

CSC 411

Computer Organization (Fall 2024)
Lecture 2: Number Systems

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Number systems

- A number system is a method for representing numbers
 - numbers are expressed in a certain **base**
- Importance in **CS**
 - to understand data representation in computers
 - to understand low-level programming and computer architecture
 - to learn how to optimize programs for performance and memory usage
- Common number systems in Computing
 - binary (base 2), decimal (base 10), hexadecimal (base 16)

Number systems

System	Base	Digits
Binary	2	0 1
Octal	8	0 1 2 3 4 5 6 7
Decimal	10	0 1 2 3 4 5 6 7 8 9
Hexadecimal	16	0 1 2 3 4 5 6 7 8 9 A B C D E F

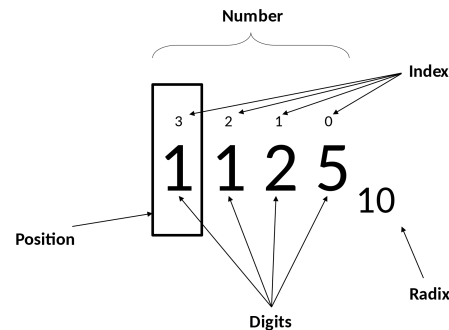
Number systems in Computing

- Binary system
 - directly represent "off" and "on" states in electronic circuits
 - facilitate efficient storage and manipulation of data
 - enables straightforward implementation of logical operations: AND, OR, NOT
- Hexadecimal system
 - compact representation of binary data
 - commonly used in modern computing for memory addresses and color codes

Humans think in **base 10**. Computers think in **base 2**.
Humans use **base 16** to easily manipulate data in **base 2**.

Positional notation

- Key concept for understanding all number systems
- The value of a digit depends on:
 - its value
 - its position in the numb
 - the base of the number



https://en.wikipedia.org/wiki/Positional_notation

Conversions to decimal

- Use positional notation
 - changing the base accordingly
- Key points:
 - the rightmost integer digit always has a weight of $b^0 = 1$
 - this method works for any base, making it a versatile tool
- Examples:

$$\begin{array}{l} 101010_2 \\ 1A2B_{16} \\ 137_8 \end{array} \longrightarrow \begin{array}{l} 42 \\ 6699 \\ 95 \end{array}$$

Conversions from decimal

▸ Method

- divide the number by the base
 - keep track of quotients and remainders
- repeat steps above until quotient becomes 0
- read the remainder digits **backwards**

Number	Result	Remainder
4123	2061	1
2061	1030	1
1030	515	0
515	257	1
257	128	1
128	64	0
64	32	0
32	16	0
16	8	0
8	4	0
4	2	0
2	1	0
1	0	1

1000000011011₂

Practice

- Convert 257 to binary
- Convert 411 to octal
- Convert 1023 to hexadecimal

Binary to hexadecimal

▸ Method

- group binary digits into sets of four, starting from the right
 - add leading zeros to the leftmost group if necessary
- convert each group into its hexadecimal equivalent

Dec	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Hex	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
Bin	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001	1010	1011	1100	1101	1110	1111

A **nibble** is a unit of digital information that consists of four bits. It represents **half of a byte**.

Practice

▸ Convert to hexadecimal:

- 10101011_2
- 11001101010101_2
- $10101010001001010010011_2$

Practice

▸ Hexadecimal to binary

- replace each hexadecimal digit with its 4-digit binary equivalent

▸ Solve:

$1A2B3C_{16}$

$FA1BFC_{16}$

Integer literals in C/C++

▸ Decimal literal

- **non-zero decimal digit**, followed by zero or more **decimal digits**

▸ Octal literal

- digit **zero** followed by zero or more **octal digits**

▸ Hex literal

- character sequence **0x** or the character sequence **0X** followed by one or more **hexadecimal digits**

▸ Binary literal

- character sequence **0b** or the character sequence **0B** followed by one or more **binary digits**

What is the output?

```
#include<stdio.h>

int main() {
    int d = 42;
    int o = 052;
    int x = 0x2a;
    int X = 0X2A;
    int b = 0b101010; // C++14

    printf("%d %d %d %d %d", d, o, x, X, b);

    return 0;
}
```