

S. No.	Date	Title	Page No.	Teacher's Sign

* Current divider formula

→ When 1 current (i_t) divides b/w 2 resistors (R_1 & R_2) in parallel

$$\text{Current across } R_1 = i_{R_1} = i_t \left(\frac{R_2}{R_1 + R_2} \right)$$

→ When 1 current (i_t) divides b/w 3 resistors (R_1, R_2, R_3) in parallel:

$$\text{Current across } R_1 = i_{R_1} = i_t \left[\frac{1/R_2}{\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}} \right]$$

* Voltage divider formula:

→ When Voltage (V_t) divides across 2 resistors R_1 & R_2 in Series

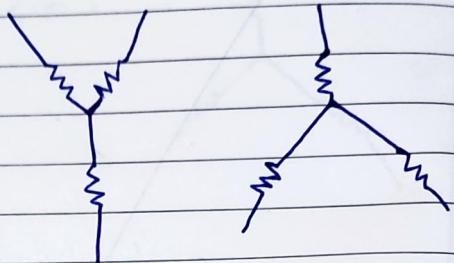
$$\text{Voltage across } R_2 = V_2 = V_t \left(\frac{R_2}{R_1 + R_2} \right)$$

→ When voltage (V_t) divides across 3 resistors R_1, R_2 & R_3 in series.

$$\text{Voltage across } R_2 = V_2 = V_t \left(\frac{R_2}{R_1 + R_2 + R_3} \right)$$

(*) Converting Star \rightarrow delta
delta \rightarrow Star.

Star : \rightarrow

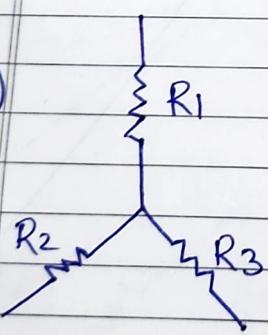


delta : \rightarrow



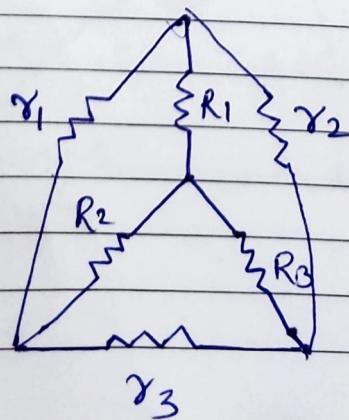
Q) Convert Star \rightarrow delta

Q)



{ Formula }

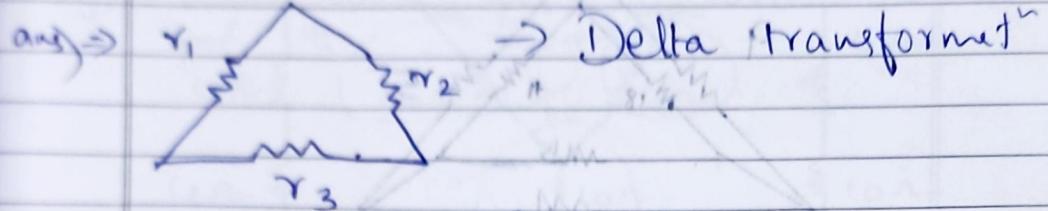
(ans)



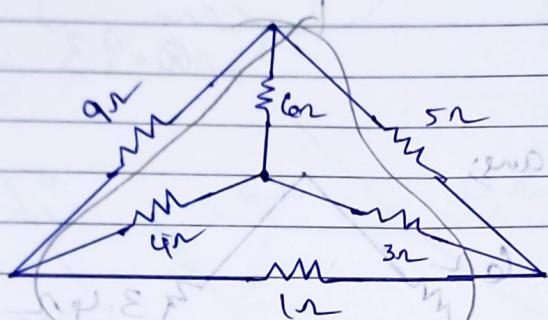
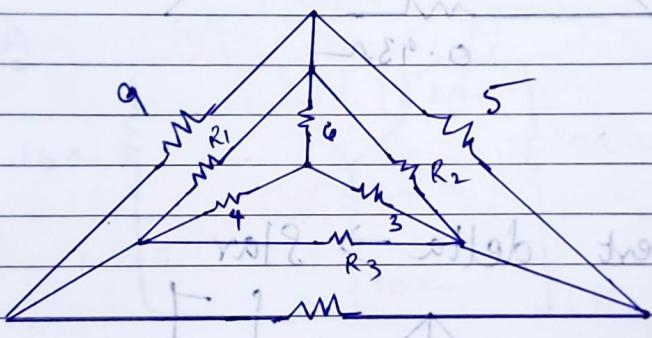
$$\gamma_1 = R_1 + R_2 + \frac{R_1 R_2}{R_3}$$

$$\gamma_2 = R_1 + R_3 + \frac{R_1 R_3}{R_2}$$

$$\gamma_3 = R_2 + R_3 + \frac{R_2 R_3}{R_1}$$



(Q)

 \rightarrow Assume R here

$$R_1 = 6 + 4 + \frac{6 \times 4}{3} = 18 \Omega$$

$$R_2 = 6 + 3 + \frac{6 \times 3}{4} = 15 \Omega$$

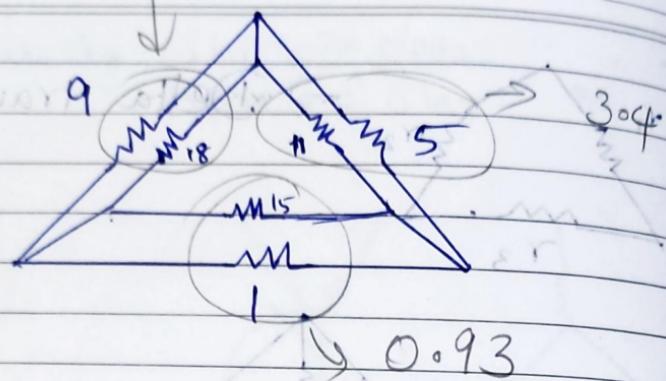
$$R_3 = 4 + 3 + \frac{4 \times 3}{6} = 11 \Omega$$

$$\frac{18 \times 15}{18+15} = 10 \Omega$$

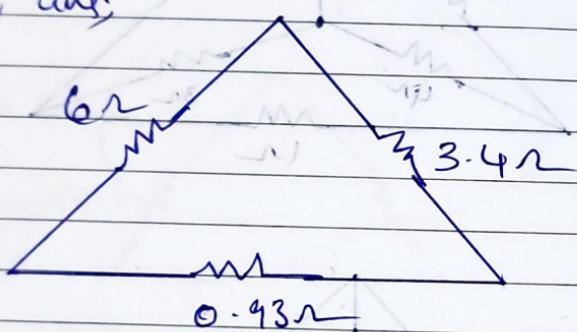
$$\frac{18 \times 11}{18+11} = 10 \Omega$$

$$R_{P\text{net}} = 6$$

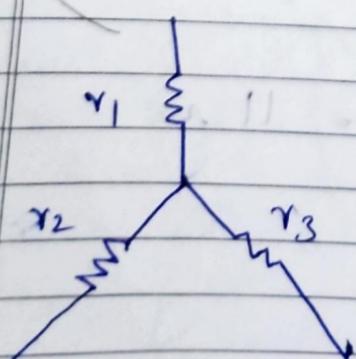
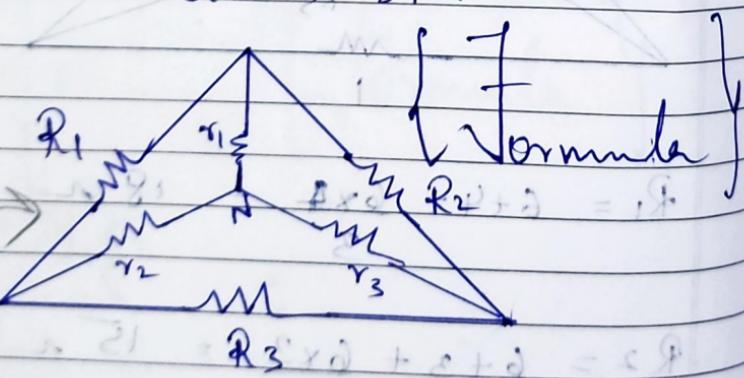
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Ref ans:



Q) Convert delta \rightarrow star.



$$\gamma_1 = \frac{R_1 \times R_2}{R_1 + R_2 + R_3}$$

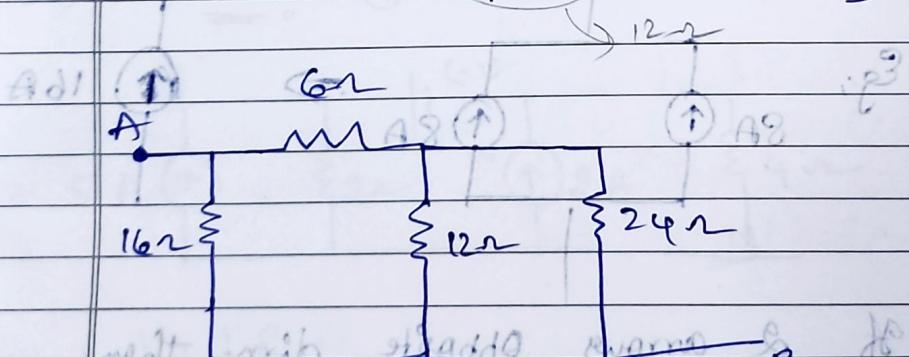
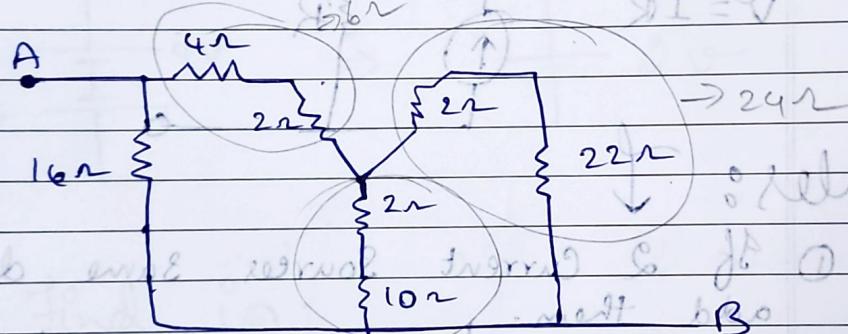
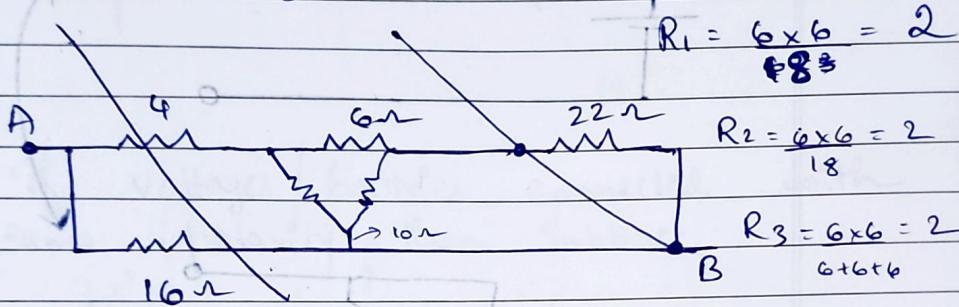
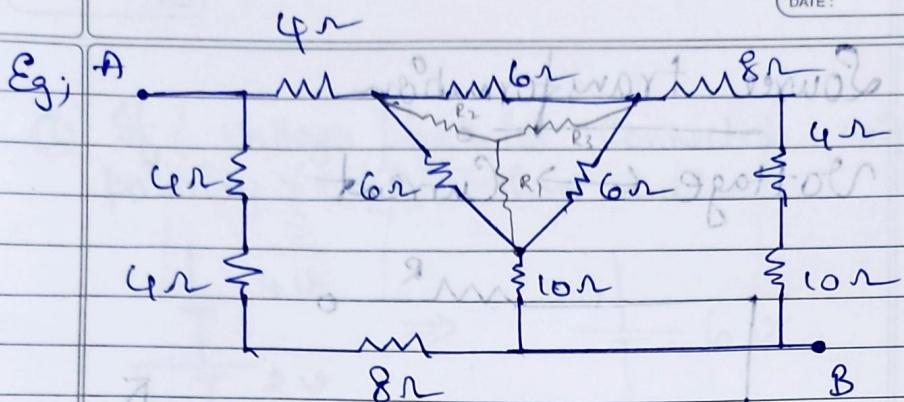
$$\gamma_2 = \frac{R_1 \times R_3}{R_1 + R_2 + R_3}$$

$$\gamma_3 = \frac{R_2 \times R_3}{R_1 + R_2 + R_3}$$

find R_{net} btw A & B

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$$\frac{1}{R_p} = \frac{1}{12} + \frac{1}{24}, R_p = 8$$

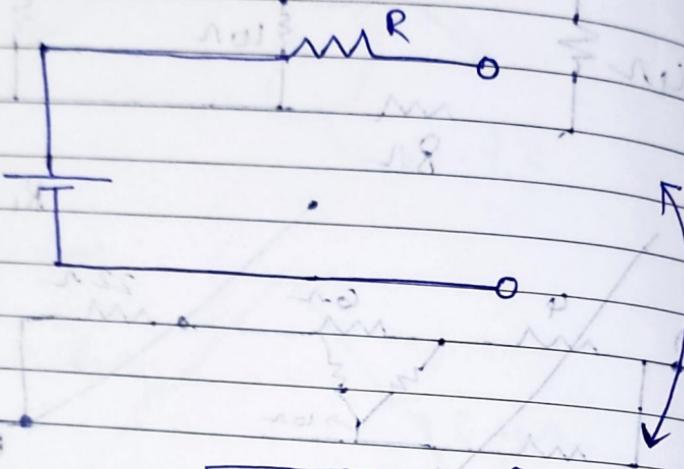
$$8+6 \Rightarrow 14\Omega$$

$$\frac{1}{R_{net}} = \frac{1}{14} + \frac{1}{16} = \frac{112}{192} = \underline{\underline{4.6\Omega}}$$

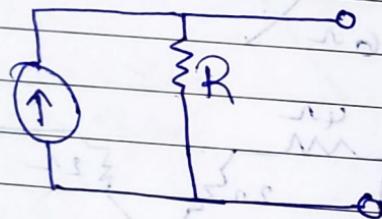
Source transformation

Voltage \leftrightarrow Current

①



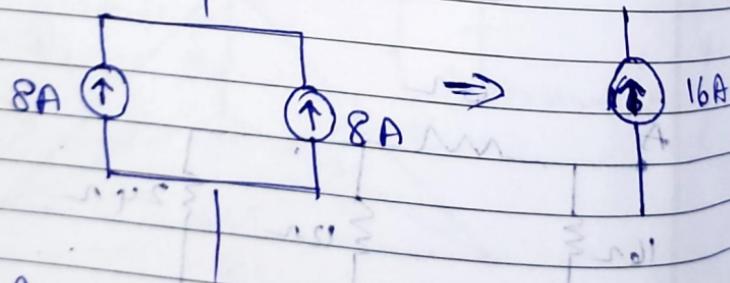
$$V = IR$$



Rules:

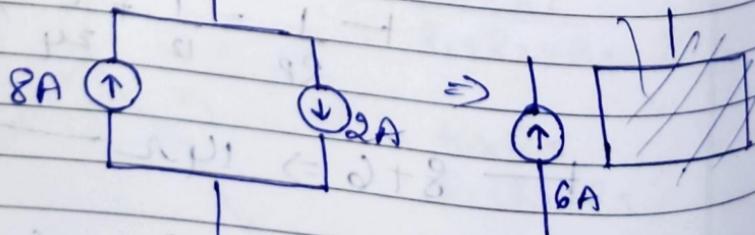
- ① If 2 Current Sources Same dirn.
add them.

Eg;

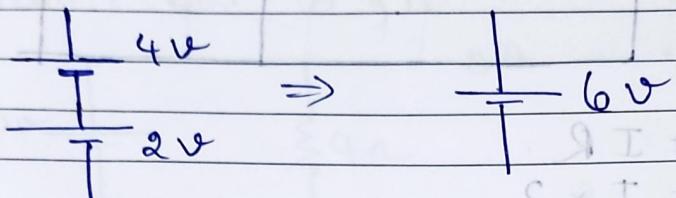


- ② If 2 arrows Opposite dirn. then
Subtract.

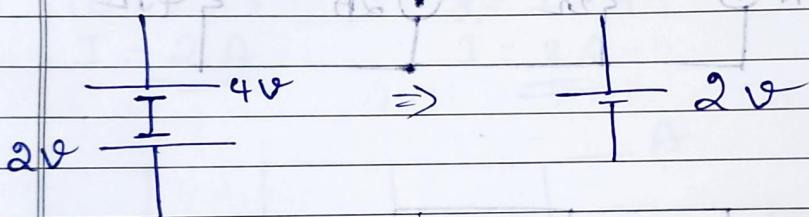
Eg;



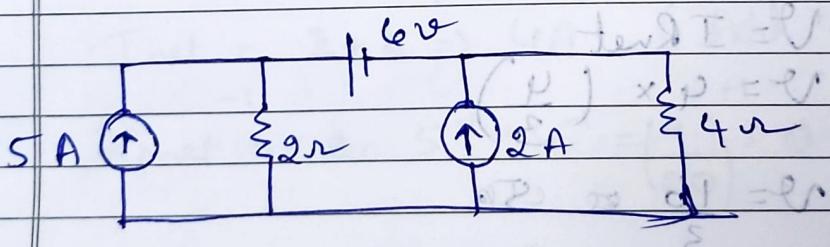
③ If voltages / batteries connected with opp. polarity (+ -) then add.



④ If voltages / batteries connected with same polarity then subtract.

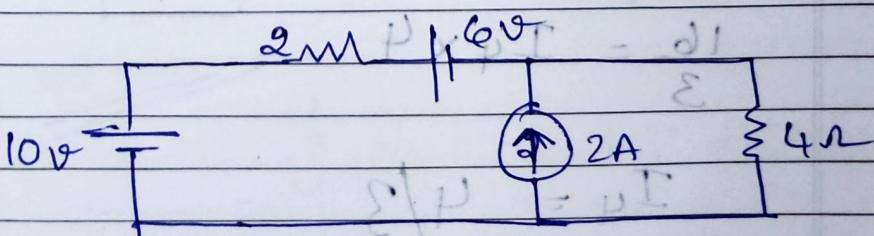


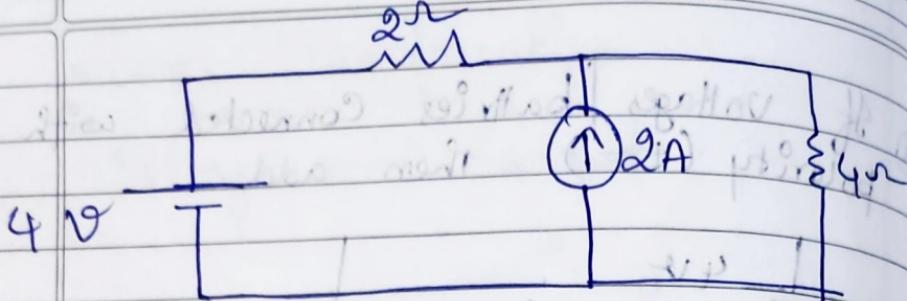
a) Find i₄:



$$V = IR$$

$$V = 5 \times 2 \Rightarrow 10$$

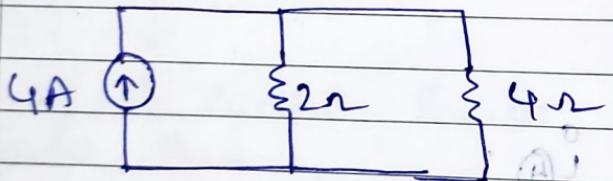
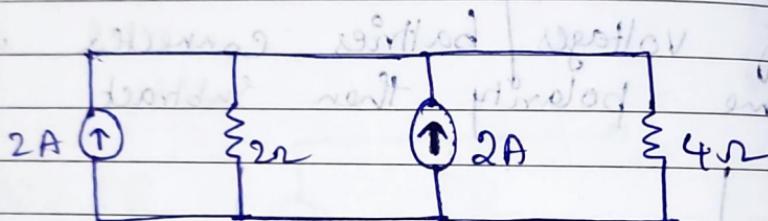




$$V = IR$$

$$V = I \times R$$

$$I = 2 \text{ A}$$



$$V = I R_{\text{net}}$$

$$V = 4 \times \left(\frac{4}{3}\right)$$

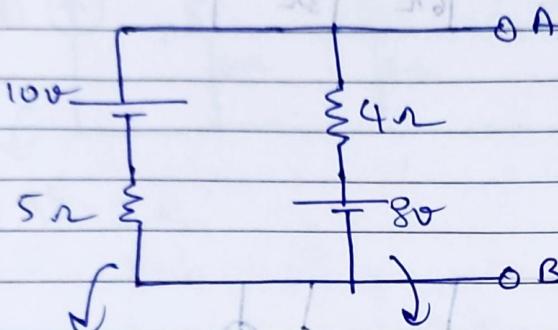
$$V = \frac{16}{3} \approx 5.33$$

$$V_4 = I_4 R$$

$$\frac{16}{3} = I_4 \times 4$$

$$I_4 = \underline{\underline{\frac{4}{3}}}$$

Q2) Convert the given ckt into a single current source in parallel with single resist. b/w A & B.



$$V = IR \quad (1)$$

Ans)

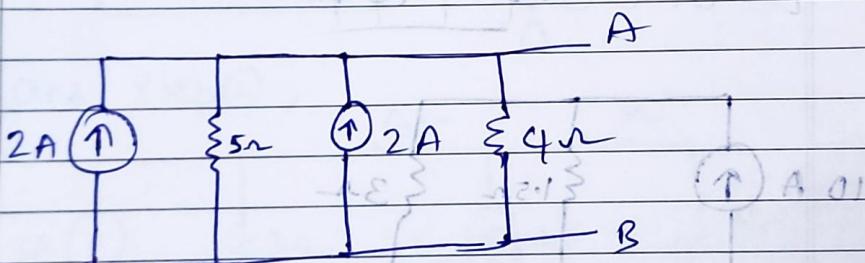
$$10 = I \times 5$$

$$\underline{I = 2 \text{ A}}$$

$$V = IR \quad (2)$$

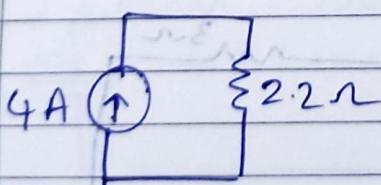
$$8 = I \times 4$$

$$\underline{I = 2 \text{ A}}$$



$$I_{\text{net}} = 2 + 2 \Rightarrow 4 \text{ A} \quad (\text{Add } \because \text{Same dir})$$

$$R_{\text{net}} = 0 \text{ ohm} \cdot 5^{-1} + 4^{-1} = \left(\frac{1}{5} + \frac{1}{4} \right)^{-1} = 2.2 \text{ ohm}$$



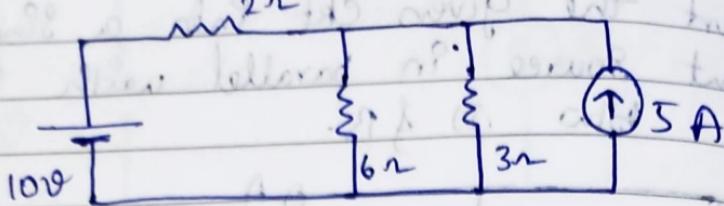
$$4 \text{ A} \times 2.2 \text{ ohm} = 8.8 \text{ V} \quad \text{Ans: } T = 8.8 \text{ V}$$

$$(\text{Ans: } T = 8.8 \text{ V}) \quad 2.2 \times T = 2.2 \times 8.8 = 20 \text{ V}$$

$$4 \text{ A} \times 2.2 \text{ ohm} = 8.8 \text{ V} \quad \text{Ans: } T = 8.8 \text{ V}$$

Find ~~I_2~~ I_3

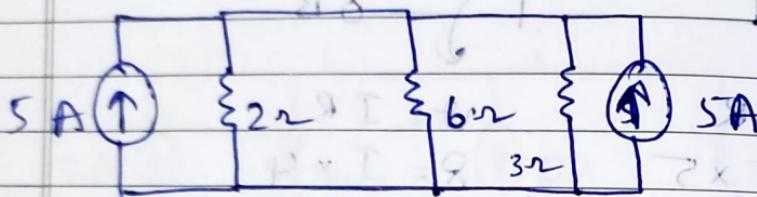
Q)



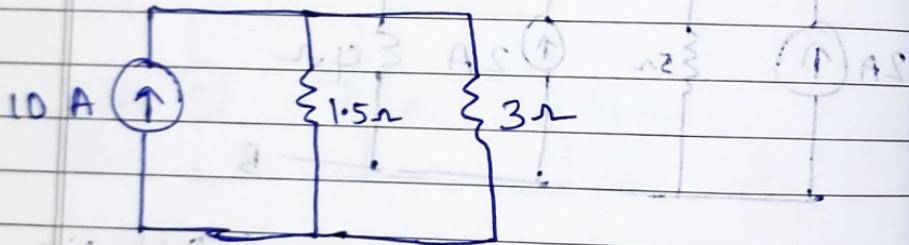
$$V = IR$$

$$10 = I \times 2$$

$$I = 5 \text{ A}$$



$$I_{\text{net}} = (5 + 5) = 10 \text{ A}$$



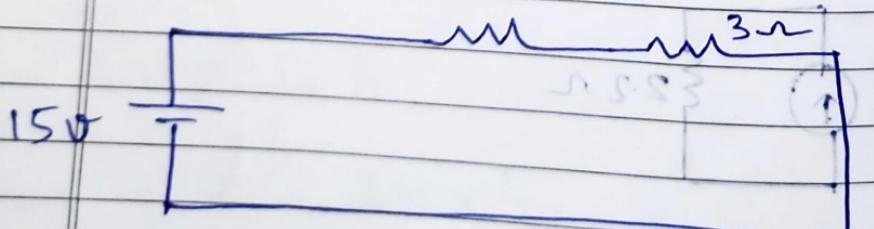
$$V = IR$$

$$V = 10 \times 1.5 \Rightarrow 10 \times 1.5 = 15 \text{ V}$$

$$V = IR$$

$$\Rightarrow 15 \text{ V}$$

1.5Ω



$$V = I R_{\text{net}}$$

$$15 = I \times 4.5$$

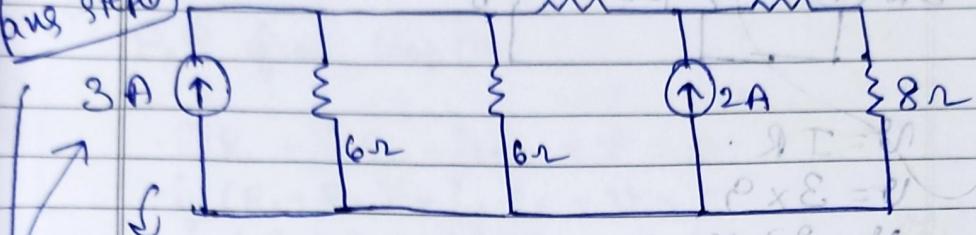
$$I = 3.33 \text{ A}$$

\because In series
Current same;

$$I_3 = 3.33 \text{ A}$$

Q) find I_8 .

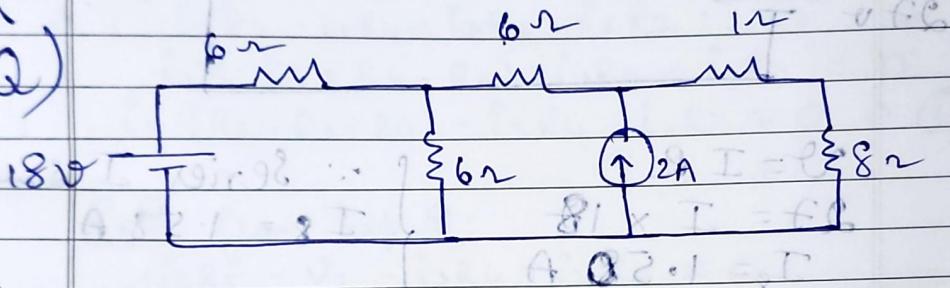
ans step(1)



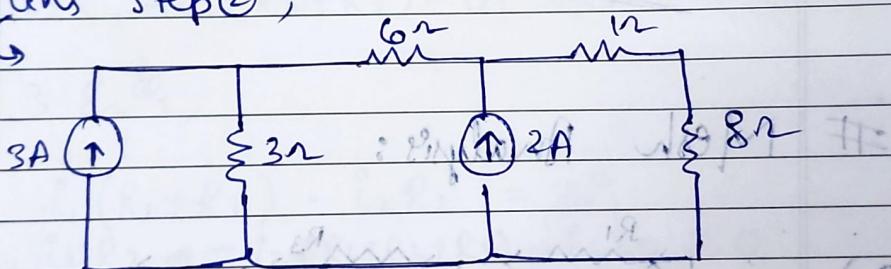
$$V = IR$$

$$V = 3 \times 6 \Rightarrow 18$$

Q)

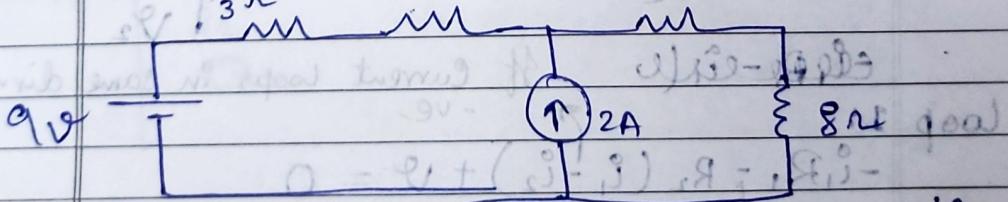


ans step(2)



$$V = IR$$

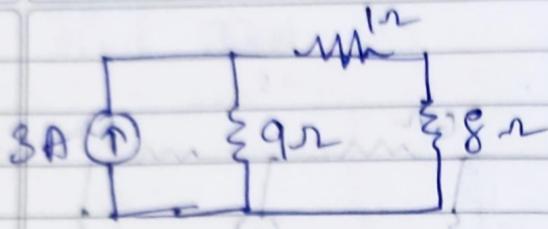
$$V = 3 \times 3 \Rightarrow 9A$$



$$V = IR$$

$$9 = I \times (6+3) \Rightarrow 1A$$

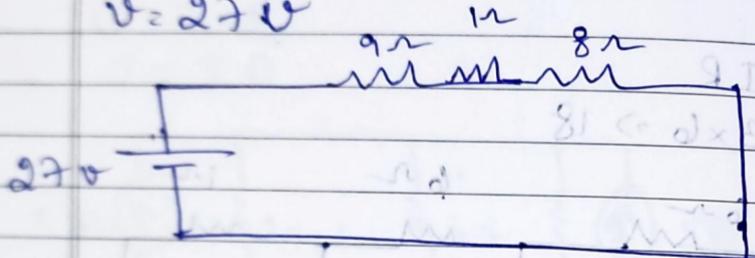
$$0 = I + 1A - 9 - (3-3) - 9 - 8 - 3 - 1A - 2A$$



$$V = IR$$

$$V = 3 \times 9$$

$$V = 27 \text{ V}$$



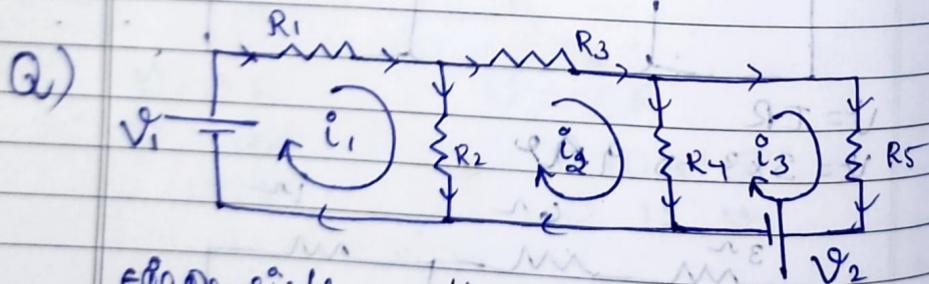
$$V = IR$$

$$27 = I \times 18$$

$$I_8 = 1.58 \text{ A}$$

\therefore Series I law
 $I_8 = 1.58 \text{ A}$

Mesh Analysis:



clockwise

Loop 1: If Current loops in same dirn -ve

$$-i_1 R_1 - R_2 (i_1 - i_2) + V = 0$$

Always -ve

Loop 2:

$$-i_2 R_3 - R_4 (i_2 - i_3) - R_2 (i_2 - i_1) = 0$$

loop 3;

$$-i_3 R_5 - V_2 - (i_3 - i_2) R_4 = 0$$

Eq④ from loop ①;

$$-i_1 R_1 - i_1 R_2 + i_2 R_2 + V = 0$$

$$-i_1 (R_1 + R_2) + i_2 R_2 + V = 0$$

$$i_1 (R_1 + R_2) - i_2 R_2 - V = 0 \Rightarrow ①$$

Eq⑤ from loop ②;

$$-i_2 R_3 - i_2 R_4 + i_3 R_4 - i_2 R_2 + i_1 R_2 = 0$$

$$i_2 (-R_3 - R_4 - R_2) + i_3 R_4 + i_1 R_2 = 0$$

$$i_2 (R_2 + R_3 + R_4) - i_3 R_4 - i_1 R_2 = 0 \Rightarrow ②$$

Eq⑥ from loop ③;

$$-i_3 R_5 - V_2 - i_3 R_4 + i_2 R_4 = 0$$

$$i_2 R_4 - i_3 (R_4 + R_5) - V_2 = 0 \Rightarrow ③$$

3 Eqs;

$$i_1 (R_1 + R_2) - i_2 R_2 = V_1$$

$$i_1 R_2 - i_2 (R_2 + R_3 + R_4) + i_3 R_4 = 0$$

$$i_2 R_4 - i_3 (R_4 + R_5) = V_2$$

$$\begin{bmatrix} i_1 (R_1 + R_2) & -R_2 & 0 \\ R_2 & -(R_2 + R_3 + R_4) & R_4 \\ 0 & R_4 & -(R_4 + R_5) \end{bmatrix}$$

$$\boxed{\begin{bmatrix} V_1 & -R_2 & 0 \\ 0 & -(R_2 + R_3 + R_4) & R_4 \\ V_2 & R_4 & -(R_4 + R_5) \end{bmatrix}}$$

in Δ_{i_1}

in Δ_{i_2}

in Δ_{i_3}

$\leftarrow \rightarrow$

$V_1, 0, V_2$

Now Gen Shortcut formula

$$\left[\begin{array}{ccc} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{array} \right] \left[\begin{array}{c} I_1 \\ I_2 \\ -I_3 \end{array} \right] = \left[\begin{array}{c} V_1 \\ V_2 \\ -V_3 \end{array} \right]$$

Main det. D (for short wif Sub. this in 1st col. for D_x, D_y, D_z)

Value of ~~the~~ unknown

(for short wif D)

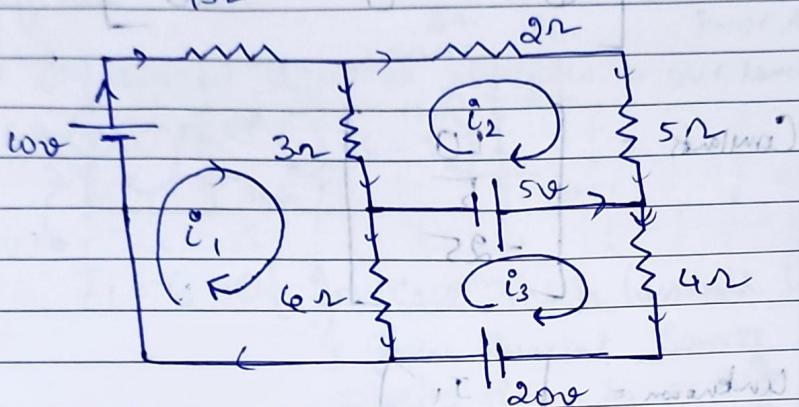
$$D_x = \underline{R_{11} + R_{21} + R_{31}} \quad D \rightarrow (\text{main det})$$

For sign of matrix elements see
 dirn. of loops. If dirn. of
 2 loops say 1 & 2 is same (clockwise)
 then R_{12} & R_{21} is +ve

If loop dirn. of 1 & 3rd loop is opp,
 then R_{13} & R_{31} is +ve

* Applicable only if direct matrix shortcut using this method

a) Find value of current through 5Ω resistor.



for Mesh ①;

$$10 - i_1(1) - (i_1 - i_2)3 - (i_1 - i_3)6 = 0$$

$$10 - i_1 - 3i_1 + 3i_2 - 6i_1 + 6i_3 = 0$$

$$10 - 10i_1 + 3i_2 + 6i_3 = 0$$

(10i₁ + 3i₂ + 6i₃) = 10

$$10i_1 - 3i_2 - 6i_3 = 10 \quad \text{---} ①$$

for Mesh 2;

$$-i_2(2) - i_2(5) - 5 - (i_2 - i_1)3 = 0$$

$$-2i_2 - 5i_2 - 5 - 3i_2 + 3i_1 = 0$$

$$-10i_2 - 5 + 3i_1 = 0 \quad \text{---} ②$$

$$3i_1 - 10i_2 = 5$$

for Mesh ③

$$5 - i_3(4) + 20 - (i_3 - i_1)6 = 0$$

$$5 - 4i_3 + 20 - 6i_3 + 6i_1 = 0$$

$$25 - 10i_3 + 6i_1 = 0$$

$$6i_1 - 10i_3 = -25$$

If loops in same dirn then
give -ve sign.

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$$Q = \begin{bmatrix} 10 & -3 & -6 \\ 3 & -10 & 0 \\ 6 & 0 & -10 \end{bmatrix}$$

If you take (-) common from both rows

It becomes +ve if whatever is inside becomes of next

Constants = $\begin{bmatrix} 10 \\ 5 \\ -25 \end{bmatrix}$ ∵ easy to find

Unknown = $\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}$ (i) Jolt ref

$$0 = \delta(i-i) - \delta(i-i) - (i)i = 001$$

$$I_1 \Rightarrow \begin{bmatrix} 10 & -3 & -6 \\ 5 & -10 & 0 \\ -25 & 0 & -10 \end{bmatrix} = 001$$

$$\begin{bmatrix} 10 \\ 5 \\ -25 \end{bmatrix} \cdot \text{Mem ref}$$

$$0 = \delta(i-i) - \delta(i-i) - (i)i =$$

$$11 \quad \text{find } I_2 \text{ & } I_3$$

Current in 5Ω resistor = I_2

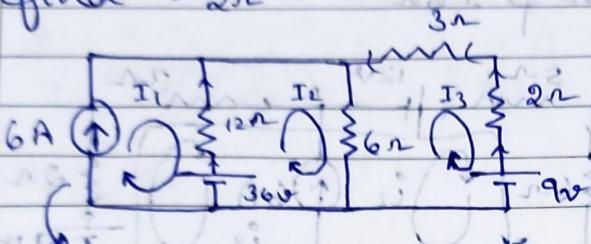
$$0 = \delta(i-i) - \delta(i-i) - 2$$

$$0 = \delta(i-i) - \delta(i-i) - 2$$

$$0 = \delta(i-i) - \delta(i-i) - 2$$

2) Mesh Analysis with Current Source

find I_{2r} .



$I_1 = 6 \Rightarrow$ In case mesh (assumed loop) dirn & given current source dirn is opposite then $I_1 = -6$

~~Mesh 1:~~

$$-(i_2 - i_1)12 - (i_2 - i_3)6 + 36 = 0$$

$$\Rightarrow -12i_1 + 18i_2 - 6i_3 = 36 \quad \text{Eq 1}$$

$$\Rightarrow 2i_1 - 3i_2 + i_3 = -6 \quad \text{Eq 2}$$

Given $i_1 = 6$

$$\Rightarrow 3i_2 - i_3 = 6 + 12$$

$$\Rightarrow 3i_2 - i_3 = 18 \quad \text{Eq 3} \quad \text{Eq 1}$$

$$\Rightarrow 3i_2 - 18 = i_3$$

~~Mesh 3:~~ $i_3(2) + i_3(3) + (i_3 - i_2)6 + 9 = 0$

~~$$2i_3 + 3i_3 - 6i_3 + 6i_2 + 9 = 0$$~~

~~$$6i_2 + i_3 = -9$$~~

$$6i_2 - 11i_3 = 9 \quad \text{Eq 2}$$

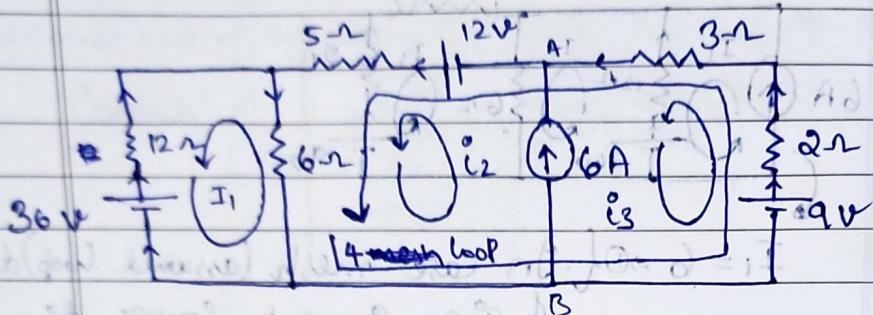
Solve Both Eq for get the Req ans

~~group ③: unknowns p1, p2, p3 are not in same circuit~~

~~so we can't solve for them~~

3) Super Mesh Analysis:

Find I_{5n} & I_{6n}



For mesh ①;

$$+i_1(12) - (i_1 - i_2)6 + 36 = 0$$

$$12i_1 - 6i_1 + 6i_2 + 36 = 0 \quad (1)$$

$$6i_1 + 6i_2 + 36 = 0 \quad (2)$$

$$i_1 + i_2 + 6 = 0 \quad (3)$$

\Rightarrow Mesh 2 & 3 will form a supermesh as it shares a common current source

Writing Eq@ for Supermesh:

$$+i_2 - i_3 = 6$$

$$+i_2 - i_3 = 6 \quad (4)$$

* If i_3 is in dirn of current source
 take those i_3 's as +ve & the ones in opp. dirn. of current source they are -ve

After writing Supermesh Eq@ ignore the complete problem making current source wire AB in this case & take a single loop that covers both mesh 2 & 3. (Single loop is loop 4 this case)

write current corresponding to that loop

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$$+9 - 2i_3 - 3i_3 + 12 - 5i_2 - 6i_2 + 6i_1 = 0$$

$$9 - 2i_3 - 3i_3 + 12 - 5i_2 - 6i_2 + 6i_1 = 0$$

$$21 - 5i_3 - 11i_2 + 6i_1 = 0$$

$$6i_1 - 11i_2 - 5i_3 + 21 = 0.$$

3 Eqs;

$$6i_1 + 6i_2 + ?$$

$$i_1 + i_2 + 0i_3 = 6$$

$$0i_1 + i_2 + 0i_3 = + (6 - 3) = 301 - 001$$

$$6i_1 - 11i_2 - 5i_3 = + 21, i_01 = , i_01 - 001$$

$$\text{In } \text{ find } i_1, i_2, i_3 - i_01 - i_{11}$$

$$I_{52} = i_2$$

in deg M ref

$$I_{62} = |i_2 - i_1|$$

Modulus. (1) w/ (2)

$$001 = 2i_00 - 01 - i_{11}$$

$$011 = 2i_00 - i_{11}$$

}

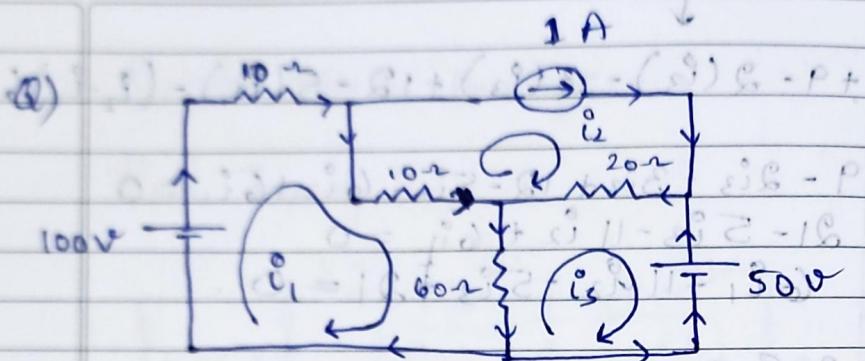
(3) loop

loop 02

$$0 = (001)(i_2 - i_1) - 02(i_3 - i_1) - 02 -$$

$$0 = i_00 + i_00 - i_00 + i_00 - 02 -$$

$$0 = i_00 + i_00 + i_00 - 02 -$$



find $i_{60\Omega}$

In Mesh ①;

$$100 - 10i_1 - (i_1 - i_2)10 - (i_1 - i_3)60 = 0$$

$$100 - 10i_1 - 10i_2 + 10i_2 - i_1 + 60i_3 = 0$$

$$-11i_1 + 100 + 10i_2 + 60i_3 = 0$$

$$11i_1 - 10i_2 - 60i_3 = 100 \quad \Rightarrow \textcircled{1} \quad \text{P.M}$$

In Mesh 2;

$$i_2 = 1A \Rightarrow \textcircled{2}$$

② in ①); when

$$11i_1 - 10 - 60i_3 = 100$$

$$11i_1 - 60i_3 = 110 \quad \Rightarrow \textcircled{2}$$

Mesh ③;

~~$-50 - 60i_3$~~

$$-50 - (i_3 - i_1)60 - (i_3 - i_2)20 = 0$$

$$-50 - 60i_3 + 60i_1 - 20i_3 + 20i_2 = 0$$

$$-50 - 80i_3 + 60i_1 + 20i_2 = 0$$

$$\therefore \dot{e}_2 = 1$$

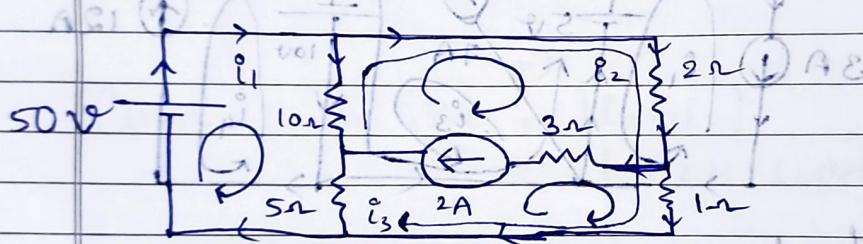
$$60\dot{i}_1 - 80\dot{i}_3 + 20 - 50 = 0 \quad (1) \quad \dot{e}_1 - \dot{e}_2$$

$$60\dot{i}_1 - 80\dot{i}_3 = 30 \quad (2)$$

from (1) & (2)

find \dot{i}_1 & \dot{i}_3 then subtract both
to get $\dot{i}_{60\Omega}$

* Supermesh with Current of resistor



Find $i_{2\Omega}$:

Mesh (1):

$$50 - (i_1 - i_2)10 - (i_1 - i_3)5 = 0$$

$$50 - 10i_1 + 10i_2 - 5i_1 + 5i_3 = 0 \quad (1)$$

$$50 - 15i_1 + 10i_2 + 5i_3 = 0$$

$$10 - 3i_1 + 2i_2 + i_3 = 0$$

$$3i_1 - 2i_2 - i_3 = 10 \quad (1) \quad \text{Eqn 1} \rightarrow (1)$$

Mesh (2):

Supermesh Eq (1); $0i_1 + i_2 - i_3 = 2 \quad (2) \rightarrow (2)$

Mesh (2 & 3):

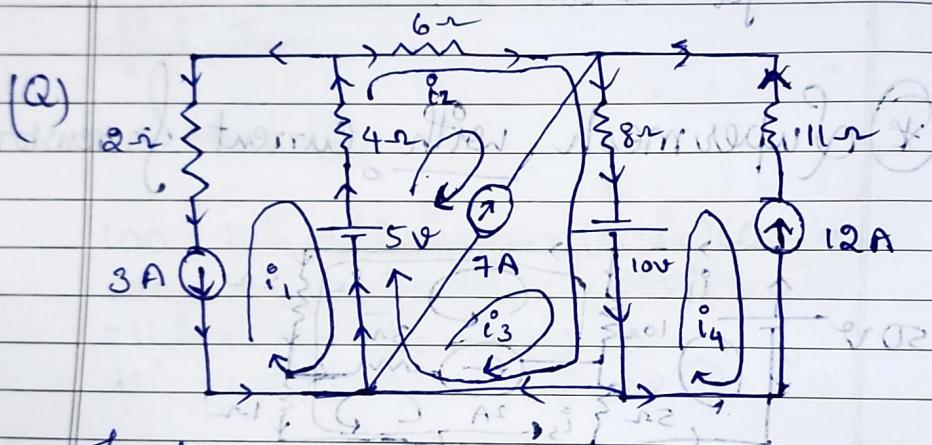
$$-i_2 2 - i_3 (1) - (i_3 - i_1)5 - (i_2 - i_1)10 = 0$$

$$-5i_1 + 4i_2 + 2i_3 = 0$$

$$5i_1 - 4i_2 - 2i_3 = 0 \quad 0.5 + 908 = 909$$

from ①, ②, ③ get i_1, i_2, i_3

To get I_{5r} ; $|I_3 - I_1|$



Find I_{8r}

In Mesh ①;

$$0 = 2(i_1 - i_2) - 6i_1(i_3 - i_1) - 0.2 \\ i_1 = 0 - 3A + (-) \text{ since current direction opp to loop direction} \\ 0 = 2i_1 + i_2 + i_3 - 0.2$$

$$i_4 = -12A \quad (i_2 = 4i_1 - 3i_3 - 0.2)$$

Supernode Eq ④;

$$i_3 - i_2 = 7 \Rightarrow i_2 - i_3 = -7$$

Big Mesh;

$$-i_2 6 - (i_3 - i_4) 8 + 10 + 5 - (i_2 - i_1) 4 = 0 \\ -6i_2 - 8i_3 + 8i_4 + 10 + 5 - 4i_2 + 4i_1 = 0 \\ 4i_1 - 10i_2 - 8i_3 + 8i_4 + 15 = 0$$

Chapter 11: [Redacted]

$$\therefore i_1 = -3$$

$$i_4 = -12 \quad \text{at node 4 and current left}$$

$$-12 - 10i_2 - 8i_3 - 9.6 + 15 = 0$$

$$10i_2 + 8i_3 = -10.6 - 9.3$$

$$i_2 = -8.27$$

$$i_3 = -10.27$$

~~Current via $\frac{8V}{R} = |i_2 - i_3|$~~

\Rightarrow

~~Current via $\frac{8V}{R} = |i_4 - i_3|$~~

$$= |-1.27 - (-12)|$$

$$= 10.73 \text{ A}$$

$$0 = 8V - AV + 10.73A - AV$$

$$0 = 8V - AV + AV + 10.73A - AV$$

prented 2A
 $(-AV) = -AV$

$$0.8 = 8V - AV$$

$$(DC) 21 - 8V - AV$$

$$0 = ST - ST + ST$$

$$0 = 0.8V + 0.8V + AV - AV$$

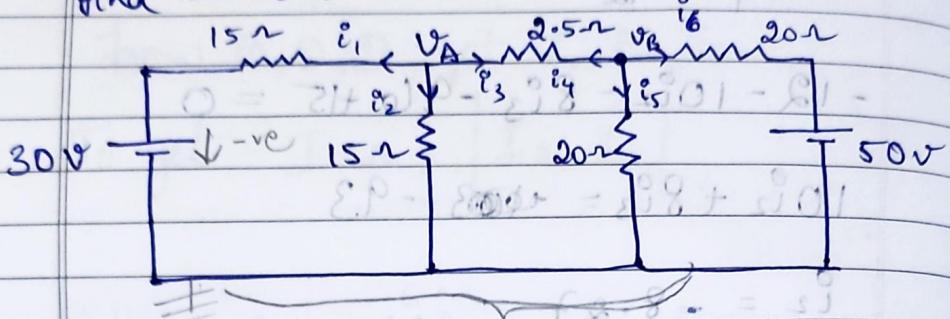
$$0.8V + 0.8V = AV$$

$$1.6V = AV$$

$$AV = 1.6V$$

Nodal Analysis

to find current b/w V_A & V_B



① No component here

Assume Ground

② Throw out current from all nodes

③ Use below formulae

Node V_A : $\frac{V_A - 30}{15} + \frac{V_A - 0}{15} + \frac{V_A - V_B}{2.5} = 0$

$$I_1 + I_2 + I_3 = 0$$

$$\frac{V_A - 30}{15} + \frac{V_A - 0}{15} + \frac{V_A - V_B}{2.5} = 0$$

-ve 30,

As battery

$\rightarrow -$ (KVL)

$$\frac{V_A - 30 + V_A + 6V_A - 6V_B}{15} = 0$$

$$8V_A - 6V_B = 30$$

$$4V_A - 3V_B = 15 \Rightarrow ①$$

Node V_B :

-ve as ...

$$I_4 + I_5 + I_6 = 0$$

$$\frac{V_B - V_A}{2.5} + \frac{V_B - 0}{20} + \frac{V_B - 50}{20} = 0$$

Solve 2 above eqns;

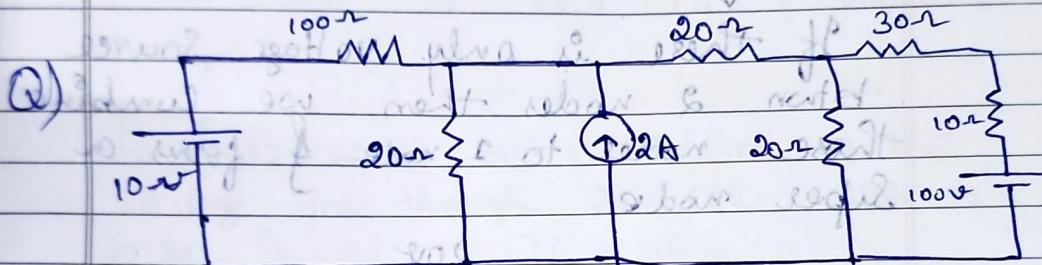
$$V_A = 18.75$$

$$V_B = 20$$

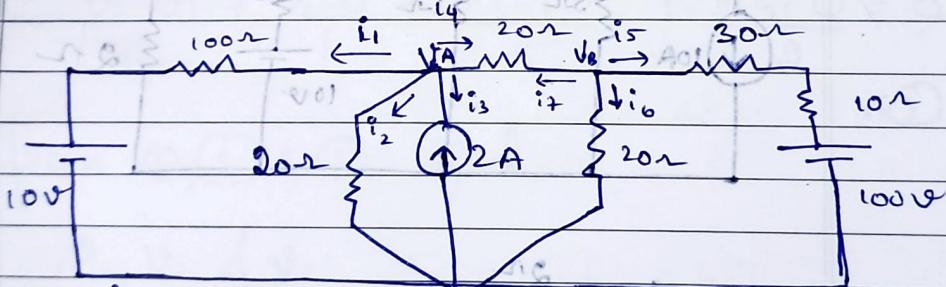
Current b/w V_A & $V_B = I_3$

$$\frac{V_A - V_B}{2.5} \approx -0.5A$$

* Nodal Analysis with Current Source.



first join all the null / zero potential wires



(a) $V_A \Rightarrow i_1 + i_2 + i_3 + i_4 = 0$

$$\frac{V_A - 10}{100} + \frac{V_A - 0}{20} - 2 + \frac{V_A - V_B}{20} = 0 \rightarrow (1)$$

{-ve : i_3 dirn & source current dirn is opposite, if same dirn then its +ve}

(b) $V_B \Rightarrow i_5 + i_6 + i_7 = 0$

$$\frac{V_B - 100}{30+10} + \frac{V_B - 0}{20} + \frac{V_B - V_A}{20} = 0 \rightarrow (2)$$

R_{net}

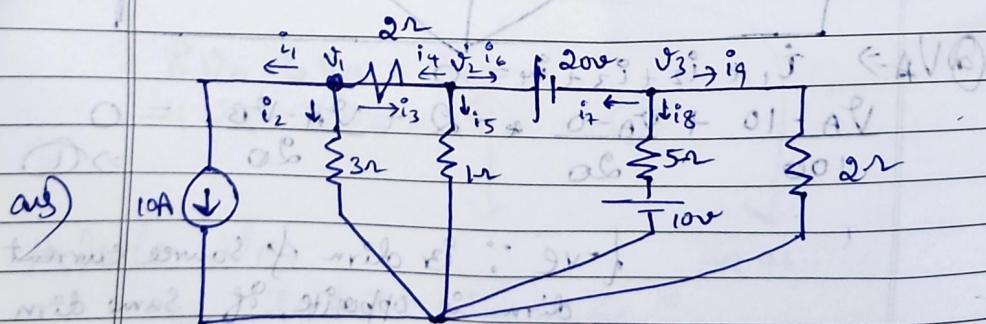
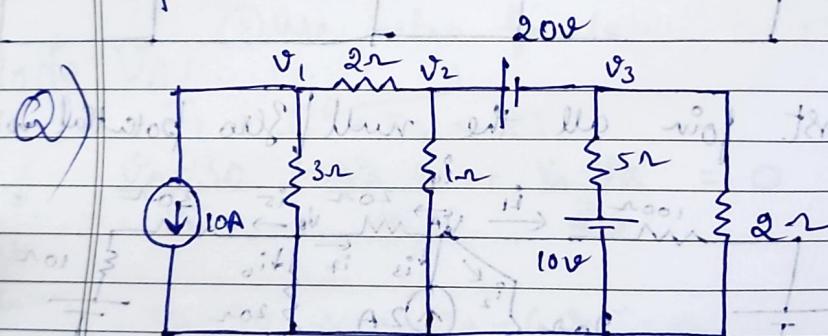
Solve ① & ② to get;

$$V_A = -10 \text{ V}$$

$$\underline{\underline{V_B = 16 \text{ V}}}$$

Super Node Analysis

If there is only voltage source between 2 nodes then we combine those nodes to 1 node & forms a Super node



$$\textcircled{2} \quad V_1 \Rightarrow i_1 + i_2 + i_3 = 0$$

$$\textcircled{2} \quad + 10 \text{ A} + \frac{v_1 - v_2}{3} + \frac{v_1 - v_2}{2} = 0 \quad \textcircled{1}$$

↑ top i, dirn & source dirn same

Now, V_2 & V_3 has voltage source
 So, this has to be made into Super node
 Supernode Σ^{\oplus} & then ignore that volt
 source

$$+V_2 - V_3 = 20 \Rightarrow ②$$

↓ volt. value

↓ -ve terminal points @ V_3

∴ +ve terminal of 20v cell points @ V_2

Now ignore the 20v cell & use nodal analysis.

i_6 & i_7 won't be considered as that voltage goes through 20v cell which is to be ignored.

$$\text{So, } i_4 + i_5 + i_8 + i_9 = 0$$

$$\frac{V_2 - V_1}{2} + \frac{V_2 - 0}{1} + \frac{V_3 - 10}{5} + \frac{V_3 - 0}{2} = 0 \Rightarrow ③$$

from ①, ② & ③ find

$$V_1, V_2 \text{ & } V_3$$

$$V_1 = 2V, V_2 = 8V, V_3 = 10V$$

→ V_1 short w.r.t V_2 & V_3

∴ ref @ V_3 voltage source

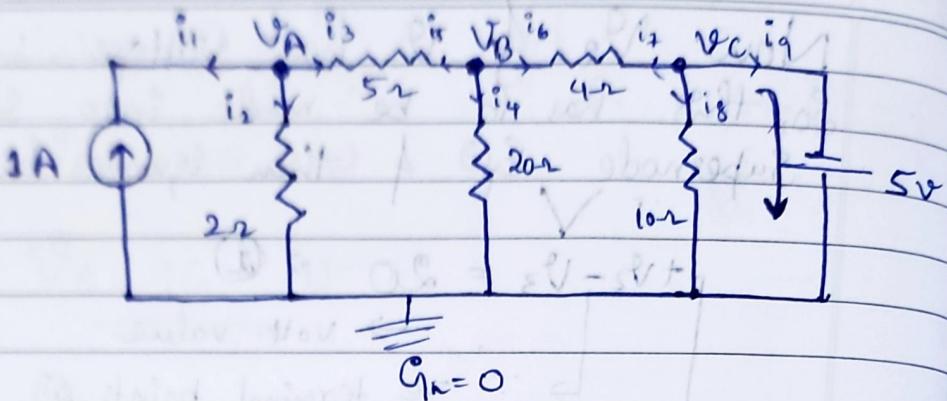
$$2V - 10V = -8V \quad 0 = 2 + 8V$$

(neglect 20v)

* here voltage source directly connected to node

PAGE NO.:
DATE:

(Q)



In V_A :

$$i_1 + i_2 + i_3 = 0$$

$$-1 + \frac{V_A}{2} + \frac{V_A - V_B}{5} = 0$$

$$2V_A - 2V_B = 10 \quad \text{--- (1)}$$

In V_B :

$$i_5 + i_4 + i_6 = 0$$

$$\frac{V_B - V_A}{5} + \frac{V_B}{20} + \frac{V_B - V_C}{4} = 0$$

$$-4V_A + 10V_B - 5V_C = 0 \quad \text{--- (2)}$$

$$4V_A - 10V_B + 5V_C = 0 \quad \text{--- (3)}$$

* Now in node V_C .

node directly connected to current source

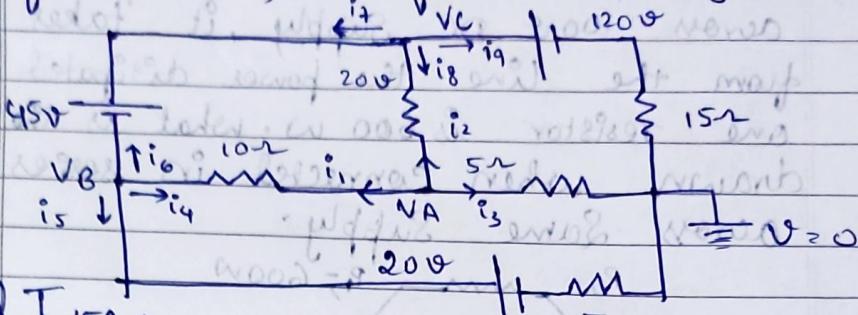
write voltage $\text{Eq } (1)$ for V_C .

$$V_C + 5 = 0 \quad (\text{+ve } 5, \text{ as } i_9 \text{ flows from } +ve \text{ end of battery})$$

$$\Rightarrow V_C = -5 \quad \text{--- (4)}$$

from ①, ② & ③ find V_A , V_B & V_C

Q)



find $I_{15\Omega}$.

$$i_1 + i_2 + i_3 = 0$$

$$\frac{V_A - V_B}{10} + \frac{V_A - V_C}{20} + \frac{V_A}{5} = 0$$

$$7V_A - 2V_B - V_C = 0 \quad \text{--- (1)}$$

\therefore There is a voltage source b/w 2 nodes it's a super node.
(here 45V is b/w V_C & V_B)

\Rightarrow write Supernode Eqn :

$$V_C - V_B = 45 \quad (\because +ve \text{ side of cell} \rightarrow V_C) \\ \Rightarrow V_C - V_B = 45 \quad (-ve \text{ side} \rightarrow V_B)$$

i_6 if it won't be considered, that current passes through 45V cell (to be ignored)

$$i_4 + i_5 + i_8 + i_9 = 0$$

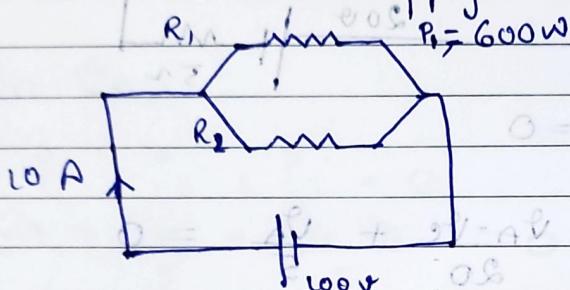
$$\frac{V_B - V_A}{10} + \frac{V_B - 20}{5} + \frac{V_C - V_A}{20} + \frac{V_C - 120}{15} = 0$$

$$9V_A - 18V_B - 7V_C = -720$$

use calc to find V_A , V_B & V_C \Rightarrow ③

$$I_{15\Omega} = I_9 = \frac{V_C - 120}{15} = -3.54 \text{ A}$$

- (Q) 2 resistors are connected in parallel across 100V DC supply. It takes 10A from the line. The power dissipated in one resistor is 600W. What is the current drawn when connected in series across same supply.



$$P_1 = \frac{V^2}{R} \Rightarrow \frac{100 \times 100}{600} = 16.66 \Omega$$

$$P_1 = \frac{V^2}{R} \Rightarrow 16.66 \Omega$$

$$R = \frac{V^2}{P} = \frac{100^2}{600} = 16.66 \Omega$$

$$V = IR_{\text{net}}$$

$$100 = 10 \times \left(\frac{16.66 \times R}{16.66 + R} \right) = 25.02$$

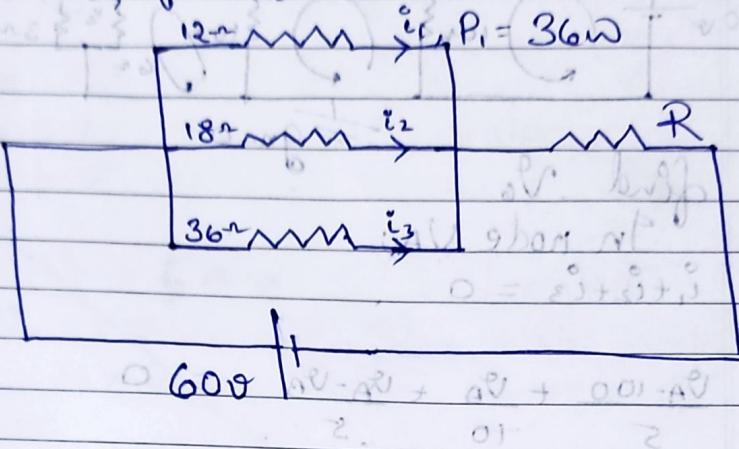
$$R_2 = 25.01 \Omega$$

$$R_{\text{series}} = 41.66 \Omega$$

$$I_{\text{series}} = \frac{V}{R_{\text{series}}} = \frac{100}{41.66} = 2.401$$

$$R_{\text{series}} = 41.66 \Omega$$

Q) Find R , if $P_{12} = 36\text{W}$



$$D = \Delta V C - \Delta V C + \Delta V + 0.08 - 0.08$$

$$\text{Or } 0.08 = \Delta V C - \Delta V Z - \Delta V$$

$$P = I^2 R$$

$$P = \frac{V^2}{R}$$

$$36 = I_1^2 \times 12$$

Volt across first box
show that

$$3 = I_1^2$$

$$36 = V^2 / 12$$

$$I_1 = \sqrt{3} = 1.7\text{A}$$

$$\Rightarrow V = 12\sqrt{3}\text{V}$$

$$R_P = \left(\frac{1}{12} + \frac{1}{18} + \frac{1}{36} \right)^{-1} = 8.06\text{ }\Omega$$

$$V = I_2 \times R_3$$

$$12\sqrt{3} = I_2 \times 18$$

$$I_2 = 1.015\text{A}$$

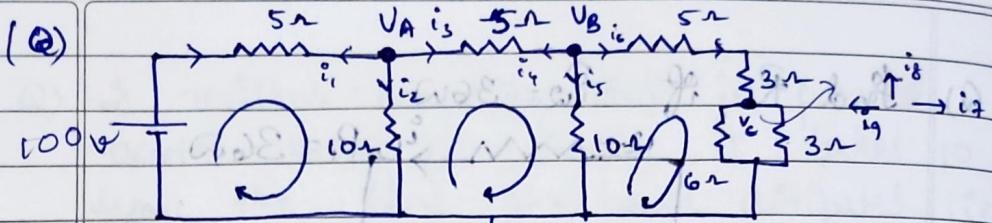
$$V = I_3 \times R_2$$

$$I_3 = \frac{12\sqrt{3}}{36} = 0.57\text{A}$$

$$V = IR_{\text{net}}$$

$$\Rightarrow 60 = (1.7 + 1.015 + 0.57)(6 + R)$$

$$\Rightarrow R = 11.54\text{ }\Omega$$



find V_B

In node V_A :

$$i_1 + i_2 + i_3 = 0$$

$$\frac{V_A - 100}{5} + \frac{V_A}{10} + \frac{V_A - V_B}{5} = 0$$

$$2V_A - 200 + V_A + 2V_A - 2V_B = 0 \\ \Rightarrow 5V_A - 2V_B = 200 \quad \rightarrow \textcircled{1}$$

In node V_B :

$$i_4 + i_5 + i_6 = 0$$

$$\frac{V_B - V_A}{5} + \frac{V_B}{10} + \frac{V_B}{5+3+2} = 0$$

$$2V_B - 2V_A + V_B + V_B = 0$$

$$4V_B - 2V_A = 0$$

$$2V_B = V_A \quad \rightarrow \textcircled{2}$$

In node V_C

$$i_7 + i_8 + i_9 = 0$$

$$\frac{V_C}{3} + \frac{V_C - V_B}{8} + \frac{V_C}{6} = 0$$

$$8V_C + 3V_C - 3V_B + 4V_C = 0$$

$$15V_C - 3V_B = 0$$

$$5V_C = V_B \Rightarrow ③$$

$$V_A = 50 \text{ V}$$

$$V_B = 25 \text{ V}$$

$$V_C = 5 \text{ V}$$

$$\therefore V_C = 5 \text{ V} \quad \because \text{In parallel}$$

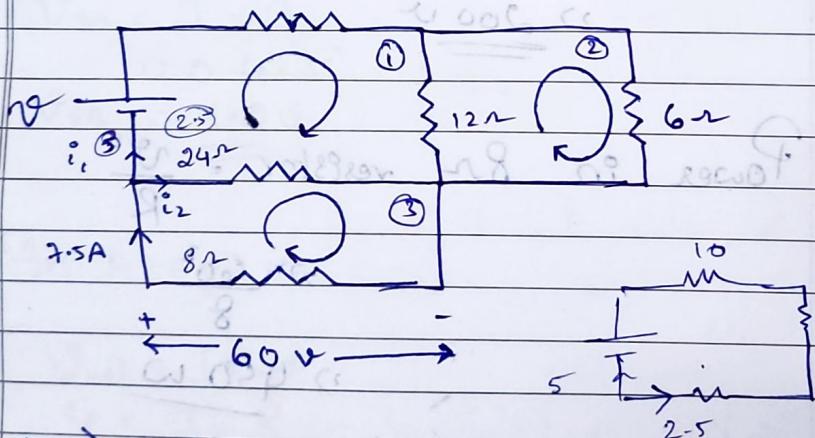
$$V_6 = 5 \text{ V}$$

$$V_6 = I_6 \times R$$

$$5 =$$

$$V_{62} = V_C = 5 \text{ V}$$

Q) find voltage source value & power in 8Ω resistor



In mesh 3,

$$V = 60 \text{ V}$$

$$R = 8 \Omega$$

$$I = \frac{V}{R} = \frac{60}{8} = 7.5 \text{ A}$$

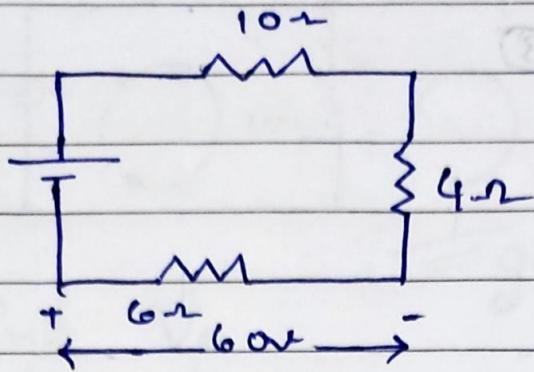
$$20 \rightarrow R$$

$$I = 2.5$$

$$V = 150$$

$$\frac{1}{R_p} = \frac{1}{24} + \frac{1}{8} \Rightarrow \underline{\underline{6 = R_p}}$$

$$\text{why } R_p = 4 \Omega$$



$$V = IR \text{ and } \therefore I = \frac{V}{R}$$

$$60 = I \times 6$$

$$\underline{I = 10 \text{ A}}$$

\therefore Series ckt $I_{\text{ckt}} = 10 \text{ A}$

$$V_{\text{net}} = I_{\text{ckt}} \times R_{\text{net}}$$

$$\Rightarrow 10 \times (10 + 4 + 6)$$

$$\Rightarrow 10 \times (20)$$

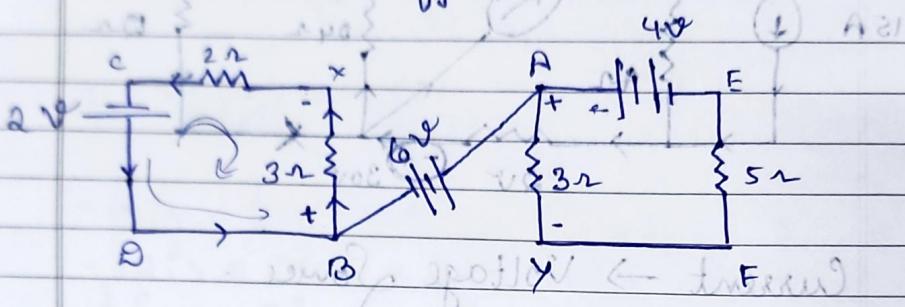
$$\Rightarrow \underline{\underline{200 \text{ V}}}$$

$$\text{Power in } 8 \Omega \text{ resistor} = \frac{V^2}{R}$$

$$\Rightarrow \frac{60^2}{8}$$

$$\Rightarrow \underline{\underline{450 \text{ W}}}$$

Q) find the potential diff b/w x & y
in the below fig.



$$V_{xy} = V_{xB} + V_{BA} + V_{AY}$$

In $C \times B \times C$

$$V_{net} = IR_{net}$$

$$2 - I \times 5$$

$$I = 0.4 A$$

$$V_{3\Omega} = I \times 3$$

$$\Rightarrow 0.4 \times 3$$

$$V_{xB} \Rightarrow 1.2 V$$

In $A E F Y A$;

$$V_{net} = IR_{net}$$

$$4 = I \times 8$$

$$I = 0.5 A$$

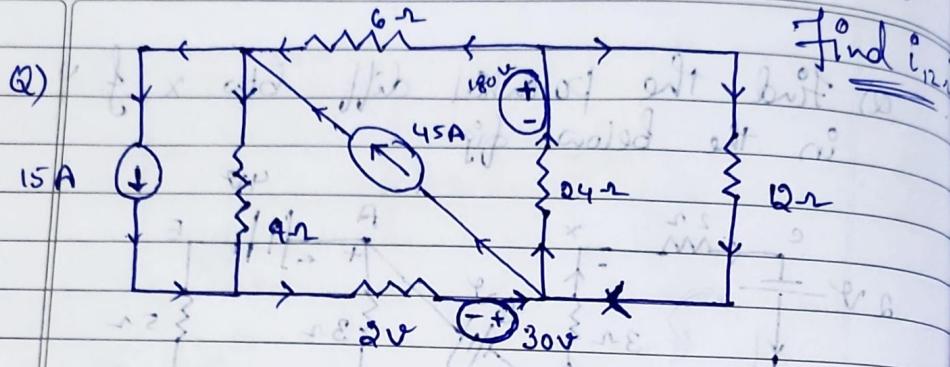
$$V_{3\Omega} = I \times 3$$

$$\Rightarrow 0.5 \times 3$$

$$V_{AY} \Rightarrow 1.5 A V$$

$$\therefore V_{xy} = 1.2 + 6 - 1.5$$

$$\Rightarrow 5.7 V$$

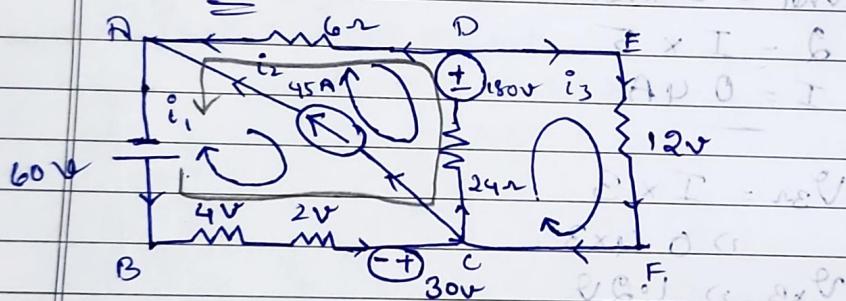


Current \rightarrow Voltage Source.

$$V = IR$$

$$\Rightarrow 15 \times 4$$

$$\therefore 60V$$



For mesh ABCDA.

$$4/60^{\circ}$$

Super mesh Eq ①

$$i_2 - i_1 = 45$$

Eq ①

In Mesh ABCDA;

$$-6i_1 + 30 - 24(i_2 - i_3) + 180 - 6i_2 = 0$$

$$-6i_1 + 30 + 24i_3 - 24i_2 + 180 - 6i_2 = 0$$

$$-i_1 + 5 + 8i_3 - i_2 = 0$$

$$-i_1 + 5 + 4i_3 - 4i_2 + 30 + i_2 = 0$$

$$i_1 + 5i_2 - 4i_3 = 35 \quad \Rightarrow \textcircled{2}$$

In mesh DEFCD;

$$-12i_3 - 24(i_3 - i_2) + 180 = 0$$

$$-12i_3 - 24i_3 + 24i_2 + 180 = 0$$

$$-i_3 - 2i_3 + 2i_2 + 15 = 0$$

$$2i_2 + 3i_3$$

$$2i_2 - 3i_3 + 15 = 0 \quad \Rightarrow \textcircled{3}$$

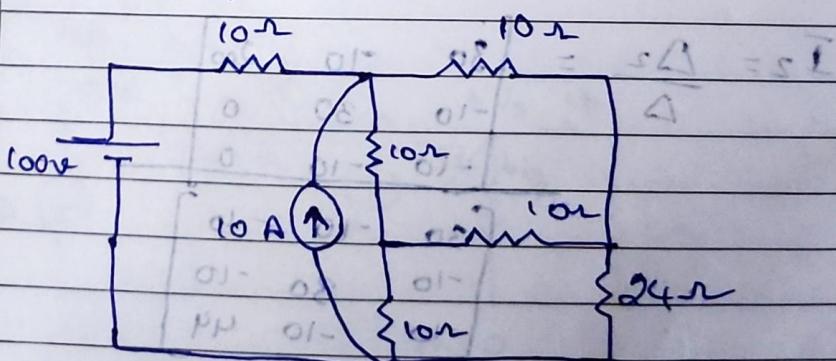
$$i_1 = -15$$

$$i_2 = 30$$

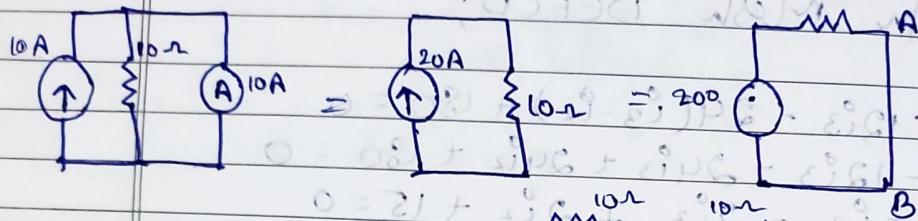
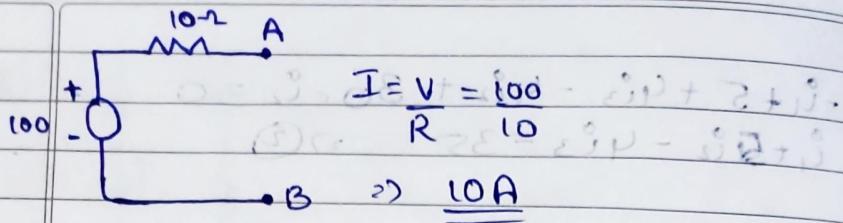
$$i_3 = 25$$

$$i_{12} = i_3 = 25 \text{ A}$$

③ Use Mesh Current Analysis to find I_{24n} .

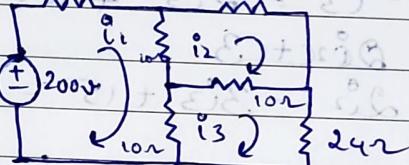


$$I = \frac{V}{R} = \frac{100}{10} = 10 \text{ A}$$



$$V = IR$$

$$\begin{aligned} & \Rightarrow 30 \times 10 \\ & \Rightarrow 300 \text{ V} \end{aligned}$$



$$\left[\begin{array}{ccc} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{array} \right] \left[\begin{array}{c} I_1 \\ I_2 \\ I_3 \end{array} \right] = \left[\begin{array}{c} V_1 \\ V_2 \\ V_3 \end{array} \right]$$

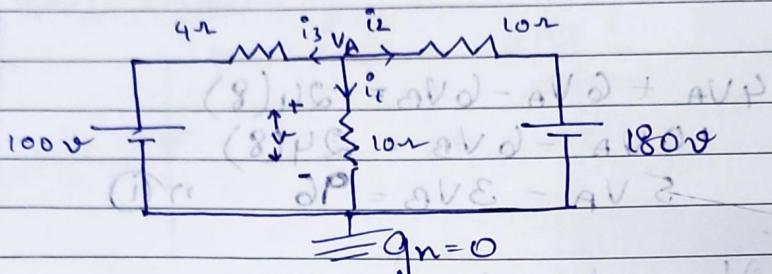
$$\left[\begin{array}{ccc} 30 & -10 & -10 \\ -10 & 30 & -10 \\ -10 & -10 & 44 \end{array} \right] \left[\begin{array}{c} I_1 \\ I_2 \\ I_3 \end{array} \right] = \left[\begin{array}{c} 200 \\ 0 \\ 0 \end{array} \right]$$

$$I_2 = \frac{\Delta_2}{\Delta} = \frac{\begin{vmatrix} 30 & -10 & 200 \\ -10 & 30 & 0 \\ -10 & -10 & 0 \end{vmatrix}}{\begin{vmatrix} 30 & -10 & -10 \\ -10 & 30 & -10 \\ -10 & -10 & 44 \end{vmatrix}}$$

$$= 2.94 \text{ A}$$

$$\underline{\underline{A}} = \underline{\underline{V}} + \underline{\underline{I}}$$

Q) Find the voltage V_A shown in the figure.



$$V_A = 0$$

At node V_A ; $0 = i_1 + i_2 + i_3 + i_4$

$$i_1 + i_2 + i_3 = 0 \quad 10V + (5) + 10V - 180$$

$$\frac{V_A - 100}{4} + \frac{V_A}{10} + \frac{V_A - 180}{10} = 0$$

$$10V_A - 1000 + 4V_A + 4V_A - 1720 = 0$$

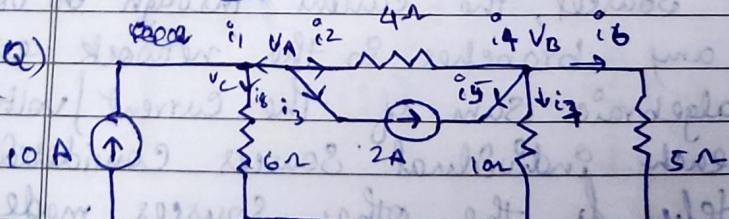
$$18V_A - 1720 = 0$$

$$V_A = 95.5 \text{ V}$$

$$V_A = 95.5 - 0$$

$$\therefore \underline{\underline{95.5 \text{ V}}}$$

(Q)



In node V_A :

$$i_1 + i_2 + i_3 = 0$$

$$-10 + \frac{V_A - 0}{6} + 2 + \frac{V_A - 4V_B}{4} = 0$$

$$\frac{V_A}{6} + \frac{V_A - V_B}{4} = 8$$

$$4V_A + 6V_A - 6V_B = 24(8)$$

$$10V_A - 6V_B = 24(8)$$

$$5V_A - 3V_B = 96 \quad \text{Eqn ①}$$

At node V_B :

$$i_4 + i_5 + i_6 + i_7 = 0$$

$$\frac{V_B - V_A}{2} + (-2) + \frac{V_B}{10} + \frac{V_B - V_B}{5} = 0$$

$$5V_B - 5V_A + V_B + 2V_B = 20$$

$$8V_B - 5V_A = 20 \Rightarrow \text{Eqn ②}$$

$$V_A = 33.12V$$

$$V_B = 23.2V$$

* No. of Sources (volt/current)

+ 1 steps used in solving problem

* Every step should have 1 source

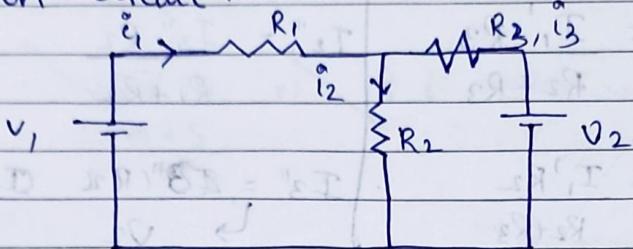
* Volt \rightarrow Short ckt.

③ Superposition Theorem Current \rightarrow Open

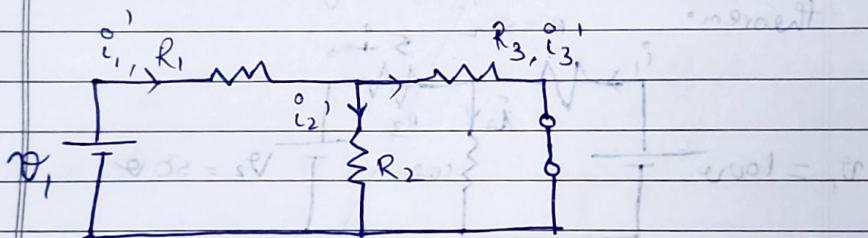
In a linear bilateral network containing several sources, the current through or voltage across any branch in the network equals the algebraic sum of the current/voltage of each individual source considered separately from the other sources made inoperative, i.e. replaced by resistance equal to their internal resistance. If the internal resistances of the sources are not known then voltage source should be replaced.

by short circuit of current source by open circuit.

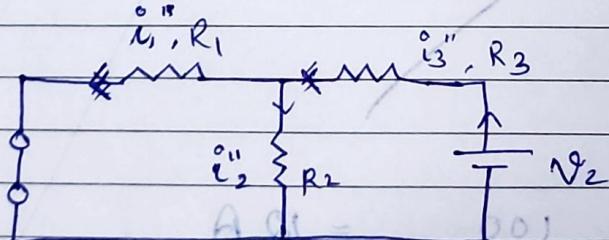
Eg;



Step 1; V_1 is considered, V_2 is replaced by short circuit.



Step 2; V_2 is considered, V_1 is replaced by short circuit.



Step 3;

$$I_1 = I_1' - I_1''$$

$$I_2 = I_2' + I_2''$$

$$I_3 = I_3' - I_3''$$

↳ Sign seeing dirn of I_3' & I_3''
in fig 1 & fig 2; & b dir opp. to

$$I_1' = \frac{V_1}{R_1 + (R_2 \parallel R_3)}$$

$$I_2' = \frac{I_1' R_3}{R_2 + R_3}$$

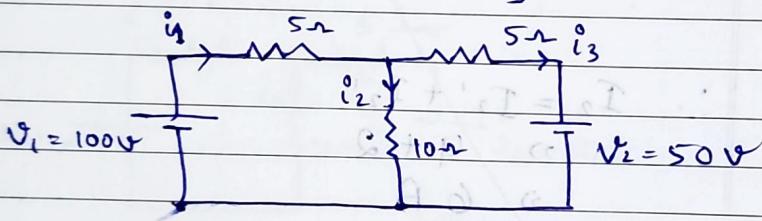
$$I_3' = \frac{I_1' R_2}{R_2 + R_3}$$

$$I_3'' = \frac{V_2}{R_3 + (R_1 \parallel R_2)}$$

$$I_2'' = \frac{I_3'' R_2}{R_1 + R_2}$$

$$I_3'' = \frac{I_3'' R_2}{R_1 + R_2}$$

Compute the current in 10Ω resistor as shown in fig using Superposition theorem.



$$i_1' = \frac{100}{5 + \left(\frac{1}{10} + \frac{1}{5}\right)^{-1}}$$

$$= \underline{\underline{12 \text{ A}}}$$

$$i_2' = \frac{12 \times 5}{10 + 5}$$

$$\Rightarrow \underline{\underline{\frac{60}{15}}}$$

$$\Rightarrow \underline{\underline{4 \text{ A}}}$$

$$I_3'' = \frac{50}{5 + \left(\frac{1}{5} + \frac{1}{10} \right)^{-1}}$$

$$\Rightarrow \underline{6A}$$

$$I_2'' = \frac{6 \times 10}{5 + 10}$$

$$\Rightarrow \underline{\frac{60}{15}}$$

$$\Rightarrow \underline{4A}$$

$$I_2 = I_2' + I_2''$$

$$\Rightarrow \underline{4+4}$$

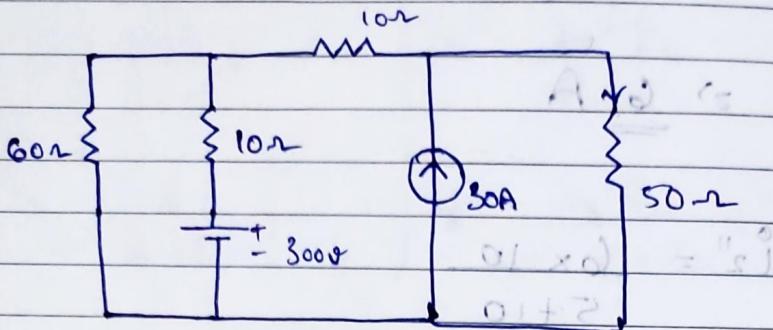
$$\Rightarrow \underline{8A}$$

$$A \text{ Z.F.}, \text{ o.d. } = \frac{V}{R} = I$$

$$A \text{ Z.F.} \times \left(\frac{0.2}{0.2+0.2} \right) \text{ Z.F.} = \underline{0.2I}$$

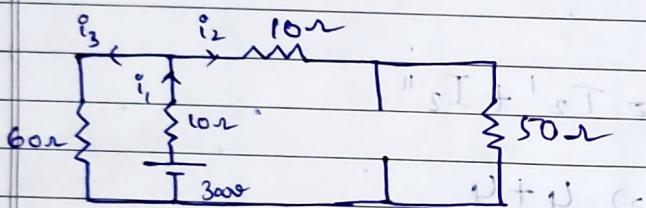
$$0.2 \text{ Z.F.} \times \left(\frac{0.2}{0.2+0.2} \right) \text{ Z.F.} = \underline{0.2I}$$

Q) Find the current in the 50Ω resistor shown in figure using Superposition theorem.



Step 1;

Consider 300 V source, replace 30 A current source by open circuit.



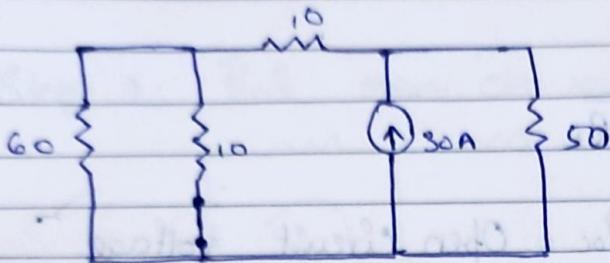
$$R_{\text{net}} = \left(\frac{1}{60} + \frac{1}{10} \right)^{-1} + 10 \rightarrow \underline{\underline{40\Omega}}$$

$$I = \frac{V}{R} = \frac{300}{40} = \underline{\underline{7.5\text{ A}}}.$$

$$I_{50\Omega} = 7.5 \left(\frac{60}{60+60} \right) \rightarrow \underline{\underline{3.75\text{ A}}}.$$

Step 2;

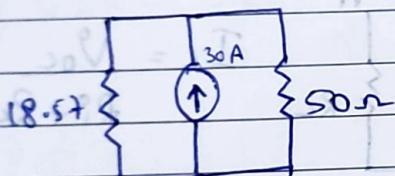
Consider 30 A source & replace 300 V by short circuit.



$$R_{eq} = 8.57 + 10 \parallel 50 \text{ 'parallel'}$$

$$\Rightarrow \left(\frac{1}{18.57} + \frac{1}{50} \right)^{-1} \Rightarrow 18.57 \approx \underline{\underline{}}$$

~~$$\Rightarrow \underline{\underline{}} \text{ or } 13.54 \text{ A.}$$~~



$$I_{50} = 30 \left(\frac{18.57}{18.57 + 50} \right)$$

$$\Rightarrow \underline{\underline{8.125 \text{ A.}}}$$

Step 3; $I_{50} = I_{50}' + I_{50}''$

$$\Rightarrow 3.75 + 8.125.$$

$$\Rightarrow \underline{\underline{11.875}}.$$

* Thévenin's Theorem;

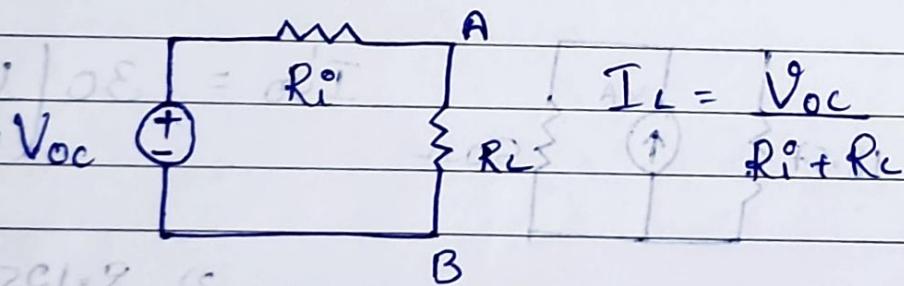
Current through the load resistance (R_L) connected across 2 terminals, A & B of a linear bilateral network is given by the relation. I_L

$$I_L = \frac{V_{oc}}{R_i + R_L}$$

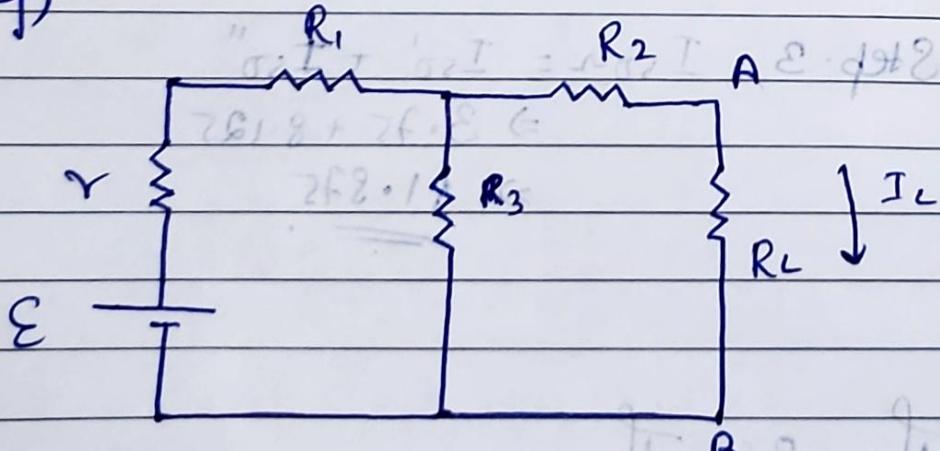
where, V_{oc} = Open circuit voltage

(i.e. Voltage across terminal AB when R_L is removed)

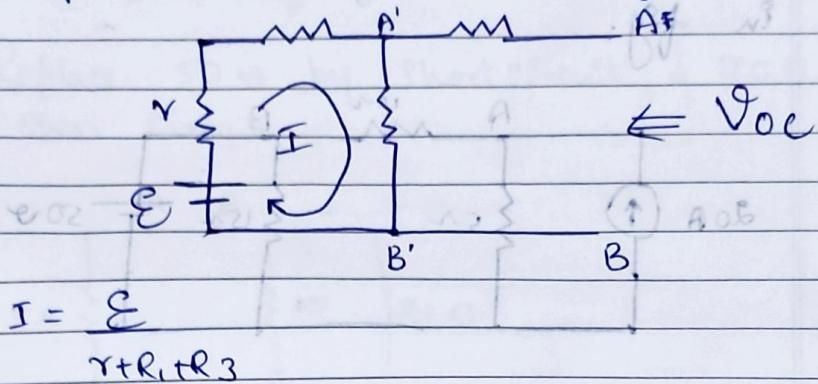
R_i = Internal resistance of network as viewed back into the open circuit end network from terminal A & B deactivating all the independent sources.



Eg;



Step: 1; find open ckt voltage. (V_{oc})

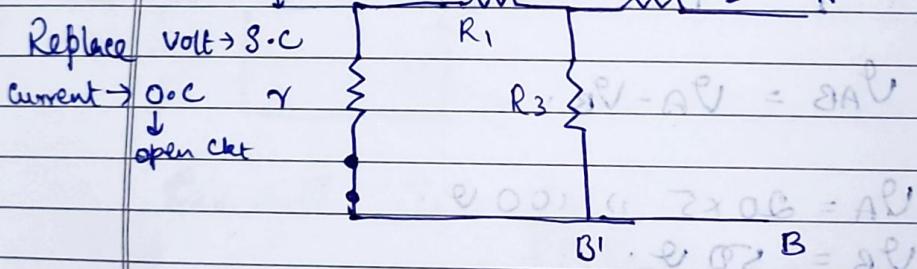


$$\therefore V_{A'B'} = V_{AB} = V_{oc}$$

$$\text{if } V_{AB} = IR_3 \quad \text{brief of.}$$

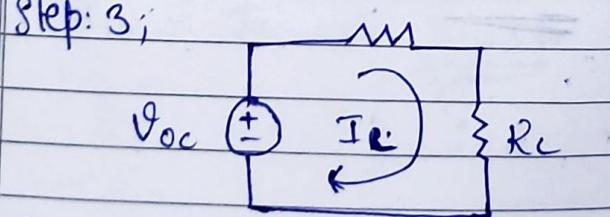
$$\Rightarrow V_{oc} = IR_3$$

Step 2; find internal resistance (R_i)



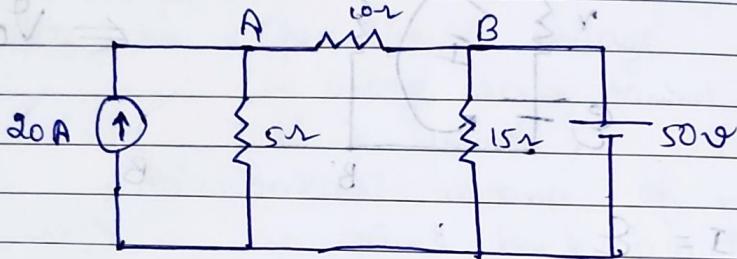
$$R_i = ((r + R_1) // R_3) + R_2$$

Step: 3;



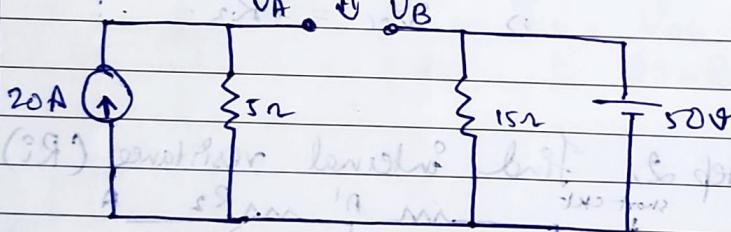
$$I_L = \frac{V_{oc}}{R_i + R_L} \Rightarrow \frac{IR_3}{((r + R_1) // R_3) + R_2 + R_L}$$

Q) Find current through 10Ω resistor shown in fig.



Step: 1;

To find V_{oc} . $V_{oc} = V_{AB}$



$$V_{AB} = V_A - V_B$$

$$V_A = 20 \times 5 \Rightarrow 100 \text{ V}$$

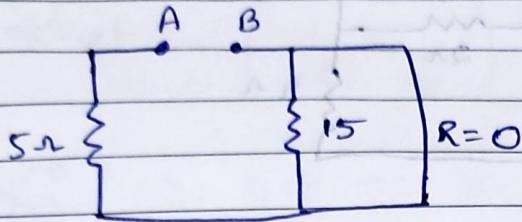
$$V_B = 50 \text{ V}$$

$$\therefore V_{AB} = 100 - 50 \Rightarrow 50 \text{ V}$$

$$\therefore \underline{\underline{V_{oc} = 50 \text{ V}}}$$

Step:2 ; to find R_i^o

Replace 5Ω by short circuit & $20A$ by open circuit.



$$R_{net} = 5\Omega = R_i^o$$

$\hookrightarrow \because$ All current flows through B to A (without 15Ω)
; we shorted circuit.

$$R_i^o = 5\Omega$$



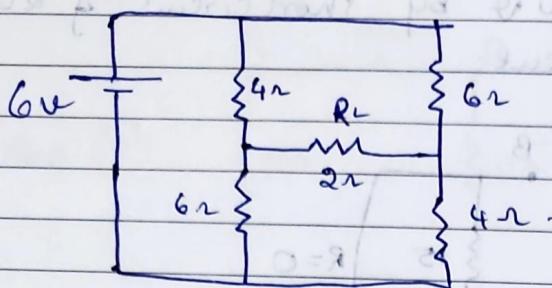
$$V_{oc} = 50 \text{ V}$$

$$R_i^o + R_L = 5 + 10 = 15 \Omega$$

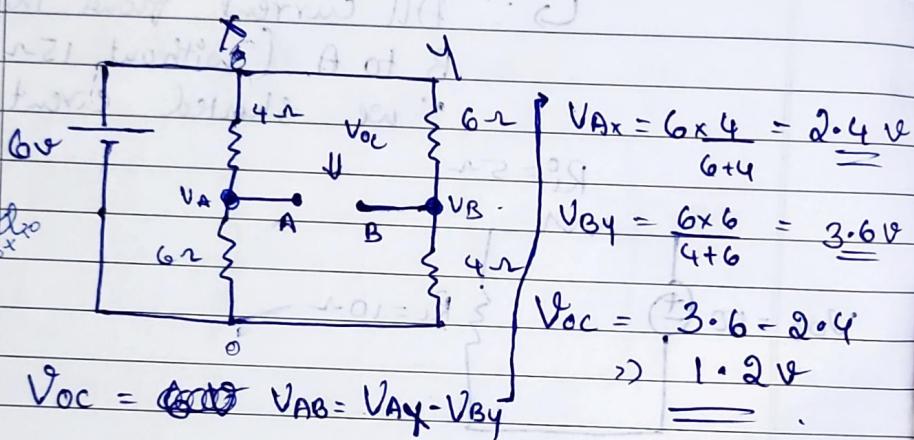
15

$$I_{10} = I_L \Rightarrow 3.33 \text{ A}$$

(Q) Find the current through 2Ω resistor using thevenin theorem.

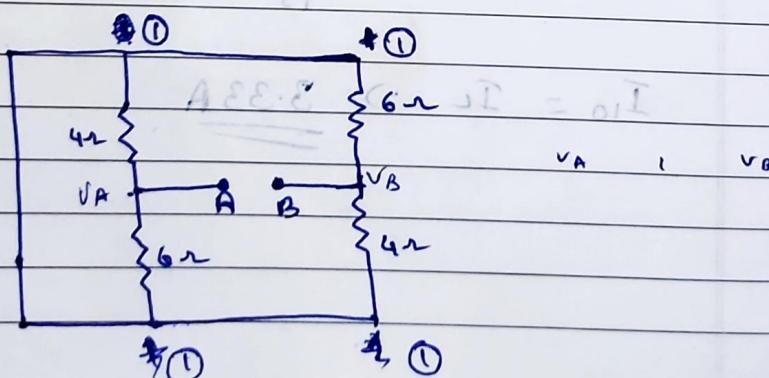


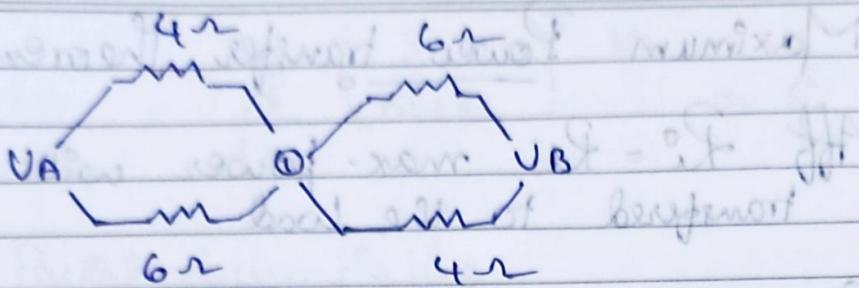
Step 1; find V_{oc}



Step 2; find R_i

Replace 6Ω by short circuit,

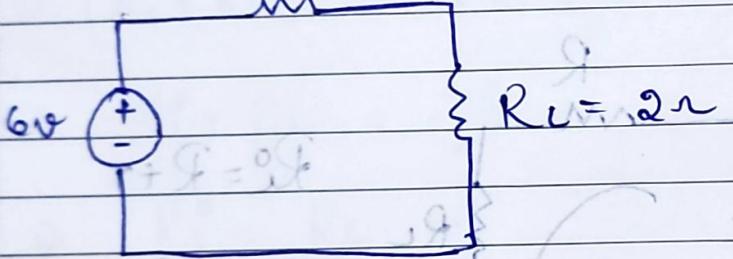




$$R_{\text{net}} = \left(\frac{1}{4} + \frac{1}{6} \right)^{-1} + \left(\frac{1}{4} + \frac{1}{6} \right)^{-1}$$

$$R_i^o \Rightarrow \underline{4.8 \Omega} \text{ derived using }$$

$$R_i^o = 4.8$$



Current through $2\Omega =$ Current in ckt

$$\Rightarrow V_o = I R_{\text{net}}$$

$$\Rightarrow I_o = \frac{V_{oc}}{R_i^o + R_L}$$

$$\Rightarrow I_L = \frac{1.2}{4.8 + 2} = \frac{1.2}{6.0} = \underline{\underline{0.200 A}}$$

$$\hookrightarrow \underline{\underline{0.17 A}}$$

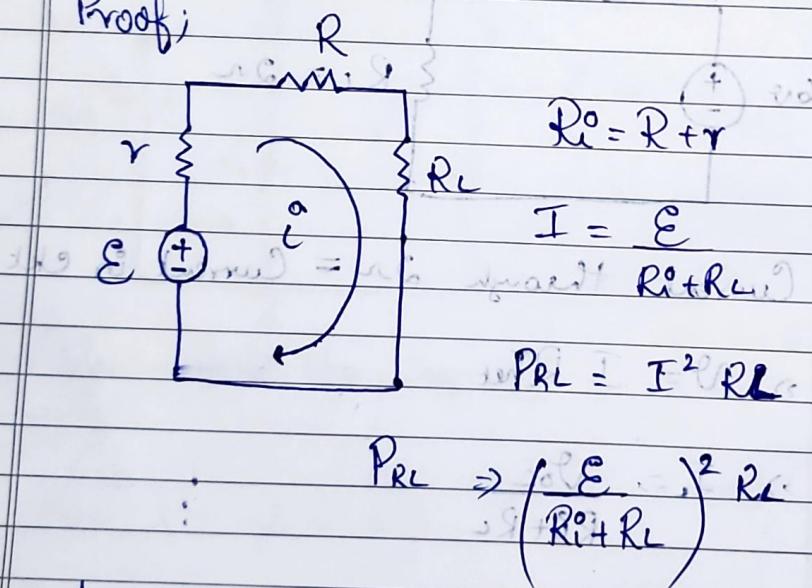
Maximum Power transfer theorem

(k)

If $R_o = R_L$ max. power will be transferred to the load.

Statement: A resistive load absorbs max power from a network when the load resistance equals the internal resistance of the network as viewed from the output terminals with all energy sources removed leaving behind their internal resistances.

Proof:



$$R_o = R + r$$

$$I = \frac{E}{R_o + R_L}$$

$$P_{RL} = I^2 R_L$$

$$P_{RL} \rightarrow \left(\frac{E}{R_o + R_L} \right)^2 R_L$$

Maxima;

$$\frac{dP_{RL}}{dR_L} = 0$$

$$\Rightarrow \frac{d}{dR_L} \left(\frac{E^2}{R_o + R_L} \right) = 0$$

$$\frac{dP_L}{dR_L} = \frac{d}{dR_L} \left(\frac{E}{R_i + R_L} \right)^2 R_L = 0$$

(, 2) x 3
, 1, 2, 3)

Partial differentiating.

$$\frac{d}{dR_L} \left[\frac{(R_i + R_L)^2 (1) - R_L (2)(R_i + R_L)(1)}{(R_i + R_L)^2)^2} \right]$$

$$\Rightarrow (R_i + R_L)^2 - 2R_L(R_i + R_L) = 0.$$

$$\Rightarrow (R_i + R_L)^2 = 2R_L(R_i + R_L)$$

$$\Rightarrow R_i + R_L = 2R_L$$

$$\Rightarrow \underline{\underline{R_i = R_L}}$$

Magnitude of Max power @ $R_o = R_e$.

$$\Rightarrow P_{max} = \left(\frac{E}{R_L + R_L} \right)^2 R_L$$

$$\Rightarrow \underline{\underline{\frac{E^2}{4R_L}}}$$

$$\text{Efficiency } (\eta) = \frac{\text{Output power} \times 100}{\text{Input power}}$$

$$= \frac{P_{max}}{E \times I}$$

$$\eta = \frac{P_{max}}{E \times (R_i + R_L)} \quad \text{Ans}$$

$$\eta = \frac{P_{max}}{E^2} \times R_i + R_L \quad \text{Ans}$$

$$\eta = \frac{E^2}{4R_i \times E^2} \times R_i + R_L \quad \text{Ans}$$

$$\eta = \frac{R_i + R_L}{4R_i} = \frac{(18+9)}{4} \quad \text{Ans}$$

$$\eta = \frac{R_i}{4R_L} + \frac{1}{4} \quad \text{Ans}$$

$$\therefore R_i = R_L$$

$$\eta = \frac{1 + \frac{1}{4}}{4} = \frac{5}{16} \quad \text{Ans}$$

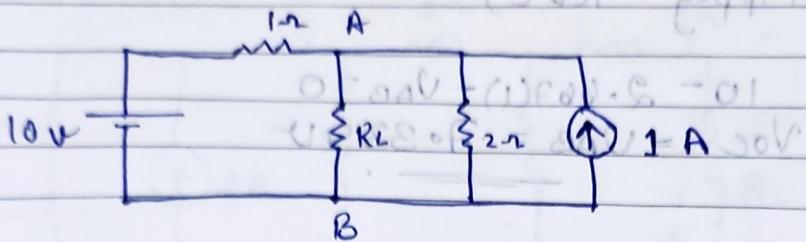
$$\eta = 31.25\% \quad \text{Ans}$$

ans η $= (\eta)$ Ans

Ans

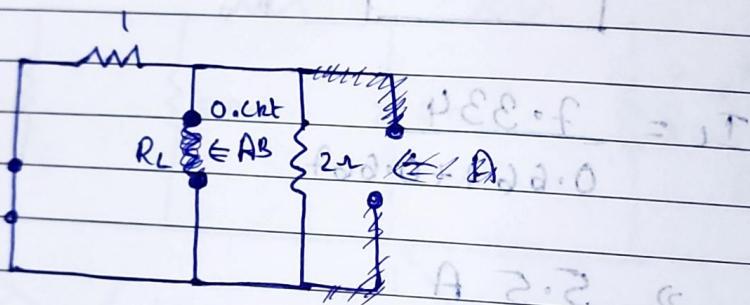
$I \times 2$

a) Calculate the value of R_L which will absorb the max power from circuit in fig. Also calculate value of P_{max} .



To find R_L : $f_{AB} = 0 - 2V$

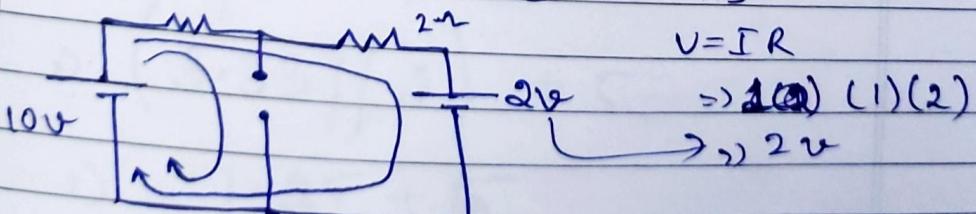
Step 1: Replace 10V with short circuit
to find R_i : $f_{AB} = 0 - 2V$



$$R_i = 2 \parallel 1 \Rightarrow \frac{2}{3} \Omega$$

$$R_i = 0.667 \Omega$$

Step 2: Find $V_{oc} = V_{AB}$



$$I = \frac{V}{R} = \frac{10 - 2}{3} = \frac{8}{3} = 2.667 \text{ A}$$

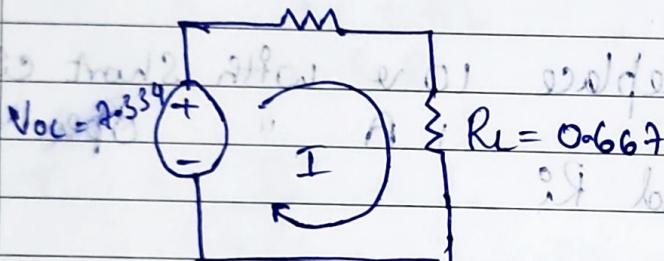
Apply KVL;

$$10 - 2.667(1) - V_{AB} = 0$$

$$V_{OC} = V_{AB} = 7.334 \text{ V}$$

Step: 3;

$$R_L = 0.667 \quad ; \quad \text{if } R_L$$



$$I_L = \frac{7.334}{0.667 + 0.667}$$

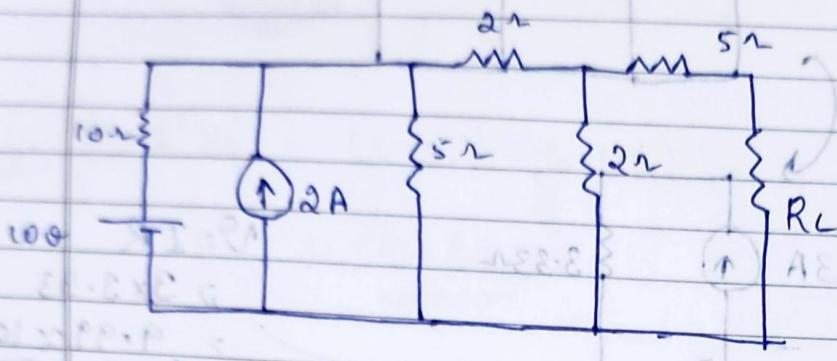
$$\Rightarrow 5.5 \text{ A}$$

$$P_{max} = I^2 R_L$$

$$\Rightarrow (5.5)^2 \times 0.667 = 30.17 \text{ W}$$

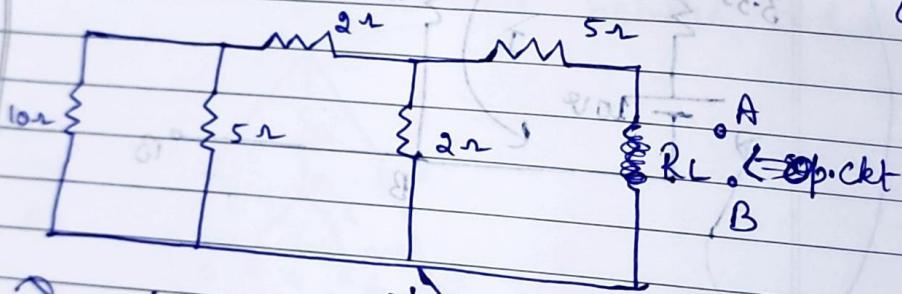
$$\underline{\underline{20.17 \text{ W}}}$$

Q) Obtain the max power transfer to the load in the ckt shown in fig & also calculate the value of R_L



To find R_L .

Step 1; Replace 10V with S.ckt & 2A with OL



~~$$R = \left(\frac{1}{\frac{1}{2} + \frac{1}{5}} \right)^{-1} = 0.473$$~~

~~$$R = \left(10 // 5 + 2 \right) // 2 + 5$$~~

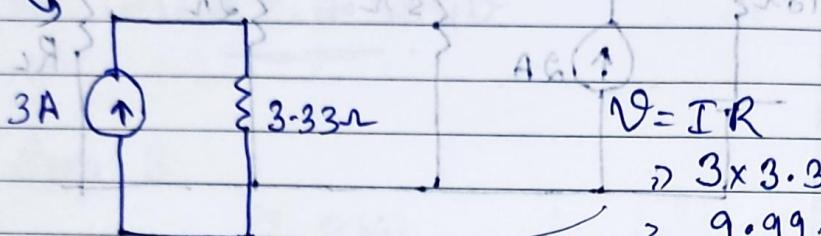
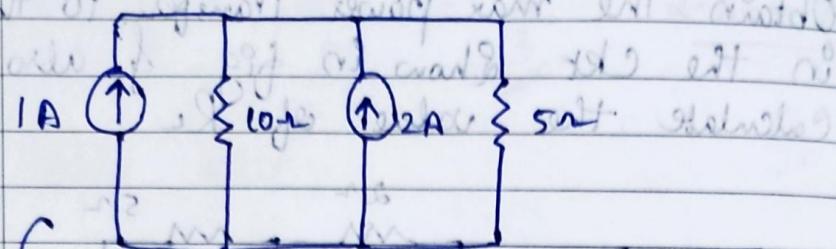
~~$$\Rightarrow (3.33 // 2) + 5$$~~

~~$$\Rightarrow 1.45 + 5$$~~

~~$$\Rightarrow 6.45 \Omega$$~~

Step 2; find V_{oc}

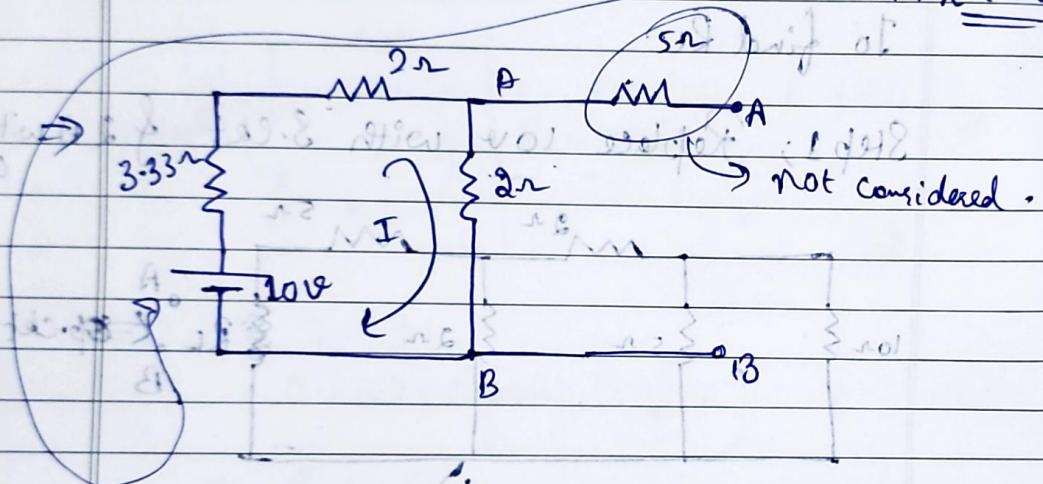
look out of inherent source now left circuit (0)



$$V = IR$$

$$\Rightarrow 3 \times 3.33$$

$$\Rightarrow 9.99 \approx 10V$$



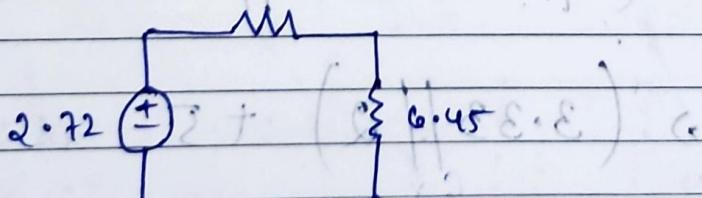
~~$I = 10$~~

~~$\frac{1.36}{3.33 + 2 + 2} A$~~

~~$2 + (2+2)$~~

$$V_{AB} = I \times 2 = 1.36 \times 2 \Rightarrow 2.72V$$

~~$Step: 3; + 5(6.45) + 2(0.1) = 8$~~



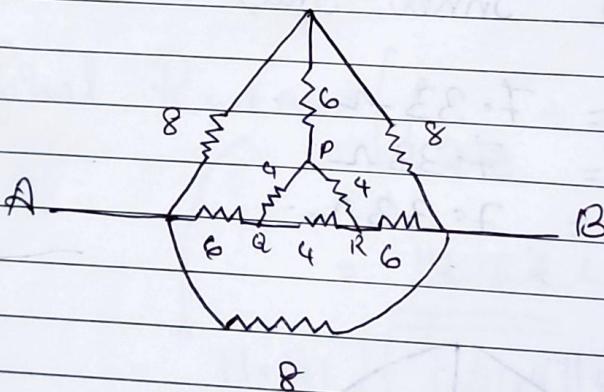
$$I = \frac{2.72}{2 \times 6.45}$$

$$= \underline{\underline{0.21}} \text{ A}$$

$$P = I^2 R_L = (0.21)^2 (6.45)$$

$$\Rightarrow \underline{\underline{0.28}} \text{ W}$$

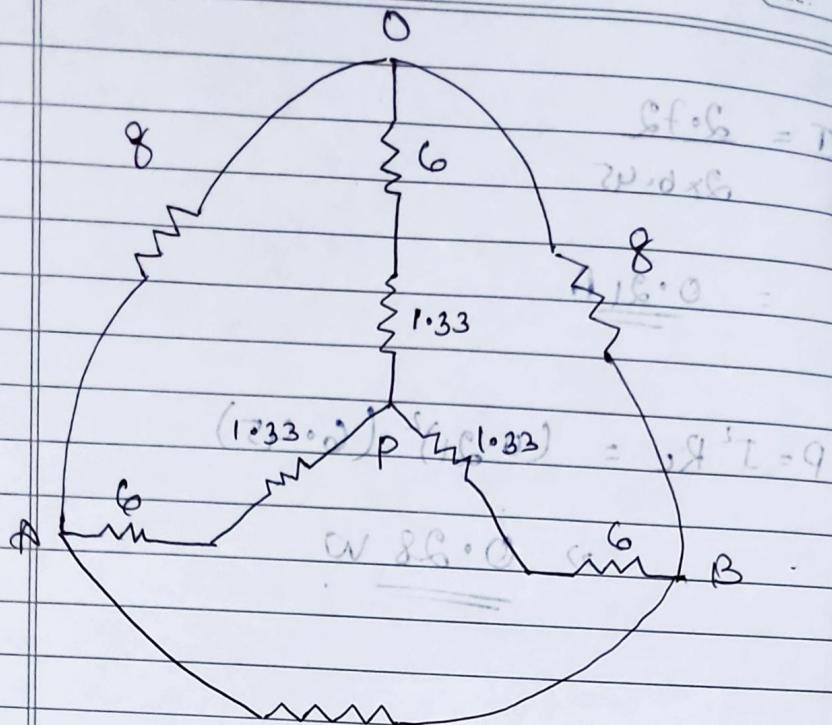
- (Q) In the network shown in fig, the nos represent value of resistors in ohms, find the value of resistance between A & B.



Step 1: Convert PQR delta \rightarrow Star.

$$R_1 = \frac{4 \times 4}{4+4+4} = R_2 = R_3$$

$$\Rightarrow R_1 = R_2 = R_3 = \underline{\underline{1.33}}$$

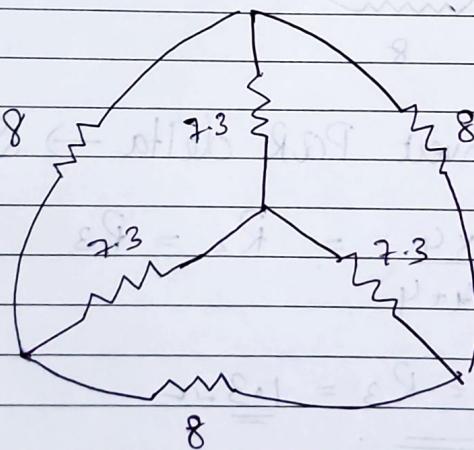


⇒ In the Inner Star;

$$R_{net OP} = 7.33 - r$$

$$R_{net PA} = 7.33 - r$$

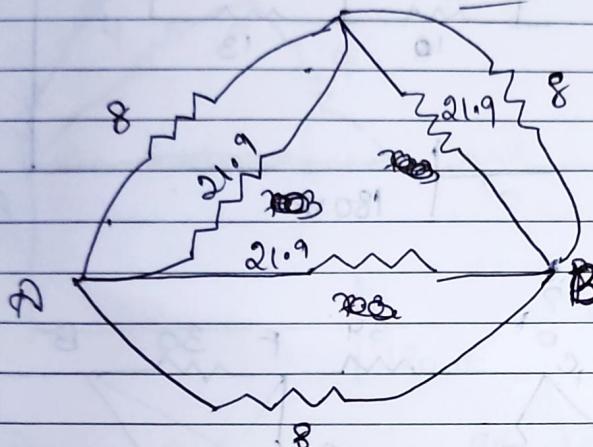
$$R_{net PB} = 7.33 - r$$



Assume a Δ b/w the 2 Systems.
Convert star $\rightarrow \Delta$.

$$\gamma_1 = 7 \cdot 3 + 7 \cdot 3 + \frac{7 \cdot 3 \times 7 \cdot 3}{7 \cdot 3} = \gamma_2 = \gamma_3$$

$$\Rightarrow \gamma_1 = \gamma_2 = \gamma_3 = \underline{\underline{21.9}} \text{ N}$$



$$\text{Final } R_{\text{net AB}} = \left(\left(\frac{1}{21.9} + \frac{1}{8} \right)^{-1} \times 2 \right) // R_{AB \text{ down}}$$

$= \underline{\underline{11.71}}$

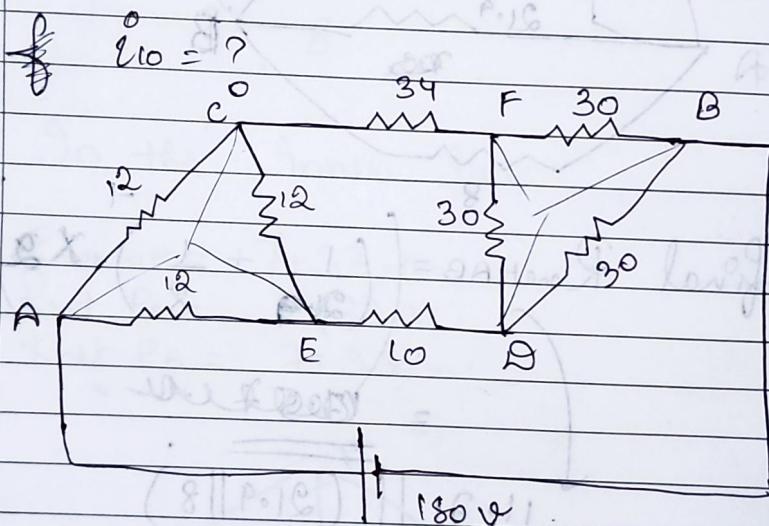
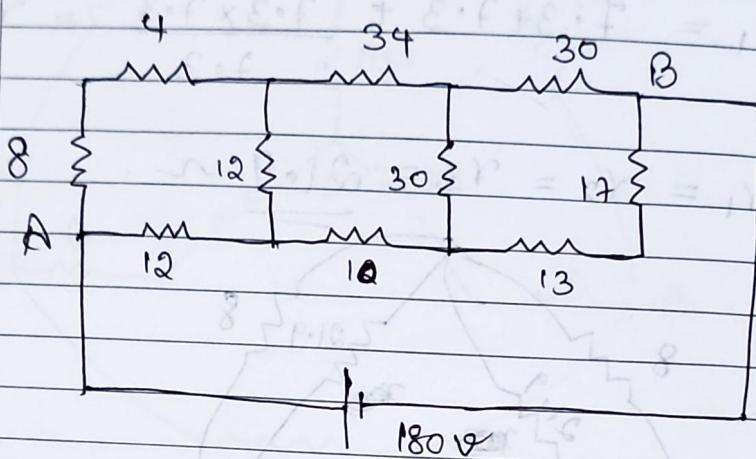
$$11.71 // (21.9 // 8)$$

$$\Rightarrow 11.71 // 5.855$$

$$\Rightarrow \underline{\underline{3.903}} \text{ N}$$

$$\approx \underline{\underline{3.90}} \text{ N}$$

Q) Find the current in 10Ω resistor in the given network using Star delta conversion.



Convert ACE delta \rightarrow Star.

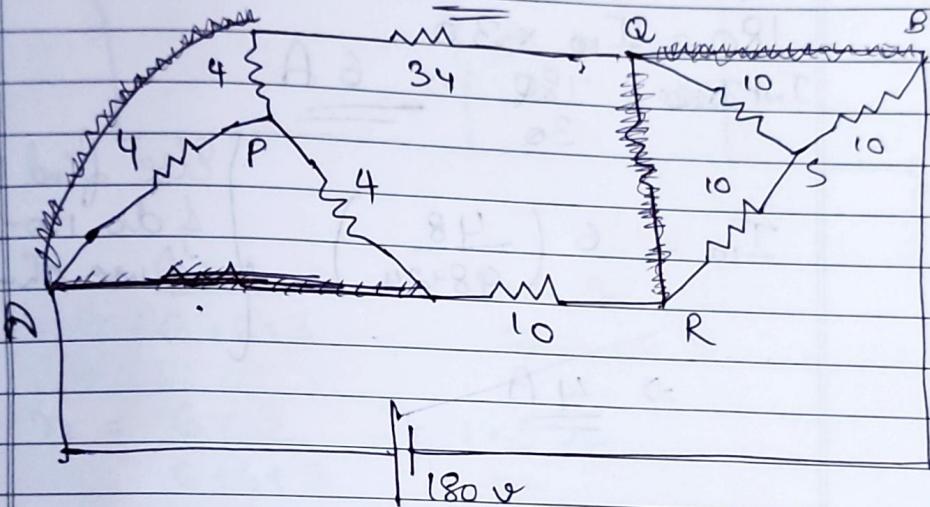
$$\gamma_1 = \frac{12 \times 12}{12 + 12 + 12} = \gamma_2 = \gamma_3$$

$$\Rightarrow 4 = \gamma_1 = \gamma_2 = \gamma_3$$

Convert Δ to Star.

$$\gamma_1 = \gamma_2 = \gamma_3 = \frac{30 \times 30}{30+30+30}$$

$$\Rightarrow \gamma_1 = \gamma_2 = \gamma_3 = 10 \Omega$$

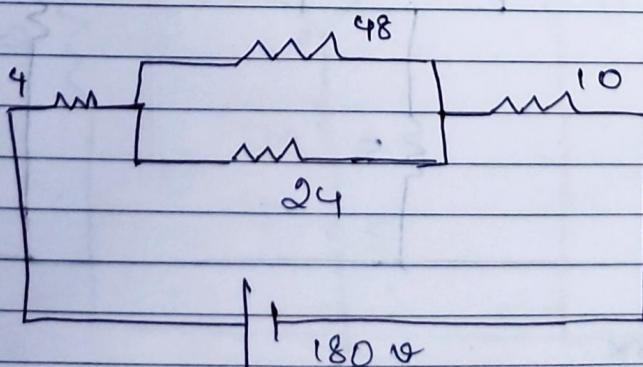


$$\text{Across } PQ = 34 + 4 = 38 \Omega$$

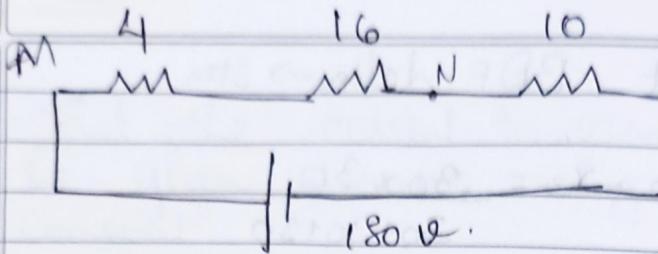
$$\text{" } PR = 4 + 10 = 14 \Omega$$

$$\text{Across } PQS = 38 + 10 = 48 \Omega$$

$$\text{" } PRS = 14 + 10 = 24 \Omega$$



$$R_{180/24} \Rightarrow \left(\frac{1}{48} + \frac{1}{24} \right)^{-1} = 16 \Omega$$



$$V = I R_{\text{net}}$$

$$180 = I \times 30$$

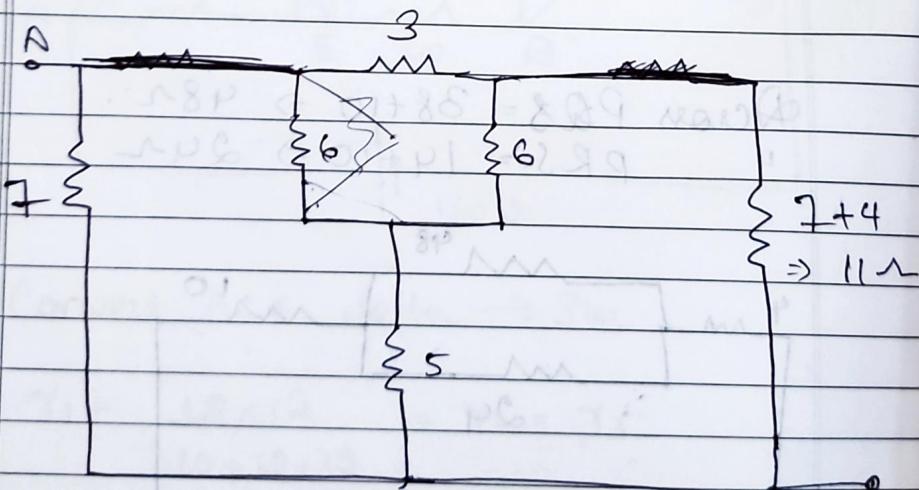
$$I_{\text{net}} = \frac{180}{30} \Rightarrow 6 \text{ A}$$

$$I_{10} = 6 \left(\frac{48}{48+24} \right)$$

} Else find V_{MN}
} if do $180 - V_{MN}$
} if use Ohm's law

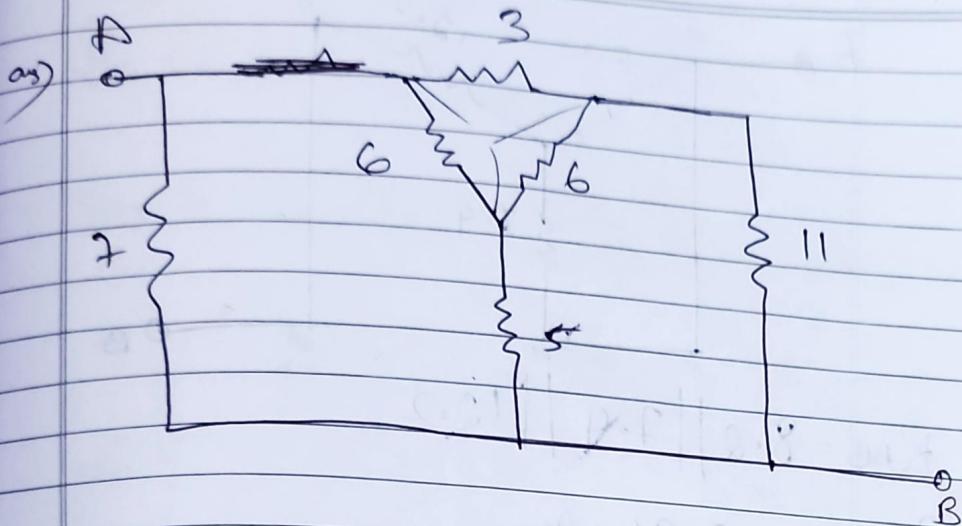
$$\Rightarrow 4 \text{ A}$$

Q) Calculate the Net b/w A & B in the figure



$$V = 16x$$

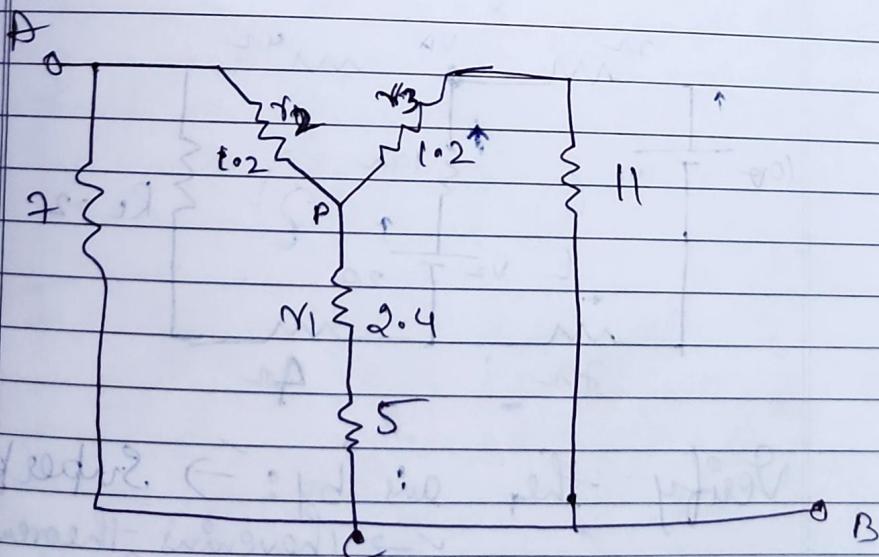
$$I = \frac{V}{R} = \frac{16x}{8P}$$



$$\gamma_1 = \frac{6 \times 6}{6+6+3} = 2.0 \Omega$$

$$\gamma_2 = \frac{6 \times 3}{6+6+3} = 1.0 \Omega$$

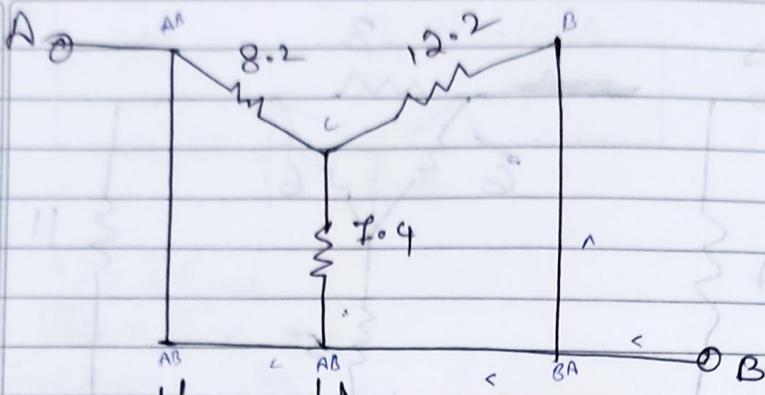
$$\gamma_3 = \frac{6 \times 3}{6+6+3} = 1.0 \Omega$$



Across $R_{net PA} = 8.2 \Omega$

Across $R_{net PB} = 12.2 \Omega$

Across $R_{net PC} = 7.4 \Omega$

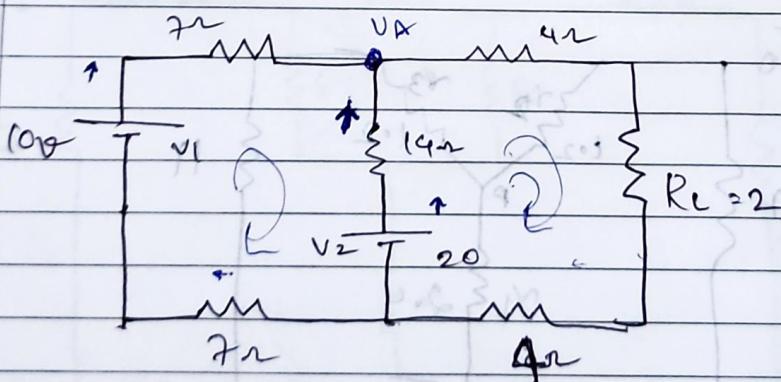


$$R_{AB} = 8.2 \parallel 7.4 \parallel 12.2$$

$R_{\text{net}} \rightarrow$ 20 ohms

$$\therefore R_{\text{net across } AB} = \frac{8.2 \times 12.2}{8.2 + 12.2} \approx 3.69 \Omega$$

Q) Find the current in load R_L using Superposition theorem:



Verify the ans by: \rightarrow Superpost
 \rightarrow Thevenin's theorem
 \rightarrow Nodal Analysis
 \rightarrow Mesh Analysis.