

7.1 The frequency response, $H(\omega)$, of a type 2, linear phase Fir filter may be expressed as (see Table 7.1)

$$H(\omega) = e^{-j\omega(N-1)/2} \sum_{n=1}^{N/2} b(n) \cos[\omega(n - \frac{1}{2})]$$

where $b(n)$ is related to the filter coefficients. Explain why filters with the response above are unsuitable as high pass filters. Use a simple case (such as $N=4$) to illustrate your answer.

Solution

The impulse responses for Type 2 filters have positive symmetry and even length. The corresponding frequency responses are always zero at half the sampling frequency ($F_s/2$) which is at the high frequency end. Thus, Type 2 filters are unsuitable as high pass filters. This point can be illustrated using the above expression for $N=4$ (where we have introduced T to highlight the link to the sampling frequency):

$$\begin{aligned} H(\omega T) &= e^{-j3\omega(N-1)/2} \sum_{n=1}^2 b(n) \cos[\omega(n - \frac{1}{2})T] \\ &= e^{-j3\omega T/2} [b(1) \cos(\omega T/2) + b(2) \cos(3\omega T/2)] \end{aligned}$$

At half the sampling frequency, $f = 1/2T$ and

$$H(\omega T) \Big|_{f=\frac{1}{2T}} = e^{-j\pi/2} [b(1) \cos(\pi/2) + b(2) \cos(3\pi/2)] = 0.$$