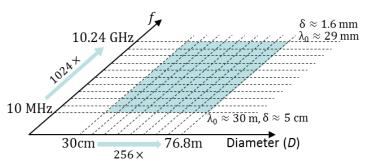
Description of Scattering Object

A semiconductor sphere of radius D/2 and conductivity 10 S/m.

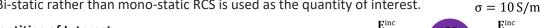
Length Scale and Frequency Range



The problems of interest cover a range of 256x in physical length scale and 1024x in frequency; the ranges are logarithmically sampled to yield 99 unique scattering problems. In these problems, the sphere sizes are in the range $0.01 \le D/\lambda_0 \le$ $2624 \text{ and } 6 \le D/\delta \le 4.75 \times 10^4$, where λ_0 is the free-space wavelength and δ is the penetration depth in the sphere.

Interesting Features

- 1. Highly accurate, Mie-series analytical solutions are available for Problem Set IB.
- 2. Bi-static rather than mono-static RCS is used as the quantity of interest.



Quantities of Interest

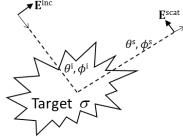
Radar cross section (RCS) definition

$$\sigma_{vu}(\theta^{s}, \phi^{s}, \theta^{i}, \phi^{i}) = \lim_{R \to \infty} 4\pi R \frac{|\hat{v}(\theta^{s}, \phi^{s}) \cdot \mathbf{E}^{\text{scat}}(\theta^{s}, \phi^{s})|^{2}}{|\hat{u}(\theta^{i}, \phi^{i}) \cdot \mathbf{E}^{\text{scat}}(\theta^{i}, \phi^{i})|^{2}} : \text{RCS (m}^{2})$$

$$\sigma_{vu,\text{dB}}(\theta^{s}, \phi^{s}, \theta^{i}, \phi^{i}) = 10 \log_{10} \sigma_{vu} : \text{RCS in dB (dBsm)}$$

$$\sigma_{vu,\text{dB}}^{TH}(\theta^{s}, \phi^{s}, \theta^{i}, \phi^{i}) = \max(\sigma_{vu,\text{dB}}, TH_{vu,\text{dB}}) - TH_{vu,\text{dB}} : \text{Thresholded RCS}$$

- 1. Set $\theta^i = 90^\circ$, $\phi^i = 0^\circ$, $\theta^s = 90^\circ$. Vary $0^\circ \le \phi^s \le 360^\circ$.
- 2. Compute both $\sigma_{\theta\theta,\mathrm{dB}}$ and $\sigma_{\phi\phi,\mathrm{dB}}$ (the VV- and HH-pol RCS in dB) at $N_{\phi}=721$ scattering directions (every $0.5^{
 m o}$ in the interval $0^{\circ} \le \phi^{\circ} \le 360^{\circ}$).



Performance Measures

Error Measure: Simulation errors shall be quantified using

$$avg. \, err_{uu, \mathrm{dB}}^{TH} = \frac{1}{2\pi} \int_0^{2\pi} \left| \sigma_{uu, \mathrm{dB}}^{TH}(\phi^s) - \sigma_{uu, \mathrm{dB}}^{\mathrm{ref}, TH}(\phi^s) \right| d\phi^s \approx \frac{1}{N_\phi} \sum_{n=1}^{N_\phi} \left| \sigma_{uu, \mathrm{dB}}^{TH}(\phi^s_n) - \sigma_{uu, \mathrm{dB}}^{\mathrm{ref}, TH}(\phi^s_n) \right| \, \, (\mathrm{dB}) \, \, \text{for} \, u \in \{\theta, \phi\}$$

where

$$TH_{uu,dB} = \max_{\phi^s} \sigma_{uu,dB}^{ref} - 80 \text{ (dB)}$$

This error measure discounts errors in RCS values smaller than TH.

Cost Measure: Simulation costs shall be quantified using observed wall-clock time and peak memory/process

$$t^{
m wall}$$
(s) and $mem^{
m maxproc}$ (bytes)

as well as the "serialized" CPU time and total memory requirement

$$t^{
m total} = N_{
m proc} imes t^{
m wall}$$
(s) and $mem^{
m max} = N_{
m proc} imes mem^{
m maxproc}$ (bytes)

Here, N_{proc} denotes the number of processes used in a parallel simulation. It is expected that results will be reported for at least 2 runs: "Efficient" (small $N_{\rm proc}$) and "Fast" (large $N_{\rm proc}$).

Study 1: Error vs. Cost Sweep

Fix frequency and fix sphere diameter. Simulate many error levels (proxy: mesh densities) for 4 cases:

Case 1: f=10 MHz, D=0.6 m Case 2: f=320 MHz, D=0.6 m Case 3: f=10 MHz, D=19.2 m Case 4: f=320 MHz, D=19.2 m

It's recommended to simulate as many error levels (mesh densities) as possible. 3-5 error levels is typical. A typical error-vs.-cost study will consist of 4x3-5=12-20 simulations.

Study 2: Frequency Sweep

Fix sphere diameter and error level (proxy: mesh density). Simulate many frequencies for 4 cases:

Case 1: D=0.6 m, error level 1 (coarsest mesh) Case 2: D=19.2 m, error level 1 (coarsest mesh)

Case 3: D=0.6 m, error level 2 (finer mesh) Case 4: D=19.2 m, error level 2 (finer mesh)

Frequencies shall be chosen as $f \in \{10, 20, 40, ..., 5120, 10240\}$ MHz. It's recommended to simulate as many frequencies as possible. A full frequency-sweep study will consist of 4x11=44 simulations.

Study 3: Size Sweep

Fix frequency and error level (proxy: mesh density). Simulate many diameters for 4 cases:

Case 1: f=10 MHz, error level 1 (coarsest mesh) Case 2: f=320 MHz, error level 1 (coarsest mesh)

Case 3: f=10 MHz, error level 2 (finer mesh) Case 4: f=320 MHz, error level 2 (finer mesh)

Diameters shall be chosen as $D \in \{0.3, 0.6, 1.2, ..., 38.4, 76.8\}$ m. It's recommended to simulate as many diameters as possible. A full size-sweep study will consist of 4x9=36 simulations.

Reference Quantities of Interest

The following RCS data are made available in the benchmark to enable participants to calibrate their simulators:

4 RCS results corresponding to the cases in study 1 found by using COMPASS-EM code [1].

References

[1] G. Kaur (2015) COMPASS-EM: Comprehensive program for analytical scattering solutions for electromagnetics. [Online]. Available: http://web.corral.tacc.utexas.edu/BioEM-Benchmarks/COMPASS-EM/index.html