

# Bond Angles

## Read-ahead

### Introduction

The chemical properties of a given molecule depend in a large part on the geometry of the molecule. One of the simplest molecules is methane,  $\text{CH}_4$ , which is the main component of natural gas. Each of the four hydrogen atoms is bonded to a single, central, carbon atom, forming a tetrahedron, as seen in Figure 1 below. In this set of problems, we determine the bond angle between any pair of hydrogen atoms.

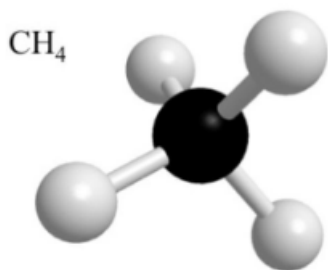


Figure 1: Methane molecule



Figure 2: A natural source of methane.

### Instructions

After reading through *Bond Angles* context and questions below, you should complete the reflection assignment in Canvas. Note: *you will have a chance to talk further with your coach before answering the questions below in detail.* The point of this read-ahead and the reflection is to "prime the pump" for further conversations with your coaches.

### Bond Angles

Draw a perpendicular line from the carbon atom (C) to the plane containing three of the hydrogen atoms. Let  $Q$  represent the foot of this perpendicular line (see figures below), and let  $y$  represent the distance between the carbon atom and any of the hydrogen atoms. Let  $a$  represent the distance from  $Q$  to one of the hydrogen atoms, and let  $x$  represent the measure of the required bond angle.

### Questions

1. Consider the angle  $\text{HQH}$  in Figure 4 below. Find the measure of this angle, in degrees.
2. Find an expression for the distance  $a$  (the length of the line segment  $\overline{HQ}$ ) in terms of the distance  $y$  and the angle  $x$ . Write your answer as an equation in the form " $a = \dots$ ".
3. Now, examine the triangle formed by two hydrogen atoms and point  $Q$ , as shown in Figure 5 below. The altitude from point  $Q$  divides the triangle  $\text{HQH}$  into two congruent triangles. So, the vertex angle  $\text{HQH}$  is divided into two angles whose measures are each  $60^\circ$ . In terms of  $a$ , what is the length of the line segment  $\overline{HT}$ ? Write your answer as an expression involving  $a$ , not as an equation.
4. Figure 6 below represents the triangle formed by the carbon atom and two hydrogen atoms. From

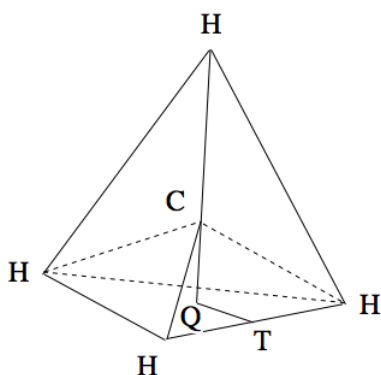


Figure 3

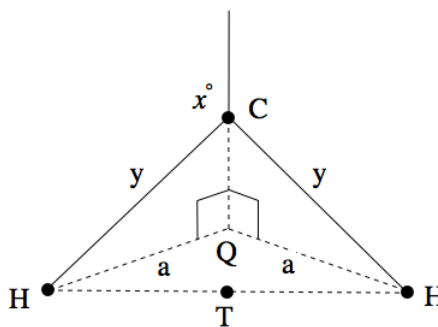


Figure 4

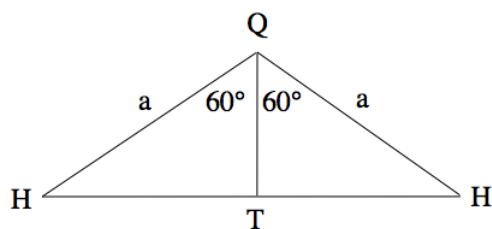


Figure 5

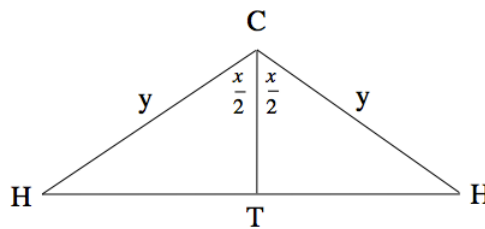


Figure 6

this figure, we see that  $\sin\left(\frac{x}{2}\right) = \frac{a\sqrt{3}}{2y}$ . Use the double angle formula  $\sin^2(\theta) = \frac{1 - \cos(2\theta)}{2}$  to rewrite the left-hand side of this equation in terms of  $\cos(x)$ , then combine the resulting equation with the expression for  $a$  you found in problem 2 above, and solve for  $\cos(x)$ . Note that there are two solutions, one positive, one negative. Round your answers to three decimal places.

5. Note that only one of the two values for  $\cos(x)$  you found in the previous part makes sense. Find  $x$  to the nearest degree.

### Instructions, part deux

After reading and reflecting on these questions, complete the pre-read assignment on Canvas. This will give your coach some insight on your thinking in order to best help you before you are required to formally answer these questions.