

Samples Periodic compounding SOLUTIONS

1. Let B be the price of the shoes, I be the amount Peter needs to invest, n be the number of compounding periods before the Congress, r be the interest compounding monthly . Then

$$r = 1 \times \frac{4.0}{12} = 0.33 \text{ percent} = 0.0033, \text{ and}$$

$$n = 19 \div 1 = 19$$

$$B = I(1+r)^n, \text{ so } I = \frac{B}{(1+r)^n}. \text{ Therefore}$$

$$\begin{aligned} I &= \frac{100}{(1+0.0033)^{19}} \\ &= \frac{100}{1.0653} \\ &\approx 93.87 \end{aligned}$$

Hence he needs to invest approximately \$93.87 .

2. Let B be the price of the shoes, I be the amount Peter needs to invest, n be the number of compounding periods before the Congress, r be the interest compounding monthly . Then

$$r = 1 \times \frac{8.0}{12} = 0.67 \text{ percent} = 0.0067, \text{ and}$$

$$n = 22 \div 1 = 22$$

$$B = I(1+r)^n, \text{ so } I = \frac{B}{(1+r)^n}. \text{ Therefore}$$

$$\begin{aligned} I &= \frac{200}{(1+0.0067)^{22}} \\ &= \frac{200}{1.1574} \\ &\approx 172.80 \end{aligned}$$

Hence he needs to invest approximately \$172.80 .

3. Let B be the price of the shoes, I be the amount Peter needs to invest, n be the number of compounding periods before the Congress, r be the interest compounding monthly . Then

$$r = 1 \times \frac{7.0}{12} = 0.58 \text{ percent} = 0.0058, \text{ and}$$

$$n = 20 \div 1 = 20$$

$$B = I(1+r)^n, \text{ so } I = \frac{B}{(1+r)^n}. \text{ Therefore}$$

$$\begin{aligned} I &= \frac{100}{(1+0.0058)^{20}} \\ &= \frac{100}{1.1234} \\ &\approx 89.02 \end{aligned}$$

Hence he needs to invest approximately \$89.02 .