CSC 411

Computer Organization (Spring 2024)
Lecture 4: Integers (signed, unsigned)

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The C Language

- Developed by Dennis Ritchie at Bell Labs in the early 1970s
- Many operating systems, including Unix and its variants (Linux), are written in C
- Allows low-level access to memory, making it efficient for system programming
- C programs are generally portable across different platforms with minimal modification
- C follows a traditional compilation process, where the source code is translated into machine code by a compiler



TIOBE Index for January 2024

- Indicator of the popularity of programming languages
 - popular search engines such as Google, Bing, Yahoo!, Wikipedia, Amazon, YouTube and Baidu are used to calculate the ratings.

Jan 2024	Jan 2023	Change	Progra	amming Language	Ratings	Change
1	1		•	Python	13.97%	-2.39%
2	2		9	С	11.44%	-4.81%
3	3		@	C++	9.96%	-2.95%
4	4		4.	Java	7.87%	-4.34%
5	5		0	C#	7.16%	+1.43%
6	7	^	JS	JavaScript	2.77%	-0.11%
7	10	^	php	PHP	1.79%	+0.40%
8	6	•	VB	Visual Basic	1.60%	-3.04%
9	8	•	SQL	SQL	1.46%	-1.04%
10	20	*		Scratch	1.44%	+0.86%

https://www.tiobe.com/tiobe-index/

Representing data

Representing data

- ► In memory, all values are stored as "bit-vectors"
 - data types are used to interpret the bits (provide meaning)
 - · each possible bit-vector assigned exclusively to one meaning
- In a bit sequence of w bits, we can represent 2^w different values
 - number of permutations with repetition given \boldsymbol{w} digits, there are two ways to choose each digit
 - example: how many different sequences can be represented in 4 bits?

$$2^4 = 16$$

Interlude: addition and multiplication

What is this program doing? #include <stdio.h> int main() { unsigned hex = 0x7e313134;

float *f = (float *) &hex;
char *s = (char *) &hex;

printf("%u %d %.4ef %c%c%c%c",

return 0; }

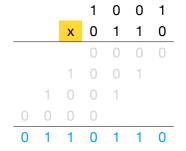
hex, hex, *f, s[0], s[1], s[2], s[3]);

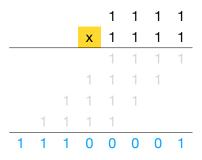
2117153076 2117153076 5.8882e+37f 411~

Binary addition

```
1 1 1
0 0 1 1 1 0 0 1
+ 0 1 1 1 0 1 1 0
1 0 1 0 1 1 1 1
```

Binary multiplication





Tricky? perform the addition row-by-row

Integer Representation (unsigned, signed)

Unsigned integers

- Bits represent the number directly
 - same as binary-to-decimal conversion
 - w bits can represent 2^w unsigned integers ranging from 0 to 2^w-1

```
      0 0 0 0 0 = 0
      1 0 0 0 = 8

      0 0 0 1 = 1
      1 0 0 1 = 9

      0 0 1 0 = 2
      1 0 1 0 = 10

      0 0 1 1 = 3
      1 0 1 1 = 11

      0 1 0 0 = 4
      1 1 0 0 = 12

      0 1 0 1 = 5
      1 1 0 1 = 13

      0 1 1 0 = 6
      1 1 1 0 = 14

      0 1 1 1 = 7
      1 1 1 1 = 15
```

Overflow

- Assume w = 8 is the bit-width
 - what happens if you try to add 1 to 11111111? => Overflow
 - there's no room for a number larger than 255!
- The arithmetic "wraps around" back to the beginning of the range
 - adding 1 to 255 in an 8-bit system results in 0 (leading bit is discarded)
 - this wrapping around behavior can be useful in certain situations
 - · applies to unsigned integers
 - basically taking the result $\mod 2^w$ or taking the lowest w bits

Overflow

- Occurs when the result of an operation is too large or too small to be represented within the allocated data type
 - in C, the runtime does not produce errors, values just "wrap"
- Can have consequences if not handled properly
 - · incorrect calculations
 - · program crashes due to unexpected behavior
 - security vulnerabilities
- To prevent overflow
 - choose appropriate data types with sufficient range
 - · implement checks and validations within the code

Gangnam Style music video 'broke' YouTube view limit

3 4 December 2014





YouTube said the video - its most watched ever - has been viewed more than **2,147,483,647** times. It has now changed the maximum view limit to **9,223,372,036,854,775,808**, or more than nine quintillion.

Zero-Day Alert: Google Chrome Under Active Attack, Exploiting New Vulnerability



Google has rolled out security updates to fix seven security issues in its Chrome browser, including a zero-day that has come under active exploitation in the wild.

Tracked as CVE-2023-6345, the high-severity vulnerability has been described as an integer overflow bug in Skia, an open source 2D graphics library.

A zero-day attack takes place when hackers exploit the flaw before developers have a chance to address it.

Signed integers

- Trivial approach (not used)
 - use MSB as the sign bit, and the remaining bits to represent the number
 - all possibilities using w = 3 bits:

 $0 \ 0 \ 0 = 0$ $0 \ 0 \ 1 = 1$

 $0 \ 1 \ 0 = 2$

0 1 1 = 3

100 = -0

110 = -

111 = -3

how is zero represented?

would addition still work? (try adding 001 and 110)

Going from x to -x (and vice-versa)

- ► One's complement of *x*:
 - flip all bits in *x*
 - called complement because x + -x = 11...11
- ► Two's complement of *x*
 - flip all bits in x and add 1 to the result
 - $\sim x + 1$ (apply bitwise)

Using w = 4 bits

Binary	Unsigned	One's complement	Two's complement
0000	0	+0	0
0001	1	1	1
0010	2	2	2
0011	3	3	3
0100	4	4	4
0101	5	5	5
0110	6	6	6
0111	7	7	7
1000	8	-7	-8
1001	9	-6	-7
1010	10	-5	-6
1011	11	-4	-5
1100	12	-3	-4
1101	13	-2	-3
1110	14	-1	-2
1111	15	-0	-1

Practice

Convert from x to -x using two's complement

The most negative number

- Exceptions to $\sim x + 1$
 - · zero becomes zero (overflow)
 - the most negative number does not have a positive counterpart impossible to represent (overflow)
- Can lead to unexpected programming bugs
 - the unary negation operator, -(-128) becomes -128
 - the absolute value may return a negative number, abs(-128) becomes -128
 - multiplication by -1 may fail, -128 * -1 becomes -128
 - division by -1 may cause an exception, -128 / -1 crashes
- In C the above behaviors are undefined

From two's complement to decimal

$$\sum_{i=0}^{w-1} x_i 2^i - x_{w-1} 2^{w-1} + \sum_{i=0}^{w-2} x_i 2^i$$

Conversion to decimal for unsigned representations

Conversion to decimal for two's complement representations

Although C does not mandate using two's complement, in practice, two's complement is the **most widely used** representation for signed integers in modern computer systems.

Two's complement (summary)

- ► Sign bit (MSB)
 - 0 for nonnegative, 1 for negative
- Non-negative numbers
 - no changes from the unsigned representation
- Negative numbers
 - two's complement of their positive counterparts
 - equivalent to their one's complement plus one

Binary	Unsigned	Signed (two's complement)
01010101	85	85
10101011	171	-85

Practice

Convert from two's complement to decimal

```
-32 16 8 4 2 1
0 0 1 1 1 0 =
1 1 0 0 0 0 =
1 0 0 0 0 0 0 =
1 1 1 1 1 1 0 =
0 0 0 0 0 0 0 =
0 0 0 0 0 0 1 =
0 1 1 1 1 1 1 =
```

Two's complement (advantages)

- Addition and subtraction of signed integers
 - use the same hardware as their unsigned counterparts
 - no need for special/additional circuitry
- Single representation for zero
 - · no negative zero
- Trivial operation for extending the sign bit
 - e.g. increasing the bit-width of a number (casting)
- Widespread adoption

Numeric ranges

Unsigned representation

• min => 00...00
$$0$$

• max => 11...11 $2^{w} - 1$

Signed representation (two's complement)

```
• min => 10...00 -2^{w-1}
• max => 01...11 2^{w-1} - 1
```

data type	binary	hexadecimal	decimal
unsigned short int (min)			
unsigned short int (max)			
short int (min)			
short int (max)			

Range of values

Data type	Size	Format	Value range
character	8	signed	-128 to 127
		unsigned	0 to 255
integer	16	signed	-32768 to 32767
		unsigned	0 to 65535
	32	signed	-2,147,483,648 to 2,147,483,647
		unsigned	0 to 4,294,967,295
	64	signed	-9,223,372,036,854,775,808 to 9,223,372,036,854,775,807
		unsigned	0 to 18,446,744,073,709,551,615

https://en.cppreference.com/w/cpp/language/types

Basic data types in C

- ► The C standard does not define the size of "integer" types, except char
 - much safer to use intN_t and uintN_t for signed and unsigned integers of different sizes (stdint.h)
- The type of each variable tells the compiler how many bytes are necessary in memory
 - necessary for translation of high level code into machine code