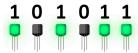
CSC 411

Computer Organization (Fall 2024) Lecture 3: Bitwise Operations

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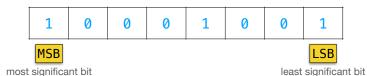
Bits

- Computers use the binary number system to represent and process data
- A bit (binary digit) is the smallest unit of data in computing
 - · can have a value of 0 or 1
 - · easy to implement in digital circuits
 - · forms the foundation for all digital information
- Bit Representation
 - bits are typically represented by electrical voltages in computer hardware
 - high voltage corresponds to 1 and low voltage to 0



Bytes

- A byte is a group of 8 bits
 - · commonly used to represent characters, numbers, and other data
 - smallest addressable unit of memory in most computer architectures



- Important calculations
 - how many different values can be stored in 1 byte?
 - ullet ow many different values can be stored in n bits?

Basic data types in C

The C language does not explicitly define data sizes. The actual sizes can vary depending on the compiler and the system architecture.

| C declaration | | Bytes | |
|---------------|-------------------------------|--------|--------|
| Signed | Unsigned | 32-bit | 64-bit |
| [signed] char | unsigned char | 1 | 1 |
| short | unsigned short | 2 | 2 |
| int | unsigned | 4 | 4 |
| long | unsigned long | 4 | 8 |
| $int32_t$ | $uint 32_t$ | 4 | 4 |
| $int 64_t$ | $\mathrm{uint}64_\mathrm{t}$ | 8 | 8 |
| char * | | 4 | 8 |
| float | | 4 | 4 |
| double | | 8 | 8 |

Boolean algebra

- Developed by George Boole in the 19th century
 - branch of mathematics dealing with binary variables and logic operations
 - · fundamental to digital circuit design and computer science
- Three basic logic operations
 - **AND**: output is 1 only if both inputs are 1 **conjunction**
 - **OR**: output is 1 if at least one input is 1 **disjunction**
 - NOT output is the opposite of the input negation
- Boolean expressions
 - formed by combining variables and logic operations

Bit vectors

- Sequences of bits that can represent various types of data
- Boolean algebra can be <u>extended</u> to operate on bit vectors
- Applications in Computer Science
 - · efficient set representation
 - · implementation of data structures
 - low-level programming and bitwise manipulation

Understanding boolean algebra with bit vectors is essential for working with binary data in computer science and digital design

Bitwise operators in C

- Operate on "integer" data types
 - long, int, short, chart, unsigned variants
- Treat arguments as bit vectors
- Corresponding logic operators are applied bitwise to operands
- Commonly used to manipulate sets and masks

| ~ | bitwise NOT | ~a | the bitwise NOT of a |
|----|---------------------|--------|--|
| & | bitwise AND | a & b | the bitwise AND of ${f a}$ and ${f b}$ |
| | bitwise OR | a b | the bitwise OR of a and b |
| ^ | bitwise XOR | a ^ b | the bitwise XOR of a and b |
| << | bitwise left shift | a << b | a left shifted by b |
| >> | bitwise right shift | a >> b | a right shifted by b |

Bitwise operators in C

| bit a | bit b | a & b (a AND b) |
|-------|-------|-----------------|
| 0 | 0 | 0 |
| 0 | 1 | 0 |
| 1 | 0 | 0 |
| 1 | 1 | 1 |

| bit a | bit b | alb (a OR b) |
|-------|-------|--------------|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 1 |

| bit a | bit b | a ^ b (a XOR b) |
|-------|-------|-----------------|
| 0 | 0 | 0 |
| 0 | 1 | 1 |
| 1 | 0 | 1 |
| 1 | 1 | 0 |

~a (NOT a) is trivial

Examples

Practice

~0×102

0xABC & 0x411

Practice

0xABC | 0x411

0x102030 & 0x00FF00

Shift operations

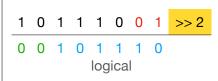
- Left shift (x << y)</p>
 - shifts each bit in x to the left by y positions
 - discards y bits on the left
 - fills y blank spaces on the right with zeros

Shift operations

- Right shift (x >> y)
 - shifts each bit in x to the right by y positions
 - discards y bits on the right

Logical shift: fill blank spaces on left with zeroes

Arithmetic shift:
fill blank spaces by replicating
original MSB (most compilers
implement it — preserves sign bit)



Practice

$$0x9A >> 3$$
 (logical)

$$0x9A >> 3$$
 (arithmetic)

Example: bit masking

- Assume an unsigned integer j that stores the value 0x1A35B127
 - define a mask to extract the most significant byte
 - write C code to store the extracted value in another variable (unsigned int)

Example: bit masking

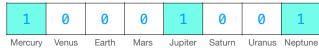
- Assume an integer j that stores the value 0x1A35B127
 - write C code to set the least significant byte of j to all ones leaving all other bytes unchanged

Practice

- Consider a genomic database
 - four DNA bases: Adenine (A), Cytosine (C), Thymine (T), and Guanine (G)
 - estimate the size in bytes of a text file storing a database of 100,000,000 DNA bases, assuming each base is represented as a single character (char)
- Determine the minimum number of bits required to uniquely represent each base
 - write a possible encoding, mapping each base to a specific bit pattern
- Assume DNA sequences are stored as integers (4 bytes)
 - calculate the maximum number of DNA bases that can be represented within a single integer
 - given the integer value 0x10012001, assuming your encoding, decode the corresponding DNA sequence
 - estimate the size in bytes of a binary file storing a database of 100,000,000 DNA bases

Encoding sets

- Arrays can be inefficient for storing sets, especially when many elements are absent
 - use bits to represent membership, each bit corresponding to a unique object
- Example:
 - consider a set of 8 objects, a char variable, can represent all possible subsets



- Questions
 - · how to add, remove, or flip individual objects from the set?
 - how to check whether an object is in the set?
 - how to perform intersection, union, symmetric difference, and complement?

Show me the code

```
enum Planet { MERCURY, VENUS, EARTH, MARS, JUPITER,
              SATURN, URANUS, NEPTUNE, NUM_PLANETS };
char add_planet(char set, enum Planet planet);
char remove_planet(char set, enum Planet planet);
char flip_planet(char set, enum Planet planet);
bool is_in_set(char set, enum Planet planet);
void print_set(char set);
int main() {
   char planets = 0;
   planets = add_planet(planets, EARTH);
    planets = add_planet(planets, MARS);
   planets = add_planet(planets, JUPITER);
   print_set(planets);
   planets = remove_planet(planets, MARS);
   print_set(planets);
   planets = flip_planet(planets, SATURN);
   print_set(planets);
   return 0;
```

Show me the code

Bitwise vs logical operators in C

- Bitwise operators
 - · operate on individual bits of integer values
 - operators: &, |, ^, ~, <<, >>
- Logical operators
 - operate on boolean values (true or false)
 - return a boolean value (true or false)
 - any non-zero value is considered true, zero is false
 - operators: !, &&, ||

Practice

!0xF3

!0x00

!!0xF3

~0xF3

0xF3 && 0xF1

0xF3 || 0xF1