# **Machine Learning Overview**

Juan Pablo Lewinger 07/02/2024

### Overview. What is Machine Learning?

Example of problem/task *not* well suited for machine learning: multiply two 5-digit numbers

- · A human can write a computer program (teach the computer/machine) exact steps/algorithm to follow
- · Computers excel at this kind of mechanical task humans no so much

#### Overview. What is Machine Learning?

- · Example of problem well suited for ML: Spam email recognition
  - Very easy for a human to do
  - But very hard for a human to translate into a well-defined sequence of steps/algorithm
- · Idea behind ML: 'feed' the computer many examples (data) of spam and nonspam emails
  - Let the machine/computer come up with its own set of 'rules'
- · 'Feeding' **features** extracted from the emails and **labels** indicating spam/no-spam

#### **Features and Labels**

- Features: Characteristics of the emails human believes relevant to determining spam/no-spam
  - Total number of words (numeric feature)
  - Appearance of keywords/phrases (e.g. 'act now', 'for free', 'save \$') (yes/no) (binary feature)
  - Single word frequencies (numeric features)
  - Pairs of words frequencies (numeric features)
  - Email sender in your contact list (yes/no)?
  - Time of day email was sent 0-24 (numeric)
  - Day of week email was sent (categorical)
- Label: spam/no-spam (binary)

### Machine Learning vs. Statistics

- Lots of overlap they share many techniques/models (e.g. linear and logistic regression, principal components)
- But goals are different
- · Statistics focuses on inference:
  - estimation and hypothesis testing of parameters of interest (e.g. odds ratio, regression slope)
  - Establishing association/causation (e.g. is smoking a risk factor for lung cancer?)
- Machine learning focuses on prediction and detection (e.g. does this patient have lung cancer? Is this patient likely to have a relapse?)
- We'll refer to both as 'prediction'

#### Machine Learning vs. Statistics

- ML Theory makes very few distributional assumptions: independent, identically distributed instances/samples
- Statistics (typically but not always) makes lots of distributional assumptions (e.g. data is normally distributed)
- ML assumes less but has the 'simpler' goal of prediction
- Statistics assumes more but has the more complex goal of establishing association/causation

#### **Prediction**

- Machine Learning emphasizes prediction
- But, why do we want to 'predict/detect'?
  - to anticipate/predict future (e.g. predict whether a prostate cancer patient likely have cancer back within 5 years based on gene expression)
  - to avoid costly/unfeasible measure (detect whether a patient has ovarian cancer based on methylation)
  - to automate/eliminate need for human intervention (e.g. spam detector)
- Two different meanings of 'prediction':
  - prediction of future outcome
  - estimation of unmeasured variable/detection

### Artificial Intelligence vs. Machine Learning

- Artificial Intelligence: "The effort to automate intellectual tasks normally performed by humans"\*
- · Machine Learning is a sub-field Al
- · Route finding algorithms (e.g. Waze app) are AI but not ML
- \* "Deep Learning with R" by Allaire and Chollet

### Supervised vs. Unsupervised Learning

- In supervised learning the instances have labels (outcomes variable) we want to predict based on their features
  - Spam detection is a typical example of a supervised learning problem
  - Analogy with learning under the supervision of a teacher that knows the correct answer (labels)
- In unsupervised learning there are features but no labels
  - Goal is to find structure (groups, clusters) in the instances and/or the features
  - Learning is unsupervised because there is 'no teacher'
  - Cluster analysis and Principal component analysis are typical unsupervised learning techniques

### Classification vs. regression

- Supervised learning problems often are of one of two types depending on the type of label
- · Classification: when label is binary (spam vs. non-spam) or categorical (3 breast cancer subtypes)
  - e.g. discriminant analysis, logistic regression, support vector machines
- · Regression: when label is quantitative/numeric (% body fat, age, survival time)
  - Linear regression, Cox proportional hazards model

### Glossary—Machine Learning vs. Statistics

- feature = predictor = independent variable = covariate = regressor = exogenous variable (economics)
- · label = outcome = dependent variable
- instance = observation (for us usually subject, patient)
- · algorithm = model
- train = fit model

### Example: predicting brain weight from head size

Data from brain weight (grams) and head size (cubic cm) for 237 adults aged 20 or above and classified by gender and age group from Middlesex Hospital, London

One of the main objects of the investigation which forms the subject of this paper, has been to obtain a series of reconstruction formulae, by which it will be possible, when in possession of certain chief measurements of the head, to predict within the limits of normal variation, the approximate weight of the brain

A Study of the Relations of the Brain to the Size of the Head Biometrika (1905)

The subject of brain-weight in man has for a long time been given considerable attention by anatomists and anthropologists. The reason for this is obvious. Since the brain is the organ of the mind it appeared to earlier workers that size of brain ought to be an index of intellectual capacity.

Biometrical Studies on Man: I. Variation and Correlation in Brain-Weight Biometrika (1905)

### Brain weight example

```
setwd("/Users/JP/My Drive/Teaching/LAs BEST/2024/Lectures/5. Machine Learning I")
brain = read.table("brain.txt", header=T)
head(brain)
    Sex Age Head.size Brain.weight
## 1
      1
        1
                4512
                           1530
                3738
                           1297
## 2
      1
        1
      1 1
## 3
               4261
                           1335
## 4 1 1
               3777
                           1282
## 5 1 1
               4177
                           1590
## 6
      1 1
                3585
                           1300
```

### Brain weight example

```
##
## 1 2
## 134 103

table(brain$Age)

##
## 1 2
## 110 127
```

· Need to convert Sex and Age to categorical variables before running lm

```
brain$Sex = factor(brain$Sex, levels=1:2, labels=c("Male", "Female"))
brain$Age = factor(brain$Age, levels=1:2, labels=c("20-46", "46+"))
```

### Linear Regression in R

```
##
## Male Female
## 134 103

table(brain$Age)

##
## 20-46 46+
## 110 127
```

- By converting to factor lm will properly treat Sex and Age:
  - **lm** will automatically create dummy variables

### Brain weight example

Split data into training (70%) and test (30%) data

```
set.seed(301)
n = nrow(brain)
n

## [1] 237

trainset = sample(1:n, floor(0.7*n))
head(trainset, 10)

## [1] 220 218 141 5 57 234 47 26 52 9
```

### Brain weight example

Split data into training (70%) and test (30%) data

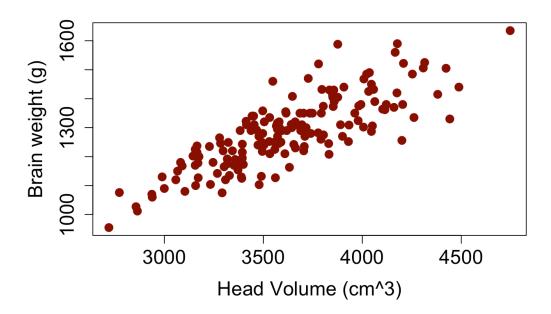
```
brain_train = brain[trainset,]; n_train = nrow(brain_train)
brain_test = brain[-trainset,]; n_test = nrow(brain_test)
dim(brain_train)

## [1] 165    4

dim(brain_test)

## [1] 72    4
```

Clear positive relationship between head volume and brain weight

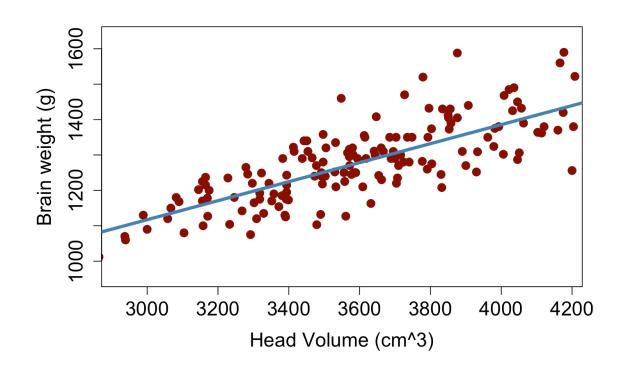


### **Linear Regression**

Will use only the training portion of the brain weight data to train the SLR model

```
brain_lm0 = lm(Brain.weight ~ Head.size, data = brain_train)
summary(brain_lm0)
## Call:
## lm(formula = Brain.weight ~ Head.size, data = brain train)
## Residuals:
       Min
                 10 Median
                                   30
                                           Max
## -183.437 -50.277 -3.188
                              47.098 235.591
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 311.29654 54.67694 5.693 5.67e-08 ***
## Head.size
                0.26860
                           0.01501 17.891 < 2e-16 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 71.58 on 163 degrees of freedom
## Multiple R-squared: 0.6626, Adjusted R-squared: 0.6605
## F-statistic: 320.1 on 1 and 163 DF, p-value: < 2.2e-16
```

## Linear Regression in R



#### **Prediction**

- Using linear regression we constructed a model that approximates brain weight based on head size in our (training) data
- · But our goal is to predict brain weight based on head size in the population
- · What population? A population such that the training data can be considered a random sample of
  - 1. Patients aged 20+ in London's Middlesex Hospital in 1905
  - 2. Population of London inhabitants aged 20 or older in 1905
  - 3. Population of London inhabitants aged 20 or older today
- If the model predicts in the population the training data was sampled from we say that the model generalizes

#### How do we know if the model generalizes?

- · Ideally we'd need to compare the brain weight predicted by the model with the true brain weight in the entire target population to *compute the average error* incurred by the model.
- Obviously we can't do that. Next best thing is to take a 'test' sample from the target population and use it to estimate the average error by the *sample average error*
- · How do I get such a sample? We set aside part of the original data for this purpose before building our model.
- We split the data into training and testing
  - Use training data for fitting the model
  - Use test data to evaluate/estimate how well the model performs

### Prediction performance metrics

 $y_i$  is the true observed outcome (e.g. brain weight) and

 $\widehat{y_i} = \widehat{\beta_0} + \widehat{\beta_1} x_i$  is the outcome predicted by the linear model for observation i

 $y_i - \widehat{y_i}$  is the error in prediction for observation i

· Mean Square error:

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_i - \widehat{y_i})^2$$

Root Mean Square error:

RMSE = 
$$\sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - \widehat{y_i})^2}$$

· Root Mean Square error is perhaps easier to interpret as it's on the same scale as the outcome (e.g. grams instead of square grams)

### Prediction performance metrics in R

· Root Mean Square error:

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (y_i - \widehat{y_i})^2}$$

```
# RMSE
RMSE_train0 = sqrt(sum((residuals(brain_lm0))^2)/nrow(brain_train))
RMSE_train0
## [1] 71.14914
```

### Prediction performance metrics

```
\mathbb{R}^2, proportion of variance explained
```

## [1] 0.662597

$$\begin{split} \mathrm{RSS} &= \sum_{i=1}^n (y_i - \widehat{y_i})^2 \\ \mathrm{TSS} &= \sum_{i=1}^n (y_i - \overline{y})^2 \\ R^2 &= \frac{\mathrm{TSS-RSS}}{\mathrm{TSS}} = 1 - \frac{\mathrm{RSS}}{\mathrm{TSS}} \\ \mathrm{RSS} &< - \sup((\mathrm{residuals}(\mathrm{brain\_lm0}))^2) \\ \mathrm{TSS} &< - \sup((\mathrm{brain\_train\$Brain.weight} - \mathrm{mean}(\mathrm{brain\_train\$Brain.weight}))^2) \\ \mathrm{R2\_train0} &= \mathbf{1} - \mathrm{RSS/TSS} \\ \mathrm{R2\_train0} \end{split}$$

### **Discussion Question**

Can we evaluate prediction performance on the same data set used for building the model, i.e. the training data?

### Evaluating (estimating) prediction performance

- Evaluating performance using training data overestimates performance
- · We'd get an underestimate of true population prediction performance
- · Why? Model was chosen so as to make MSE as small as possible in the training data.
- · Analogous to using a practice exam to assess students
- · Need to assess performance in yet unseen/unused data
- We reserved test data only for assessing performance
- · Trade-off between:
  - better model (more training data) and
  - more accurate performance evaluation (more test data)
- · Common split is train=70-80% and test=20-30% of data

#### Prediction performance in weight data

```
pred0 = predict(brain lm0, newdata=brain test)
head(pred0)
                                                      13
## 1523.241 1315.341 1274.245 1327.966 1267.261 1289.018
head(cbind(brain_test, predicted=pred0))
             Age Head.size Brain.weight predicted
##
       Sex
## 1 Male 20-46
                                   1530 1523.241
                      4512
## 2 Male 20-46
                     3738
                                   1297
                                         1315.341
## 6 Male 20-46
                     3585
                                         1274.245
                                   1300
## 7 Male 20-46
                     3785
                                         1327.966
                                   1400
## 8 Male 20-46
                     3559
                                   1255
                                         1267.261
## 13 Male 20-46
                                   1355
                                         1289.018
                     3640
```

### Prediction performance in weight data

```
n_test = nrow(brain_test)

RMSE_test0 = sqrt(sum((brain_test$Brain.weight - pred0)^2)/n_test)

RMSE_test0

## [1] 74.83068

RMSE_train0

## [1] 71.14914

As expected, RMSE_{test} > RMSE_{train}
```

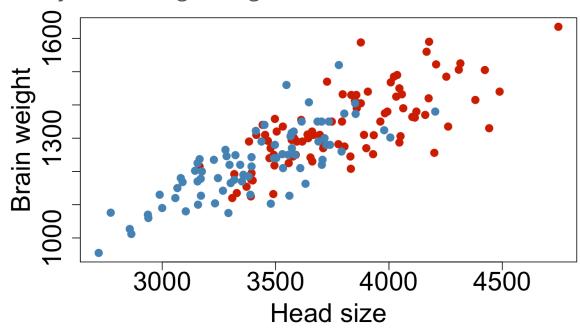
### Prediction performance in weight data

### Linear Regression for machine learning

- · Want to predict the outcome using a linear function of the features
- $\widehat{Y} = f(X) = \beta_0 + \beta_1 X_1 + \ldots + \beta_p X_p$
- · Model is  $Y = \beta_0 + \beta_1 X_1 + \ldots + \beta_p X_p + \epsilon$
- where  $\epsilon = Y \widehat{Y}$
- The residual/error term simply captures the discrepancy between the outcome and the predicted value due to:
  - noise
  - predictive variables not included the model
  - true relationship not being linear
- · BUT, we will not assume linearity or that  $\epsilon$  is normally distributed or that it has the same variance across observations

### Fitting a more complex model

· Plot by Sex, distinguishing Males (red) and Females (blue)



Separate intercepts may improve prediction

### Multiple Linear Regression in R

```
brain_lm1 = lm(Brain.weight ~ Head.size + Sex, data = brain_train)
summary(brain lm1)
##
## Call:
## lm(formula = Brain.weight ~ Head.size + Sex, data = brain_train)
## Residuals:
       Min
                 10 Median
                                  30
                                          Max
## -183.796 -50.258 -3.397 48.411 233.505
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 334.03647 68.47214 4.878 2.54e-06 ***
## Head.size
                0.26328
                          0.01786 14.742 < 2e-16 ***
## SexFemale -7.35880 13.28798 -0.554
                                              0.58
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 71.74 on 162 degrees of freedom
## Multiple R-squared: 0.6632, Adjusted R-squared: 0.6591
## F-statistic: 159.5 on 2 and 162 DF, p-value: < 2.2e-16
```

### Multiple Linear Regression in R

Computed train and test RMSE and  ${\it R}^{\it 2}$  for this modes (code not shown):

```
## RMSE_train0 RMSE_test0 RMSE_train1 RMSE_test1 ## 71.15 74.83 71.08 74.17
```

· Adding **Sex** to the linear regression model yields only a marginal improvement in prediction performance

# Your turn! Do the linear regression lab