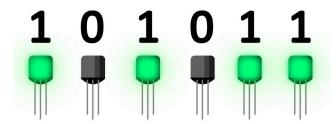
CSC 411

Computer Organization (Fall 2024)
Lecture 3: Bitwise Operations

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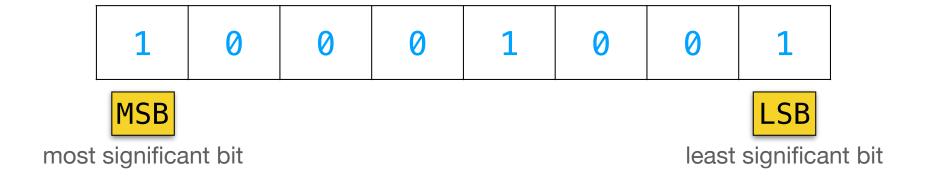
Bits

- Computers use the binary number system to represent and process data
- A bit (binary digit) is the smallest unit of data in computing
 - can have a value of 0 or 1
 - easy to implement in digital circuits
 - forms the foundation for all digital information
- Bit Representation
 - bits are typically represented by electrical voltages in computer hardware
 - high voltage corresponds to 1 and low voltage to 0



Bytes

- A byte is a group of 8 bits
 - commonly used to represent characters, numbers, and other data
 - <u>smallest addressable unit of memory</u> in most computer architectures



- Important calculations
 - how many different values can be stored in 1 byte?
 - ow many different values can be stored in n bits?

Basic data types in C

The C language does not explicitly define data sizes. The actual sizes can vary depending on the compiler and the system architecture.

C declaration	Bytes		
Signed	Unsigned	32-bit	64-bit
[signed] char	unsigned char	1	1
short	unsigned short	2	2
int	unsigned	4	4
long	unsigned long	4	8
$int32_t$	$uint32_t$	4	4
$int64_t$	$uint64_t$	8	8
char *		4	8
float		4	4
double		8	8

Boolean algebra

- Developed by George Boole in the 19th century
 - branch of mathematics dealing with binary variables and logic operations
 - fundamental to digital circuit design and computer science
- Three basic logic operations
 - AND: output is 1 only if both inputs are 1 conjunction
 - OR: output is 1 if at least one input is 1 disjunction
 - NOT output is the opposite of the input negation
- Boolean expressions
 - formed by combining variables and logic operations

Bit vectors

- Sequences of bits that can represent various types of data
- Boolean algebra can be <u>extended</u> to operate on bit vectors
- Applications in Computer Science
 - efficient set representation
 - implementation of data structures
 - low-level programming and bitwise manipulation

Understanding boolean algebra with bit vectors is essential for working with binary data in computer science and digital design

Bitwise operators in C

- Operate on "integer" data types
 - long, int, short, chart, unsigned variants
- Treat arguments as bit vectors
- Corresponding logic operators are applied bitwise to operands
- Commonly used to manipulate sets and masks

~	bitwise NOT	~a	the bitwise NOT of a
&	bitwise AND	a & b	the bitwise AND of a and b
	bitwise OR	a b	the bitwise OR of a and b
^	bitwise XOR	a ^ b	the bitwise XOR of a and b
<<	bitwise left shift	a << b	a left shifted by b
>>	bitwise right shift	a >> b	a right shifted by b

Bitwise operators in C

bit a	bit b	a & b (a AND b)
0	0	0
0	1	0
1	0	0
1	1	1

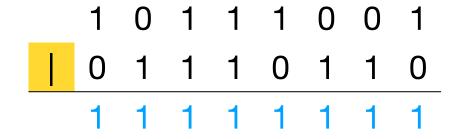
bit a	bit b	a I b (a OR b)
0	0	0
0	1	1
1	0	1
1	1	1

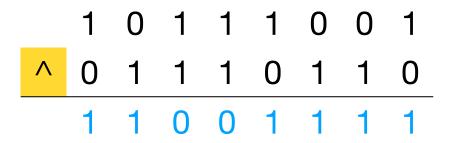
bit a	bit b	a ^ b (a XOR b)
0	0	0
0	1	1
1	0	1
1	1	0

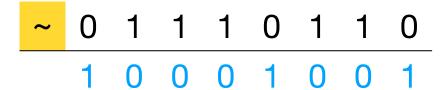
~a (NOT a) is trivial

Examples









 $\sim 0 \times 102$

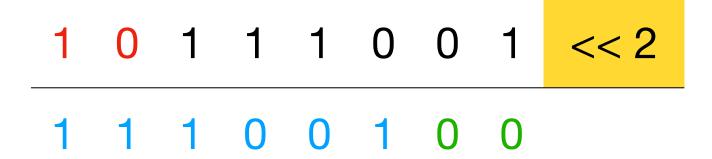
0xABC & 0x411

0xABC | 0x411

0x102030 & 0x00FF00

Shift operations

- Left shift (x << y)</p>
 - shifts each bit in x to the left by y positions
 - discards y bits on the left
 - fills y blank spaces on the right with zeros



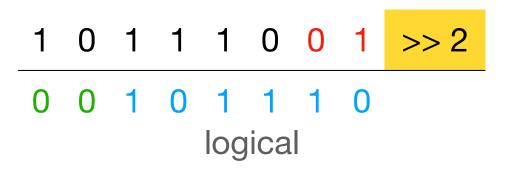
Shift operations

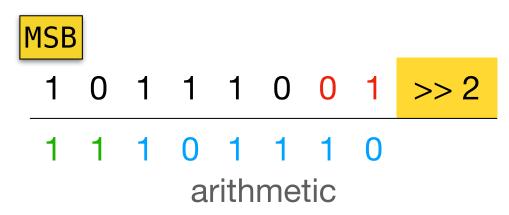
- Right shift (x >> y)
 - shifts each bit in x to the right by y positions
 - discards y bits on the right

Logical shift: fill blank spaces on left with zeroes

Arithmetic shift:

fill blank spaces by replicating
original MSB (most compilers
implement it — preserves sign bit)





0xF3 << 2

0x9A >> 3 (logical)

0x9A >> 3 (arithmetic)

Example: bit masking

- Assume an unsigned integer j that stores the value 0x1A35B127
 - define a mask to extract the most significant byte

 write C code to store the extracted value in another variable (unsigned int)

Example: bit masking

- Assume an integer j that stores the value 0x1A35B127
 - write C code to set the least significant byte of j to all ones leaving all other bytes unchanged

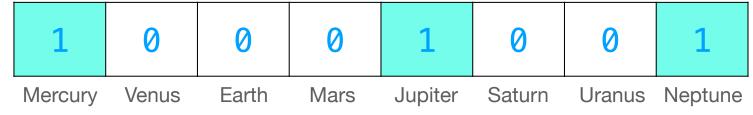
- Consider a genomic database
 - four DNA bases: Adenine (A), Cytosine (C), Thymine (T), and Guanine (G)
 - estimate the size in bytes of a text file storing a database of 100,000,000 DNA bases, assuming each base is represented as a single character (char)
- Determine the minimum number of bits required to uniquely represent each base
 - write a possible encoding, mapping each base to a specific bit pattern
- Assume DNA sequences are stored as integers (4 bytes)
 - calculate the maximum number of DNA bases that can be represented within a single integer
 - given the integer value 0x10012001, assuming your encoding, decode the corresponding DNA sequence
 - estimate the size in bytes of a binary file storing a database of 100,000,000 DNA bases

Encoding sets

- Arrays can be inefficient for storing sets, especially when many elements are absent
 - use bits to represent membership, each bit corresponding to a unique object

Example:

 consider a set of 8 objects, a char variable, can represent all possible subsets



Questions

- how to add, remove, or flip individual objects from the set?
- how to check whether an object is in the set?
- how to perform intersection, union, symmetric difference, and complement?

Show me the code

```
enum Planet { MERCURY, VENUS, EARTH, MARS, JUPITER,
              SATURN, URANUS, NEPTUNE, NUM_PLANETS };
int main() {
    char planets = 0;
    planets = add_planet(planets, EARTH);
    planets = add_planet(planets, MARS);
    planets = add_planet(planets, JUPITER);
    print_set(planets);
    planets = remove_planet(planets, MARS);
    print set(planets);
    planets = flip_planet(planets, SATURN);
    print_set(planets);
    return 0;
```

Show me the code

```
char add planet(char set, enum Planet planet) {
    return set | (1 << planet);
char remove planet(char set, enum Planet planet) {
    return set & \sim(1 << planet);
char flip_planet(char set, enum Planet planet) {
    return set ^ (1 << planet);
bool is_in_set(char set, enum Planet planet) {
    return (set & (1 << planet)) != 0;
}
void print set(char set) {
    const char* planet_names[] = {"Mercury", "Venus", "Earth",
         "Mars", "Jupiter", "Saturn", "Uranus", "Neptune"};
    printf("Set: ");
    for (enum Planet p = 0 ; p < NUM_PLANETS ; p++) {</pre>
        if (is in set(set, p)) {
            printf(" %s", planet_names[p]);
    printf("\n");
```

Bitwise vs logical operators in C

- Bitwise operators
 - operate on individual bits of integer values
 - operators: &, |, ^, ~, <<, >>
- Logical operators
 - operate on boolean values (true or false)
 - return a boolean value (true or false)
 - operators: !, &&,

any non-zero value
is considered true,
 zero is false

!0xF3

!0x00

!!0xF3

 $\sim 0xF3$

0xF3 && 0xF1

0xF3 || 0xF1

0xF3 & 0xF1