

Find  $h[n]$   
Partial Fraction Expansion

$$H(z) = \frac{2}{(1 + 0.5z^{-1})(1 - 0.5z^{-1})} = \frac{A}{1 + 0.5z^{-1}} + \frac{B}{1 - 0.5z^{-1}}$$

To Find A,

1. multiply by  $1 + 0.5z^{-1}$
2. let  $z = -0.5$

$$\frac{2}{\cancel{(1 + 0.5z^{-1})}(1 - 0.5z^{-1})} = \frac{A \cancel{(1 + 0.5z^{-1})}}{\cancel{1 + 0.5z^{-1}}(1 - 0.5z^{-1})} + \frac{B(1 + 0.5z^{-1})}{(1 - 0.5z^{-1})}$$

$$\frac{2}{1 - 0.5/(-0.5)} = A + B \frac{(1 + 0.5/(-0.5))}{1 - 0.5/(-0.5)} \quad \leftarrow \text{term} = \text{ZERO}$$

$$\boxed{1 = A}$$

Then do the same thing to find B

$$\boxed{B = 1}$$

so

$$H(z) = \frac{1}{1 + 0.5z^{-1}} + \frac{1}{1 - 0.5z^{-1}}$$

using table

$$\boxed{h[n] = (-0.5)^n u[n] + (0.5)^n u[n]}$$