

Searching for dark matter with GPS and global networks of atomic clocks

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Outline:

Outline

Ultralight DM +
TDs

Variation in clock
frequencies

GPS

Initial search/
first results

Bayesian search

Testing method

Possible
outcomes

- Ultra light dark matter; “clumps”, e.g. Topological defects
- Transient signals: Global networks of precision devices
- GPS: 50,000km aperture sensor array
 - ~ 30 satellite clocks, > 15 years of archived data
- Initial search: domain walls
- limits: orders of magnitude improvement for certain models
- Looking forward: Bayesian search technique

Ultralight Dark Matter:

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WIMPs

- long-time “favourite” DM candidate
- Masses $\sim 10 - 1000$ GeV
- Many null WIMP results
- Increased interest in other forms of DM

Ultralight fields (e.g., axions)

- Masses $\sim 10^{-24} - 1$ eV
- Classical oscillating field: $\phi = a \cos(m_a t)$
- Stable topological defects: monopoles, strings, walls
 - Also: Q-balls, solitons, “clumps”
- Peccei & Quinn '77, Weinberg '78, Dine & Fischler '82, ...

Topological Defect DM

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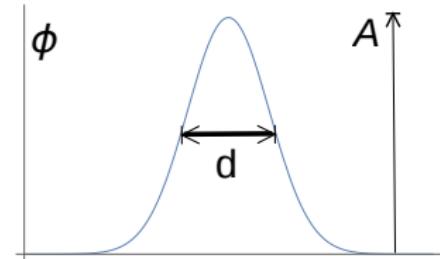
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Topological Defects

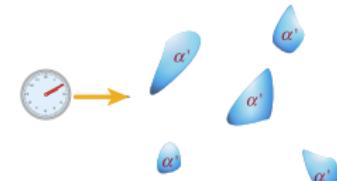
- monopoles, strings, walls,
- Defect width: $d \sim 1/m_\phi$
- Earth-scale object $\sim 10^{-14}$ eV



$$\text{Inside: } \phi^2 \rightarrow A^2, \quad \text{Outside: } \phi^2 \rightarrow 0$$

Dark matter: Gas of defects

- DM: galactic speeds: $v_g \sim 10^{-3} c$
- $A^2, d, \mathcal{T}_{\text{b/w}}$ collisions $\implies \rho_{\text{DM}}$



$$A^2 = \rho_{\text{DM}} v_g d \mathcal{T},$$

- Sikivie '82, Preskil '83, Vilekin '85, Coleman '85, Lee '89, ...

Possible DM–SM interactions

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Pseudoscalar (axionic) portal:

- e.g., $\mathcal{L}^{\text{PS}} = \partial_\mu a \bar{\psi} \gamma^\mu \gamma^5 \psi$
- Leads to magnetic-like interactions: magnetometry
 - GNOME: Global network of magnetometers (1)

Quadratic scalar portal:

- Effective local shifts in values of fundamental constants
- Leads to shifts in clock frequencies
 - GPS.DM: \implies Global network of atomic clocks (2)

1. Pospelov, Pustelny, Ledbetter, Kimball, Gawlik, Budker, PRL **110**, 21803 (2013).
2. Derevianko, Pospelov, Nat. Phys. **10**, 933 (2014).

- Also: Interferometry etc.: Arvanitaki, Graham, Hogan, Rajendran, Van Tilburg (2016); Stadnik, Flambaum (2016)...

Variation of fundamental constants

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$$-\mathcal{L}^{S^2} = \phi^2(r, t) \left(\frac{m_f \bar{\psi}_f \psi_f}{\Lambda_f^2} + \frac{1}{4\Lambda_\alpha^2} F_{\mu\nu}^2 + \dots \right),$$

c.f. \mathcal{L}^{SM} \implies transient additions to fundamental constants

$$\alpha^{\text{eff}}(r, t) = \alpha \left(1 + \frac{\phi^2(r, t)}{\Lambda_\alpha^2} \right), \quad m_f^{\text{eff}}(r, t) = m_f \left(1 + \frac{\phi^2(r, t)}{\Lambda_f^2} \right),$$

\implies shifts in energy levels \implies shifts in clock frequencies

$$\frac{\delta\omega(r, t)}{\omega_0} = \phi^2(r, t) \sum_x \frac{K_x}{\Lambda_x} \quad K_\alpha : \text{Sensitivity of } \omega \text{ to } \delta\alpha$$

Flambaum, Tedesco, PRC, **73**, 55501 ('06); Flambaum, Dzuba, Can. J. Phys., **87**, 25 ('09).

Shift in atomic clock frequencies

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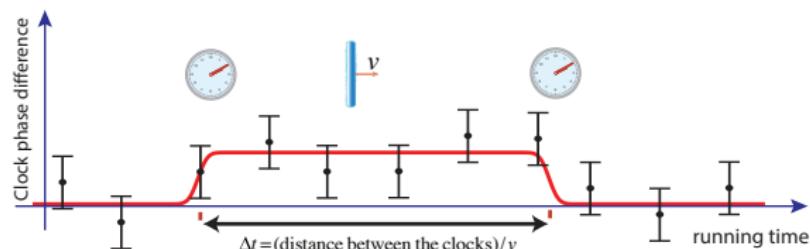
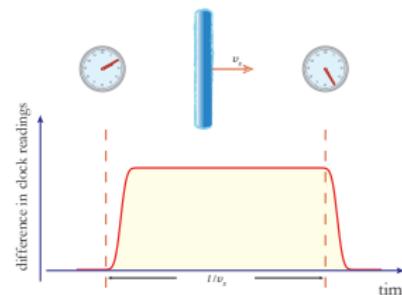
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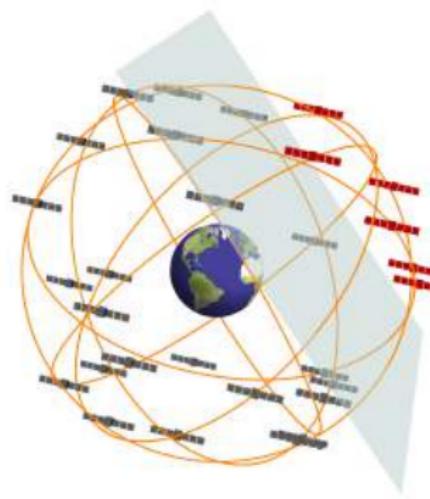
Monitor Atomic Clocks

- Temporary frequency shift → bias (phase) build-up
- Initially synchronised clocks become desynchronised



GPS: 50,000 km DM observatory

- 32 satellite clocks (Rb/Cs), ~ 16 years of high-quality data
- Also several H-maser ground-based clocks.
- Data from JPL: (sideshow.jpl.nasa.gov/pub/jpligsac/)
 - 30s sampled data; 0.01–0.1 ns precision
- Correlated, directional signal, with $v_g \sim 300$ km/s



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DM Walls: Initial search/limits

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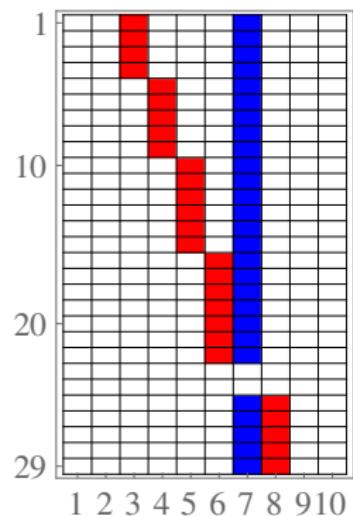
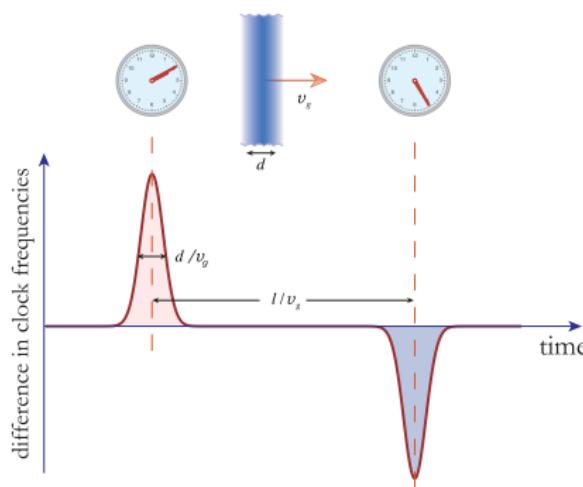
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- Thin wall: brief (< 30 s) frequency excursion



- \vec{v} encoded in time-delay and signal ordering: $\Delta t \sim \text{minutes}$

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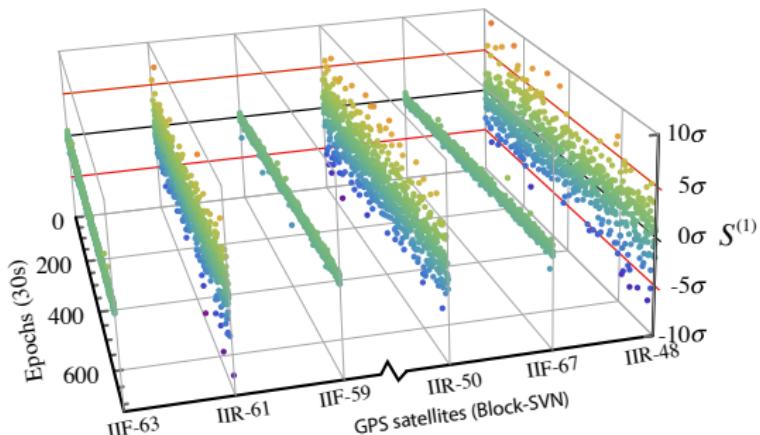
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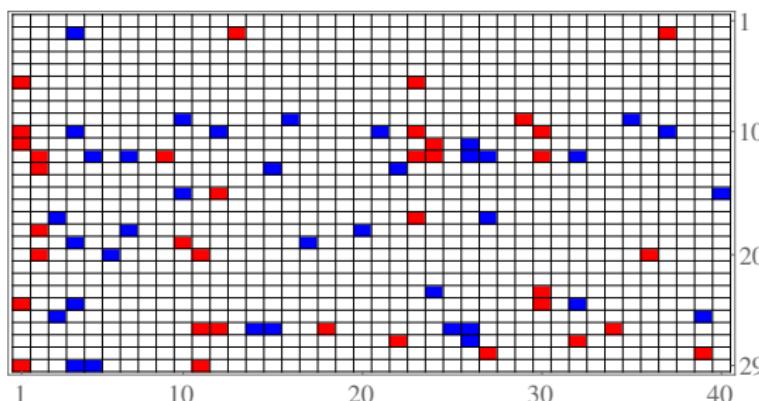
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Apply S_{cut} \implies



Scan the data

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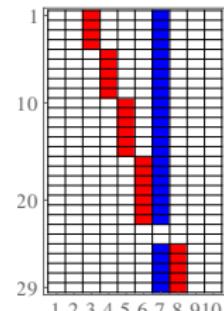
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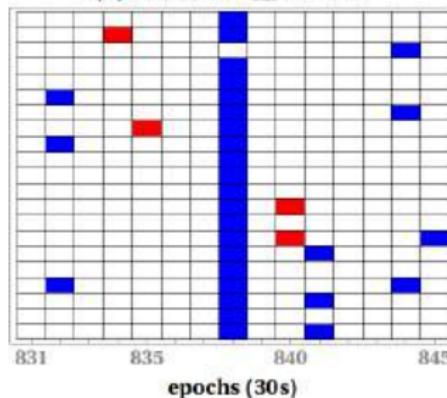
Possible
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Simple pattern search

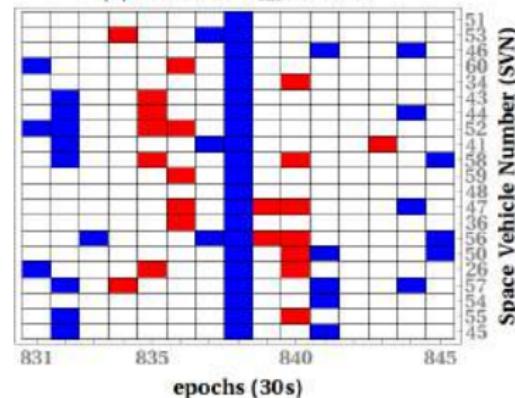
- Match data windows against expected signals
- Reduce S_{cut} until signal can no longer be ruled out
- This case: excluded since $\text{ref} > \text{rest}$



(b) GPS data: $S_{\text{cut}}^{(1)} = 0.18 \text{ ns}$



(c) GPS data: $S_{\text{cut}}^{(1)} = 0.13 \text{ ns}$



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Initial search/
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Sensitivity

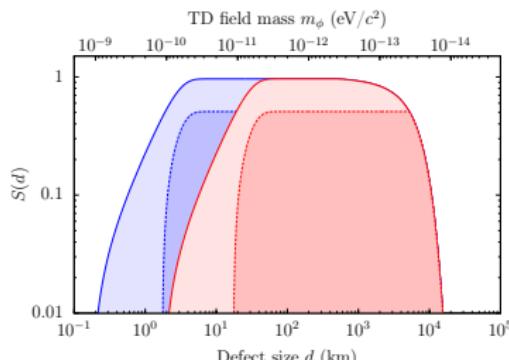
- 3D parameter space (Λ_X , \mathcal{T} , d):

$$S = \hbar c \sqrt{\pi} \rho_{\text{DM}} \frac{K_X d^2 \mathcal{T}}{\Lambda_X^2}$$

$$\rho_{\text{inside}} = \frac{\rho_{\text{DM}} v_g}{d} \mathcal{T}$$

Not equally sensitive to each width, d

- Assumes standard halo model
- “Servo time”: $\tau = d/v_\perp > \tau_{\text{servo}} \approx 0.01 - 0.1 \text{ s}$
- Wall must be “thin” enough: $\tau = d/v_\perp < 30 \text{ s}$



- Fraction of events we could “see”
- 90% C.L. (assuming SHM)

Setting Limits

Outline

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What we see in the data:

- $S_{\text{lim}}^{(1)}$: largest signal size that can't be ruled out
- Assume Poisson distribution, and SHM
 - $S_{\text{lim}}^{(1)} \sim 0.5 \text{ ns}$
 - $T_{\text{obs}} = 16 \text{ years}$

$$\frac{\Lambda_{\text{eff}}/\text{TeV}}{d/\text{km}} > 2 \times 10^3 \sqrt{\frac{T_{\text{obs}} s(d)/\text{yr}}{\lambda S_{\text{lim}}^{(1)}/\text{ns}}}.$$

Results: Limits

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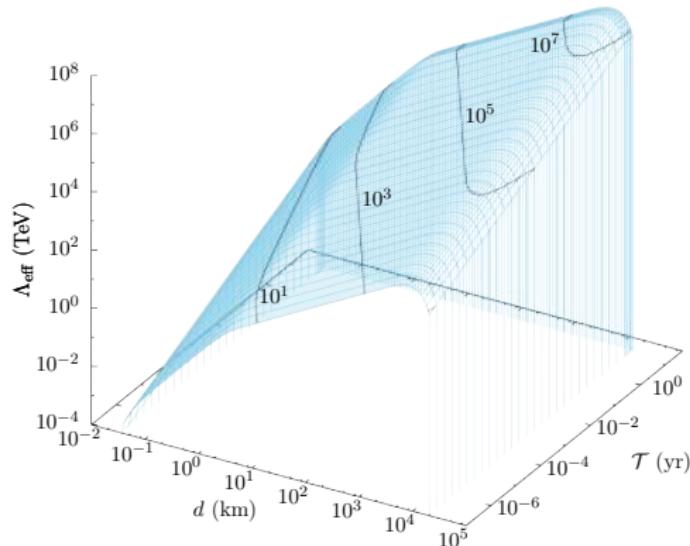
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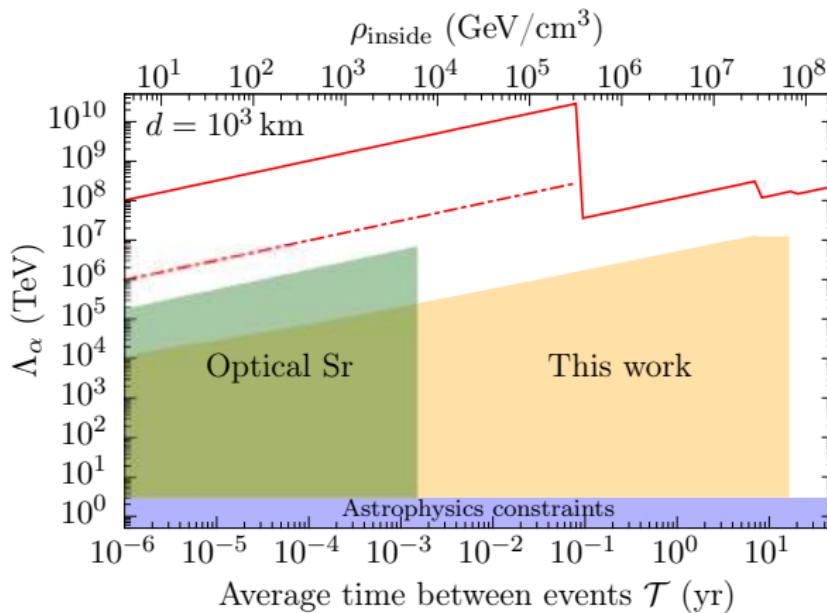


Rb sub-network

- Λ_{eff} : combination of α , $m_{e,p}$, m_q
- Until recently, existing limits did not exceed 10 TeV
- $\mathcal{T} = 1 \text{ yr} \& d = 10^3 \text{ km} \implies \rho_{\text{inside}} \approx 10^6 \text{ GeV/cm}^3$
 - c.f. $\rho_{\text{water}} \sim 10^{24} \text{ GeV/cm}^3$

Results: Limits - Λ_α (photon)

- (Assume this coupling dominates)



Sr: Wcislo, Morzynski, Bober, Cygan, Lisak, Ciurylo, Zawada, Nat. Astron. 1, 9 (2016).
Astro: Olive, Pospelov, Phys. Rev. D. 77, 43524 (2008).

Results: Limits - fermion masses

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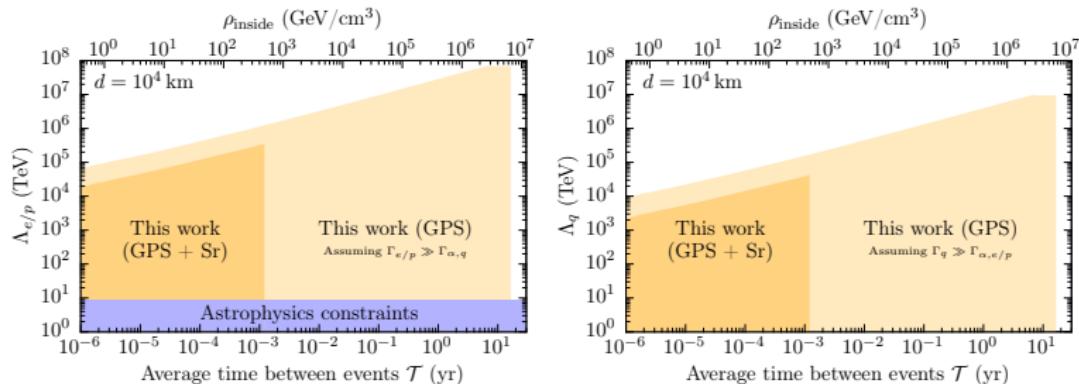
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Combine Rb, Cs, and Sr (optical)

- Three different combo's of three couplings



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How to improve upon this?

- There may be events “hiding” below the noise.
- Other geometries: monopoles, strings, thicker walls

Bayesian Analysis

- Marginalise (integrate) all parameters (In-built Occam’s Razor)
 - Time, velocity, object size, impact parameter
- Form odds ratios

$$\underbrace{p(D_{j_0} | m, I)}_{\text{Likelihood}} = K \underbrace{\int dx_1 \dots \int dx_n}_{\text{marginalise parameters}} \underbrace{p(x_1 \dots x_n | m, I)}_{\text{Priors}} \underbrace{\exp(-\chi_s)}_{\text{Gaussian likelihood}}$$

$$\chi_s = \sum_i \sum_{jl} \left(d_j^i - s_j^i \right) \widehat{H_{jl}^i} \left(d_l^i - s_l^i \right) \quad \text{co-variance}$$

- Should be able to detect events as small as:

$$s \approx \sigma / \sqrt{N} \approx 0.001 \text{ ns (for the best clocks)}$$

Test the method:

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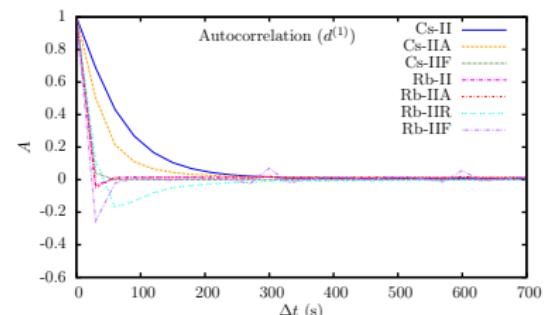
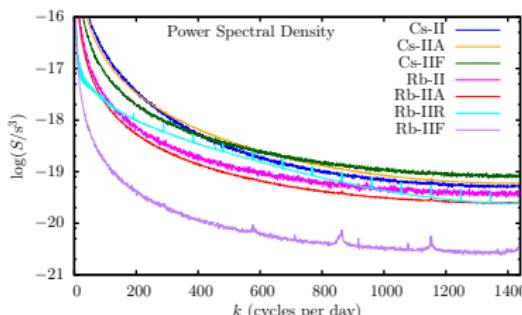
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Statistical properties of data:

- Power-spectrums, Auto-correlation functions, Allan variance, ...



- Generate “fake” data: mimics properties of the real data
 - y : Input white noise, S : PSD, z : Simulated data

$$z = FT^{-1}(FT(y)\sqrt{S^{\text{target}}/Sy})$$

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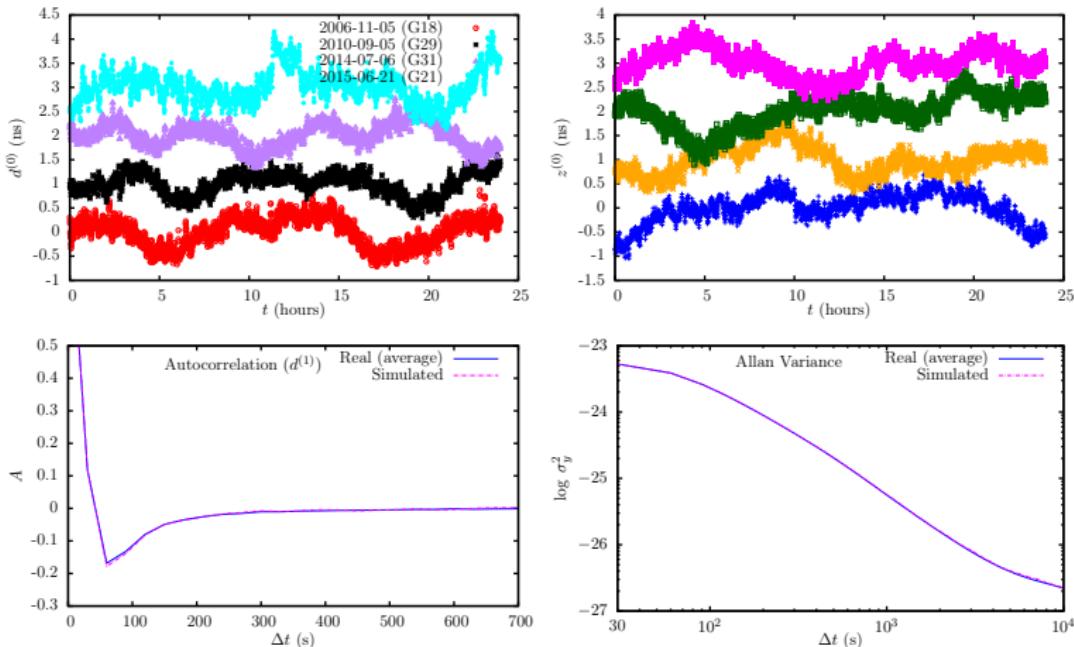
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Test the method:



- Inject fake events: True positive rate
- Don't inject events: False positive rate
- Currently running large-scale simulations. Results promising!

Possible outcomes:

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a) See (\sim few) very good candidate events

- Large odds ratio, good fit to model
- “best” case scenario: Analyse these in great detail
- Check against other precision experiments

b) we don't

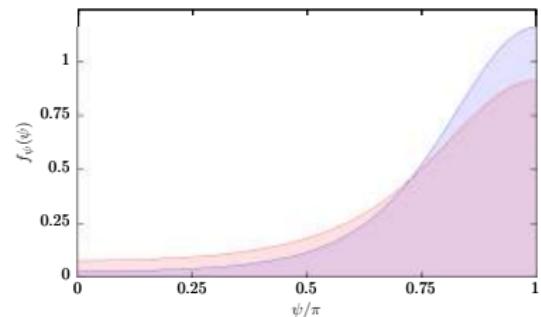
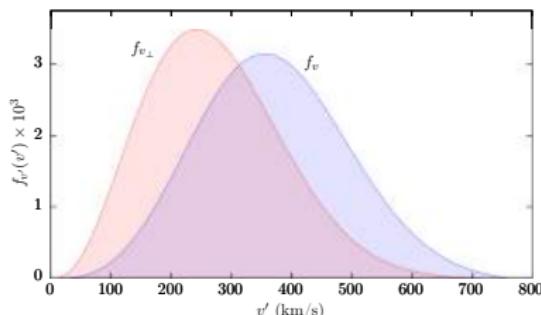
- Set limits.
- Is that all?
- Case when there is a large number of small events?

Possible outcomes:

- All actual events should* have same sign

Vector velocity resolution:

- > 30 clocks: quite good speed/direction resolution
- Potential to resolve velocity distribution (SHM)



- False positives will have different distribution
- But: have to “discount” priors for this analysis)

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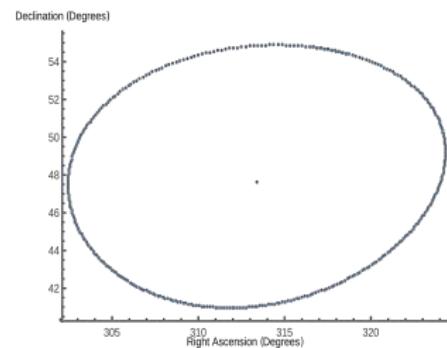
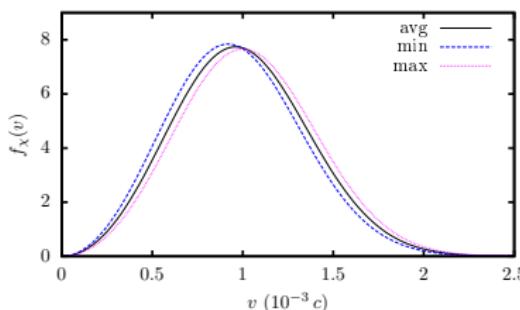
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Possible outcomes:

Annual variation:



Lower threshold. Lots of false-positives

- Assymetry in event 'sign' & resolve SHM predictions, +
- Annual modulation:
 - Event rate
 - Average velocity
 - Most-common incident direction

May extend discovery reach for $\mathcal{T} \ll 1$ yr and $d \ll R_{\text{GPS}}$

Some references:

Axions, ultralight scalar DM:

- R. D. Peccei and H. R. Quinn, Phys. Rev. Lett. 38, 1440 (1977).
- P. Sikivie, Phys. Rev. Lett. 51, 1415 (1983); Phys. Rev. Lett. 48, 1156 (1982).

Topological defect DM:

- T. W. B. Kibble, Phys. Rep. 67, 183 (1980).
- A. Vilenkin, Phys. Rep. 121, 263 (1985).

non-topological solitons, Q-balls:

- S. Coleman, Nucl. Phys. B 262, 263 (1985).
- K. Lee, J. A. Stein-Schabes, R. Watkins, and L. M. Widrow, Phys. Rev. D 39, 1665 (1989).
- A. Kusenko and P. J. Steinhardt, Phys. Rev. Lett. 87, 141301 (2001).

Other non-gravitational TD searches:

- M. Pospelov, S. Pustelny, M. P. Ledbetter, D. F. J. Kimball, W. Gawlik, and D. Budker, Phys. Rev. Lett. 110, 21803 (2013).
- Y. V. Stadnik, V. V. Flambaum, Phys. Rev. Lett. 113, 151301 (2014); PRL 114, 161301 (2015).
- E. D. Hall, T. Callister, V. V. Frolov, H. Mller, M. Pospelov, and R. X. Adhikari, arXiv:1605.01103.
- P. Wcisło, Morzynski, Bober, Cygan, Lisak, Ciuryło, M. Zawada, Nat. Astron. 1, 9 (2016).

Conclusion:

GPS: 50,000km aperture DM observatory

- Topological defect dark matter/transient exotic physics
- GPS: 50,000km aperture sensor array
 - ~ 30 satellite clocks, many earth clocks, > 15 years of clock data
- DM walls: Orders of magnitude improvement for certain models
- Looking forward: Bayesian search technique
 - Monopoles, strings, signals below σ_{clock}
- General technique: archived, time-stamped data

More: see [arXiv:1704.06844](https://arxiv.org/abs/1704.06844), BMR¹, G. Blewitt¹, C. Dailey¹, M. Pospelov^{2,3}, A. Rollings¹, J. Sherman⁴, W. Williams¹, and A. Derevianko¹.

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Aside: challenges of re-purposed data

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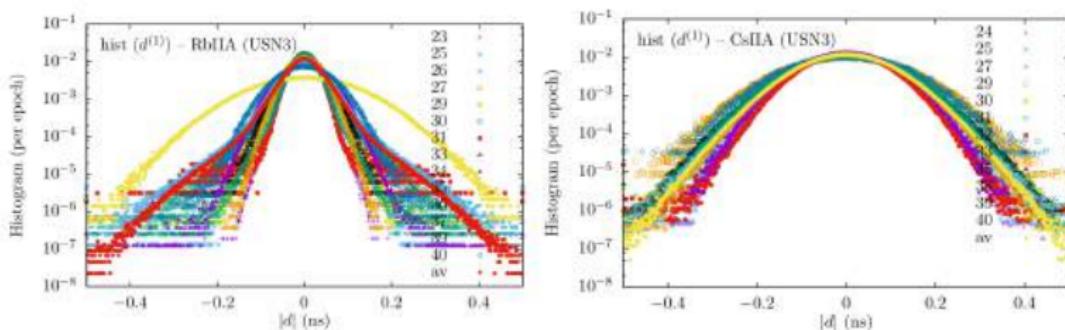
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data from JPL: Histogram



- Possible that some clocks mis-identified
(Here, one of the “Rb” clocks is probably Cs).
- Same discrepancy in autocorrelation function, Allan variance etc.

Clock stability: Mixed network

Outline

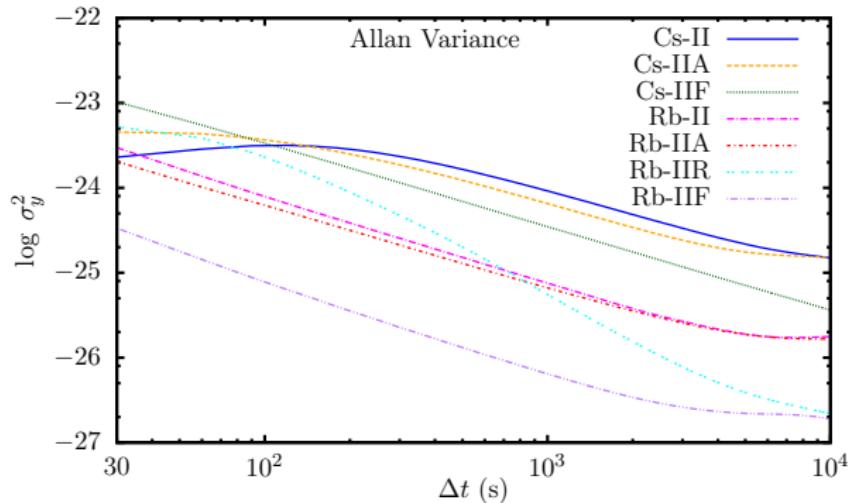
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Launched:

- 1989–1997: II + IIA = $\sim 17\,000$ clock-days
- 1997–2009: IIR = $\sim 64\,000$ clock-days
- 2010–2016: IIF = $\sim 8\,000$ clock-days
- Block III: Due in 2016 2017 2018(?)