<u>Background:</u> A function called a "raised cosine" is a useful pulse shape in communications because it has many fewer high-frequency side lobes than a rectangular pulse, thus requires less bandwidth. The raised cosine can be expressed as:

$$f(t) = \begin{cases} 1 + \cos(2\pi t) & |t| < 0.5 \\ 0 & \text{elsewhere} \end{cases}$$

- 1. Sketch f(t) by hand or with a graphing resource (website, etc. be sure to include in Doc statement!). It looks sort of Gaussian doesn't it? Look up the Fourier transform of a Gaussian, which is also a Gaussian, and sketch it by hand or with a graphing resource. A Gaussian pulse has very small tails (i.e., fewer higher frequency terms) in both the time and frequency domain!
- 2. Plot the raised cosine pulse, f(t) over the interval  $-1 \le t \le 1$ , using Python or MATLAB. There are different approaches, but here is one approach in MATLAB:

3. Mathematically (using the Fourier coefficient integral) find the exponential Fourier-series coefficients,  $F_n$ , for the raised-cosine pulse, over the interval (-1,1), where

$$f(t) = \sum_{n=-N}^{N} F_n e^{jn\omega_0 t}$$

- 4. Using Python or MATLAB, plot the signal defined by your answer to Problem 3 **superimposed** over your plot from Problem 2 for N = 1, N = 2, N = 3, and  $N = N_{perfect}$ , where  $N_{perfect}$  is the value of N where the sum nearly matches the plot perfectly (as subjectively determined by you). What is your value of  $N_{perfect}$ ? Include your code along with your 4 figures.
- 5. Repeat Problem 4 over the interval (-5, 5). How does your plot differ from the original signal that you plotted in Problems 2 and 4? Explain.