

ASSIGNMENT 5 - Problem 4 Utility

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Rocky : $2\text{km/hr} = 30\text{min/km}$

Sandy : $3\text{km/hr} = 20\text{min/km}$

Smooth : $5\text{km/hr} = 12\text{min/km}$

PART 1 : Expected Time for each Route

R1 (5km):

$$\left. \begin{array}{l} 20\% \text{ Sandy} \rightarrow 5 \times 20 \times 0.2 = 20 \text{ min} \\ 30\% \text{ Smooth} \rightarrow 5 \times 12 \times 0.3 = 18 \text{ min} \\ 50\% \text{ Rocky} \rightarrow 5 \times 30 \times 0.5 = 75 \text{ min} \end{array} \right\} \begin{array}{l} \text{R1} \\ \text{sum} = 113 \text{ minutes} \end{array}$$

R2 (7km):

$$\left. \begin{array}{l} 40\% \text{ Sandy} \rightarrow 7 \times 20 \times 0.4 = 56 \text{ min} \\ 20\% \text{ Smooth} \rightarrow 7 \times 12 \times 0.2 = 16.8 \text{ min} \\ 40\% \text{ Rocky} \rightarrow 7 \times 30 \times 0.4 = 84 \text{ min} \end{array} \right\} \begin{array}{l} \text{R2} \\ \text{sum} = 156.8 \text{ minutes} \end{array}$$

R3 (6km):

$$\left. \begin{array}{l} 50\% \text{ Sandy} \rightarrow 6 \times 20 \times 0.5 = 60 \text{ min} \\ 40\% \text{ Smooth} \rightarrow 6 \times 12 \times 0.4 = 28.8 \text{ min} \\ 10\% \text{ Rocky} \rightarrow 6 \times 30 \times 0.1 = 18 \text{ min} \end{array} \right\} \begin{array}{l} \text{R3} \\ \text{sum} = 106.8 \text{ minutes} \end{array}$$

ROUTE 3

PART 2 : R1 + crater ; R3 + bridge

$$\begin{aligned} \text{R1 (70\% } -20\text{min ; 30\% } +15\text{min)} &\Rightarrow (0.7 \times (-20)) + (0.3 \times 15) = -9.5 \text{ min} \\ &\Rightarrow 113 - 9.5 = \underline{103.5 \text{ min}} \end{aligned} \quad \text{ROUTE 1}$$

$$\begin{aligned} \text{R3 (60\% } +40\text{min)} &\Rightarrow (0.6 \times 40) = 24 \text{ min} \\ &\Rightarrow 106.8 + 24 = \underline{130.8 \text{ min}} \end{aligned}$$

PART 3 : satellite confirmed R2 not rocky

$$\left. \begin{array}{l} 67\% \text{ Sandy : } 7 \times 20 \times 0.67 = 93.8 \text{ min} \\ 33\% \text{ Smooth : } 7 \times 12 \times 0.33 = 27.7 \text{ min} \end{array} \right\} \begin{array}{l} \text{R2} \\ \text{Total} = \underline{121.5 \text{ min}} \end{array}$$

PART 4: probability that satellite will tell us this $\rightarrow P(\text{R2 not rocky}) = \underline{60\% \text{ chance}}$

PART 5: if R2 is rocky, we should take the $\underline{\text{new R1} \Rightarrow 103.5 \text{ min}}$

PART 6: should we wait? no

$$\begin{aligned} &\Rightarrow 60\% \text{ Not Rocky of } (121.5 \text{ min}) + 40\% \text{ Rocky of R1 - best route } 103.5 \\ &\Rightarrow (0.6 \times 121.5) + (0.4 \times 103.5) = 114.3 \text{ min} \\ &\Rightarrow 114.3 > 103.5 ; \text{ so } \underline{\text{we should not wait for the satellite, and just take Route 1.}} \end{aligned}$$