

## ESS 411/511 Geophysical Continuum Mechanics Class #14

Highlights from Class #13 – Maleen Kidiwela  
Today's highlights on Monday – \_\_\_\_\_

Our text doesn't cover our next topics very thoroughly, so we will use a few other sources, which are posted on the class web site under READING & NOTES. <https://courses.washington.edu/ess511/NOTES/notes.shtml>

For Monday class – Please read

- Stein and Wyss session 5.7.2
- Stein and Wyss session 5.7.3/4
- Raymond notes on failure

Also see slides about upcoming topics

- Failure and Mohr's circles – slides

Your short CR/NC Pre-class prep writing assignment (1 point) in Canvas

- It will be due in Canvas at the start of class.
- I will send another message when it is posted in Canvas.

## ESS 411/511 Geophysical Continuum Mechanics

### Broad Outline for the Quarter

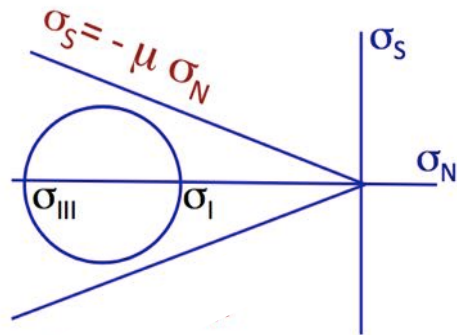
- Continuum mechanics in 1-D
- 1-D models with springs, dashpots, sliding blocks
- Attenuation
- Mathematical tools – vectors, tensors, coordinate changes
- Stress – principal values, Mohr's circles for 3-D stress
- Coulomb failure, pore pressure, crustal strength
- Measuring stress in the Earth
- Strain – Finite strain; infinitesimal strains
- Moments – lithosphere bending; Earthquake moment magnitude
- Conservation laws
- Constitutive relations for elastic and viscous materials
- Elastic waves; kinematic waves

## Class-prep questions for today (break-out rooms)

### Failure of materials

Faults can slip when shear stress  $\sigma_S$  is large enough to overcome frictional resistance. Frictional resistance to failure can be modeled as increasing proportional to the normal traction  $\sigma_N$ .

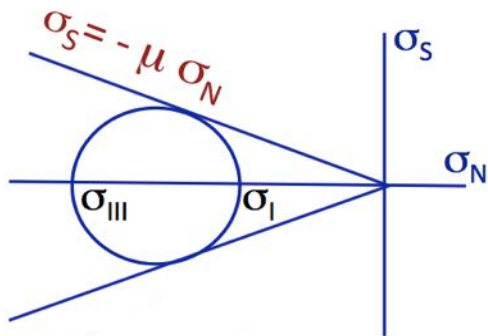
In stress space, if a stress state  $\sigma_N$  and  $\sigma_S$  exists that intersects or touches the frictional line, then the plane represented at that point can fail.



In the diagrams, all principal stresses are negative.

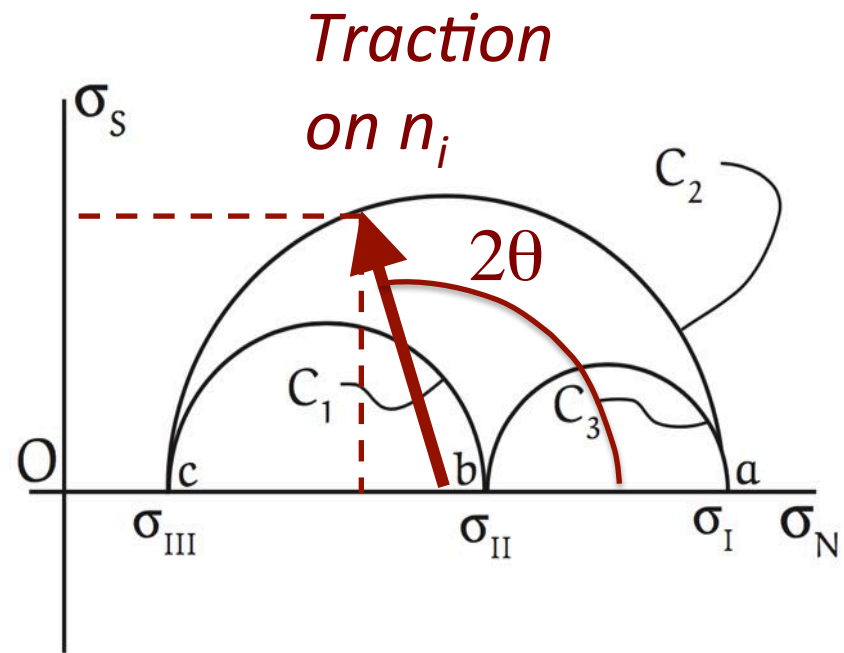
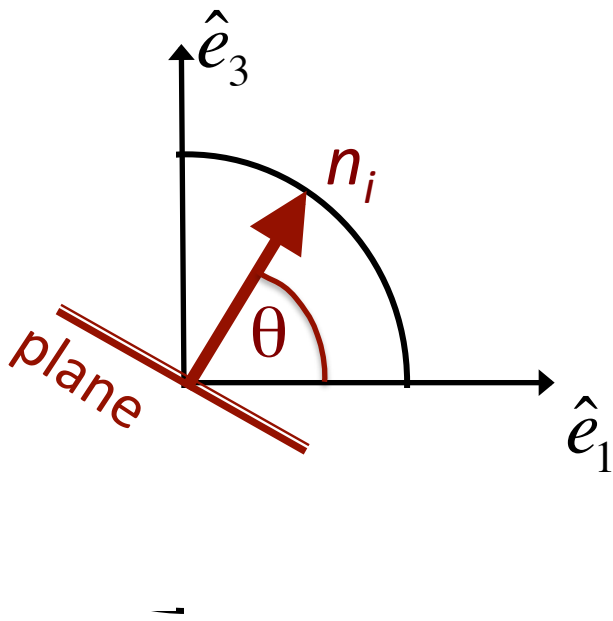
- Are they compressive or extensile?
- In the first diagram, do any stress states exist outside the circle shown?
- Can any faults fail in this stress field?

In the second diagram (below):



- What has changed in the stress field?
- Can any faults fail in this new stress field?
- If yes, how many different faults can fail?
- How could you identify the orientation(s) from the Mohr's circle?

## Mohr's circle in 2-D view



# Cartesian Space vs Stress Space

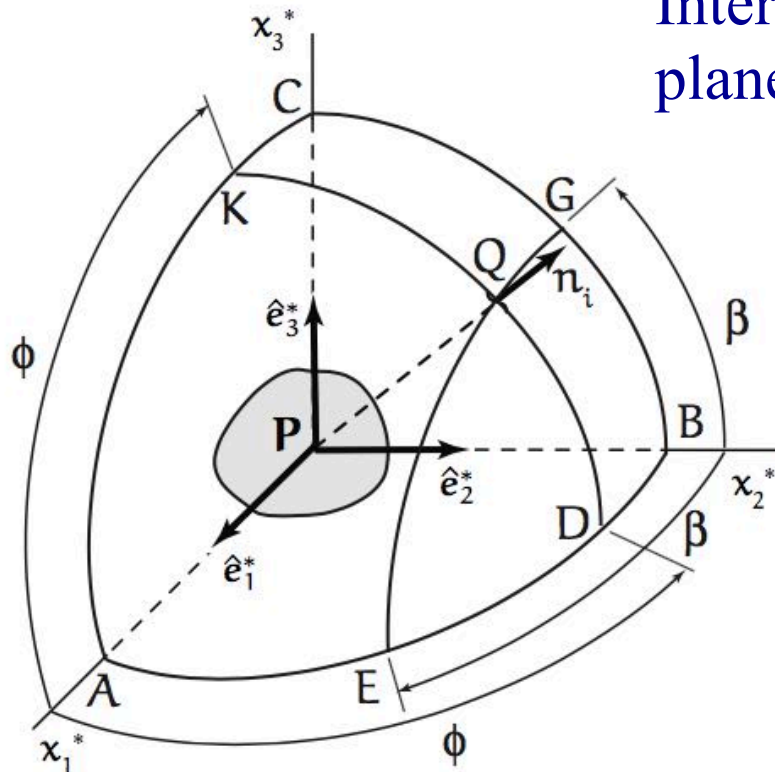
$\hat{e}_i^*$  are principal directions defining principal planes at **P**.

Small circles in Cartesian space (e.g. EQG) map onto circles (e.g. eqg) concentric with primary Mohr's circles (e.g. akc).

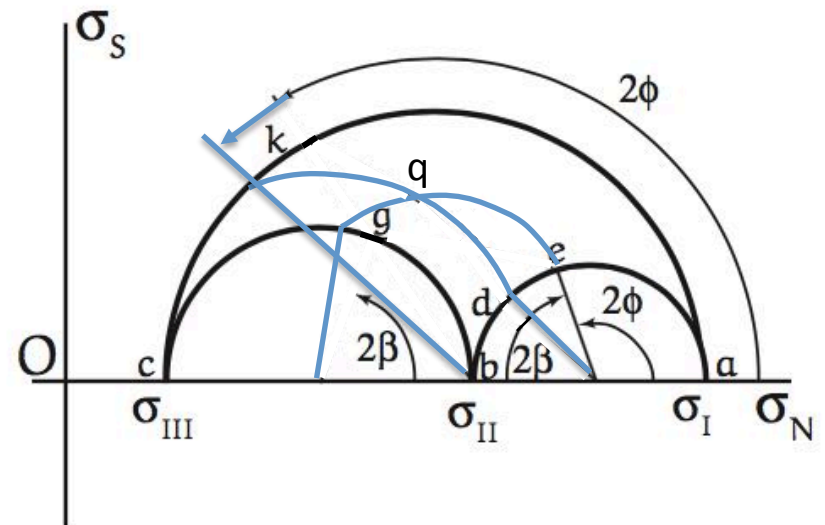
Similarly, KQD maps onto kqd.

Intersection at **q** shows  $\sigma_N$  and  $\sigma_s$  on plane defined by normal vector  $n_i$  at **Q**.

(I have attempted to (sort of) correct the stress-plane figure below. ☺ )

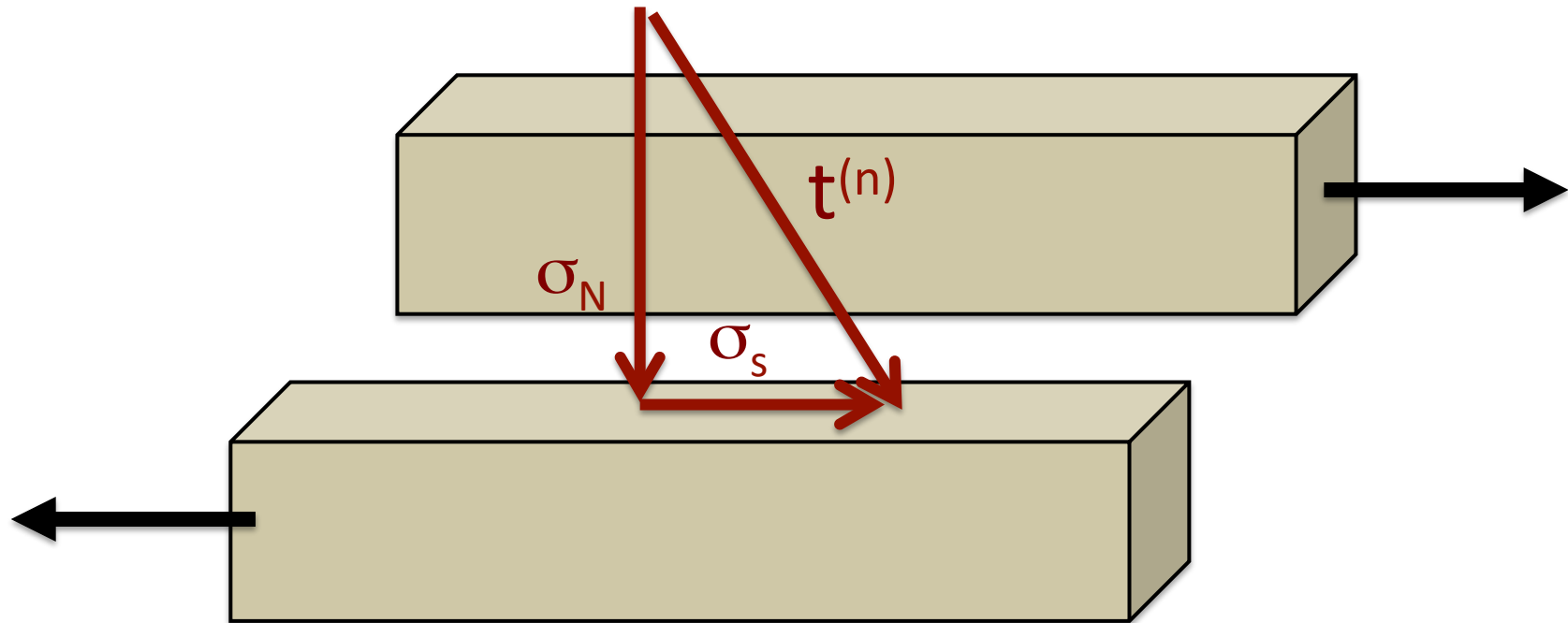


(a) Reference angles  $\phi$  and  $\beta$  for intersection point **Q** on surface of body octant.



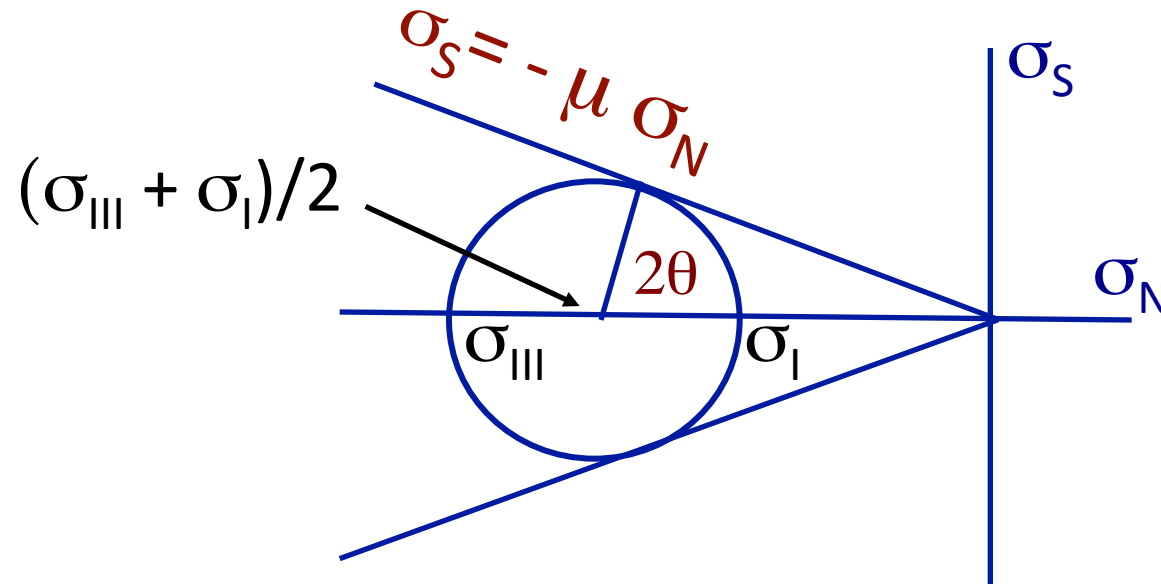
(b) Mohr's stress semicircle for octant of Fig. 3.15(a).

## Sliding friction



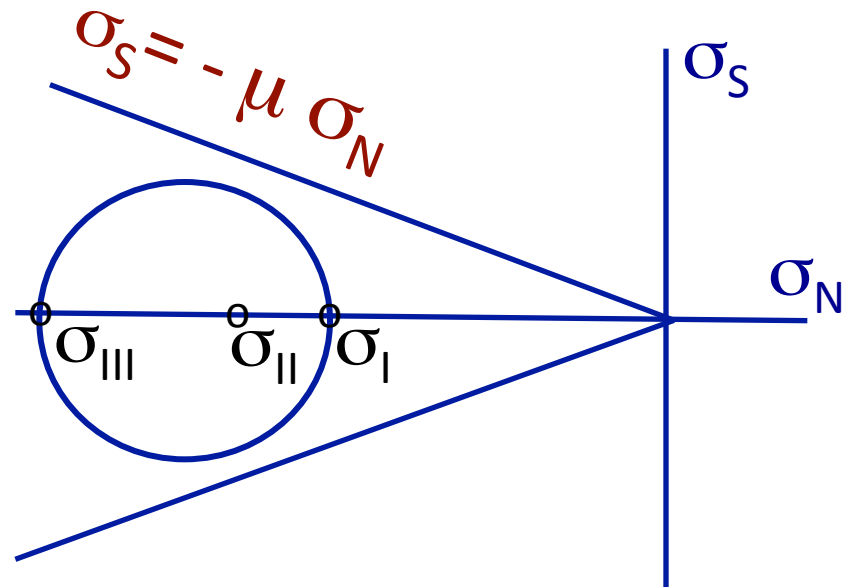
$$\sigma_s = -\mu \sigma_N \quad \mu \text{ is } \textit{coefficient of friction} \text{ for sliding on a pre-existing break}$$

## Frictional sliding



$\sigma_S = -\mu \sigma_N$   $\mu$  is **coefficient of friction** for sliding on a pre-existing break

## Differential stress $\sigma_{III} - \sigma_I$

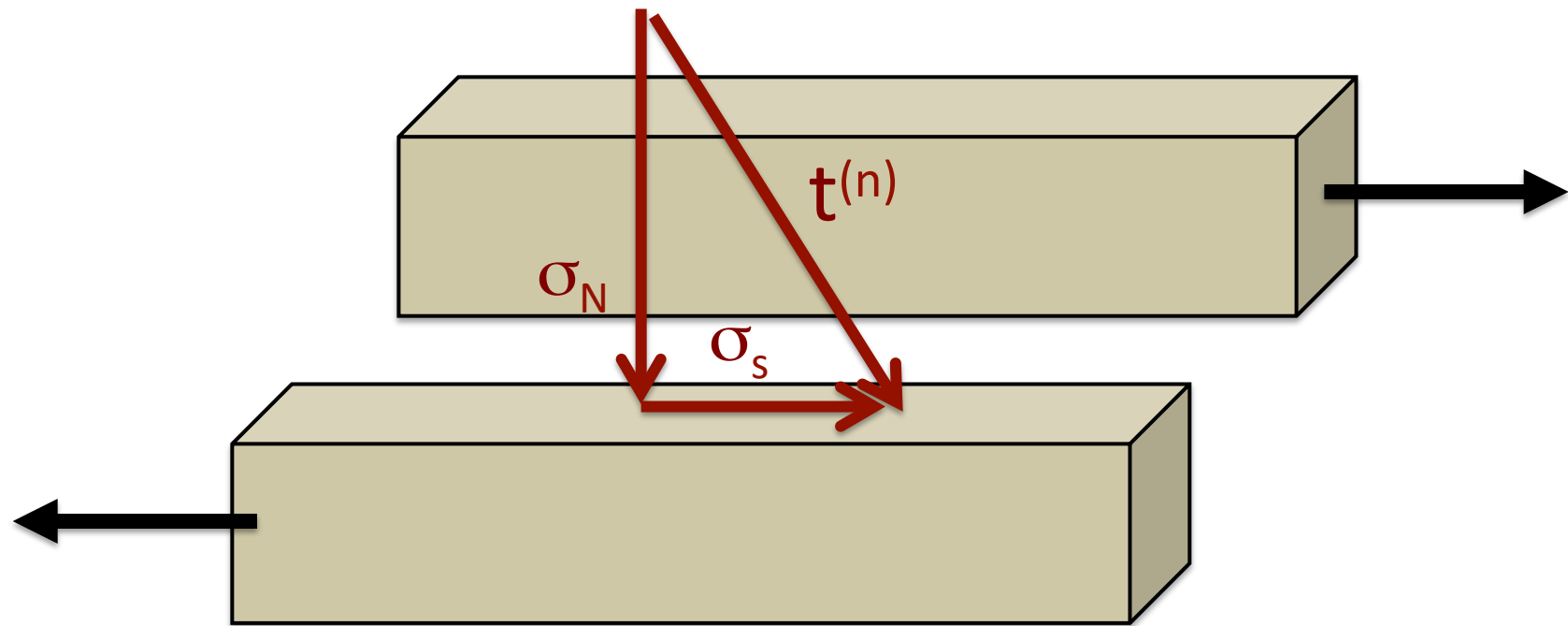


But, if  $\sigma_{III} = \sigma_I$ , all 3 principal stresses are equal

- What do the 3 Mohr's circle look like?
- Describe this state of stress inside the body.
- Is frictional failure possible, if differential stress is zero?



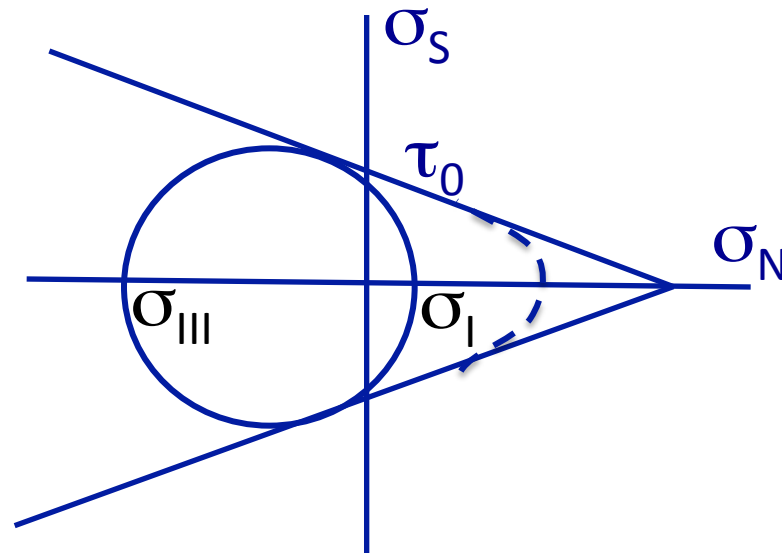
## Mohr-Coulomb Fracture



$$\sigma_s = \tau_0 + \eta \sigma_N$$

$\eta$  is *coefficient of internal friction* for fracture on a new fault surface  
 $\tau_0$  is cohesion of the material

# Mohr-Coulomb Fracture



$\sigma_S = \tau_0 + n \sigma_N$   $n$  is *coefficient of internal friction for fracture on a new fault surface*  
 $\tau_0$  is cohesion of the material