

Samples Equation of a straight line SOLUTIONS

1. To find the equation of the new line, we first need the gradient of the original line. Now,

$$50 = -5y - 5x, \text{ so}$$

$$5y = -5x - 50$$

$$y = -x - 10$$

Hence, the gradient of the original line is $m = -1$.

The new line is parallel to the original line, so it has the same gradient as the original line. Thus the equation of the line is $y = -x + c$ and we can substitute the coordinates of the point $(x_1, y_1) = (3, -1)$ into this equation to get the value for c .

$$-1 = -1 \times 3 + c, \text{ so } -1 = -3 + c. \text{ Hence } c = -1 - (-3) = 2.$$

Hence the equation of the line is $y = -x + 2$.

2. To find the equation of the new line, we first need the gradient of the original line. Now,

$$-7y + 7x = 0, \text{ so}$$

$$-7y = -7x$$

$$y = x$$

Hence, the gradient of the original line is $m = 1$.

The new line is parallel to the original line, so it has the same gradient as the original line. Thus the equation of the line is $y = x + c$ and we can substitute the coordinates of the point $(x_1, y_1) = (-6, -5)$ into this equation to get the value for c .

$$-5 = 1 \times (-6) + c, \text{ so } -5 = -6 + c. \text{ Hence } c = -5 - (-6) = 1.$$

Hence the equation of the line is $y = x + 1$.

3. To find the equation of the new line, we first need the gradient of the original line. Now,

$$-8 = 2x - 2y, \text{ so}$$

$$2y = 2x + 8$$

$$y = x + 4$$

Hence, the gradient of the original line is $m = 1$.

The new line is parallel to the original line, so it has the same gradient as the original line. Thus the equation of the line is $y = x + c$ and we can substitute the coordinates of the point $(x_1, y_1) = (-5, -3)$ into this equation to get the value for c .

$$-3 = 1 \times (-5) + c, \text{ so } -3 = -5 + c. \text{ Hence } c = -3 - (-5) = 2.$$

Hence the equation of the line is $y = x + 2$.