

## Window Characteristics<sup>a</sup>

Window (length N)	Main Lobe Width	Side-lobe Level (dB)	Transition Bandwidth	Passband Ripple (dB)	Stopband Attenuation (dB)
rectangular	$4\pi/N$	-13.5	$1.8\pi/N$	0.75	21
Bartlett	$8\pi/N$	-27	$6.1\pi/N$	0.45	25
von Hann	$8\pi/N$	-32	$6.2\pi/N$	0.055	44
Hamming	$8\pi/N$	-43	$6.6\pi/N$	0.019	53
Blackman	$12\pi/N$	-57	$11\pi/N$	0.0017	74

<sup>a</sup>Other window names: rectangular=boxcar, Bartlett=triangular, von Hann=Hann=Hanning. NA: the von Sump window is a figment of my imagination and yet to be invented.

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## Common $z$ -Transforms

$x[n]$	$X^z(z)$	ROC
$\delta[n]$	1	All $z$
$u[n]$	$\frac{1}{1 - z^{-1}}$	$ z  > 1$
$a^n u[n]$	$\frac{1}{1 - az^{-1}}$	$ z  >  a $
$na^n u[n]$	$\frac{az^{-1}}{(1 - az^{-1})^2}$	$ z  >  a $
$-a^n u[-n - 1]$	$\frac{1}{1 - az^{-1}}$	$ z  <  a $
$-na^n u[-n - 1]$	$\frac{az^{-1}}{(1 - az^{-1})^2}$	$ z  <  a $
$\cos(\theta_0 n) u[n]$	$\frac{1 - z^{-1} \cos(\theta_0)}{1 - 2z^{-1} \cos(\theta_0) + z^{-2}}$	$ z  > 1$
$\sin(\theta_0 n) u[n]$	$\frac{z^{-1} \sin(\theta_0)}{1 - 2z^{-1} \cos(\theta_0) + z^{-2}}$	$ z  > 1$
$a^n \cos(\theta_0 n) u[n]$	$\frac{1 - az^{-1} \cos(\theta_0)}{1 - 2az^{-1} \cos(\theta_0) + a^2 z^{-2}}$	$ z  >  a $
$a^n \sin(\theta_0 n) u[n]$	$\frac{az^{-1} \sin(\theta_0)}{1 - 2az^{-1} \cos(\theta_0) + a^2 z^{-2}}$	$ z  >  a $

$$X(z) = \sum_{n=-\infty}^{\infty} x[n] z^{-n}$$

$$w' = \frac{2}{T} \tan\left(\frac{\theta}{2}\right)$$

$$\theta = 2 \tan^{-1}\left(\frac{T}{2} \cdot w'\right)$$

$$s = \frac{2}{T} \left( \frac{1 - z^{-1}}{1 + z^{-1}} \right)$$

$$z = -\left( \frac{s + \frac{2}{T}}{s - \frac{2}{T}} \right)$$

Type	I	II	III	IV
Order (length)	even (odd)	odd (even)	even (odd)	odd (even)
Symmetry of $h[n]$	symmetric	symmetric	anti-symmetric	anti-symmetric
Symmetry of $A(\theta)$	symmetric	symmetric	anti-symmetric	anti-symmetric
Period of $A(\theta)$	$2\pi$	$4\pi$	$2\pi$	$4\pi$
$\phi_0$	0	0	$0.5\pi$	$0.5\pi$
$F(\theta)$ in (9.23)	1	$\cos(0.5\theta)$	$\sin \theta$	$\sin(0.5\theta)$
$K$ in (9.23)	$N/2$	$(N-1)/2$	$(N-2)/2$	$(N-1)/2$
$g[n]$ in (9.23)	see (9.5)	see (9.10)	see (9.16)	see (9.21)
$H^f(0)$	arbitrary	arbitrary	0	0
$H^f(\pi)$	arbitrary	0	0	arbitrary
Uses	LP, HP, BP, BS, Multiband filters	LP, BP	Differentiators, Hilbert transformers	

Table 9.1 Properties and parameters of the four FIR filter types.