

Problem 4:

Rocky Terrain: 2 km/h

$$\rightarrow \frac{60}{2} = 30 \text{ min/km}$$

Sandy Terrain: 3 km/h

$$\rightarrow \frac{60}{3} = 20 \text{ min/km}$$

Smooth Terrain: 5 km/h

$$\rightarrow \frac{60}{5} = 12 \text{ min/km}$$

Route 1: 5 km

$$20\% \text{ Sandy: } 0.2 \times 20 = 4 \text{ min}$$

$$30\% \text{ Smooth: } 0.3 \times 12 = 3.6 \text{ min}$$

$$50\% \text{ Rocky: } 0.5 \times 30 = 15 \text{ min}$$

$$\text{Time/km} = 4 + 3.6 + 15 = 22.6 \text{ min/km}$$

$$\text{total time} = 22.6 \times 5 = 113 \text{ min}$$

Route 2: 7 km

$$40\% \text{ Sandy: } 0.4 \times 20 = 8 \text{ min}$$

$$20\% \text{ Smooth: } 0.2 \times 12 = 2.4 \text{ min}$$

$$40\% \text{ Rocky: } 0.4 \times 30 = 12 \text{ min}$$

$$\text{Time/km} = 8 + 2.4 + 12 = 22.4 \text{ min/km}$$

$$\text{total time} = 22.4 \times 7 = 156.8 \text{ min}$$

Route 3: 6 km

$$50\% \text{ Sandy: } 0.5 \times 20 = 10 \text{ min}$$

$$40\% \text{ Smooth: } 0.4 \times 12 = 4.8 \text{ min}$$

$$10\% \text{ Rocky: } 0.1 \times 30 = 3 \text{ min}$$

$$\text{Time/km} = 10 + 4.8 + 3 = 17.8 \text{ min/km}$$

$$\text{total time} = 17.8 \times 6 = 106.8 \text{ min}$$

Best route is route 3

$\rightarrow$  which takes 106.8 min

Route 1 with crater:

30% wall damage = +15 min

70% intact walls = -20 min

$$\rightarrow (0.3 \times 15) + (0.7 \times (-20)) = 4.5 - 14 = -9.5 \text{ min}$$

Route 1 updated time:

$$\rightarrow 113 - 9.5 = \underline{103.5 \text{ min}}$$

Route 3 with bridge:

60% bridge damage = +40 min

40% bridge intact = no change

$$\rightarrow (0.6 \times 40) + (0.4 \times 0) = 24 \text{ min}$$

Route 3 updated time:

$$\rightarrow 106.8 + 24 = \underline{130.8 \text{ min}}$$

Route 1 = 103.5 min  $\rightarrow$  best option

Route 2 = 156.8 min

Route 3 = 130.8 min

Route 2: Satellite  $\rightarrow$  not Rocky

$$\text{Adjusted sandy probability} = \frac{40}{40+20} \cdot \frac{2}{3} = 66.7$$

$$\text{Adjusted smooth probability} = \frac{20}{40+20} = \frac{1}{3} = 33.3$$

$$\text{Sandy} \rightarrow \frac{2}{3} \times 20 = 13.33 \text{ min/km}$$

$$\text{Smooth} \rightarrow \frac{1}{3} \times 12 = 4 \text{ min/km}$$

$$\text{time per km} = 13.33 + 4 = 17.33 \text{ min/km}$$

$$\text{total time} = 17.33 \times 7 = \underline{121.3 \text{ min}}$$

What's the probability that the satellite tells us this?

$$1 - P(\text{rocky}) = 1 - 0.4 = 60\%$$

Satellite tells us it's rocky

Route 2  $\rightarrow$  100% rocky

$$\frac{60}{2} = 30 \text{ min/km}$$

$$\text{total time} = 30 \times 7 = 210 \text{ min}$$

We would never wait for the satellite because Route 1 would be faster either way?