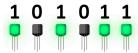
# **CSC 411**

Computer Organization (Fall 2024) Lecture 3: Bitwise Operations

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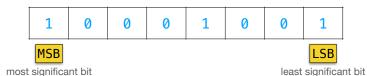
#### **Bits**

- Computers use the binary number system to represent and process data
- A bit (binary digit) is the smallest unit of data in computing
  - · can have a value of 0 or 1
  - · easy to implement in digital circuits
  - · forms the foundation for all digital information
- Bit Representation
  - bits are typically represented by electrical voltages in computer hardware
    - high voltage corresponds to 1 and low voltage to 0



## **Bytes**

- A byte is a group of 8 bits
  - · commonly used to represent characters, numbers, and other data
  - smallest addressable unit of memory in most computer architectures



- Important calculations
  - how many different values can be stored in 1 byte?
  - ullet ow many different values can be stored in n bits?

# Basic data types in C

The C language does not explicitly define data sizes. The actual sizes can vary depending on the compiler and the system architecture.

| C declaration |                               | Bytes  |        |
|---------------|-------------------------------|--------|--------|
| Signed        | Unsigned                      | 32-bit | 64-bit |
| [signed] char | unsigned char                 | 1      | 1      |
| short         | unsigned short                | 2      | 2      |
| int           | unsigned                      | 4      | 4      |
| long          | unsigned long                 | 4      | 8      |
| $int32\_t$    | $uint 32\_t$                  | 4      | 4      |
| $int 64\_t$   | $\mathrm{uint}64\_\mathrm{t}$ | 8      | 8      |
| char *        |                               | 4      | 8      |
| float         |                               | 4      | 4      |
| double        |                               | 8      | 8      |

### **Boolean algebra**

- Developed by George Boole in the 19th century
  - branch of mathematics dealing with binary variables and logic operations
  - · fundamental to digital circuit design and computer science
- Three basic logic operations
  - **AND**: output is 1 only if both inputs are 1 **conjunction**
  - **OR**: output is 1 if at least one input is 1 **disjunction**
  - NOT output is the opposite of the input negation
- Boolean expressions
  - formed by combining variables and logic operations

#### **Bit vectors**

- Sequences of bits that can represent various types of data
- Boolean algebra can be <u>extended</u> to operate on bit vectors
- Applications in Computer Science
  - · efficient set representation
  - · implementation of data structures
  - low-level programming and bitwise manipulation

Understanding boolean algebra with bit vectors is essential for working with binary data in computer science and digital design

## Bitwise operators in C

- Operate on "integer" data types
  - long, int, short, chart, unsigned variants
- Treat arguments as bit vectors
- Corresponding logic operators are applied bitwise to operands
- Commonly used to manipulate sets and masks

| ~  | bitwise NOT         | ~a     | the bitwise NOT of <b>a</b>              |
|----|---------------------|--------|--|
| &  | bitwise AND         | a & b  | the bitwise AND of ${f a}$ and ${f b}$   |
|    | bitwise OR          | a   b  | the bitwise OR of <b>a</b> and <b>b</b>  |
| ^  | bitwise XOR         | a ^ b  | the bitwise XOR of <b>a</b> and <b>b</b> |
| << | bitwise left shift  | a << b | <b>a</b> left shifted by <b>b</b>        |
| >> | bitwise right shift | a >> b | <b>a</b> right shifted by <b>b</b>       |

# **Bitwise operators in C**

| bit a | bit b | a & b (a AND b) |
|-------|-------|-----------------|
| 0     | 0     | 0               |
| 0     | 1     | 0               |
| 1     | 0     | 0               |
| 1     | 1     | 1               |

| bit a | bit b | alb (a OR b) |
|-------|-------|--------------|
| 0     | 0     | 0            |
| 0     | 1     | 1            |
| 1     | 0     | 1            |
| 1     | 1     | 1            |

| bit a | bit b | a ^ b (a XOR b) |
|-------|-------|-----------------|
| 0     | 0     | 0               |
| 0     | 1     | 1               |
| 1     | 0     | 1               |
| 1     | 1     | 0               |

~a (NOT a) is trivial

### **Examples**

#### **Practice**

~0×102

0xABC & 0x411

### **Practice**

0xABC | 0x411

0x102030 & 0x00FF00

# **Shift operations**

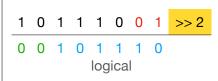
- Left shift (x << y)</p>
  - shifts each bit in x to the left by y positions
    - discards y bits on the left
  - fills y blank spaces on the right with zeros

## **Shift operations**

- Right shift (x >> y)
  - shifts each bit in x to the right by y positions
    - discards y bits on the right

Logical shift: fill blank spaces on left with zeroes

Arithmetic shift:
fill blank spaces by replicating
original MSB (most compilers
implement it — preserves sign bit)



#### **Practice**

$$0x9A >> 3$$
 (logical)

$$0x9A >> 3$$
 (arithmetic)

## **Example: bit masking**

- Assume an unsigned integer j that stores the value 0x1A35B127
  - define a mask to extract the most significant byte
  - write C code to store the extracted value in another variable (unsigned int)

# **Example: bit masking**

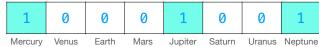
- Assume an integer j that stores the value 0x1A35B127
  - write C code to set the least significant byte of j to all ones leaving all other bytes unchanged

#### **Practice**

- Consider a genomic database
  - four DNA bases: Adenine (A), Cytosine (C), Thymine (T), and Guanine (G)
  - estimate the size in bytes of a text file storing a database of 100,000,000 DNA bases, assuming each base is represented as a single character (char)
- Determine the minimum number of bits required to uniquely represent each base
  - write a possible encoding, mapping each base to a specific bit pattern
- Assume DNA sequences are stored as integers (4 bytes)
  - calculate the maximum number of DNA bases that can be represented within a single integer
  - given the integer value 0x10012001, assuming your encoding, decode the corresponding DNA sequence
  - estimate the size in bytes of a binary file storing a database of 100,000,000 DNA bases

### **Encoding sets**

- Arrays can be inefficient for storing sets, especially when many elements are absent
  - use bits to represent membership, each bit corresponding to a unique object
- Example:
  - consider a set of 8 objects, a char variable, can represent all possible subsets



- Questions
  - · how to add, remove, or flip individual objects from the set?
  - how to check whether an object is in the set?
  - how to perform intersection, union, symmetric difference, and complement?

#### Show me the code

#### Show me the code

## Bitwise vs logical operators in C

- Bitwise operators
  - · operate on individual bits of integer values
  - operators: &, |, ^, ~, <<, >>
- Logical operators
  - operate on boolean values (true or false)
  - return a boolean value (true or false)
  - operators: !, &&, ||

any non-zero value
is considered true,
 zero is false

### **Practice**

!0xF3

!0x00

!!0xF3

~0xF3

0xF3 && 0xF1

0xF3 || 0xF1

0xF3 & 0xF1