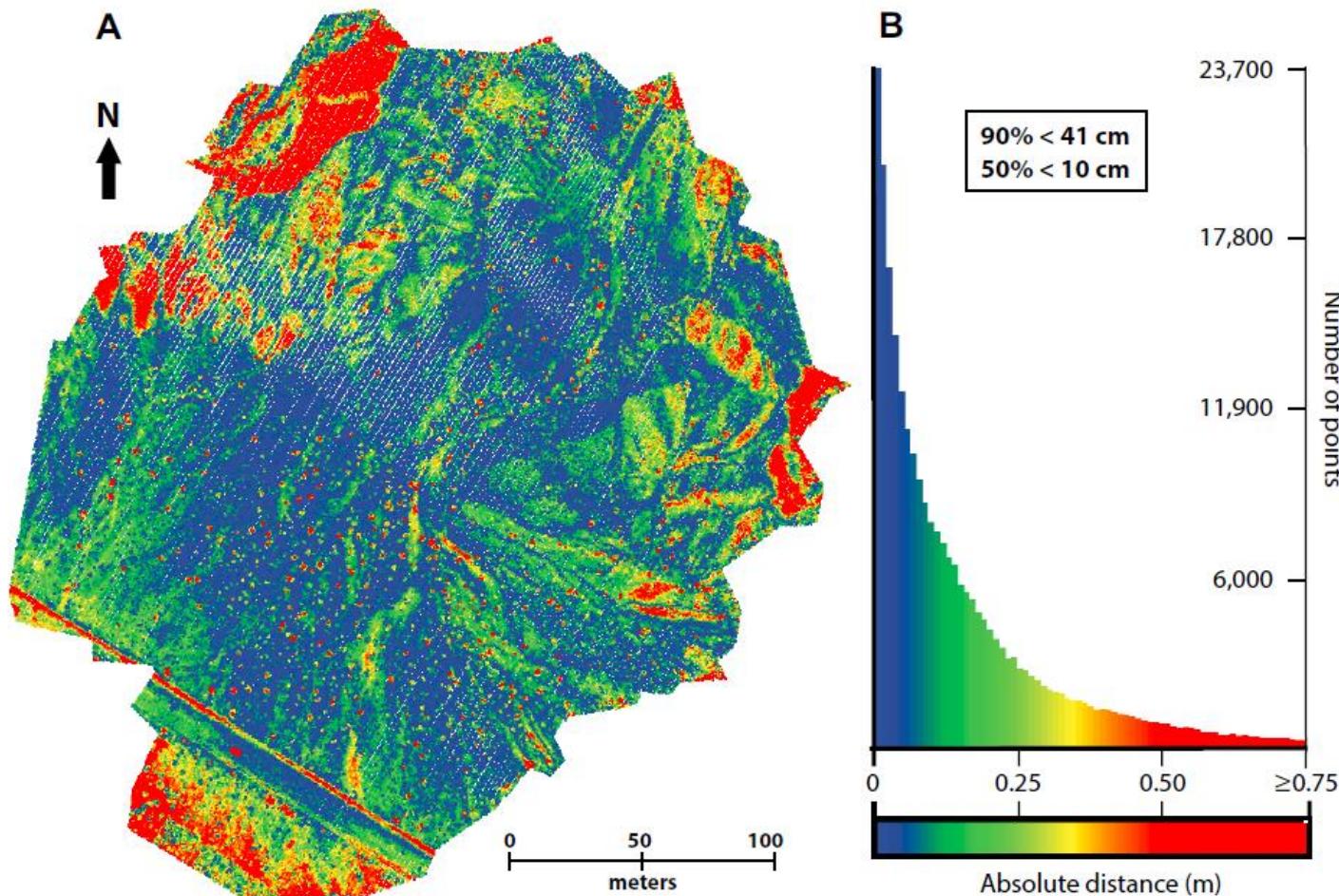
0.5 - 1 m resolution DEM



**SfM** ~700 pts/m<sup>2</sup>

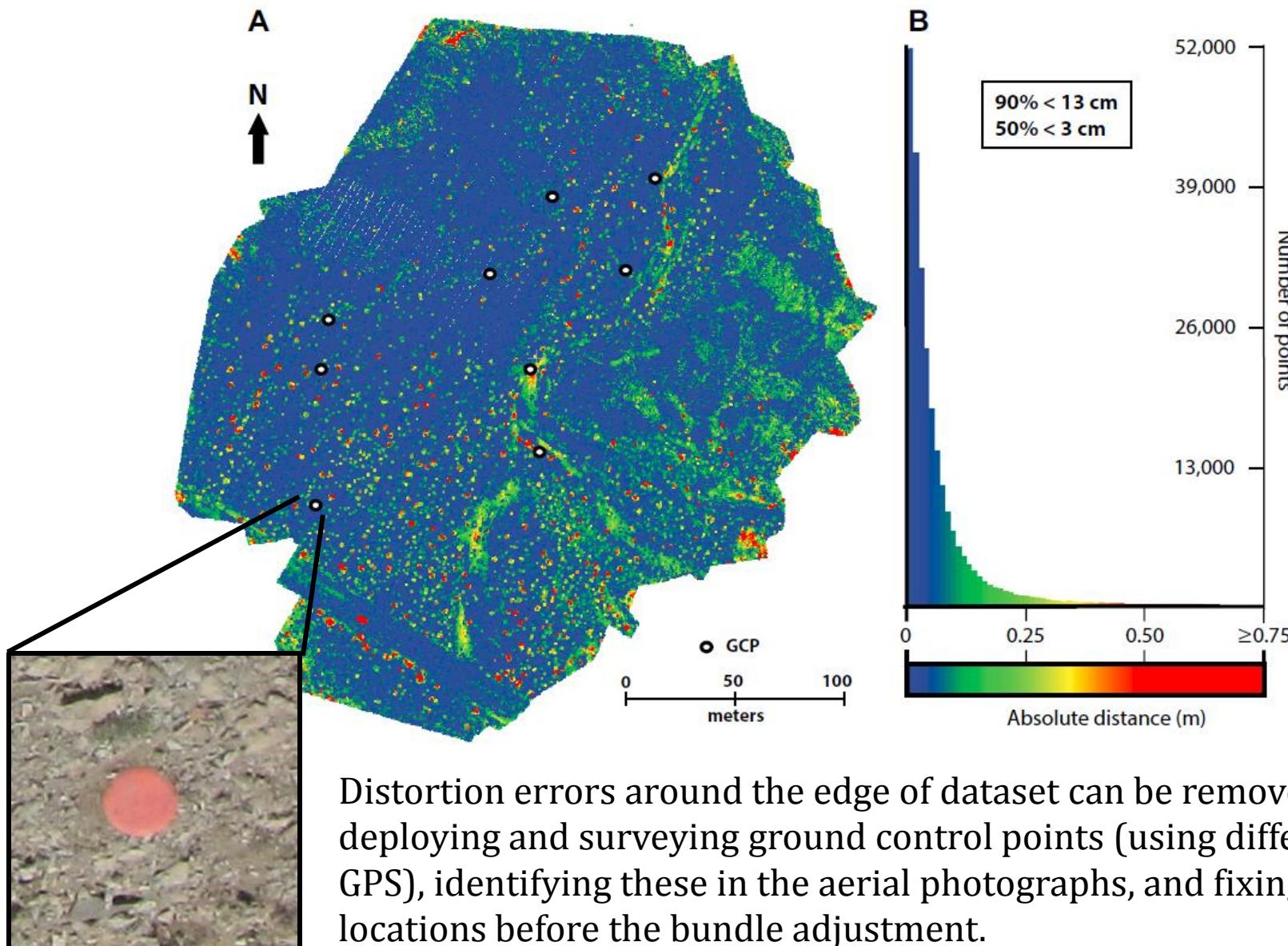
5 cm resolution DEM

# Resolution and precision of SfM topography



Note errors of >50 cm concentrated around edge of dataset. These probably reflect a trade-off in the bundle adjustment between estimates of the radial distortion of the camera lens and the topography

# Resolution and precision of SfM topography



Distortion errors around the edge of dataset can be removed by deploying and surveying ground control points (using differential GPS), identifying these in the aerial photographs, and fixing the locations before the bundle adjustment.