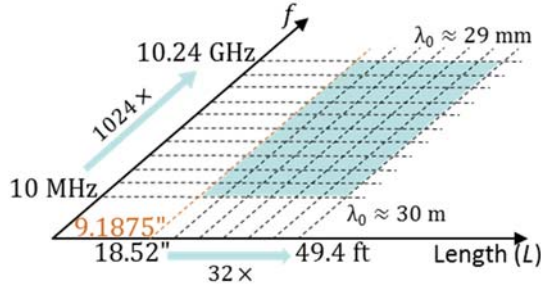


### Description of Scattering Object

A perfect electrically conducting (PEC) complex aircraft model.

### Length Scale and Frequency Range



The problems of interest cover a range of  $\sim 64\times$  in physical length scale and  $1024\times$  in frequency; the ranges are logarithmically sampled to yield 99 scattering problems. Because the aircrafts are PEC, there are only  $17 + 12$  unique scattering problems in Problem Set IVA. In these problems, the model sizes are in the range  $0.007 \leq L/\lambda_0 \leq 514$ , where  $\lambda_0$  is the free-space wavelength.

### Interesting Features

1. The logarithmic sampling is distorted along the size axis for the smallest model: the smallest Closed-Duct PRIME aircraft has  $L=9.1875''$  (instead of  $L\approx 9.261''$ ). The sampling is also distorted along the frequency axis: scattering from the smallest aircraft at frequencies  $f \in \{10, 20, 40, 80, 160, 320, 640, 1280, 2580, 5120, 7000, 10250\}$  MHz are included in the problem set. These distortions are because of publicly available measurement data [1] and add 12 unique scattering problems to the set.

2. The model cannot be described sufficiently with a few equations, drawings, or pictures [1]; it presents modeling, meshing, and reproducibility challenges.

### Quantities of Interest

Radar cross section (RCS) definition

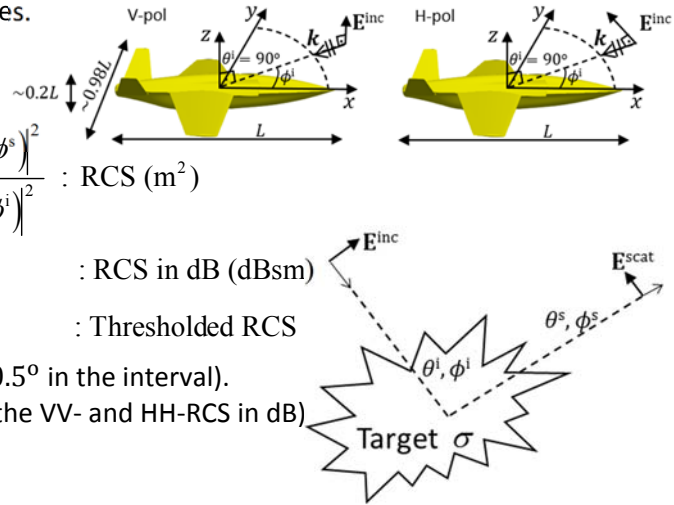
$$\sigma_{vu}(\theta^s, \phi^s, \theta^i, \phi^i) = \lim_{R \rightarrow \infty} 4\pi R^2 \frac{|\hat{v}(\theta^s, \phi^s) \cdot \mathbf{E}^{\text{scat}}(\theta^s, \phi^s)|^2}{|\hat{u}(\theta^i, \phi^i) \cdot \mathbf{E}^{\text{inc}}(\theta^i, \phi^i)|^2} : \text{RCS (m}^2\text{)}$$

$$\sigma_{vu,\text{dB}}(\theta^s, \phi^s, \theta^i, \phi^i) = 10 \log_{10} \sigma_{vu} : \text{RCS in dB (dBsm)}$$

$$\sigma_{vu,\text{dB}}^{\text{TH}}(\theta^s, \phi^s, \theta^i, \phi^i) = \max(\sigma_{vu,\text{dB}}, TH_{vu,\text{dB}}) - TH_{vu,\text{dB}} : \text{Thresholded RCS}$$

1. Set  $\theta^i = 90^\circ$ . Vary  $0^\circ \leq \phi^i \leq 180^\circ$  (every  $0.5^\circ$  in the interval).

2. Compute back-scattered  $\sigma_{\theta\theta,\text{dB}}$  and  $\sigma_{\phi\phi,\text{dB}}$  (the VV- and HH-RCS in dB) at  $N_\phi = 361$  scattering directions.



### Performance Measures

**Error Measure:** Simulation errors shall be quantified using

$$\text{avg. err}_{uu,\text{dB}}^{\text{TH}} = \frac{1}{2\pi} \int_0^{2\pi} |\sigma_{uu,\text{dB}}^{\text{TH}}(\phi^s) - \sigma_{uu,\text{dB}}^{\text{ref},\text{TH}}(\phi^s)| d\phi^s \approx \frac{1}{N_\phi} \sum_{n=1}^{N_\phi} |\sigma_{uu,\text{dB}}^{\text{TH}}(\phi^s) - \sigma_{uu,\text{dB}}^{\text{ref},\text{TH}}(\phi^s)| \text{ (dB) for } u \in \{\theta, \phi\}$$

where

$$TH_{uu,\text{dB}} = \max_{\phi^s} \sigma_{uu,\text{dB}}^{\text{ref}} - 80 \text{ (dB)}$$

This error measure discounts errors in RCS values below  $TH$ .

**Cost Measure:** Simulation costs shall be quantified using observed wall-clock time and peak memory/core

$$t_{\text{main}}^{\text{wall}} \text{ (s) and } mem_{\text{main}}^{\text{maxcore}} \text{ (bytes)}$$

as well as the “serialized” CPU time and total memory requirement

$$t_{\text{main}}^{\text{total}} = N_{\text{proc}} \times t_{\text{main}}^{\text{wall}} \text{ (s) and } mem_{\text{main}}^{\text{max}} = N_{\text{proc}} \times mem_{\text{main}}^{\text{maxcore}} \text{ (bytes)}$$

Here,  $N_{\text{proc}}$  denotes the number of processes used in a parallel simulation. It is expected that results will be reported for at least 2 runs: “Efficient” (small  $N_{\text{proc}}$ ) and “Fast” (large  $N_{\text{proc}}$ ).

### Study 1: Error vs. Cost Sweep

Fix frequency and fix aircraft dimensions. Simulate many error levels (proxy: mesh densities) for 4 cases:

Case 1:  $f=10$  MHz,  $L=9.1875$  in

Case 2:  $f=7$  GHz,  $L=9.1875$  in

Case 3:  $f=10$  MHz,  $L \approx 49.4$  ft (592.763 in)

Case 4:  $f=320$  MHz,  $L \approx 49.4$  ft (592.763 in)

It’s recommended to simulate as many error levels (mesh densities) as possible. 3-5 error levels is typical.

A typical error-vs.-cost study will consist of  $4 \times 3 \times 5 = 12 \times 5 = 60$  simulations.

### Study 2: Frequency Sweep

Fix aircraft dimensions and error level (proxy: mesh density). Simulate many frequencies for 4 cases:

Case 1:  $L \approx 18.52$  in, error level 1 (coarsest mesh)

Case 2:  $L \approx 49.4$  ft, error level 1 (coarsest mesh)

Case 3:  $L \approx 18.52$  in, error level 2 (finer mesh)

Case 4:  $L \approx 49.4$  ft, error level 2 (finer mesh)

Frequencies shall be chosen as  $f \in \{10, 20, 40, \dots, 5120, 10240\}$  MHz. It’s recommended to simulate as many frequencies as possible. A full frequency-sweep study will consist of  $4 \times 11 = 44$  simulations.

### Study 3: Size Sweep

Fix frequency and error level (proxy: mesh density). Simulate many sizes for 4 cases:

Case 1:  $f=10$  MHz, error level 1 (coarsest mesh)

Case 2:  $f=320$  MHz, error level 1 (coarsest mesh)

Case 3:  $f=10$  MHz, error level 2 (finer mesh)

Case 4:  $f=320$  MHz, error level 2 (finer mesh)

Dimensions shall be chosen as  $L \in \{9.1875, 18.524, 37.04, \dots, 296.3815, 592.763\}$  in. It’s recommended to simulate as many sizes as possible. A full size-sweep study will consist of  $4 \times 7 = 28$  simulations.

### Reference Quantities of Interest

The following RCS data are made available in the benchmark to enable participants to calibrate their simulators:

8 RCS measurement results corresponding to the smallest aircraft ( $L=9.1875$  in) at frequencies  $f \in \{2580, 5120, 7000, 10250\}$  MHz. These measurements were made using two aircraft scale models [1]: one was of size  $L=9.375$  in and the other was scaled up 2x in all dimensions. These data are provided for  $\phi^i$  sampled every  $0.25^\circ$ .

4 RCS simulation results for the smallest aircraft at the above 4 frequencies found by using the ARCHIE-AIM code, a frequency-domain FFT-accelerated integral-equation solver developed at UT Austin [2]-[4].

### References

- [1] J. T. Kelley, A. Maicke, D. A. Chamulak, C. C. Courtney, and A. E. Yilmaz, “Adding a reproducible airplane model to the Austin RCS Benchmark Suite,” in *Proc. Applied Comp. Electromagnetics Society (ACES) Symp.*, July 2020.
- [2] M. F. Wu, G. Kaur, and A. E. Yilmaz, “A multiple-grid adaptive integral method for multi-region problems,” *IEEE Trans. Antennas Propag.*, vol. 58, no. 5, pp. 1601-1613, May 2010.
- [3] F. Wei and A. E. Yilmaz, “A more scalable and efficient parallelization of the adaptive integral method part I: algorithm,” *IEEE Trans. Antennas Propag.*, vol. 62, no.2, pp. 714-726, Feb. 2014.
- [4] J. W. Massey, V. Subramanian, C. Liu, and A. E. Yilmaz, “Analyzing UHF band antennas near humans with a fast integral-equation method,” in *Proc. EUCAP*, Apr. 2016.