

**Samples                      Functions and their graphs SOLUTIONS**

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1. (1)  $2y + 5x^2 = 16y + 10x^2 + 1$ , so  $14y = -5x^2 - 1$ . This equation includes an  $x^2$  term with a negative coefficient, so the graph is a parabola which turns downwards. Also, the  $y$ -intercept is negative. Hence the matching graph is Graph T.
- (2)  $y = e^{3x}$ , which is a graph of exponential growth. Hence the matching graph is Graph K.
- (3)  $11y - 7 = 5x - 7$ , so  $11y = 5x$ . Hence this is a straight line, with positive gradient and passing through the origin. Hence the matching graph is Graph F.
- (4)  $-15y + 9 = x^2 + 9$ , so  $15y = -x^2$ . This equation includes an  $x^2$  term with a negative coefficient, so the graph is a parabola which turns downwards. Also, the  $y$ -intercept is 0. Hence the matching graph is Graph S.
- (5)  $11x - 8 = -3y + 11x - 10$ , so  $3y = -2$ , so  $y = -\frac{2}{3}$ . Hence this is a horizontal line, with  $y$  negative. Hence the matching graph is Graph D.
- (6)  $-7y + 8x - 4 = 9y + 7$ , so  $16y = 8x - 11$ . Hence this is a straight line, with positive gradient and negative  $y$ -intercept. Hence the matching graph is Graph E.
- (7)  $1 = -13x$ , so  $x = -\frac{1}{13}$ . Hence this is a vertical line, with  $x$  negative. Hence the matching graph is Graph A.
- (8)  $y = e^{-x}$ , which is a graph of exponential decay. Hence the matching graph is Graph L.
2. (1)  $-14y - 6x^2 + 7 = -15y - 9x^2 - 16$ , so  $y = -3x^2 - 23$ . This equation includes an  $x^2$  term with a negative coefficient, so the graph is a parabola which turns downwards. Also, the  $y$ -intercept is negative. Hence the matching graph is Graph T.
- (2)  $9x - 4 = 13x$ , so  $-4x = 4$ , so  $x = -1$ . Hence this is a vertical line, with  $x$  negative. Hence the matching graph is Graph A.
- (3)  $y = e^{3x}$ , which is a graph of exponential growth. Hence the matching graph is Graph K.
- (4)  $6y - 15 = -16$ , so  $6y = -1$ , so  $y = -\frac{1}{6}$ . Hence this is a horizontal line, with  $y$  negative. Hence the matching graph is Graph D.
- (5)  $y = 8 \times |9x|$ , which is a graph of absolute value. Hence the matching graph is Graph N.
- (6)  $12y - 5 = 14y - 15x + 13$ , so  $2y = 15x - 18$ . Hence this is a straight line, with positive gradient and negative  $y$ -intercept. Hence the matching graph is Graph E.
- (7)  $14x + 5 = 15x - 1$ , so  $-x = -6$ , so  $x = 6$ . Hence this is a vertical line, with  $x$  positive. Hence the matching graph is Graph B.
- (8)  $-x - 5 = -10y - 16x - 14$ , so  $10y = -15x - 9$ . Hence this is a straight line, with negative gradient and negative  $y$ -intercept. Hence the matching graph is Graph J.

3. (1)  $9y + 8x - 9 = 12y + 8x - 10$ , so  $-3y = -1$ , so  $y = \frac{1}{3}$ . Hence this is a horizontal line, with  $y$  positive. Hence the matching graph is Graph C.
- (2)  $-9y + 5x - 2 = 16y + 8x - 9$ , so  $25y = -3x + 7$ . Hence this is a straight line, with negative gradient and positive  $y$ -intercept. Hence the matching graph is Graph H.
- (3)  $y = 2 \times |-13x|$ , so  $y = 2 \times |13x|$ , which is a graph of absolute value. Hence the matching graph is Graph N.
- (4)  $y = -5 \times |8x|$ , which is a graph of negative absolute value. Hence the matching graph is Graph M.
- (5)  $4y + 6x - 14 = 6y - 5x - 14$ , so  $2y = 11x$ . Hence this is a straight line, with positive gradient and passing through the origin. Hence the matching graph is Graph F.
- (6)  $-4y - 13 = -9y + 5x^2$ , so  $5y = 5x^2 + 13$ . This equation includes an  $x^2$  term with a positive coefficient, so the graph is a parabola which turns upwards. Also, the  $y$ -intercept is positive. Hence the matching graph is Graph O.
- (7)  $15x^2 = 5y$ . This equation includes an  $x^2$  term with a positive coefficient, so the graph is a parabola which turns upwards. Also, the  $y$ -intercept is 0. Hence the matching graph is Graph P.
- (8)  $7y = 15y + 6x^2 + 15$ , so  $8y = -6x^2 - 15$ . This equation includes an  $x^2$  term with a negative coefficient, so the graph is a parabola which turns downwards. Also, the  $y$ -intercept is negative. Hence the matching graph is Graph T.