9 strains

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This experiment supersedes all previous ones. It is a factorial manipulation of diversity of the three groups. It takes about 50 hours to run while using 12 cores.

Setup

 \mathbf{R}

```
# rm(list = ls())
knitr::opts_knit$set(
 progress = TRUE,
 verbose = FALSE,
  cache = TRUE
microxanox_release <- "0.3.0"
#tmplib <- tempfile()</pre>
#dir.create(tmplib)
### From '?remotes::install_github`:
# auth_token
    To install from a private repo, generate a personal access token (PAT) in
    "https://github.com/settings/tokens" and supply to this argument. This is
   safer than using a password because you can easily delete a PAT without
   affecting any others. Defaults to the GITHUB_PAT environment variable.
# remotes::install_github(
   "opetchey/microxanox",
#
  ref = microxanox_release,
   # auth_token = "ENTER YOUR TOKEN or PROVED AS ENVIRONMENT VARIABLE",
#
  build_vignettes = FALSE,
   force = TRUE,
#
   upgrade = FALSE,
#
    lib = tmplib
# )
#library(microxanox, lib.loc = tmplib)
```

```
library(microxanox)
if (packageVersion("microxanox") < package_version("0.3.0")) {</pre>
  stop("microxanox version needs to be at least 0.3.0!")
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
## v ggplot2 3.3.5 v purrr 0.3.4
## v tibble 3.1.4 v dplyr 1.0.7
## v tidyr 1.1.3 v stringr 1.4.0
## v readr 2.0.1 v forcats 0.5.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
library(patchwork)
library(here)
## here() starts at /Users/owenpetchey/Desktop/microxanox/diversity_envresp1
source(here("R/various_useful_functions.r"))
zero <- 0 ## don't change
unity <- 1 ## don't change!!!
options(mc.cores = 7)
eval_dynamics_flag <- FALSE</pre>
plot_ss_results <- FALSE</pre>
```

Version of microxanox package used: 0.3.0

General simulation conditions

```
num_CB_strains <- 9
num_SB_strains <- 9
num_PB_strains <- 9

sp <- new_strain_parameter(
    n_CB = num_CB_strains,
    n_PB = num_SB_strains,
    n_SB = num_PB_strains,
    values_initial_state = "bush_ssfig3"
)

parameter <- new_runsim_parameter(
    dynamic_model = bushplus_dynamic_model,
    event_definition = event_definition_1,
    event_interval = 100,</pre>
```

```
noise_sigma = 0,
minimum_abundances = rep(1, 3),
sim_duration = 2000,
sim_sample_interval = 100,
strain_parameter = sp,
log10a_series = c(
   log10(sp$a_0),
   log10(sp$a_0)
)
)
names(parameter$minimum_abundances) <- c("CB", "PB", "SB")
rm(sp)</pre>
```

Define diversity

```
## multiplier of SBPB variation
CB_var_multiplier <- 2
SBPB_var_multiplier <- 6

CB_gmax_div <- 0.015789474 * CB_var_multiplier
CB_h_div <- -0.08 * CB_var_multiplier
SB_gmax_div <- 0.015789474 * SBPB_var_multiplier
SB_h_div <- -0.323 * SBPB_var_multiplier
PB_gmax_div <- 0.015789474 * SBPB_var_multiplier
PB_h_div <- -0.323 * SBPB_var_multiplier
PB_h_div <- -0.323 * SBPB_var_multiplier</pre>
num_div_treatment_levels <- 20
```

Create diversity

```
var_expt <- create_diversity_factorial(
  zero = zero, unity = unity,
  num_div_treatment_levels = num_div_treatment_levels,
  CB_gmax_div = CB_gmax_div, CB_h_div = CB_h_div,
  SB_gmax_div = SB_gmax_div, SB_h_div = SB_h_div,
  PB_gmax_div = PB_gmax_div, PB_h_div = PB_h_div,
  default_9strain = new_strain_parameter(
    n_CB = num_CB_strains,
    n_SB = num_SB_strains,
    n_PB = num_PB_strains,
    values_initial_state = "bush_ssfig3"
  )
}</pre>
```

Display diversity

```
display_diversity(
            400.
            var_expt = var_expt,
            num_CB_strains = num_CB_strains,
            num_SB_strains = num_SB_strains,
            num_PB_strains = num_PB_strains
)
                                                                                                                                                                                                                                                                                                                                                                                                          (phototrophic sulphur bacte 0.0750 - 0.0725 - 0.0700 - 0.0700 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.0675 - 0.
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           Maximum growth rate
                                           0.0510
                           (cyanobacteria)
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                                          0.0500 -
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           Realised growth rate (cyanobacteria)
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                                                       0.03
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                                                                                                                                                                                                                                     0.0050 -
                                                       0.02
                                                                                                                                                                                                                                     0.0025 -
                                                        0.01 -
```

Temporal switching

Reduced sulphur concent

in the environment

(log10 uM per litre)

```
## Here we get some rows of var_expt that correspond with particular diversity levels
var_expt_levels <- var_expt[, 1:6]</pre>
no_diversity <- which(rowSums(abs(var_expt_levels)) == 0)</pre>
max_diversty_all <- which(</pre>
  max(rowSums(abs(var_expt_levels))) == rowSums(abs(var_expt_levels))
max_only_CB_diversity <- which(</pre>
  max(rowSums(abs(var_expt_levels[, 1:2]))) == rowSums(abs(var_expt_levels[, 1:2])) &
  rowSums(abs(var expt levels[,3:6])) == 0
```

0

in the environment

(log10 uM per litre)

Oxygen concentration

in the environment

(log10 uM per litre)

Oxygen concentration

```
# var_expt_levels[381,]

max_only_SBPB_diversity <- which(
  max(rowSums(abs(var_expt_levels[, 3:6]))) == rowSums(abs(var_expt_levels[, 3:6])) &
  rowSums(abs(var_expt_levels[, 1:2])) == 0
)

#var_expt_levels[20,]

medium_diverity_varexp_row <- 311</pre>
```

Oxic to anoxic

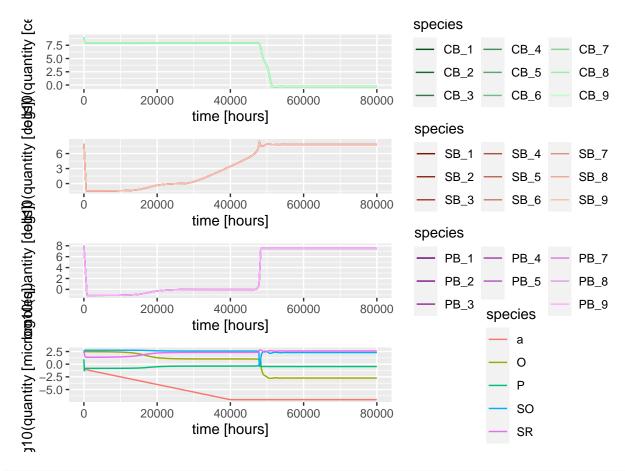
No diversity

```
parameter$sim_duration <- 80000

parameter$log10a_series <- c(-1, -7, -7)
parameter$strain_parameter <- var_expt$pars[[no_diversity]]
parameter$strain_parameter$initial_state <- new_initial_state(
    num_CB_strains,
    num_PB_strains,
    num_SB_strains,
    values = "bush_ssfig3"
)
parameter$strain_parameter$initial_state[grep("CB_", names(parameter$strain_parameter$initial_state))]
sim_res_novar1 <- run_simulation(parameter)
saveRDS(sim_res_novar1, here("experiments/9_strains/data/sim_res_novar1.RDS"))

sim_res_novar1 <- readRDS(here("experiments/9_strains/data/sim_res_novar1.RDS"))

plot_dynamics(sim_res_novar1)</pre>
```

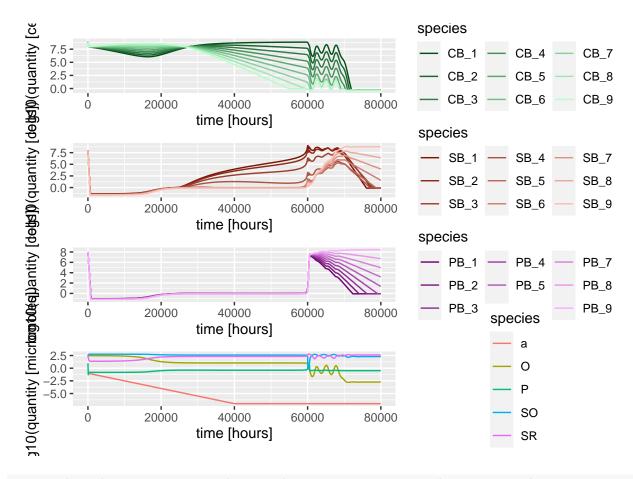


#ggsave(here("simulations/expt2/figures/switching_novar.pdf"), width = 10)

With diversity

```
parameter$strain_parameter <- var_expt$pars[[medium_diverity_varexp_row]]
parameter$strain_parameter$initial_state <- sim_res_novar1$strain_parameter$initial_state
sim_res_highvar1 <- run_simulation(parameter)
saveRDS(sim_res_highvar1, here("experiments/9_strains/data/sim_res_highvar1.RDS"))</pre>
```

sim_res_highvar1 <- readRDS(here("experiments/9_strains/data/sim_res_highvar1.RDS"))
plot_dynamics(sim_res_highvar1)</pre>



#ggsave(here("simulationsexpt2/figures/switching_highvar.pdf"), width = 10)

Anoxic to oxic

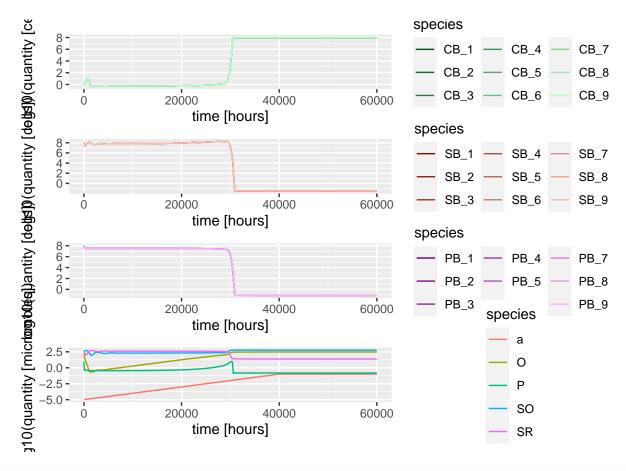
No diversity

```
parameter$sim_duration <- 60000

parameter$log10a_series <- c(-5, -3, -1, -1)
parameter$strain_parameter <- var_expt$pars[[no_diversity]]
parameter$strain_parameter$initial_state <- new_initial_state(
    num_CB_strains,
    num_PB_strains,
    num_SB_strains,
    values = "bush_ssfig3"
))
parameter$strain_parameter$initial_state[grep("CB_", names(parameter$strain_parameter$initial_state))]
sim_res_novar2 <- run_simulation(parameter)
saveRDS(sim_res_novar2, here("experiments/9_strains/data/sim_res_novar2.RDS"))

sim_res_novar2 <- readRDS(here("experiments/9_strains/data/sim_res_novar2.RDS"))

plot_dynamics(sim_res_novar2)</pre>
```



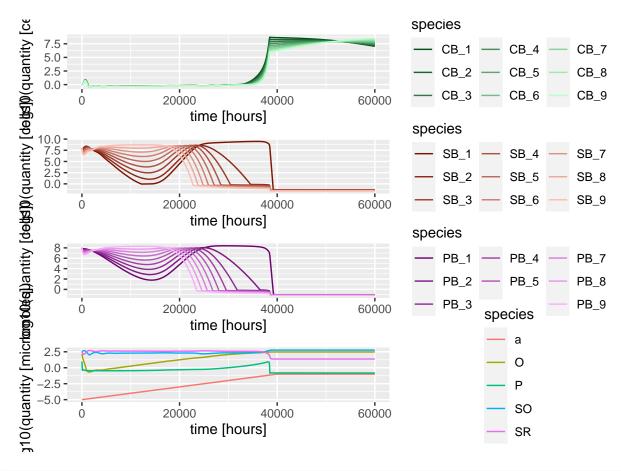
#ggsave(here("simulations/expt2/figures/switching_novar.pdf"), width = 10)

With diversity

plot_dynamics(sim_res_highvar2)

```
parameter$strain_parameter <- var_expt$pars[[medium_diverity_varexp_row]]
parameter$strain_parameter$initial_state <- sim_res_novar2$strain_parameter$initial_state
sim_res_highvar2 <- run_simulation(parameter)
saveRDS(sim_res_highvar2, here("experiments/9_strains/data/sim_res_highvar2.RDS"))</pre>
```

sim_res_highvar2 <- readRDS(here("experiments/9_strains/data/sim_res_highvar2.RDS"))</pre>



#ggsave(here("simulationsexpt2/figures/switching_highvar.pdf"), width = 10)

Anoxic to oxic to anoxic

No diversity

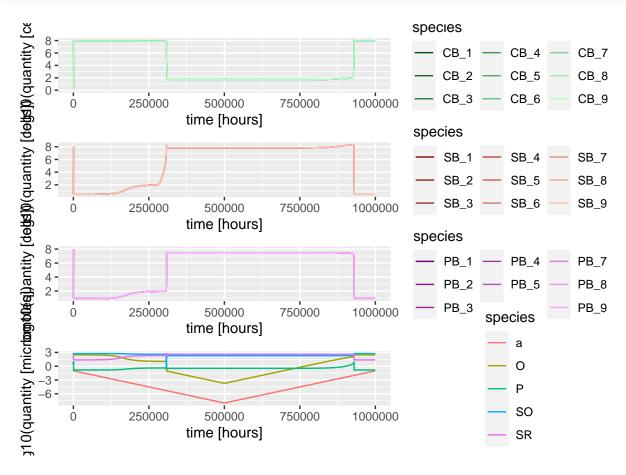
```
parameter$sim_duration <- 1000000

parameter$minimum_abundances <- rep(100, 3)
names(parameter$minimum_abundances) <- c("CB", "PB", "SB")

parameter$log10a_series <- c(-1, -8, -1)
parameter$strain_parameter <- var_expt$pars[[no_diversity]]
parameter$strain_parameter$initial_state <- new_initial_state(
    num_CB_strains,
    num_PB_strains,
    num_SB_strains,
    values = "bush_ssfig3"
)

parameter$strain_parameter$initial_state[grep("CB_", names(parameter$train_parameter$initial_state))]
sim_res_novar3 <- run_simulation(parameter)
saveRDS(sim_res_novar3, here("experiments/9_strains/data/sim_res_novar3.RDS"))</pre>
```

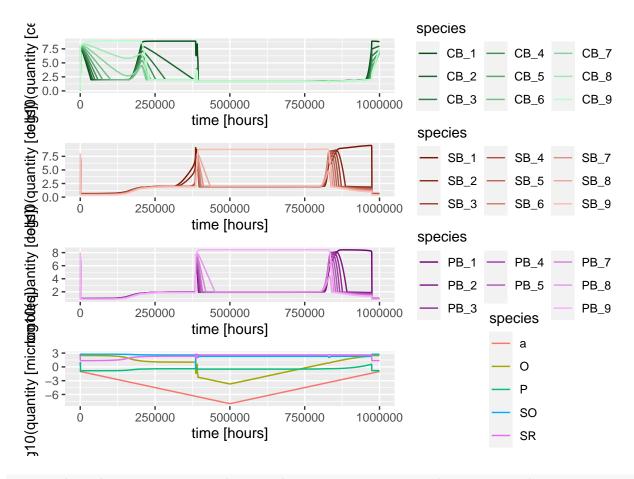
sim_res_novar3 <- readRDS(here("experiments/9_strains/data/sim_res_novar3.RDS"))
plot_dynamics(sim_res_novar3)</pre>



#ggsave(here("simulations/expt2/figures/switching_novar.pdf"), width = 10)

With diversity

```
parameter$strain_parameter <- var_expt$pars[[medium_diverity_varexp_row]]
parameter$strain_parameter$initial_state <- sim_res_novar3$strain_parameter$initial_state
sim_res_highvar3 <- run_simulation(parameter)
saveRDS(sim_res_highvar3, here("experiments/9_strains/data/sim_res_highvar3.RDS"))
sim_res_highvar3 <- readRDS(here("experiments/9_strains/data/sim_res_highvar3.RDS"))
plot_dynamics(sim_res_highvar3)</pre>
```



#ggsave(here("simulationsexpt2/figures/switching_highvar.pdf"), width = 10)

Ecosystem-environment relationship

Stable state finding

Finding

Setup parameter

```
options(mc.cores = 7)

minimum_abundances <- rep(0, 3)
names(minimum_abundances) <- c("CB", "PB", "SB")

grid_num_a <- 1000 #usually 1000 ## number of a_0 values
#grid_num_a <- 10 ## FOR TEST
a_0s <- 10^seq(-7, -0.5, length=grid_num_a) ## sequence of a_0 values
grid_num_N <- 2 ## number of N values
initial_CBs <- 10^seq(0, 10, length=grid_num_N) ## sequence of N values
initial_PBs <- 1e8 ## not varied
initial_SBs <- 1e8 ## not varied</pre>
```

```
# next line creates all possible combinations
ss_expt <- expand.grid(N_CB = initial_CBs,</pre>
                      N PB = initial PBs,
                      N SB = initial SBs,
                      a 0 = a 0s)
parameter <- new_ss_by_a_N_parameter(</pre>
  dynamic_model = parameter$dynamic_model,
  event definition = parameter$event definition,
  event_interval = 1000000,
  noise_sigma = parameter$noise_sigma,
  minimum_abundances = minimum_abundances,
  sim_duration = 1000000,
  sim_sample_interval = 1000000,
 log10a_series = parameter$log10a_series,
 solver_method = parameter$solver_method,
  ss_expt = ss_expt
rm(minimum_abundances, grid_num_a, a_Os, grid_num_N, initial_CBs, initial_PBs, initial_SBs, ss_expt)
saveRDS(parameter, here("experiments/9 strains/data/parameter 1e6 x2x6 factorial.RDS"))
saveRDS(var expt, here("experiments/9 strains/data/var expt 1e6 x2x6 factorial.RDS"))
```

Run stable state finding

*Careful, this simulation takes about 600 hours on a single core

```
run_ss_var_experiment(
   parameter = readRDS(here("experiments/9_strains/data/parameter_1e6_x2x6_factorial.RDS")),
   var_expt = readRDS(here("experiments/9_strains/data/var_expt_1e6_x2x6_factorial.RDS"))) %>%
saveRDS(here("experiments/9_strains/data/ss_data_1e6_x2x6_factorial.RDS")))
```

Process the stable state data

Bring in various stable state datasets

```
cluster <- multidplyr::new_cluster(7)
multidplyr::cluster_library(cluster, c("microxanox", "dplyr"))

## sim length 1'000'000, 20 SBPBgrad, 2xCB variation, 6xSBPB variation
readRDS(here("experiments/9_strains/data/ss_data_1e6_x2x6_factorial_small.RDS")) %>%
    mutate(sim_length = 1000000) %>%
    multidplyr::partition(cluster) %>%
    mutate(stability_measures = list(get_stability_measures(ss_res))) %>%
    collect() %>%
    unnest(cols = c(stability_measures)) %>%
    saveRDS(here("experiments/9_strains/data/stab_data_1e6_x2x6_factorial_small.RDS"))
```

```
## find various combinations of diversity
var_expt <- readRDS(here("experiments/9_strains/data/ss_data_1e6_x2x6_factorial.RDS"))
stab_data <- readRDS(here("experiments/9_strains/data/stab_data_1e6_x2x6_factorial.RDS"))</pre>
```

Display results

```
p1 <- plot_ss_result1(var_expt,</pre>
                result_index = no_diversity,
                filename prefix = NULL,
                save_image_file = FALSE)
p1
p2 <- plot_ss_result1(var_expt,</pre>
                result_index = max_diversty_all,
                filename_prefix = NULL,
                save_image_file = FALSE)
p2
p3 <- plot_ss_result1(var_expt,
                result_index = max_only_CB_diversity,
                filename_prefix = NULL,
                save_image_file = FALSE)
рЗ
p4 <- plot_ss_result1(var_expt,
                result_index = max_only_SBPB_diversity,
                filename_prefix = NULL,
                save_image_file = FALSE)
p4
p_overlay1 <- plot_ss_result2(var_expt[no_diversity,]$ss_res[[1]],</pre>
```

```
var_expt[max_diversty_all,]$ss_res[[1]],
                              xlims = c(-7, -1))
p_overlay1
p_overlay2 <- plot_ss_result2(var_expt[no_diversity,]$ss_res[[1]],</pre>
                              var_expt[max_only_CB_diversity,]$ss_res[[1]],
                              xlims = c(-7, -1))
p_overlay2
p_overlay3 <- plot_ss_result2(var_expt[no_diversity,]$ss_res[[1]],</pre>
                              var expt[max only SBPB diversity,]$ss res[[1]],
                              xlims = c(-7, -1))
p_overlay3
tempp1 <- var_expt[no_diversity,]$ss_res[[1]] %>%
  filter(initial_N_CB == 1e10,
         log10(a_0) > -4.5, log10(a_0) < -4)
tempp2 <- var_expt[max_only_SBPB_diversity,]$ss_res[[1]] %>%
  filter(initial_N_CB == 1e10,
         log10(a_0) > -4.5, log10(a_0) < -4)
ggplot() +
  geom_line(mapping = aes(x = log10(tempp1$a_0),
                           y = log10(tempp1\$0))) +
  geom_line(mapping = aes(x = log10(tempp2$a_0)),
                          y = log10(tempp2\$0)),
            col = "blue")
ggplot() +
  geom\_histogram(mapping = aes(x = log10(tempp1$0) - log10(tempp2$0)),
            col = "blue")
ggplot() +
  geom_line(mapping = aes(x = log10(tempp1a_0),
    y = log10(tempp1$P) - log10(tempp2$P)),
           col = "blue")
CB_vars <- unique(stab_data$CB_var_gmax_s)</pre>
SB_vars <- unique(stab_data$SB_var_gmax_s)</pre>
CB_stab_data <- stab_data %>%
  filter(SB_var_gmax_s == 0) %>%
  mutate(var_treat = "CB",
         var_gmax = CB_var_gmax_s)
SBPB_stab_data <- stab_data %>%
  filter(CB_var_gmax_s == 0) %>%
  mutate(var_treat = "SB-PB",
         var_gmax = SB_var_gmax_s)
for_join <- tibble(CB_var_gmax_s = CB_vars,</pre>
```

Raw

```
all stab results %>%
  filter(Species == "0") %>%
  ggplot(aes(x = var_gmax, y = hyst_range_raw, col=var_treat, shape = as_factor(sim_length))) +
  geom_point() +
  xlab("Amount of trait variation\n[see text for units]") +
  ylab("Extent of bistability region\n[log10 oxygen diffusivity]") +
  labs(col = "Variation in\nonly these\nfunctional groups")
##ggsave("manuscript/figures/extent_of_bistab1.pdf", height = 4)
all_stab_results %>%
  #filter(var_treat == "CB") %>%
  filter(Species == "0",
         sim_length == 1e6) %>%
  ggplot(aes(x = var_gmax,
            ymin = hyst_min_raw,
             ymax = hyst_max_raw,
             fill=var_treat)) +
  geom_ribbon(alpha = 0.5) +
  facet_wrap( ~ var_treat, nrow = 3) +
  xlab("Amount of trait variation\n[see text for units]") +
  ylab("Oxygen diffusivity\n[log10 uM per hour]") +
  labs(fill = "Variation in\nonly these\nfunctional groups") +
  coord_flip() +
  theme(
   strip.background = element_blank(),
   strip.text.x = element_blank()
##ggsave("manuscript/figures/extent_of_bistab2.pdf", height = 4)
```

Log transformed

```
all_stab_results %>%
  filter(Species == "0") %>%
  ggplot(aes(x = var_gmax, y = hyst_range_log, col=var_treat, shape = as_factor(sim_length))) +
  geom_point() +
  xlab("Amount of trait variation\n[see text for units]") +
  ylab("Extent of bistability region\n[log10 oxygen diffusivity]") +
  labs(col = "Variation in\nonly these\nfunctional groups")
##ggsave("manuscript/figures/extent_of_bistab1.pdf", height = 4)
all stab results %>%
  #filter(var_treat == "CB") %>%
  filter(Species == "0",
         sim_length == 1e6) %>%
  ggplot(aes(x = var_gmax,
             ymin = hyst_min_log,
             ymax = hyst_max_log,
            fill=var_treat)) +
  geom_ribbon(alpha = 0.5) +
  facet_wrap( ~ var_treat, nrow = 3) +
  xlab("Amount of trait variation\n[see text for units]") +
  ylab("Oxygen diffusivity\n[log10 uM per hour]") +
  labs(fill = "Variation in\nonly these\nfunctional groups") +
  coord_flip() +
  theme(
   strip.background = element_blank(),
   strip.text.x = element_blank()
##ggsave("manuscript/figures/extent_of_bistab2.pdf", height = 4)
stab_data %>%
  filter(Species == "0",
         sim_length == 1e6) %>%
  ggplot(aes(x = CB_var_gmax_s, y = SB_var_gmax_s, fill = hyst_range_log, col = hyst_range_log)) +
  geom_point(size = 3)
```