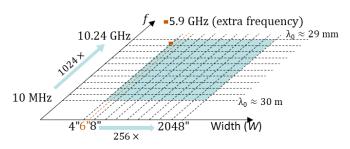
## **Description of Scattering Object**

A perfect electrically conducting (PEC) zero-thickness plate of size  $W \times 7W/4$ .

### **Length Scale and Frequency Range**



The problems of interest cover a range of 512x in physical length scale and 1024x in frequency; the ranges are logarithmically sampled to yield 110 scattering problems. Because the plates are PEC, there are only 20 + 1 + 12 unique scattering problems in Problem Set IIA. In these problems, the plate widths are in the range  $0.0034 \le W/\lambda_0 \le 1776$ , where  $\lambda_0$  is the freespace wavelength.

### **Interesting Features**

- 1. The set includes 1 extra frequency for W=4 in because of publicly available measurement data [1].
- 2. The logarithmic sampling is distorted along the length axis and an extra plate of W=6 in is introduced because of publicly available measurement data corresponding to this size [2]. The sampling is also distorted along the frequency axis: Scattering from the plate of W=6 in at frequencies  $f\in\{10,$ 20, 40, 80, 160, 320, 640, 1280, 2560, 5120, 7000, 10240} MHz are included in the problem set because of measurement data in [2]. These distortions add 12 unique scattering problems to the set. The solutions of these 12 problems can be compared to the corresponding problems in problem set IIB.
- 3. Zero thickness prevents various formulations and exercises others.

#### **Quantities of Interest**

Radar cross section (RCS) definition

$$\sigma_{vu}(\theta^{s}, \phi^{s}, \theta^{i}, \phi^{i}) = \lim_{R \to \infty} 4\pi R \frac{|\hat{v}(\theta^{s}, \phi^{s}) \cdot \mathbf{E}^{\text{scat}}(\theta^{s}, \phi^{s})|^{2}}{|\hat{u}(\theta^{i}, \phi^{i}) \cdot \mathbf{E}^{\text{scat}}(\theta^{i}, \phi^{i})|^{2}} : \text{RCS}(m^{2})$$

$$= (\theta^{s}, \phi^{s}, \theta^{i}, \phi^{i}) = 10 \log_{10} \sigma_{10}$$

$$= RCS \text{ in dB}$$

 $\sigma_{vu,dB}(\theta^{s},\phi^{s},\theta^{i},\phi^{i}) = 10 \log_{10} \sigma_{vu}$ : RCS in dB (dBsm)

 $\sigma_{vu,dB}^{TH}(\theta^{s},\phi^{s},\theta^{i},\phi^{i}) = \max(\sigma_{vu,dB},TH_{vu,dB}) - TH_{vu,dB} \qquad : \text{Thresholded RCS}$ 

- 1. Set  $\theta^i = 80^\circ$ . Vary  $0^\circ \le \phi^i \le 90^\circ$  (every  $0.5^\circ$  in the interval).
- 2. Compute back-scattered  $\sigma_{\theta\theta,\mathrm{dB}}$  and  $\sigma_{\phi\phi,\mathrm{dB}}$  (the VV- and HH-pol RCS in dB) at  $N_{\phi}=181$  directions.



Error Measure: Simulation errors shall be quantified using

$$avg. err_{uu, \text{dB}}^{TH} = \frac{1}{2\pi} \int_0^{2\pi} \left| \sigma_{uu, \text{dB}}^{TH}(\phi^s) - \sigma_{uu, \text{dB}}^{\text{ref}, TH}(\phi^s) \right| d\phi^s \approx \frac{1}{N_\phi} \sum_{n=1}^{N_\phi} \left| \sigma_{uu, \text{dB}}^{TH}(\phi^s_n) - \sigma_{uu, \text{dB}}^{\text{ref}, TH}(\phi^s_n) \right|$$
 (dB) for  $u \in \{\theta, \phi\}$ 

where

$$TH_{uu,dB} = \max_{\phi^s} \sigma_{uu,dB}^{ref} - 80 \text{ (dB)}$$

This error measure discounts errors in RCS values smaller than TH.

Cost Measure: Simulation costs shall be quantified using observed wall-clock time and peak memory/process

$$t^{\text{wall}}$$
(s) and  $mem^{\text{maxproc}}$ (bytes)

as well as the "serialized" CPU time and total memory requirement

$$t^{\rm total} = N_{\rm proc} \times t^{\rm wall}$$
(s) and  $mem^{\rm max} = N_{\rm proc} \times mem^{\rm maxproc}$  (bytes)

Here,  $N_{\rm proc}$  denotes the number of processes used in a parallel simulation. It is expected that results will be reported for at least 2 runs: "Efficient" (small  $N_{\rm proc}$ ) and "Fast" (large  $N_{\rm proc}$ ).

# Study 1: Error vs. Cost Sweep

Fix frequency and fix plate dimensions. Simulate many error levels (proxy: mesh densities) for 4 cases:

Case 1: f=10 MHz, W=4 in Case 2: f=5.12 GHz, W=4 in Case 3: f=10 MHz, W=128 in Case 4: f=320 MHz, W=128 in

It's recommended to simulate as many error levels (mesh densities) as possible. 3-5 error levels is typical. A typical error-vs.-cost study will consist of 4x3-5=12-20 simulations.

#### **Study 2: Frequency Sweep**

Fix plate dimensions and error level (proxy: mesh density). Simulate many frequencies for 4 cases:

Case 1: W=4 in, error level 1 (coarsest mesh) Case 2: W=128 in, error level 1 (coarsest mesh)

Case 3: W=4 in, error level 2 (finer mesh) Case 4: W=128 in, error level 2 (finer mesh)

Frequencies shall be chosen as  $f \in \{10, 20, 40, ..., 5120, 10240\}$  MHz. It's recommended to simulate as many frequencies as possible. A full frequency-sweep study will consist of 4x11=44 simulations.

#### Study 3: Size Sweep

Fix frequency and error level (proxy: mesh density). Simulate many sizes for 4 cases:

Case 1: f=10 MHz, error level 1 (coarsest mesh) Case 2: f=320 MHz, error level 1 (coarsest mesh)

Case 3: f=10 MHz, error level 2 (finer mesh) Case 4: f=320 MHz, error level 2 (finer mesh)

Diameters shall be chosen as  $D \in \{4, 8, 16, ..., 1012, 2048\}$  in. It's recommended to simulate as many sizes as possible. A full size-sweep study will consist of 4x9=36 simulations.

### **Study 4: Thin PEC Plate Comparison**

Fix frequency and error level (proxy: mesh density). Simulate the frequencies  $f \in \{2560, 5120, 7000, 10240\}$  MHz for W=6 in and compare the results to those from the W=6 in thin PEC plate (of 64 mil thickness) in problem set II-B. For this comparison, change the zero-thickness plate's orientation so that it resides on the z-y plane, not the x-y plane. Also set  $\theta^i=90^\circ$  as in problem set II-B.

#### **Reference Quantities of Interest**

The following RCS data are made available in the benchmark to enable participants to calibrate their simulators:

4 RCS results corresponding to the cases in study 1 found by using ARCHIE-AIM code, a frequency-domain FFT-accelerated integral-equation solver developed at UT Austin [3]-[5].

4 RCS results corresponding to the cases in study 4 found by using ARCHIE-AIM code [3]-[5].

#### References

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