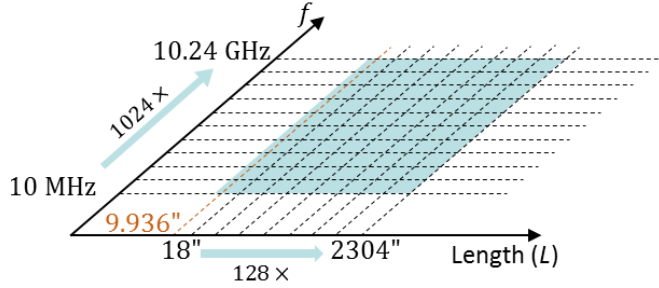


### Description of Scattering Object

A perfect electrically conducting (PEC) almond proportional to the dimensions in [1].

### Length Scale and Frequency Range



The problems of interest cover a range of  $\sim 256\times$  in physical length scale and  $1024\times$  in frequency; the ranges are logarithmically sampled to yield 99 scattering problems. Because the almonds are PEC, there are only  $19 + 12$  unique scattering problems in Problem Set IIIA. In these problems, the almond sizes are in the range  $0.0076 \leq L/\lambda_0 \leq 1998$ , where  $\lambda_0$  is the free-space wavelength.

### Interesting Features

1. The logarithmic sampling is distorted along the length axis for the smallest almond: the smallest almond has  $L=9.936''$  (instead of  $L=9$  in) because of publicly available measurement data corresponding to this size [1],[2]. The sampling is also distorted along the frequency axis: scattering from the smallest almond at frequencies  $f \in \{10, 20, 40, 80, 160, 320, 640, 1280, 3500, 5125, 7000, 10250\}$  MHz are included in the problem set because of publicly available measurement data [2]. These distortions add 12 unique scattering problems to the set.
2. The non-trivial shape and tip of the almond presents modeling and meshing challenges.

### Quantities of Interest

Radar cross section (RCS) definition

$$\sigma_{vu}(\theta^s, \phi^s, \theta^i, \phi^i) = \lim_{R \rightarrow \infty} 4\pi R \frac{|\hat{v}(\theta^s, \phi^s) \cdot \mathbf{E}^{\text{scat}}(\theta^s, \phi^s)|^2}{|\hat{u}(\theta^i, \phi^i) \cdot \mathbf{E}^{\text{scat}}(\theta^i, \phi^i)|^2} : \text{RCS (m}^2\text{)}$$

$$\sigma_{vu,\text{dB}}(\theta^s, \phi^s, \theta^i, \phi^i) = 10 \log_{10} \sigma_{vu} : \text{RCS in dB (dBsm)}$$

$$\sigma_{vu,\text{dB}}^{TH}(\theta^s, \phi^s, \theta^i, \phi^i) = \max(\sigma_{vu,\text{dB}}, TH_{vu,\text{dB}}) - TH_{vu,\text{dB}} : \text{Thresholded RCS}$$

1. Set  $\theta^i = 90^\circ$ . Vary  $0^\circ \leq \phi^i \leq 180^\circ$  (every  $0.5^\circ$  in the interval).
2. Compute back-scattered  $\sigma_{\theta\theta,\text{dB}}$  and  $\sigma_{\phi\phi,\text{dB}}$  (the VV- and HH-pol RCS in dB) at  $N_\phi = 361$  scattering directions.

### Performance Measures

*Error Measure:* Simulation errors shall be quantified using

$$\text{avg. err}_{uu,\text{dB}}^{TH} = \frac{1}{2\pi} \int_0^{2\pi} |\sigma_{uu,\text{dB}}^{TH}(\phi^s) - \sigma_{uu,\text{dB}}^{\text{ref},TH}(\phi^s)| d\phi^s \approx \frac{1}{N_\phi} \sum_{n=1}^{N_\phi} |\sigma_{uu,\text{dB}}^{TH}(\phi_n^s) - \sigma_{uu,\text{dB}}^{\text{ref},TH}(\phi_n^s)| \text{ (dB) for } u \in \{\theta, \phi\}$$

where

$$TH_{uu,\text{dB}} = \max_{\phi^s} \sigma_{uu,\text{dB}}^{\text{ref}} - 80 \text{ (dB)}$$

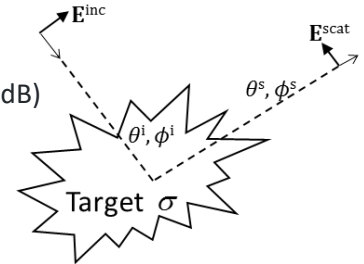
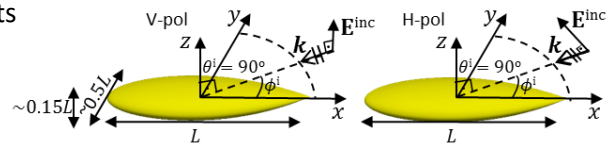
This error measure discounts errors in RCS values smaller than  $TH$ .

*Cost Measure:* Simulation costs shall be quantified using observed wall-clock time and peak memory/process

$$t^{\text{wall}}(\text{s}) \text{ and } mem^{\text{maxproc}}(\text{bytes})$$

as well as the “serialized” CPU time and total memory requirement

$$t^{\text{total}} = N_{\text{proc}} \times t^{\text{wall}}(\text{s}) \text{ and } mem^{\text{max}} = N_{\text{proc}} \times mem^{\text{maxproc}}(\text{bytes})$$



Here,  $N_{\text{proc}}$  denotes the number of processes used in a parallel simulation. It is expected that results will be reported for at least 2 runs: “Efficient” (small  $N_{\text{proc}}$ ) and “Fast” (large  $N_{\text{proc}}$ ).

### Study 1: Error vs. Cost Sweep

Fix frequency and fix almond dimensions. Simulate many error levels (proxy: mesh densities) for 4 cases:

Case 1:  $f=10$  MHz,  $L=9.936$  in

Case 2:  $f=7$  GHz,  $L=9.936$  in

Case 3:  $f=10$  MHz,  $L=288$  in

Case 4:  $f=320$  MHz,  $L=288$  in

It’s recommended to simulate as many error levels (mesh densities) as possible. 3-5 error levels is typical. A typical error-vs.-cost study will consist of  $4 \times 3 \times 5 = 12 \times 5 = 60$  simulations.

### Study 2: Frequency Sweep

Fix almond dimensions and error level (proxy: mesh density). Simulate many frequencies for 4 cases:

Case 1:  $L=18$  in, error level 1 (coarsest mesh) Case 2:  $L=288$  in, error level 1 (coarsest mesh)

Case 3:  $L=18$  in, error level 2 (finer mesh) Case 4:  $L=288$  in, error level 2 (finer mesh)

Frequencies shall be chosen as  $f \in \{10, 20, 40, \dots, 5120, 10240\}$  MHz. It’s recommended to simulate as many frequencies as possible. A full frequency-sweep study will consist of  $4 \times 11 = 44$  simulations.

### Study 3: Size Sweep

Fix frequency and error level (proxy: mesh density). Simulate many sizes for 4 cases:

Case 1:  $f=10$  MHz, error level 1 (coarsest mesh) Case 2:  $f=320$  MHz, error level 1 (coarsest mesh)

Case 3:  $f=10$  MHz, error level 2 (finer mesh) Case 4:  $f=320$  MHz, error level 2 (finer mesh)

Dimensions shall be chosen as  $L \in \{9.936, 18, 36, \dots, 1152, 2304\}$  in. It’s recommended to simulate as many sizes as possible. A full size-sweep study will consist of  $4 \times 9 = 36$  simulations.

### Reference Quantities of Interest

The following RCS data are made available in the benchmark to enable participants to calibrate their simulators:

8 RCS measurement results corresponding to the smallest almond ( $L=9.936$  in) at frequencies  $f \in \{3500, 5125, 7000, 10250\}$  MHz. These measurements were made using two almonds [2]: One was of size  $L=9.936$  in and the other was scaled up 2x in all dimensions. These data are the same as those plotted in Figs. 11-12 of [2]; they are provided for  $\phi^i$  sampled every  $0.25^\circ$ .

4 RCS simulation results for the smallest almond at the above 4 frequencies found by using the ARCHIE-AIM code, a frequency-domain FFT-accelerated integral-equation solver developed at UT Austin [3]-[5]. These data are the same as the finest mesh ( $\approx 0.6$ -mm average edge length) results in [2].

### References

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