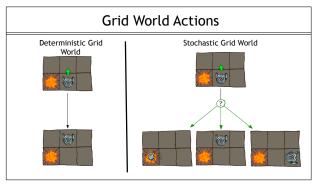
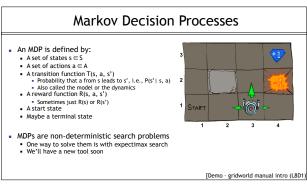


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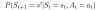


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What is Markov about MDPs?

- "Markov" generally means that given the present state, the future and the past are independent
- For Markov decision processes, "Markov" means action outcomes depend only on the current state

$$P(S_{t+1} = s' | S_t = s_t, A_t = a_t, S_{t-1} = s_{t-1}, A_{t-1}, \dots S_0 = s_0)$$
=



 This is just like search, where the successor function could only depend on the current state (not the history)



Andrey Markov

Policies

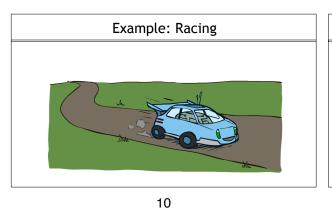
- In deterministic single-agent search problems, we wanted an optimal plan, or sequence of actions, from start to a goal
- For MDPs, we want an optimal policy π^* : $S \to A$
- A policy π gives an action for each state
- An optimal policy is one that maximizes expected utility if followed
- An explicit policy defines a reflex agent
- Expectimax didn't compute entire policies
 It computed the action for a single state only

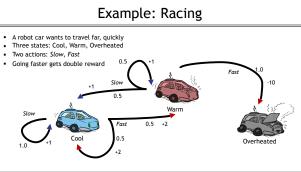


Optimal policy when R(s, a, s') = -0.03 for all non-terminals s

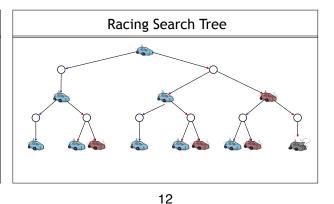
Optimal Policies R(s) = -0.04 R(s) = -2.0

7 8 9



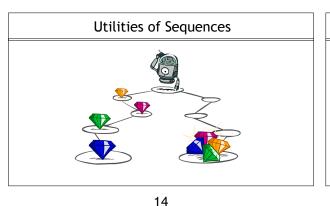


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MDP Search Trees • Each MDP state projects an expectimax-like search tree (s,a,s') called a transition T(s,a,s') = P(s'|s,a)R(s,a,s')

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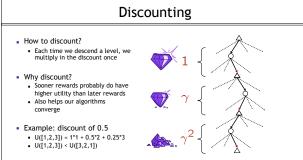


Utilities of Sequences • What preferences should an agent have over reward sequences? • More or less? [1, 2, 2] or [2, 3, 4] • Now or later? [0, 0, 1] or [1, 0, 0]

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Discounting





Stationary Preferences • Theorem: if we assume stationary preferences: $[a_1, a_2, \ldots] \succ [b_1, b_2, \ldots]$ $[r, a_1, a_2, \ldots] \succ [r, b_1, b_2, \ldots]$ • Then: there are only two ways to define utilities - Additive utility: $U([r_0,r_1,r_2,\ldots])=r_0+r_1+r_2+\cdots$ \bullet Discounted utility: $U([r_0,r_1,r_2,\ldots])=r_0+\gamma r_1+\gamma^2 r_2\cdots$

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Quiz: Discounting

Given:

10		\otimes	1

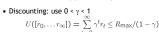
- Actions: East, West, and Exit (only available in exit states a, e)
- Transitions: deterministic
- Quiz 1: For $\gamma = 1$, what is the optimal policy?

?	10		\otimes	1

- Quiz 2: For γ = 0.1, what is the optimal policy? 10
- Quiz 3: For which γ are West and East equally good when in state d?

Infinite Utilities?!

- Problem: What if the game lasts forever? Do we get infinite rewards?
- Solutions:
 - Finite horizon: (similar to depth-limited search)
 - Terminate episodes after a fixed T steps (e.g. life)
 - Gives nonstationary policies (π depends on time left)



- Absorbing state: guarantee that for every policy, a terminal state will eventually be reached (like "overheated" for racing)

Recap: Defining MDPs

- Markov decision processes:
- Set of states S
- Start state s₀
- Set of actions A
- Transitions P(s'|s,a) (or T(s,a,s'))
 Rewards R(s,a,s') (and discount γ)



- MDP quantities so far:
 - Policy = Choice of action for each state
 - Utility = sum of (discounted) rewards

19 20 21

Solving MDPs

