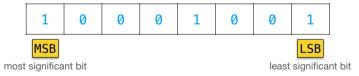
CSC 411

Computer Organization (Fall 2024) Lecture 3: Bitwise Operations

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Bytes

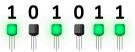
- ► A group of 8 bits is called a byte
 - bytes are commonly used to represent characters, numbers, and other data in computer systems



- → How many different values can be stored in 1 byte?
- ► How many different values can be stored in n bits?

Bits

- Computers use the binary system to represent data
- A bit is the smallest unit of data in computing
 - can have a value of 0 or 1, easy to embed in digital devices
 - bits are the building blocks, forming the foundation for all digital information
- Bit Representation
 - bits are often represented by electrical voltages, where high voltage corresponds to 1 and low voltage to 0



Basic data types in C

The C language does not explicitly define data sizes. The actual sizes can vary depending on the compiler and the system architecture.

C declaration		Bytes	
Signed	Unsigned	32-bit	64-bit
[signed] char	unsigned char	1	1
short	unsigned short	2	2
int	unsigned	4	4
long	unsigned long	4	8
$int32_t$	$uint 32_t$	4	4
$int64_t$	$uint 64_t$	8	8
char *		4	8
float		4	4
double		8	8

Boolean algebra

- Developed by George Boole in the 19th century
 - branch of mathematics that deals with binary variables and logic operations
 - · binary values represent logical states true or false
- Three fundamental logic operations
 - AND: output is 1 only if both inputs are 1 conjunction
 - **OR**: output is 1 if at least one input is 1 **disjunction**
 - **NOT** output is the opposite of the input **negation**
- Boolean expressions
 - · formed by combining variables and logic operations

Bit vectors

- Bit vectors are just sequences of bits
 - boolean algebra can be extended to operate on bit vectors
- Applications in Computer Science
 - · representing sets of elements efficiently
 - implementing data structures
 - performing bitwise manipulation in low-level programming

Understanding boolean algebra with bit vectors is essential for working with binary data in computer science and digital design

Basic boolean operations (AND, OR, NOT)

Logical operation	Operator	Notation	Alternative notations	Definition
Conjunction	AND	$x \wedge y$	x AND y, Kxy	$x \land y = 1 \text{ if } x = y = 1, x \land y = 0 \text{ otherwise}$
Disjunction	OR	$x \vee y$	x OR y, Axy	$x \lor y = 0$ if $x = y = 0$, $x \lor y = 1$ otherwise
Negation	NOT	¬ <i>x</i>	NOT x , N x , \overline{x} , x' , ! x	$\neg x = 0 \text{ if } x = 1, \ \neg x = 1 \text{ if } x = 0$

x	y	$x \wedge y$	xee y
0	0	0	0
1	0	0	1
0	1	0	1
1	1	1	1

x	$\neg x$
0	1
1	0

Bitwise operators in C

- Used with "integer" data types
 - · long, int, short, chart, unsigned
 - · arguments are treated as bit vectors
 - corresponding binary logic operators are applied bitwise to operands
- Bitwise operators are commonly used to manipulate sets and masks

~	bitwise NOT	~a	the bitwise NOT of a
&	bitwise AND	a & b	the bitwise AND of a and b
	bitwise OR	a b	the bitwise OR of a and b
^	bitwise XOR	a ^ b	the bitwise XOR of a and b
<<	bitwise left shift	a << b	a left shifted by b
>>	bitwise right shift	a >> b	a right shifted by b

Bitwise operators in C

bit a	bit b	a & b (a AND b)
0	0	0
0	1	0
1	0	0
1	1	1

bit a	bit b	alb (a OR b)
0	0	0
0	1	1
1	0	1
1	1	1

bit a	bit b	a ^ b (a XOR b)
0	0	0
0	1	1
1	0	1
1	1	0

~a (NOT a) is trivial

Examples





Practice

~0×102

0xABC & 0x411

Practice

0xABC | 0x411

0×102030 & 0×00FF00

Shift operations

- Left shift (x << y)</p>
 - shifts each bit in x to the left by the number of positions indicated by y
 - throw away y bits on left
 - · blank spaces on right are filled up by zeroes

Practice

$$0x9A >> 3$$
 (logical)

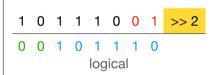
$$0x9A >> 3$$
 (arithmetic)

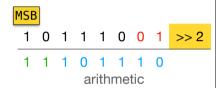
Shift operations

- Right shift (x >> y)
 - shifts each bit in x to the right by the number of positions indicated by y
 - throw away y bits on right

Logical shift: fill blank spaces on left with zeroes

Arithmetic shift: fill blank spaces by replicating original MSB (most compilers implement it preserves sign bit)





Example: bit masking

- Assume unsigned an integer j that stores the value 0x1A35B127
 - define a mask to extract the most significant byte
 - write C code to store the extracted value in another variable (unsigned int)

Example: bit masking

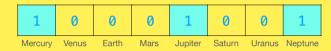
- Assume an integer j that stores the value 0x1A35B127
 - write C code to set the least significant byte of j to all ones leaving all other bytes unchanged

Practice

- ► Assume 4 DNA bases: A C T G
- How many bits are necessary per base? Write a possible encoding.
- If we store bases using integers (4 bytes), how many bases can we store in a single integer?
- Write the DNA sequence stored in 0x10012001

Example: encoding sets

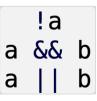
- Instead of using arrays, we can store information more efficiently using bits
- Example:
 - assume we are encoding sets (8 different objects)
 - we can use a char variable, such that each bit represents 1 object



- How to add, remove, or flip individual objects from the set?
- How to check whether an object is in the set?
- How to perform intersection, union, symmetric difference, and complement?

Bitwise vs logical operators in C

- Logical operators
 - NOT, AND, OR
 - apply to boolean values operands (true or false)
 - zero is considered false, and any non-zero value is considered true
 - · always return a boolean value (true or false)



Practice

!0xF3

!0x00

!!0xF3

0xF3 && 0xF1

0xF3 || 0xF1