Robot Learning

Learning from human feedback





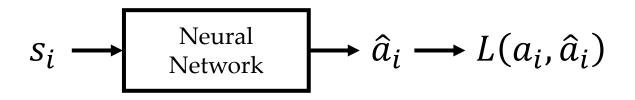
Last time...

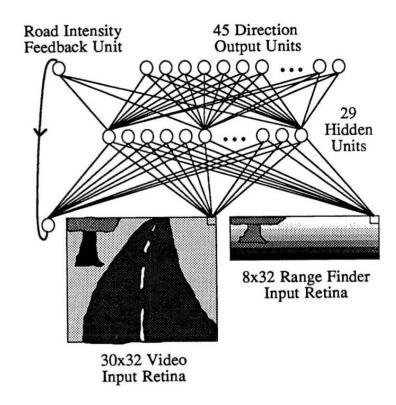
Imitation learning

- Inverse reinforcement learning (IRL)
 - Apprenticeship learning
 - Maximum margin planning
 - Max-Ent IRL

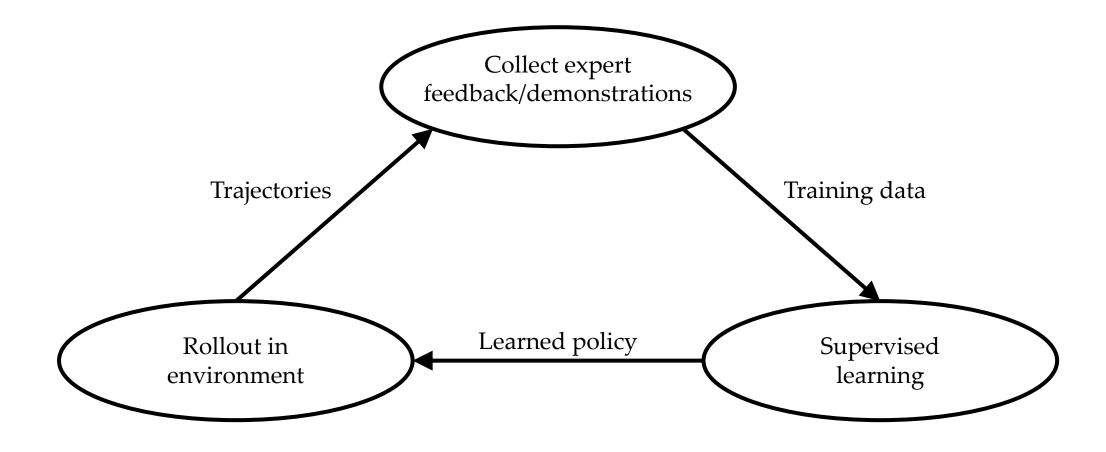
Behavioral cloning

Train a neural network to map states into expert actions.





Direct policy learning



Apprenticeship learning

We iteratively improve the learned *w* and policy.

Compute the optimal features $\phi(\pi^*)$

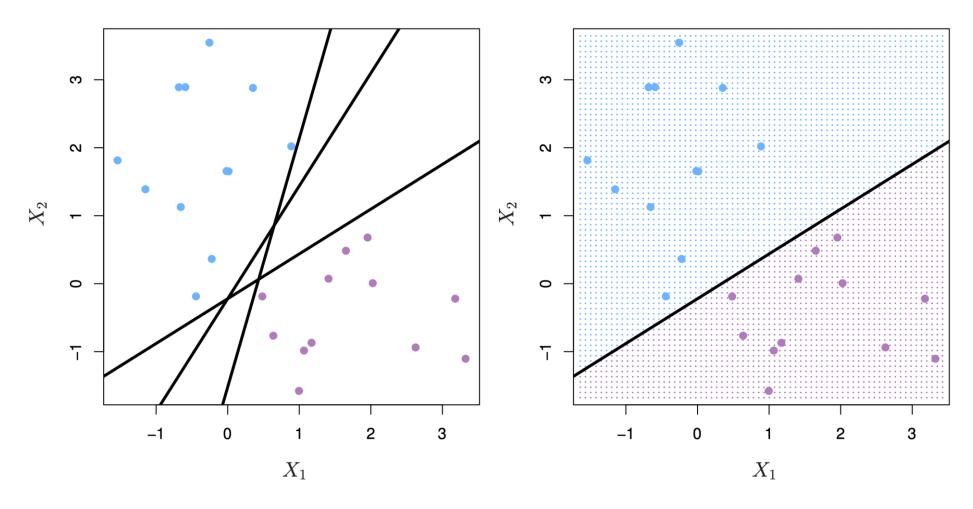
Initialize a policy π_0

Loop i = 0,1,...:

Find w_i that best separates π^* from π_i

Assuming w_i is true weights, learn π_{i+1} optimizing the reward

Maximal margin classifiers



Maximum margin planning (MMP)

Let's allow the expert to be suboptimal by adding a slack variable.

We could also be more tolerant to the policies that are similar to π^* .

```
minimize ||w||_2 + Cv
subject to w^T \phi(\pi^*) - w^T \phi(\pi) \ge 1 - v + d(\pi^*, \pi) for all \pi \ne \pi^*
```

Max-Ent IRL

- 1. Initialize w
- 2. Perform RL to learn a policy that optimizes the reward with w
- 3. Roll out the learned policy to compute:

$$w \leftarrow w - \mathbb{E}_{\xi \sim P(\xi|w)}[\phi(\xi)] - \phi(\pi^*)$$

4. Repeat from step 2

Max-Ent IRL

Assumption: Experts are noisily optimal, i.e., the probability that they demonstrate trajectory ξ is:

$$P(\xi \mid w) = \frac{\exp(w^{\mathsf{T}}\phi(\xi))}{\int \exp(w^{\mathsf{T}}\phi(\xi')) d\xi'}$$

where $\phi(\xi)$ is the cumulative discounted features of trajectory ξ .

Today...

- Learning from human feedback
 - Suboptimal demonstrations
 - Pairwise comparisons
 - Reinforcement learning from human feedback (RLHF)

Assume we have some (partial) ranking over expert demonstrations. How would that help?

Demonstrations

$$\xi_1 = (s_0^1, a_0^1, s_1^1, a_1^1, \dots)$$

$$\xi_2 = (s_0^2, a_0^2, s_1^2, a_1^2, \dots)$$

•

$$\xi_L = (s_0^L, a_0^L, s_1^L, a_1^L, \dots)$$

Scores

 β_{1}

 β_2

•

.

 β_L

Update Scores

Imitation Learning / IRL Model Inner Loss

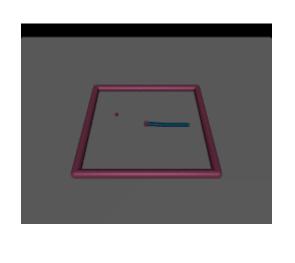
Update Model

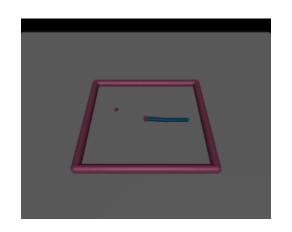
Outer Loss

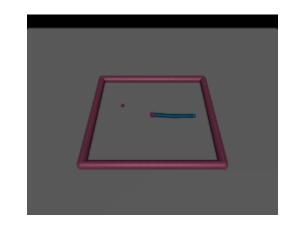
Confidence Ranking

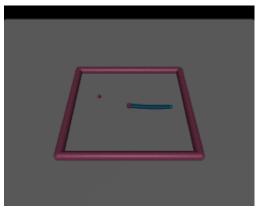
$$\xi_5 \geqslant \xi_8 \geqslant \xi_1 \geqslant \xi_6$$

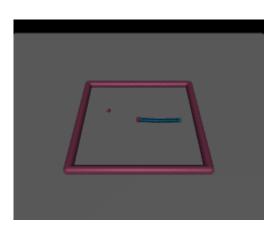
- Inner loss to learn a policy / reward
 - Uses the demonstrations ξ_i weighted with their confidence scores β_i
 - Learns a policy (or a reward function)
- Outer loss to learn confidence scores
 - Evaluates how well the demonstrations match the given (partial) ranking under the learned policy (or reward) to update β_i 's.

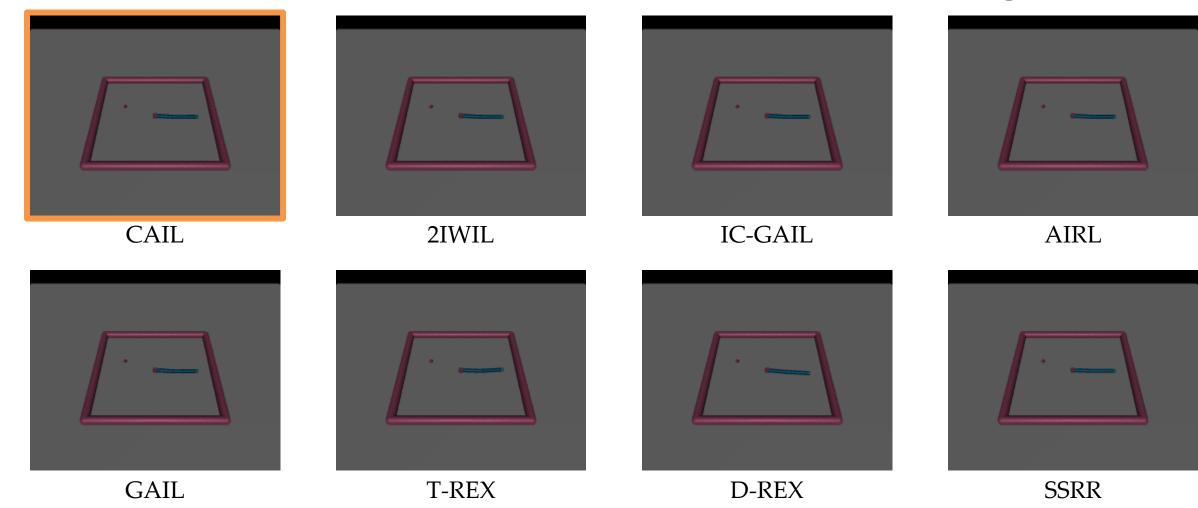












Further questions to think about

- What if the demonstrators' suboptimality is context-dependent?
 - Example: I can teleoperate a robot well in coarse actions, but I am not good at precise manipulation motions.
- How do we choose the expert to query if we have that ability?

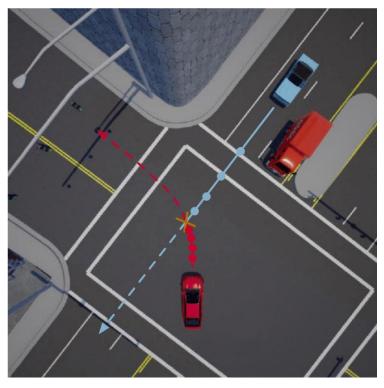
Today...

- Learning from human feedback
 - Suboptimal demonstrations
 - Pairwise comparisons
 - Reinforcement learning from human feedback (RLHF)

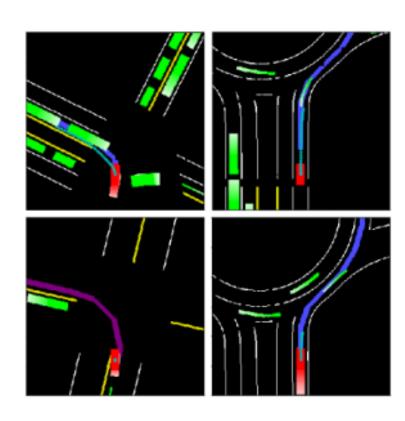
Learning from demonstrations (LfD)



Codevilla et al. ICRA'18



Cao et al. RSS'20



Chen et al. IROS'19

Why does LfD fail?

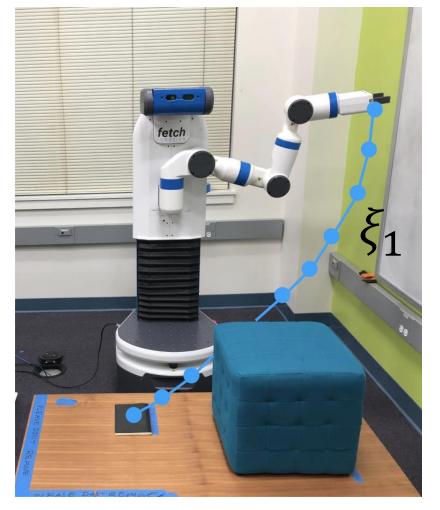
Demonstrations: $\mathbf{D} = \{\xi_1, \xi_2, ..., \xi_L\}$

Trajectory features: $\phi(\xi_i) = \phi_i \in \mathbb{R}^d$

- Final distance to the notebook
- Minimum distance to the obstacle
- Average speed

- ...

Reward function : $R(\xi_i) = f_{\underline{w}}(\phi_i)$



Bayesian inverse reinforcement learning

$$\operatorname{argmax} P(w \mid \mathcal{D})$$

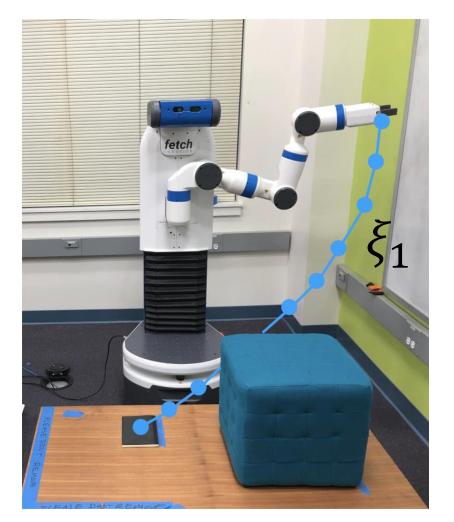
$$P(w \mid \mathcal{D}) \propto P(w) P(\mathcal{D} \mid w)$$

$$= P(w) \prod_{i=1}^{L} P(\xi_i \mid w)$$



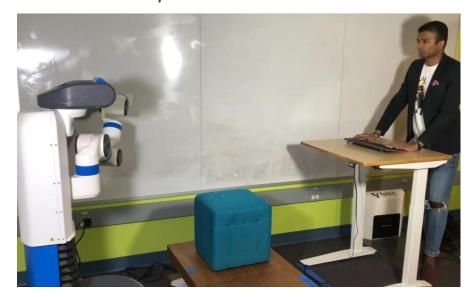
$$\propto P(w) \prod_{i=1}^{L} \exp f_w(\xi_i)$$

(Noisy humans)



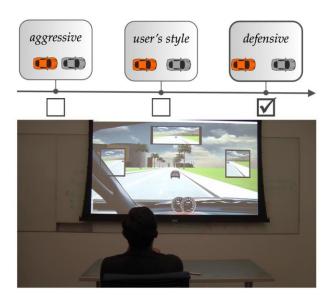
Humans are Suboptimal

Robots with high degrees of freedom are hard to teleoperate.



Palan et al. RSS'19

Humans do not like their own demonstrations.



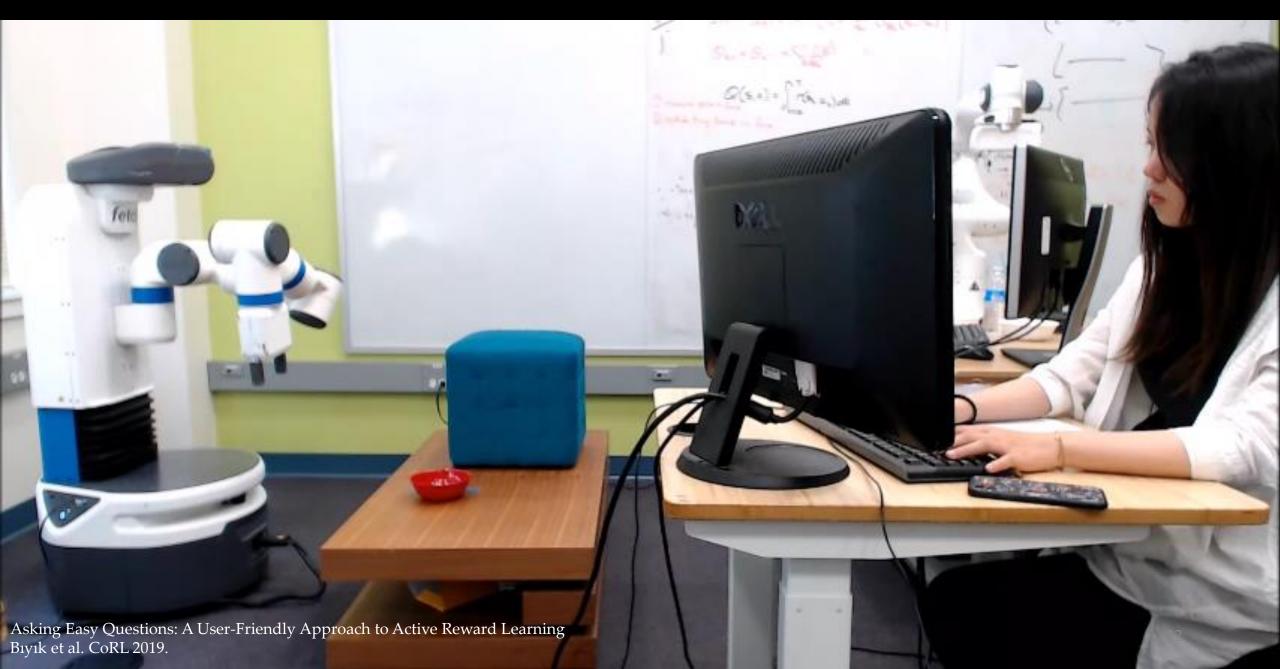
Basu et al. HRI'17

Humans take suboptimal actions in risky situations.



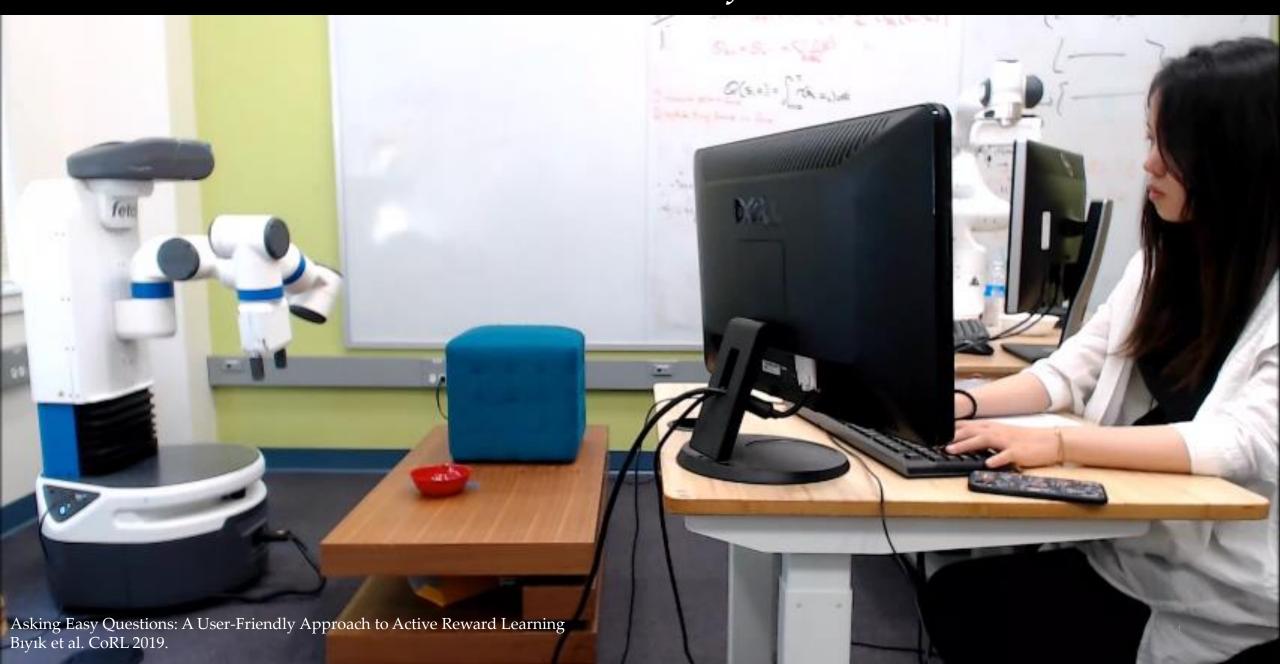
Kwon et al. HRI'20

We can let the human evaluate a robot demonstration



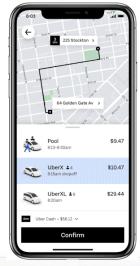
How dark is this blue?

Human evaluations are often unreliable

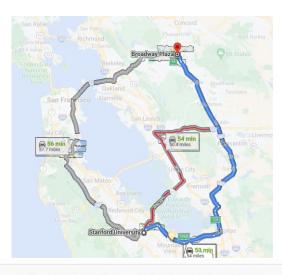


Which blue is darker?

Comparison data











Café Nim 71K views • 5 years ago







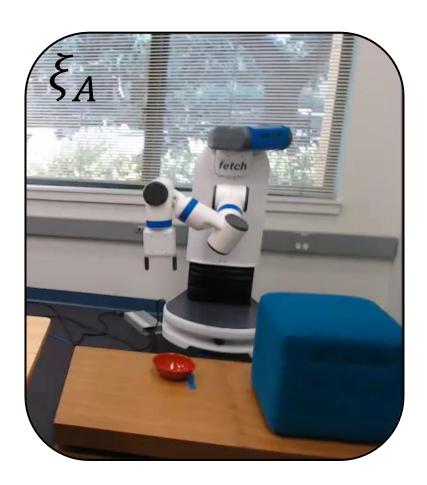


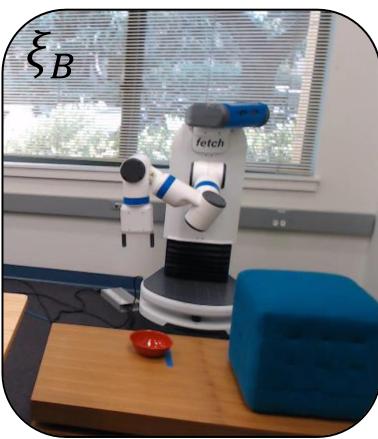
Unicorn Darts 6.6M views • 4 years ago



Carlsen - Nepomniachtchi | Game 8 | World Chess Championship | Howell,... chess24 2 24K watching

Incorporating Comparisons





 ξ_A or ξ_B ?



Incorporating Comparisons

Demonstrations: $\mathbf{D} = \{\xi_1, \xi_2, ..., \xi_L\}$

Comparisons:
$$C = \{ (\xi_A^{(1)}, \xi_B^{(1)}, q^{(1)}), \dots, (\xi_A^{(N)}, \xi_B^{(N)}, q^{(N)}) \}$$

Trajectory features: $\phi(\xi_i) = \phi_i \in \mathbb{R}^d$

- Final distance to the notebook
- Minimum distance to the obstacle
- Average speed

- . . .

Reward function : $R(\xi_i) = f_{\underline{w}}(\phi_i)$

Incorporating Comparisons

$$\underset{w}{\operatorname{argmax}} P(w \mid \mathcal{D}, \mathcal{C})$$

$$P(w \mid \mathcal{D}, \mathcal{C}) \propto P(w)P(\mathcal{D} \mid w)P(\mathcal{C} \mid w)$$

$$= P(w) \prod_{i=1}^{L} P(\xi_i \mid w) \left(\prod_{i=1}^{N} P\left(q^{(i)} \mid w, \xi_A^{(i)}, \xi_B^{(i)} \right) \right)$$
How do we compute this?

- Inner loss to learn a policy / reward
 - Uses the demonstrations ξ_i weighted with their confidence scores β_i
 - Learns a policy (or a reward function)
- Outer loss to learn confidence scores
 - Evaluates how well the demonstrations match the given (partial) ranking under the learned policy (or reward) to update β_i 's.

How does this exactly work?

Given a reward w, what's the probability that the human gives that ranking?

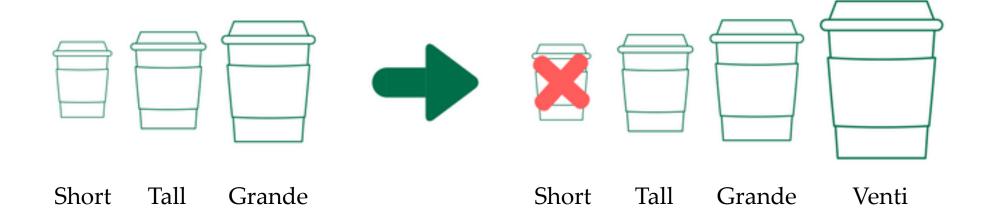
Luce's choice axiom

The probability of selecting one item over another from a pool of many items is not affected by the presence or absence of other items in the pool.

Selection of this kind is said to have *independence from irrelevant* alternatives.

Counterexamples for fun

• Starbucks: "Compromise Effect"



From: Kent Hendricks CSCI 699: Robot Learning - Lecture 6 32

Counterexamples for fun

• Coca Cola vs. Pepsi







1985 (Spring) (was successful only in LA)



1985 (Summer)

Regardless...

The probability of selecting one item over another from a pool of many items is not affected by the presence or absence of other items in the pool.

Selection of this kind is said to have *independence from irrelevant* alternatives.

Corollary

$$P(\xi_i \geqslant \xi_j \geqslant \xi_k) = P(\xi_i \geqslant \xi_j, \xi_k) P(\xi_j \geqslant \xi_k)$$

We only need to model the probability that the human chooses trajectory ξ over a pool of many trajectories.

Incorporating comparisons

$$\underset{w}{\operatorname{argmax}} P(w \mid \mathcal{D}, \mathcal{C})$$

$$P(w \mid \mathcal{D}, \mathcal{C}) \propto P(w)P(\mathcal{D} \mid w)P(\mathcal{C} \mid w)$$

$$= P(w) \prod_{i=1}^{L} P(\xi_i \mid w) \left(\prod_{i=1}^{N} P\left(q^{(i)} \mid w, \xi_A^{(i)}, \xi_B^{(i)} \right) \right)$$
How do we compute this?

Models from discrete choice theory

$$P(q \mid w, \xi_A, \xi_B)$$

Thurstonian Model:

• Add Gaussian noise to the rewards:

•
$$u_A = f_w(\phi(\xi_A)) + z_A$$

•
$$u_B = f_w(\phi(\xi_B)) + z_B$$

where z_A , $z_b \sim \mathcal{N}(0, \sigma^2)$.

• The human choice is the noisy winner:

•
$$q = \begin{cases} A, & if \ u_A > u_B \\ B, & otherwise \end{cases}$$

$$P(q = A) = P(u_A > u_B)$$

$$= P(f_w(\phi(\xi_A)) + z_A > f_w(\phi(\xi_B)) + z_B)$$

$$= P(z_A - z_B > f_w(\phi(\xi_B)) - f_w(\phi(\xi_A)))$$

Models from discrete choice theory

$$P(q \mid w, \xi_A, \xi_B)$$

Bradley-Terry Model:

• The probability that the user chooses an option is proportional to the exponentials of the rewards:

$$P(q = A) = \frac{e^{\beta f_w(\phi(\xi_A))}}{e^{\beta f_w(\phi(\xi_A))} + e^{\beta f_w(\phi(\xi_B))}}$$

Incorporating comparisons

$$\underset{w}{\operatorname{argmax}} P(w \mid \mathcal{D}, \mathcal{C})$$

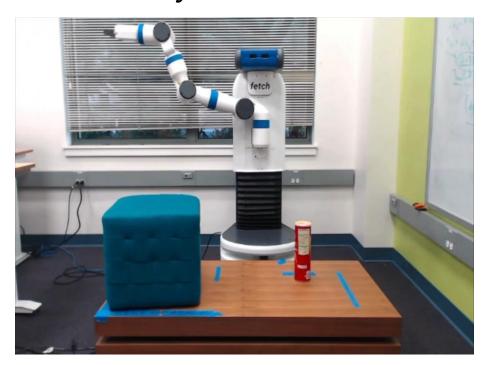
$$P(w \mid \mathcal{D}, \mathcal{C}) \propto P(w)P(\mathcal{D} \mid w)P(\mathcal{C} \mid w)$$

$$= P(w) \prod_{i=1}^{L} P(\xi_i \mid w) \prod_{i=1}^{N} P(q^{(i)} \mid w, \xi_A^{(i)}, \xi_B^{(i)})$$

$$\propto P(w) \prod_{i=1}^{L} \exp f_{w}(\xi_{i}) \prod_{i=1}^{N} \frac{\exp f_{w}(\xi_{q^{(i)}})}{\exp f_{w}(\xi_{q^{(i)}}^{(i)}) + \exp f_{w}(\xi_{\neg q^{(i)}}^{(i)})}$$

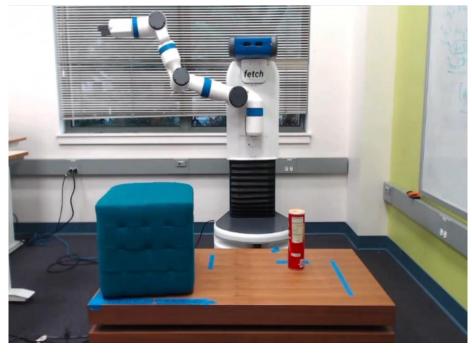
Benefit of comparisons

Bayesian IRL

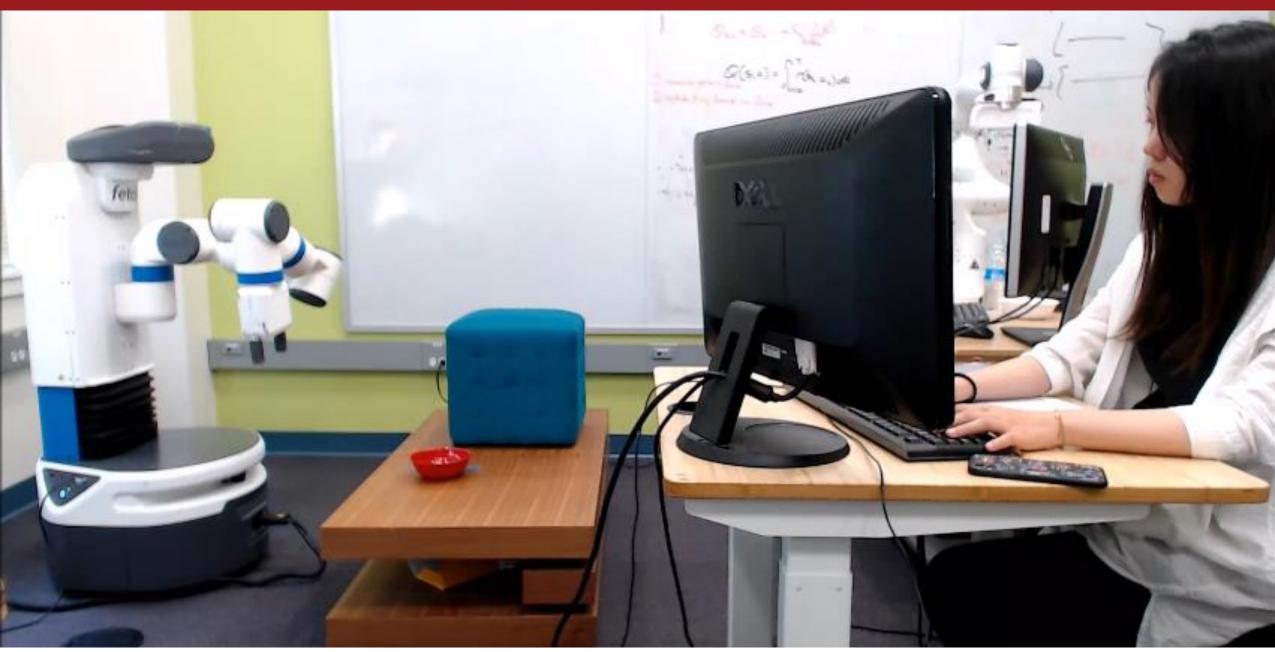


5 demonstrations

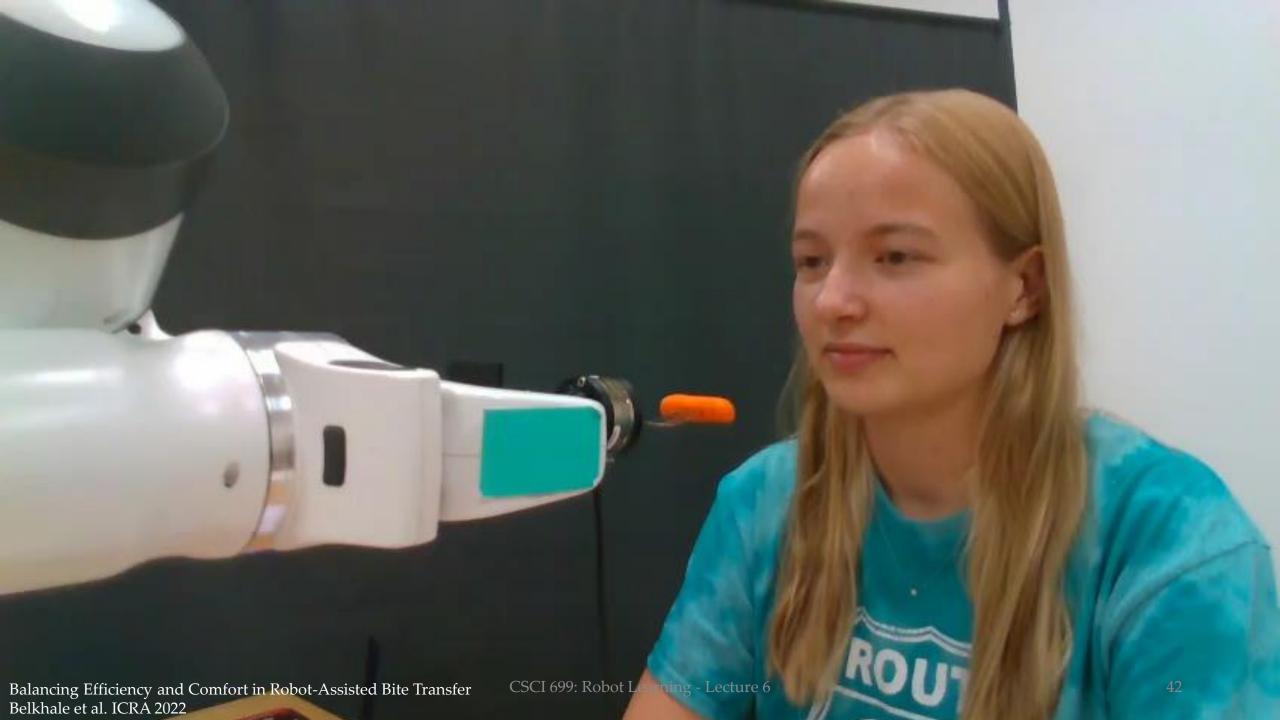
Ours

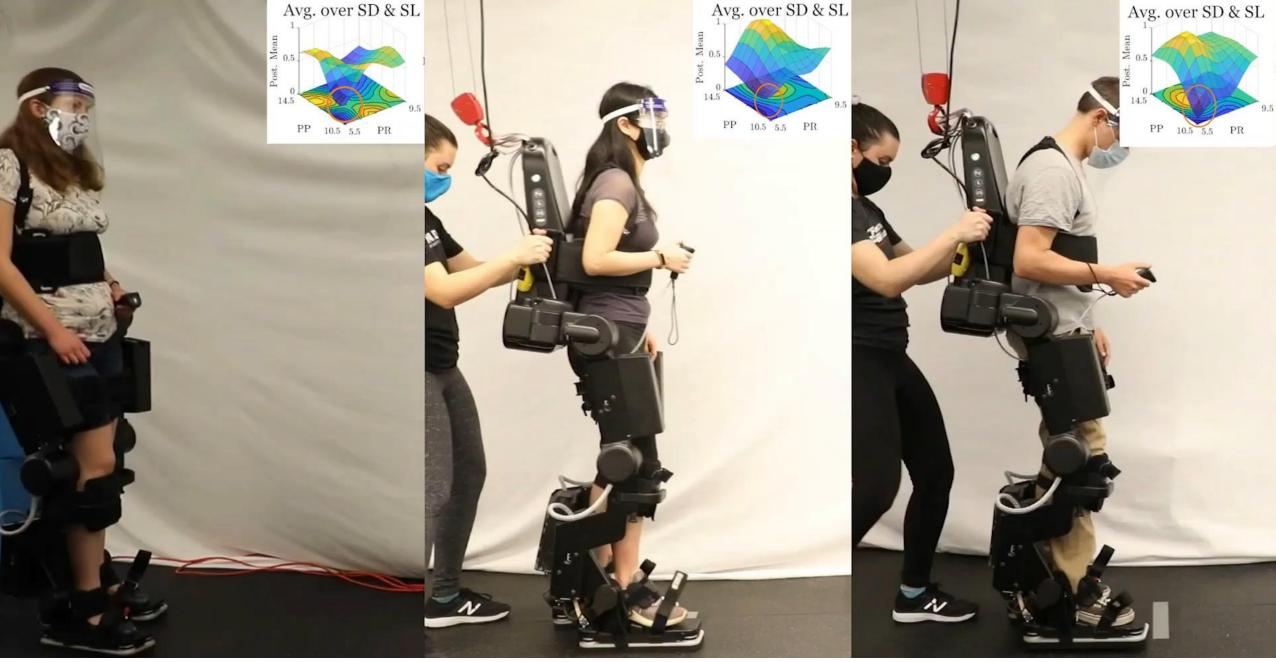


1 demonstration + 15 comparisons



Asking Easy Questions: A User-Friendly Approach to Active Reward Learning
Bıyık et al. CoRL 2019.

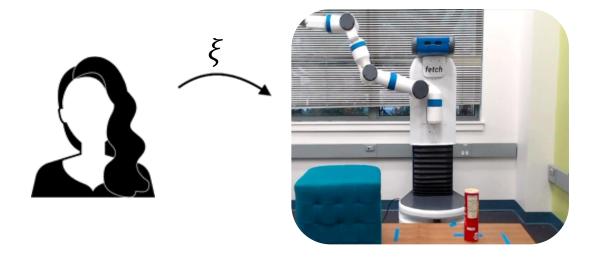




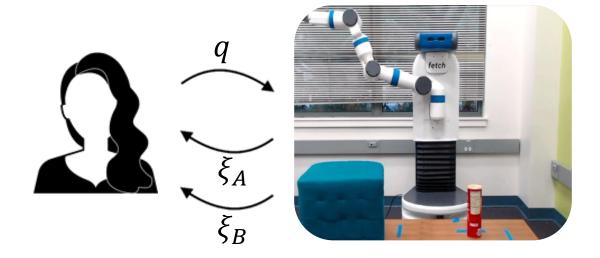
ROIAL: Region of Interest Active Learning for Characterizing Exoskeleton Gait Preference Landscapes Li et al., ICRA 2021

Choosing Queries

Demonstrations



<u>Comparisons</u>



How do we quantify information?

Surprise

$$95\% \rightarrow X = \text{Heads} \longrightarrow \text{Surprise: } \log_2 \frac{1}{0.95} \cong 0.074$$

5\%
$$\rightarrow X = \text{Tails}$$
 Surprise: $\log_2 \frac{1}{0.05} \cong 4.322$

Entropy (a measure of uncertainty)

$$95\% \rightarrow X = \text{Heads} \longrightarrow \text{Surprise: } \log_2 \frac{1}{0.95} \cong 0.074$$

5%
$$\rightarrow X = \text{Tails}$$
 Surprise: $\log_2 \frac{1}{0.05} \cong 4.322$

Entropy is the expected surprise.

Entropy:
$$H(X) = 0.95 \times \log_2 \frac{1}{0.95} + 0.05 \times \log_2 \frac{1}{0.05} \approx 0.286$$

Another example

$$50\% \rightarrow X = \text{Heads}$$

$$50\% \rightarrow X = \text{Tails}$$

Another example

$$50\% \rightarrow X = \text{Heads} \longrightarrow \text{Surprise: } \log_2 \frac{1}{0.50} = 1$$

 $50\% \rightarrow X = \text{Tails} \longrightarrow \text{Surprise: } \log_2 \frac{1}{0.50} = 1$

Another example

$$50\% \rightarrow X = \text{Heads}$$
 \longrightarrow Surprise: $\log_2 \frac{1}{0.50} = 1$
 $50\% \rightarrow X = \text{Tails}$ \longrightarrow Surprise: $\log_2 \frac{1}{0.50} = 1$

Entropy:
$$H(X) = 0.50 \times \log_2 \frac{1}{0.50} + 0.50 \times \log_2 \frac{1}{0.50} \cong 1$$

Uncertainty

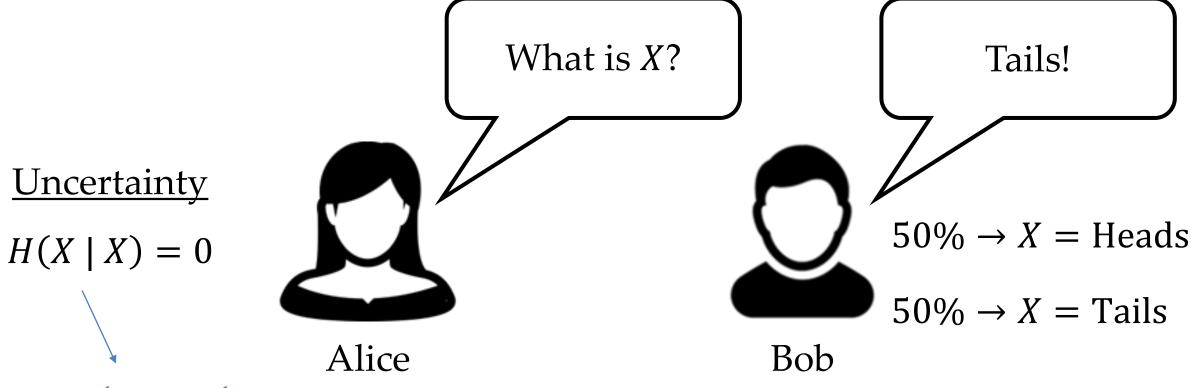
$$H(X) = 1$$



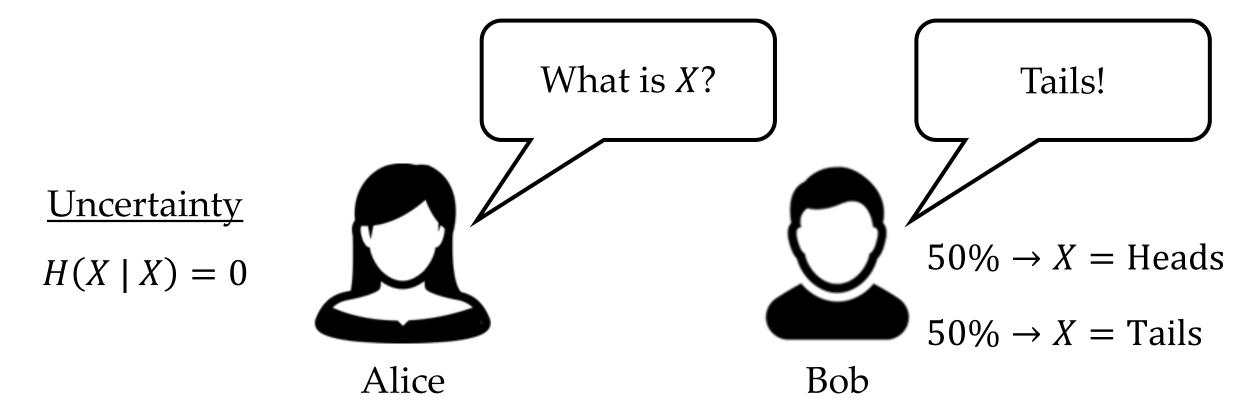


 $50\% \rightarrow X = \text{Heads}$

 $50\% \rightarrow X = \text{Tails}$



$$0 \times \log \frac{1}{0} + 1 \times \log \frac{1}{1} = 0$$
This is 0 in information theory.

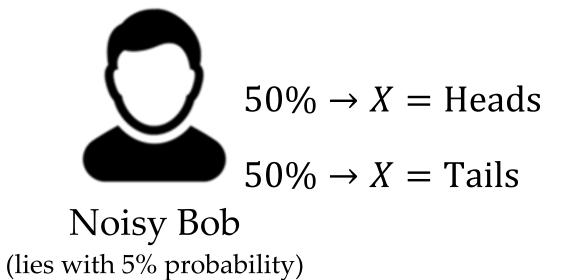


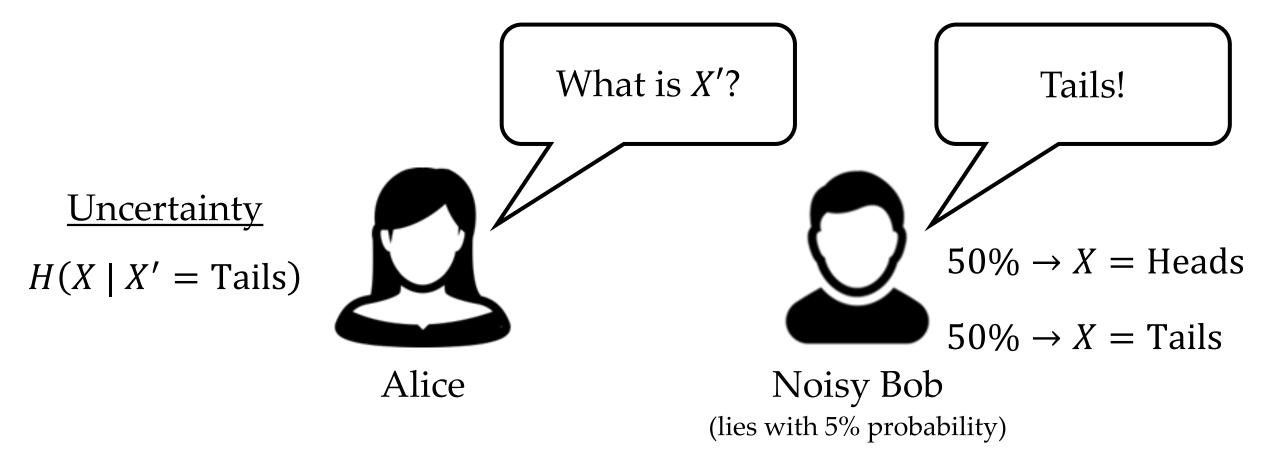
Mutual Information = Reduction in Entropy: $I(X; X) = H(X) - H(X \mid X)$ = 1 - 0 = 1_{CSCI 699: Robot Learning - Lecture 6}

Uncertainty

$$H(X) = 1$$

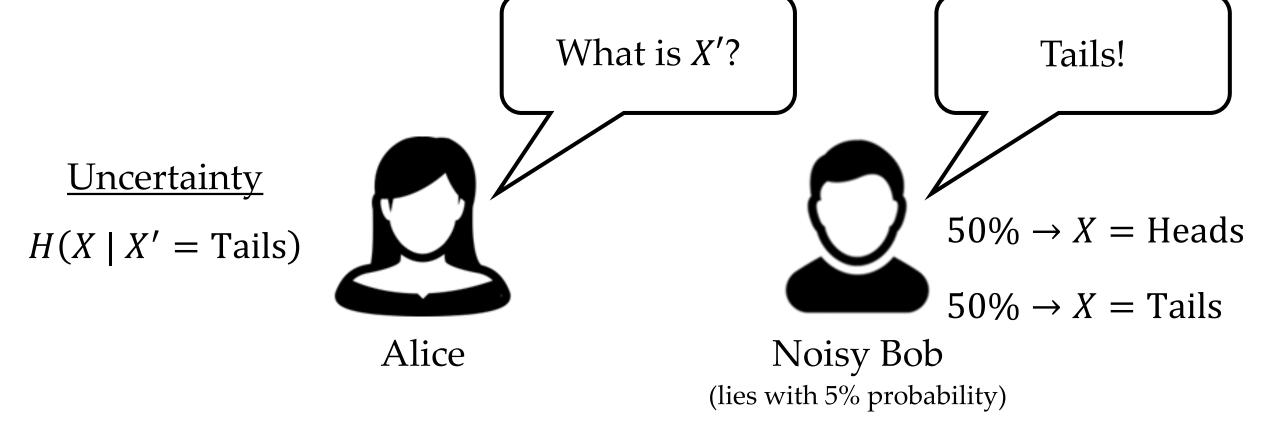






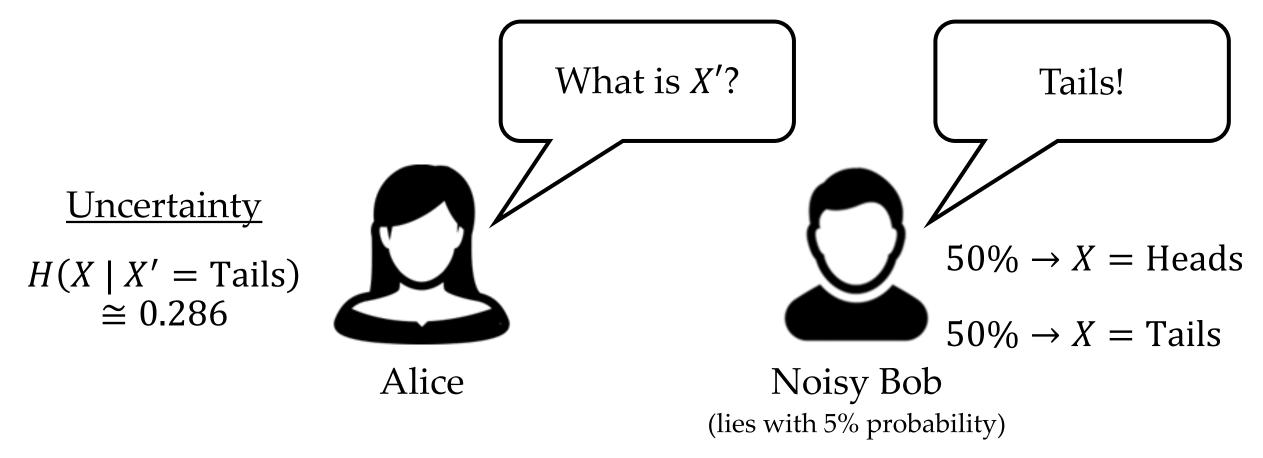
$$P(X = \text{Tails} \mid X' = \text{Tails}) \propto P(X' = \text{Tails} \mid X = \text{Tails})P(X = \text{Tails})$$

 $P(X = \text{Heads} \mid X' = \text{Tails}) \propto P(X' = \text{Tails} \mid X = \text{Heads})P(X = \text{Heads})$



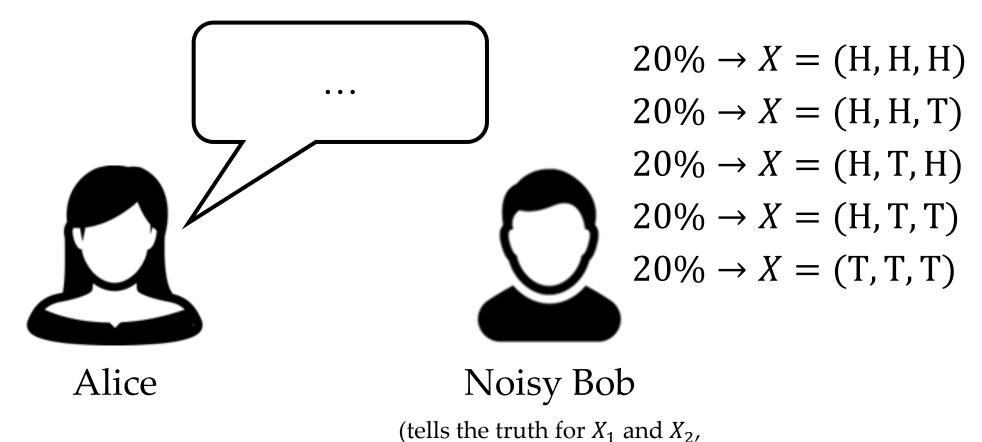
$$P(X = \text{Tails} \mid X' = \text{Tails}) = 0.95$$

 $P(X = \text{Heads} \mid X' = \text{Tails}) = 0.05$



Mutual Information = Reduction in Entropy: $I(X; X') = H(X) - H(X \mid X')$ CSCI 699: Robot Learning - Lecture 6 $\cong 1 - 0.286 = 0.714$

Mutual information: what do you ask?

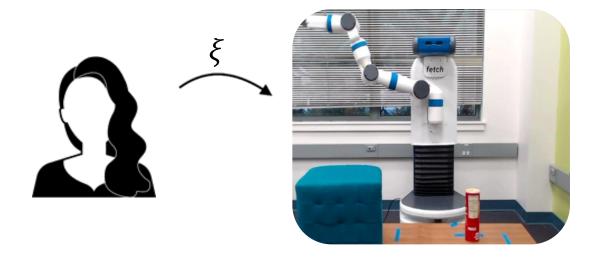


lies with 5% probability for X_3)

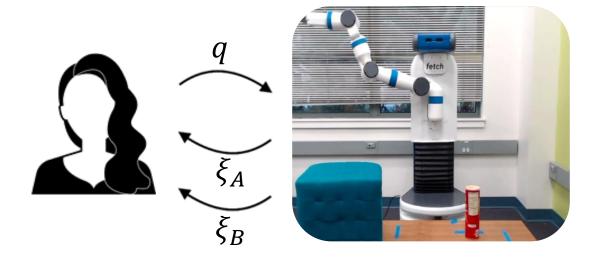
CSCI 699: Robot Learning - Lecture 6

Choosing queries

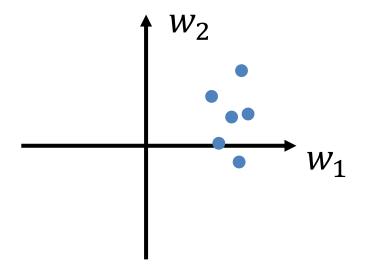
Demonstrations

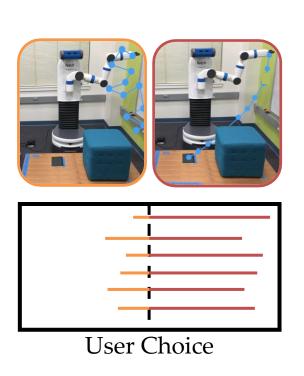


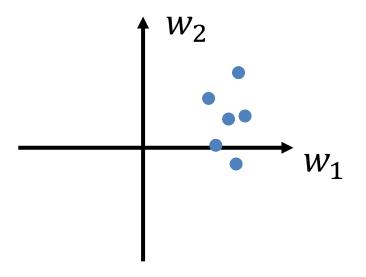
Comparisons

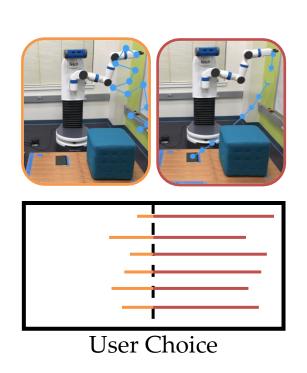


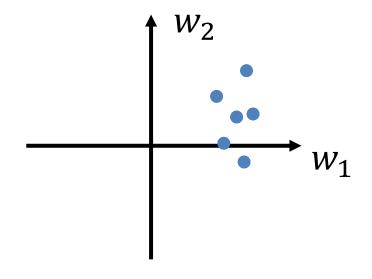
The robot can query the user with the query that will give the most information.

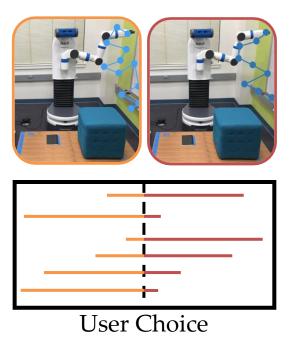


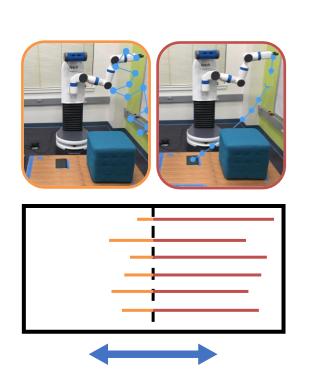


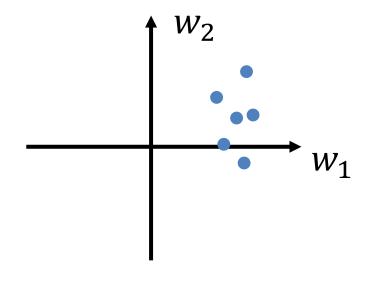


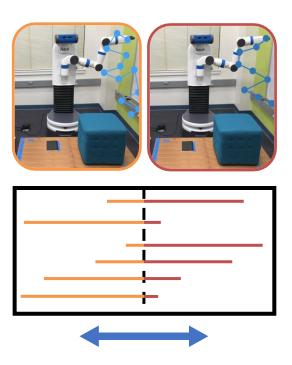




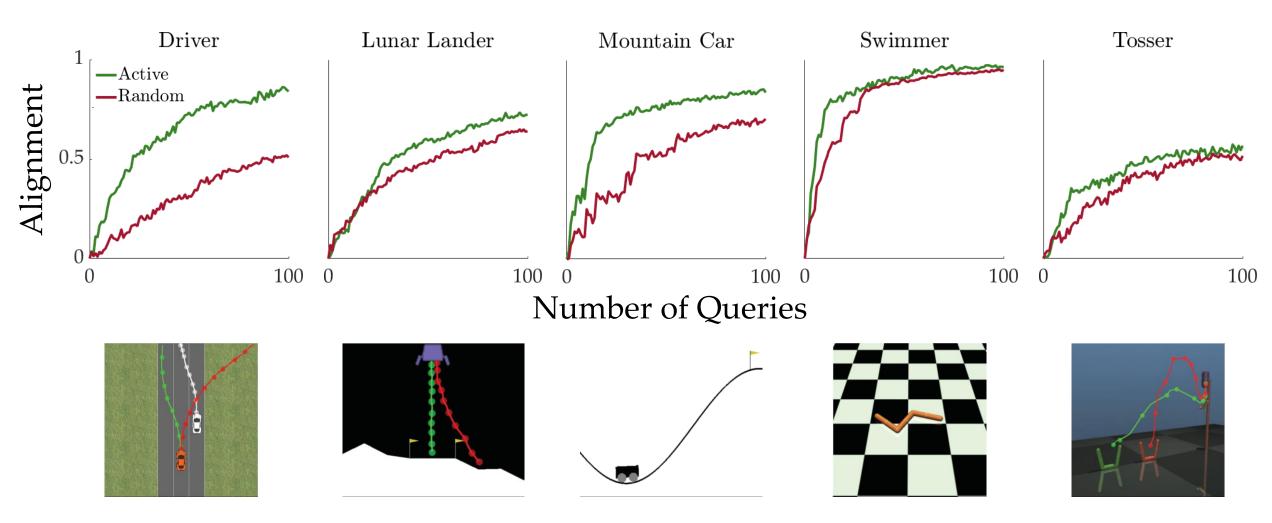




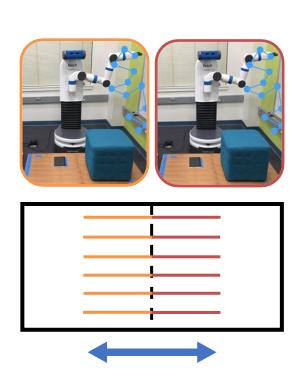


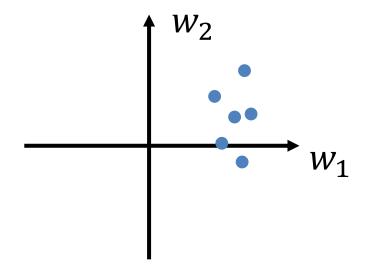


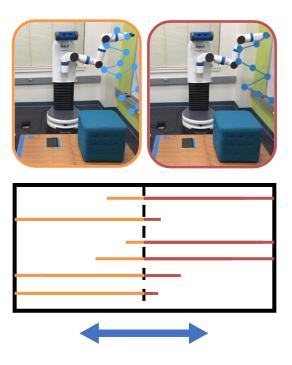
Active vs. random querying

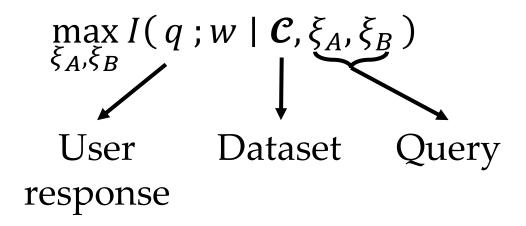


Batch Active Preference-Based Learning of Reward Functions Bıyık and Sadigh, CoRL 2018







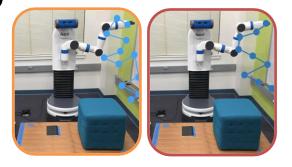


$$\max_{\xi_A,\xi_B} I(q; w \mid \mathcal{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A,\xi_B} H(q \mid \boldsymbol{\mathcal{C}}, \xi_A, \xi_B) - H(q \mid \boldsymbol{\mathcal{C}}, \xi_A, \xi_B, w)$$



Model Uncertainty User Uncertainty





User Choice

User Choice

$$\max_{\xi_{A},\xi_{B}} I(q; w \mid \boldsymbol{C}, \xi_{A}, \xi_{B})$$

$$\max_{\xi_{A},\xi_{B}} H(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B}) - H(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B}, w)$$

$$\max_{\xi_{A},\xi_{B}} -\mathbb{E}_{q\mid\boldsymbol{C},\xi_{A},\xi_{B}} [\log P(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B})] + \mathbb{E}_{q,w\mid\boldsymbol{C},\xi_{A},\xi_{B}} [\log P(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B}, w)]$$
No w here!

Asking Easy Questions: A User-Friendly Approach to Active Reward Learning Bıyık et al. CoRL 2019

$$\max_{\xi_A, \xi_B} I(q; w \mid \boldsymbol{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A, \xi_B} H(q \mid \boldsymbol{C}, \xi_A, \xi_B) - H(q \mid \boldsymbol{C}, \xi_A, \xi_B, w)$$

$$\max_{\xi_A, \xi_B} -\mathbb{E}_{q, w \mid \boldsymbol{C}, \xi_A, \xi_B} [\log P(q \mid \boldsymbol{C}, \xi_A, \xi_B)] + \mathbb{E}_{q, w \mid \boldsymbol{C}, \xi_A, \xi_B} [\log P(q \mid \boldsymbol{C}, \xi_A, \xi_B, w)]$$

$$\max_{\xi_{A},\xi_{B}} I(q; w \mid \boldsymbol{C}, \xi_{A}, \xi_{B})$$

$$\max_{\xi_{A},\xi_{B}} H(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B}) - H(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B}, w)$$

$$\max_{\xi_{A},\xi_{B}} \mathbb{E}_{q,w \mid \boldsymbol{C},\xi_{A},\xi_{B}} [\log P(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B}, w) - \log P(q \mid \boldsymbol{C}, \xi_{A}, \xi_{B})]$$

$$\max_{\xi_A,\xi_B} I(q; w \mid \boldsymbol{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A,\xi_B} H(q \mid \boldsymbol{C}, \xi_A, \xi_B) - H(q \mid \boldsymbol{C}, \xi_A, \xi_B, w)$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w \mid \boldsymbol{C},\xi_A,\xi_B} [\log P(q \mid \xi_A, \xi_B, w) - \log P(q \mid \boldsymbol{C}, \xi_A, \xi_B)]$$

$$\max_{\xi_A, \xi_B} \mathbb{E}_{q, w \mid \mathcal{C}, \xi_A, \xi_B} \left[\log P(q \mid \xi_A, \xi_B, w) - \log \int P(q, w' \mid \mathcal{C}, \xi_A, \xi_B) dw' \right]$$

$$P(w' \mid \mathcal{C}, \xi_A, \xi_B) P(q \mid \mathcal{C}, \xi_A, \xi_B, w')$$

$$= P(w' \mid \mathcal{C}) P(q \mid \xi_A, \xi_B, w')$$

$$\max_{\xi_{A},\xi_{B}} I(q; w \mid \mathcal{C}, \xi_{A}, \xi_{B})$$

$$\max_{\xi_{A},\xi_{B}} H(q \mid \mathcal{C}, \xi_{A}, \xi_{B}) - H(q \mid \mathcal{C}, \xi_{A}, \xi_{B}, w)$$

$$\max_{\xi_{A},\xi_{B}} \mathbb{E}_{q,w \mid \mathcal{C},\xi_{A},\xi_{B}} [\log P(q \mid \xi_{A}, \xi_{B}, w) - \log P(q \mid \mathcal{C}, \xi_{A}, \xi_{B})]$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w \mid \mathcal{C},\xi_A,\xi_B} \left[\log P(q \mid \xi_A,\xi_B,w) - \log \int P(w' \mid \mathcal{C}) P(q \mid \xi_A,\xi_B,w') dw' \right]$$

This is an expectation over $w' \mid C$ Take samples from $w' \mid C$ to compute.

$$\max_{\xi_A, \xi_B} I(q; w \mid \mathcal{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A, \xi_B} H(q \mid \mathcal{C}, \xi_A, \xi_B) - H(q \mid \mathcal{C}, \xi_A, \xi_B, w)$$

$$\max_{\xi_A, \xi_B} \mathbb{E}_{q, w \mid \mathcal{C}, \xi_A, \xi_B} [\log P(q \mid \xi_A, \xi_B, w) - \log P(q \mid \mathcal{C}, \xi_A, \xi_B)]$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w \mid \mathcal{C},\xi_A,\xi_B} \left[\log P(q \mid \xi_A,\xi_B,w) - \log \frac{1}{|\Omega|} \sum_{w' \in \Omega} P(q \mid \xi_A,\xi_B,w') \right]$$

$$\max_{\xi_A, \xi_B} I(q; w \mid \boldsymbol{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A, \xi_B} H(q \mid \boldsymbol{C}, \xi_A, \xi_B) - H(q \mid \boldsymbol{C}, \xi_A, \xi_B, w)$$

$$\max_{\xi_A, \xi_B} \mathbb{E}_{q, w \mid \boldsymbol{C}, \xi_A, \xi_B} [\log P(q \mid \xi_A, \xi_B, w) - \log P(q \mid \boldsymbol{C}, \xi_A, \xi_B)]$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w|\mathcal{C},\xi_A,\xi_B} \left[\log P(q \mid \xi_A,\xi_B,w) - \log \sum_{w' \in \Omega} P(q \mid \xi_A,\xi_B,w') \right]$$

$$\max_{\xi_A,\xi_B} I(q; w \mid \mathcal{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A,\xi_B} H(q \mid \mathcal{C}, \xi_A, \xi_B) - H(q \mid \mathcal{C}, \xi_A, \xi_B, w)$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w \mid \mathcal{C},\xi_A,\xi_B} [\log P(q \mid \xi_A, \xi_B, w) - \log P(q \mid \mathcal{C}, \xi_A, \xi_B)]$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w \mid \mathcal{C},\xi_A,\xi_B} \left[\log \frac{P(q \mid \xi_A, \xi_B, w)}{\sum_{w' \in \Omega} P(q \mid \xi_A, \xi_B, w')} \right]$$

$$P(q,w \mid \mathcal{C},\xi_A,\xi_B) = P(w \mid \mathcal{C},\xi_A,\xi_B)P(q \mid \mathcal{C},\xi_A,\xi_B,w)$$

$$= P(w \mid \mathcal{C})P(q \mid \xi_A,\xi_B,w)$$

$$\max_{\xi_A,\xi_B} I(q; w \mid \mathcal{C}, \xi_A, \xi_B)$$

$$I(a \mid \mathcal{C}, \xi_A, \xi_B) - H(a \mid \mathcal{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A,\xi_B} H(q \mid \boldsymbol{C}, \xi_A, \xi_B) - H(q \mid \boldsymbol{C}, \xi_A, \xi_B, w)$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w|\mathcal{C},\xi_A,\xi_B} [\log P(q \mid \xi_A,\xi_B,w) - \log P(q \mid \mathcal{C},\xi_A,\xi_B)]$$

$$\max_{\xi_A, \xi_B} \mathbb{E}_{q, w \mid \xi_A, \xi_B} \left[\log \frac{P(q \mid \xi_A, \xi_B, w)}{\sum_{w' \in \Omega} P(q \mid \xi_A, \xi_B, w')} \right]$$

$$\max_{\xi_A,\xi_B} \frac{1}{|\Omega|} \sum_{w \in \Omega} \mathbb{E}_{q|\xi_A,\xi_B,w} \left[\log \frac{P(q|\xi_A,\xi_B,w)}{\sum_{w' \in \Omega} P(q|\xi_A,\xi_B,w')} \right]$$

$$\max_{\xi_A,\xi_B} I(q; w \mid \mathcal{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A,\xi_B} H(q \mid \mathcal{C}, \xi_A, \xi_B) - H(q \mid \mathcal{C}, \xi_A, \xi_B, w)$$

$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w \mid \mathcal{C}, \xi_A, \xi_B} [\log P(q \mid \xi_A, \xi_B, w) - \log P(q \mid \mathcal{C}, \xi_A, \xi_B)]$$

$$\max_{\xi_A, \xi_B} \mathbb{E}_{q, w \mid \xi_A, \xi_B} \left[\log \frac{P(q \mid \xi_A, \xi_B, w)}{\sum_{w' \in \Omega} P(q \mid \xi_A, \xi_B, w')} \right]$$

$$\max_{\xi_A, \xi_B} \sum_{w \in \Omega} \mathbb{E}_{q \mid \xi_A, \xi_B, w} \left[\log \frac{P(q \mid \xi_A, \xi_B, w)}{\sum_{w' \in \Omega} P(q \mid \xi_A, \xi_B, w')} \right]$$

$$\max_{\xi_A,\xi_B} I(q; w \mid \mathcal{C}, \xi_A, \xi_B)$$

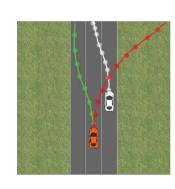
$$\max_{\xi_A,\xi_B} H(q \mid \mathcal{C}, \xi_A, \xi_B) - H(q \mid \mathcal{C}, \xi_A, \xi_B, w)$$

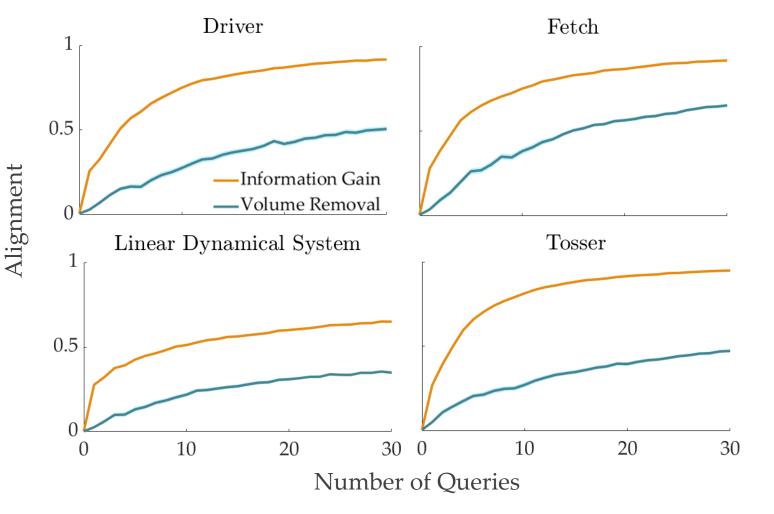
$$\xi_A,\xi_B$$

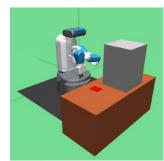
$$\max_{\xi_A,\xi_B} \mathbb{E}_{q,w|\mathcal{C},\xi_A,\xi_B} [\log P(q \mid \xi_A,\xi_B,w) - \log P(q \mid \mathcal{C},\xi_A,\xi_B)]$$

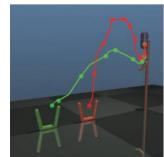
$$\max_{\xi_A, \xi_B} \mathbb{E}_{q, w \mid \xi_A, \xi_B} \left[\log \frac{P(q \mid \xi_A, \xi_B, w)}{\sum_{w' \in \Omega} P(q \mid \xi_A, \xi_B, w')} \right]$$

$$\max_{\xi_A,\xi_B} \sum_{w \in \Omega} \sum_{q} P(q \mid \xi_A,\xi_B,w) \left[\log \frac{P(q \mid \xi_A,\xi_B,w)}{\sum_{w' \in \Omega} P(q \mid \xi_A,\xi_B,w')} \right]$$





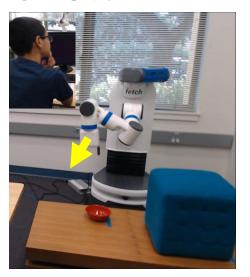




Volume Removal

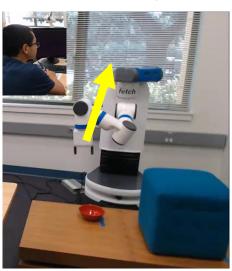
Similar Trajectories

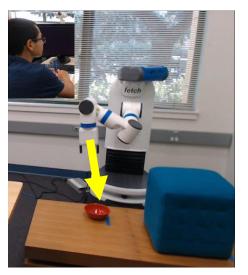


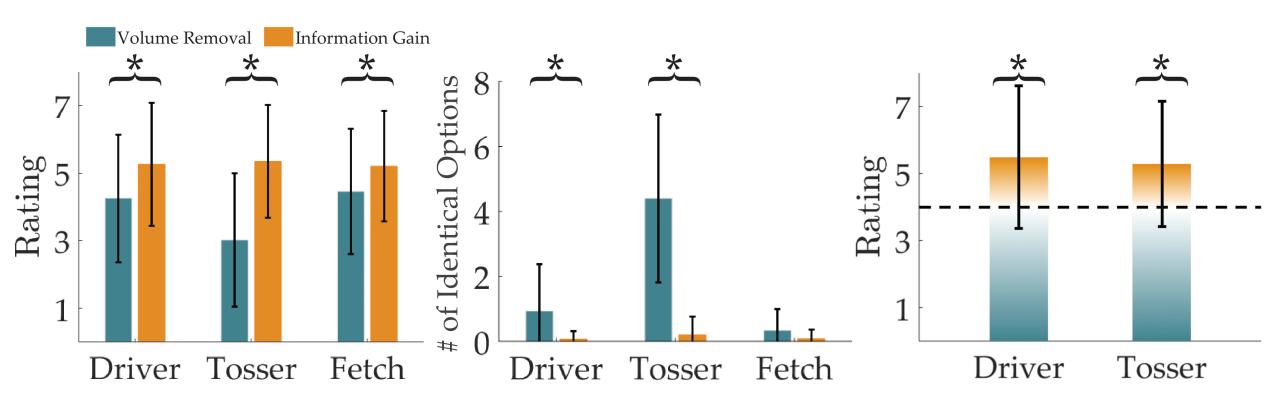


Information Gain

More Distinguishable Query







Other types of human feedback

Fee	edback	Constraint	Probabilistic
Cor	mparisons	$r(\xi_1) \geq r(\xi_2)$	$\mathbb{P}(\xi_1 \mid r, \mathcal{C}) = \frac{\exp(\beta \cdot r(\xi_1))}{\exp(\beta \cdot r(\xi_1)) + \exp(\beta \cdot r(\xi_2))}$
Der	monstrations	$r(\xi_D) \ge r(\xi) \forall \ \xi \in \Xi$	$\mathbb{P}(\xi_D \mid r, \Xi) = \frac{\exp(\beta \cdot r(\xi_D))}{\sum_{\xi \in \Xi} \exp(\beta \cdot r(\xi))}$
Cor	rrections	$r(\xi_R + A^{-1}\Delta q) \ge r(\xi_R + A^{-1}\Delta q') \forall \Delta q' \in Q - Q$	$\mathbb{P}(\Delta q' \mid r, Q - Q) = \frac{\exp(\beta \cdot r(\xi_R + A^{-1}\Delta q))}{\sum_{\Delta q \in Q - Q} \exp(\beta \cdot r(\xi_R + A^{-1}\Delta q))}$
Imp	provement	$r(\xi_{ ext{improved}}) \geq r(\xi_R)$	$\mathbb{P}(\xi_{\text{improved}} \mid r, \mathcal{C}) = \frac{\exp(\beta \cdot r(\xi_{\text{improved}}))}{\exp(\beta \cdot r(\xi_{\text{improved}})) + \exp(\beta \cdot r(\xi_{R}))}$
Off	•	$r(\xi_R^{0:t}\xi^t\dots\xi^t) \ge r(\xi_R)$	$\mathbb{P}(\text{off} \mid r, \mathcal{C}) = \frac{\exp(\beta \cdot r(\xi_R^{0:t} \xi^t \dots \xi^t))}{\exp(\beta \cdot r(\xi_R^{0:t} \xi^t \dots \xi^t)) + \exp(\beta \cdot r(\xi_R))}$
Lar	nguage	$\mathbb{E}_{\xi \sim \text{Unif}(G(\lambda^*))} \big[r(\xi) \big] \ge \mathbb{E}_{\xi \sim \text{Unif}(G(\lambda))} \big[r(\xi) \big] \ \forall \lambda \in \Lambda$	$\mathbb{P}(\lambda^* \mid r, \Lambda) = \frac{\exp(\beta \cdot \mathbb{E}_{\xi \sim \text{Unif}(G(\lambda^*))}[r(\xi)])}{\sum_{\lambda \in \Lambda} \exp(\beta \cdot \mathbb{E}_{\xi \sim \text{Unif}(G(\lambda))}[r(\xi)])}$
Pro	oxy Rewards	$\mathbb{E}_{\tilde{\xi} \sim \pi(\tilde{\xi} \tilde{r})} \big[r(\tilde{\xi}) \big] \ge \mathbb{E}_{\tilde{\xi} \sim \pi(\tilde{\xi} c)} \big[r(\tilde{\xi}) \big] \forall c \in \tilde{\mathcal{R}}$	$\mathbb{P}(\tilde{r} \mid r, \tilde{\mathcal{R}}) = \frac{\sum_{\lambda \in \Lambda} \exp(\beta \cdot \mathbb{E}_{\xi \sim \text{Unif}(G(\lambda))}[r(\xi)])}{\exp(\beta \cdot \mathbb{E}_{\tilde{\xi} \sim \pi(\tilde{\xi} \tilde{r})}[r(\tilde{\xi})])}$ $\sum_{c \in \tilde{\mathcal{R}}} \exp(\beta \cdot \mathbb{E}_{\tilde{\xi} \sim \pi(\tilde{\xi} c)}[r(\tilde{\xi})])$
Rev	ward/Punish	$r(\xi_R) \geq r(\xi_{ ext{expected}})$	$\mathbb{P}(+1 \mid r, \mathcal{C}) = \frac{\sum_{c \in \tilde{\mathcal{R}}} \exp(\beta \cdot \mathbb{E}_{\tilde{\xi} \sim \pi(\tilde{\xi} c)} \lfloor r(\xi) \rfloor)}{\exp(\beta \cdot r(\xi_R))}$ $= \frac{\exp(\beta \cdot r(\xi_R))}{\exp(\beta \cdot r(\xi_R)) + \exp(\beta \cdot r(\xi_{\text{expected}}))}$
	ial state	$\mathbb{E}_{\mathcal{E} \sim \psi(s^*)}[r(s^*)] \geq \mathbb{E}_{\mathcal{E} \sim \psi(s)}[r(s)] orall s \in \mathcal{S}$	$\mathbb{P}(s^* \mid r, \mathcal{S}) = \frac{\exp(\beta \cdot r(\xi_R)) + \exp(\beta \cdot r(\xi_{\text{expected}}))}{\exp(\beta \cdot \mathbb{E}_{\xi \sim \psi(s^*)}[r(\xi)])}$ $\mathbb{P}(s^* \mid r, \mathcal{S}) = \frac{\exp(\beta \cdot \mathbb{E}_{\xi \sim \psi(s)}[r(\xi)])}{\sum_{s \in S} \exp(\beta \cdot \mathbb{E}_{\xi \sim \psi(s)}[r(\xi)])}$
		3 7(3) 1 73	$ \frac{\mathbb{E}(S \mid r, \mathcal{S}) = \sum_{s \in S} \exp(\beta \cdot \mathbb{E}_{\xi \sim \psi(s)}[r(\xi)])}{\exp(\beta_0 \cdot \mathbb{E}_{\xi \sim \psi_0(\mathcal{C}_i)}[r(\xi)])} $
	ta-choice	$\mathbb{E}_{\xi \sim \psi(\mathcal{C}_i)}[r(\xi)] \ge \mathbb{E}_{\xi \sim \psi(\mathcal{C}_j)}[r(\xi)] \forall j \in [n]$	$\mathbb{P}(\mathcal{C}_i \mid r, \mathcal{C}_0) = \frac{\exp\left(\beta_0 \cdot \mathbb{E}_{\xi \sim \psi_0(\mathcal{C}_i)}[r(\xi)]\right)}{\sum_{j \in [n]} \exp\left(\beta_0 \cdot \mathbb{E}_{\xi \sim \psi_0(\mathcal{C}_j)}[r(\xi)]\right)}$ $\exp\left(\beta \cdot r(\xi^*)\right)$
Cre	edit assignment	$r(\xi^*) \ge r(\xi) \forall \ \xi \in \mathcal{C}$	$\mathbb{P}(\xi^* \mid r, \mathcal{C}) = \frac{\exp(\beta \cdot r(\xi^*))}{\sum_{\xi \in \mathcal{C}} \exp(\beta \cdot r(\xi))}$

Today...

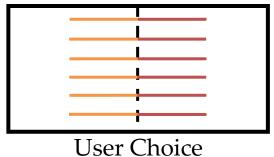
- Learning from human feedback
 - Suboptimal demonstrations
 - Pairwise comparisons
 - Reinforcement learning from human feedback (RLHF)

$$\max_{\xi_A,\xi_B} I(q; w \mid \mathcal{C}, \xi_A, \xi_B)$$

$$\max_{\xi_A,\xi_B} H(q \mid \boldsymbol{\mathcal{C}}, \xi_A, \xi_B) - H(q \mid \boldsymbol{\mathcal{C}}, \xi_A, \xi_B, w)$$

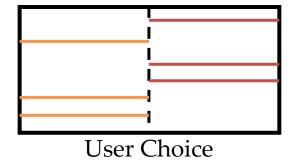


Model Uncertainty User Uncertainty



Where do these trajectories come from in the first place?





Incorporating comparisons

$$\underset{w}{\operatorname{argmax}} P(w \mid \mathcal{D}, \mathcal{C})$$

$$P(w \mid \mathcal{D}, \mathcal{C}) \propto P(w)P(\mathcal{D} \mid w)P(\mathcal{C} \mid w)$$

How do we solve this optimization problem?

$$= P(w) \prod_{i=1}^{L} P(\xi_i \mid w) \prod_{i=1}^{N} P(q^{(i)} \mid w, \xi_A^{(i)}, \xi_B^{(i)})$$

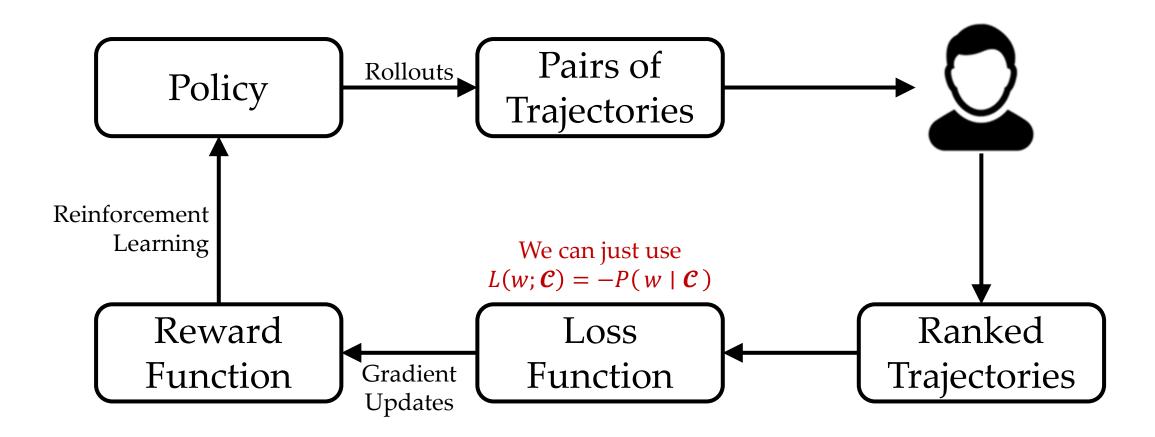
$$\propto P(w) \prod_{i=1}^{L} \exp f_w(\xi_i) \prod_{i=1}^{N} \frac{\exp f_w\left(\xi_{q^{(i)}}^{(i)}\right)}{\exp f_w\left(\xi_{q^{(i)}}^{(i)}\right) + \exp f_w\left(\xi_{\neg q^{(i)}}^{(i)}\right)}$$

RLHF

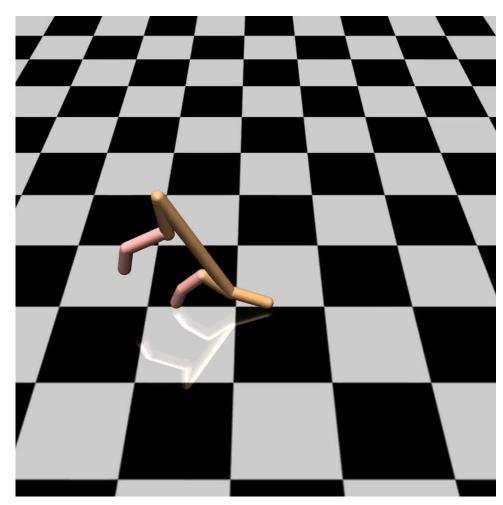
Two major changes to preference-based reward learning:

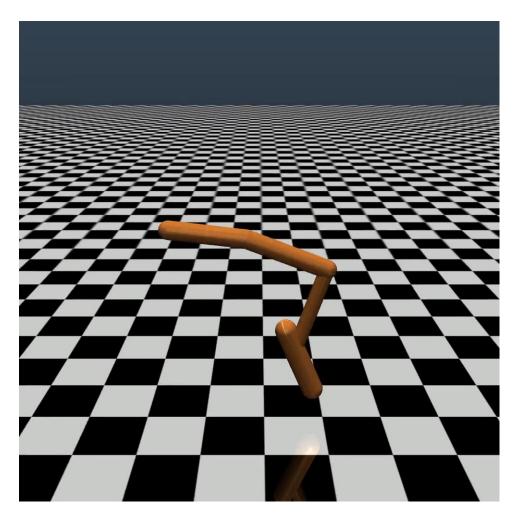
- 1. Instead of Bayesian learning, write a loss function and learn with gradient updates
- 2. After learning a reward, train a policy to generate new trajectories for the next iteration of reward learning

RLHF



RLHF





InstructGPT

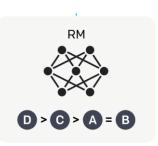
A prompt and several model outputs are sampled.



A labeler ranks the outputs from best to worst.



This data is used to train our reward model.



Today...

- Learning from human feedback
 - Suboptimal demonstrations
 - Pairwise comparisons
 - Reinforcement learning from human feedback (RLHF)

Next time...

A day full of presentations!

- Myers et al., Active Reward Learning from Online Preferences (2023).
- Bajcsy et al., Learning Robot Objectives from Physical Human Interaction (2017).
- Bobu et al., Inducing Structure in Reward Learning by Learning Features (2022).
- Hadfield-Menell et al., Inverse Reward Design (2017).
- Kwon et al., When Humans aren't Optimal: Robots that Collaborate with Risk-aware Humans (2020).
- Chan et al., Human Irrationality: Both Bad and Good for Reward Inference (2021).
- Jeon et al., Shared Autonomy with Learned Latent Actions (2020).