

More on the FFT: the amazing Butterfly

Sorry if we got bogged down today in class on Figure 10-11 from Ziemer.

Normally after hitting the high points of the 8 point FFT structure, I go over the simplest case: the two point DFT ($N=2$), also known as the **Butterfly**. From here we then show how a 4 point DFT ($N=4$) can be made from 2 stages of butterflies.... Then show how this process can be repeated to make an 8-point FFT (fig 10-11) (or 3 stages of butterflies). ... and then this can be extended on and on and on....

Your textbook, I&J, does this in Section 3.5, starting on page 121. Figures 3.4 and 3.5 illustrate the butterflies. (note: he draws the “flow graph” in a different style than Ziemer)

Speaking of Ziemer (if you don’t like I&J’s notation), in section 10-3, starting on page 492, he does the same thing. [this chapter is posted on the [website under lesson 10](#) if you can’t seem to find your Ziemer text]. Figure 10-5 he illustrates the 2-point butterfly. Example 10-4 and Figure 10-6 he illustrates the 4-point DFT. Then in Section 10-4, he goes through the mathematical derivation of the FFT, showing how the generic DFT can be decomposed into several stages of simple butterflies.

How about that $N\log(N)$ thing?

Ziemer discusses this at the bottom of page 502. [Cadet Miller](#), check out equation 10-48. I&J discuss the speed up and computation issues on page 121 and on page 132.

These readings are most fascinating!