1.
$$f(x) = (\sqrt{6x})^2$$

1. $f(x) = (\sqrt{6x})^2$ When determining the domain of this function, we need to keep in mind the following:

- we can square any number;
- we can only take the square root of positive numbers or 0, so $6x \ge 0$.

Hence, the domain of this function is $[0, \infty)$, i.e. $x \ge 0$.

2.
$$f(z) = \frac{2}{-7\sqrt{z}}$$

When determining the domain of this function, we need to keep in mind the following:

- denominator of a fraction cannot be 0, so $-7\sqrt{z} \neq 0$;
- we can only take the square root of positive numbers or 0, so z > 0.

Hence, the domain of this function is $(0, \infty)$, i.e. z > 0.

3.
$$f(x) = 4\sqrt{\frac{4}{x}}$$

When determining the domain of this function, we need to keep in mind the following:

- we can only take the square root of positive numbers or 0, so $\frac{4}{r} \ge 0$;
- denominator of a fraction cannot be 0, so x > 0.

Hence, the domain of this function is $(0, \infty)$, i.e. x > 0.