experiment 1

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This experiment supercedes all previous ones. It is a factorial manipulation of diversity of the three groups. It takes about 50 hours to run while using 12 cores.

Setup

\mathbf{R}

```
rm(list = ls())
knitr::opts_knit$set(progress = TRUE, verbose = FALSE, cache = TRUE)
microxanox_release <- "0.2"
#tmplib <- tempfile()</pre>
#dir.create(tmplib)
### From '?remotes::install_github`:
# auth_token
   To install from a private repo, generate a personal access token (PAT) in
   "https://github.com/settings/tokens" and supply to this argument. This is
  safer than using a password because you can easily delete a PAT without
   affecting any others. Defaults to the GITHUB_PAT environment variable.
# remotes::install_qithub(
  "opetchey/microxanox",
# ref = microxanox_release,
  # auth_token = "ENTER YOUR TOKEN or PROVED AS ENVIRONMENT VARIABLE",
  build_vignettes = FALSE,
   force = TRUE,
   upgrade = FALSE,
    lib = tmplib
#library(microxanox, lib.loc = tmplib)
library(microxanox)
library(tidyverse)
```

Version of microxanox package used: 0.2.1

General simulation conditions

```
default_dynamic_model <- bushplus_dynamic_model
default_event_definition <- event_definition_1
default_event_interval <- 100
default_noise_sigma <- 0
default_minimum_abundances <- rep(1, 3)
names(default_minimum_abundances) <- c("CB", "PB", "SB")
default_sim_duration <- 80000
default_sim_sample_interval <- 100
initial_pars_from <- "bush_ssfig3"
## note that next line (log10a_series is over-ridden with getting stable states)
#default_log10a_series <- c(-2, -2, -2, -10, -10, -10, -10, -10)</pre>
```

Define diversity

```
num_CB_strains <- 9
num_SB_strains <- 9
num_PB_strains <- 9

## multiplier of SBPB variation
CB_var_multiplier <- 2
SBPB_var_multiplier <- 6</pre>
```

```
CB_gmax_div <- 0.015789474 * CB_var_multiplier

CB_h_div <- 0.08 * CB_var_multiplier

SB_gmax_div <- 0.015789474 * SBPB_var_multiplier

SB_h_div <- 0.323 * SBPB_var_multiplier

PB_gmax_div <- 0.015789474 * SBPB_var_multiplier

PB_h_div <- 0.323 * SBPB_var_multiplier

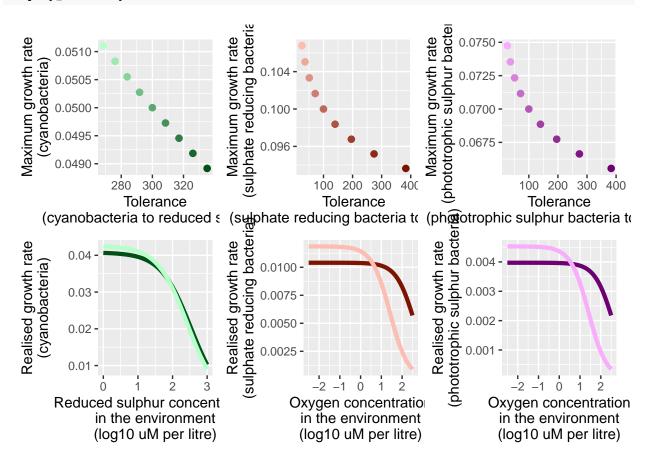
PB_h_div <- 0.323 * SBPB_var_multiplier
```

Create diversity

```
var_expt <- create_diversity_factorial()</pre>
```

Display diversity

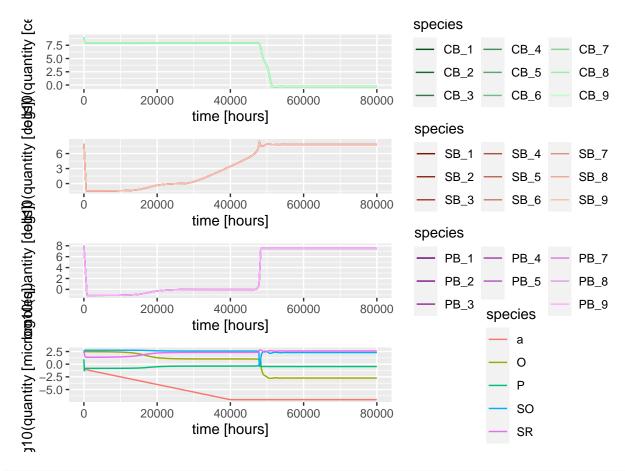
display_diversity(400)



Temporal switching

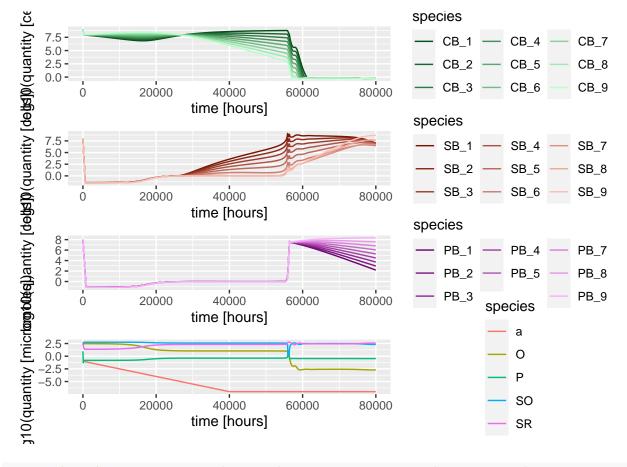
Oxic to anoxic

No diversity



#ggsave(here("simulations/expt2/figures/switching_novar.pdf"), width = 10)

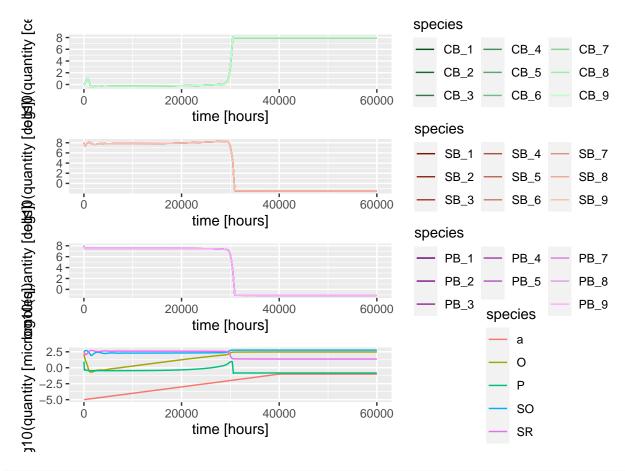
Maximum diversity



#ggsave(here("simulationsexpt2/figures/switching_highvar.pdf"), width = 10)

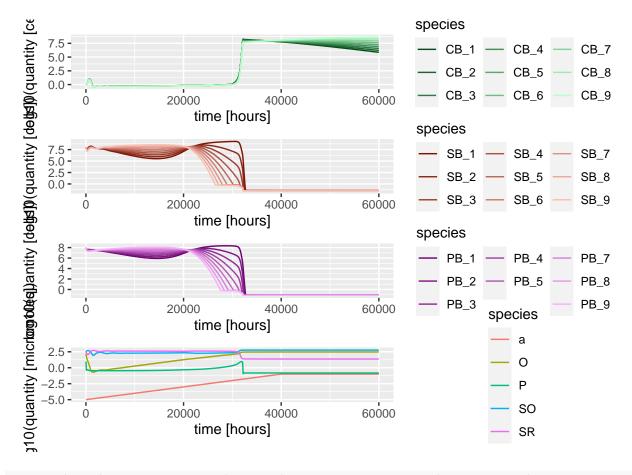
Anoxic to oxic

No diversity



#ggsave(here("simulations/expt2/figures/switching_novar.pdf"), width = 10)

Maximum diversity

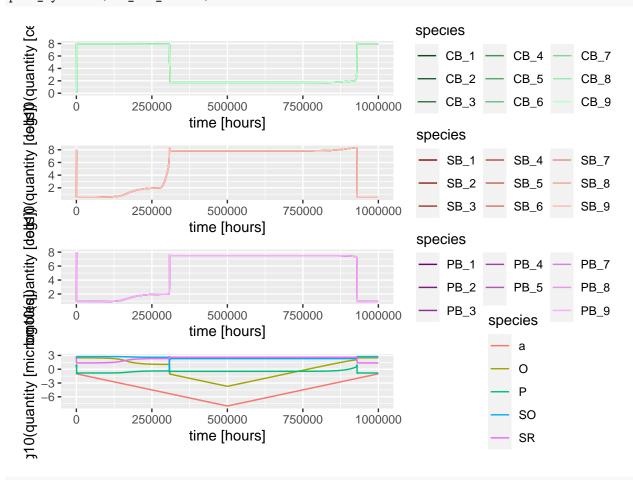


#ggsave(here("simulationsexpt2/figures/switching_highvar.pdf"), width = 10)

Anoxic to oxic to anoxic

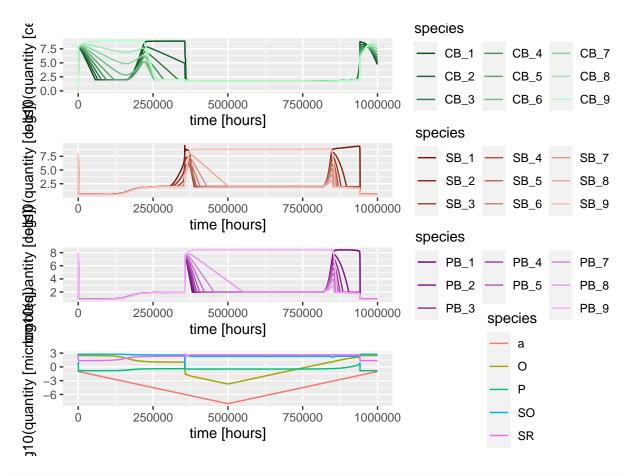
No diversity

sim_res_novar3 <- readRDS(here("experiments/experiment 1/data/sim_res_novar3.RDS"))
plot_dynamics(sim_res_novar3)</pre>



#ggsave(here("simulations/expt2/figures/switching_novar.pdf"), width = 10)

Maximum diversity



#qqsave(here("simulationsexpt2/figures/switching_highvar.pdf"), width = 10)

Visualise

```
visualise_temporal_env_eco()
```

Stable state finding

Finding

```
options(mc.cores = 12)

default_sim_duration <- 1000000
ssfind_minimum_abundances <- rep(0, 3)
names(ssfind_minimum_abundances) <- c("CB", "PB", "SB")
ssfind_simulation_duration <- default_sim_duration
ssfind_simulation_sampling_interval <- ssfind_simulation_duration
ssfind_event_interval <- ssfind_simulation_duration
grid_num_a <- 1000 #usually 1000 ## number of a_0 values
a_0s <- 10^seq(-7, -0.5, length=grid_num_a) ## sequence of a_0 values</pre>
```

Run stable state finding

*Careful, this simulation takes about 600 hours on a single core

```
var_expt <- run_ss_var_experiment()
saveRDS(var_expt, here("experiments/experiment 1/data/ss_data_1e6_x2x6_factorial.RDS"))</pre>
```

Process the stable state data

Bring in various stable state datasets

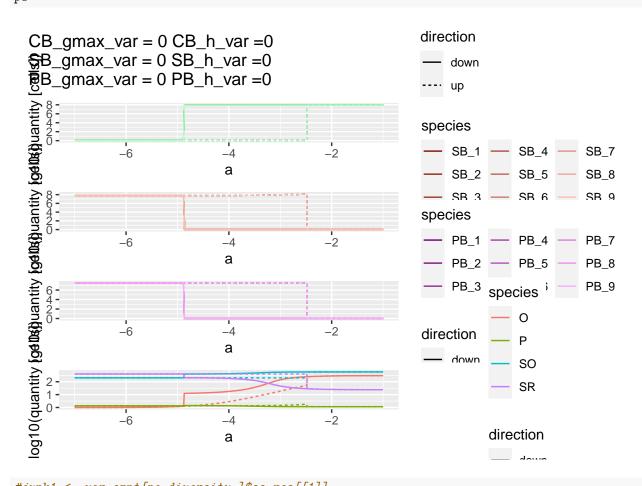
```
## sim length 80'000, 20 x 20 factorial, reference maximum diversity
var_expt1 <- readRDS(here("experiments/experiment 1/data/ss_data_80000.RDS")) %>%
  mutate(sim length = 80000)
stab_data1 <- var_expt1 %>%
  group_by(CB_var_gmax_s, CB_var_h_s,
           SB_var_gmax_s, SB_var_h_s,
           PB_var_gmax_s, PB_var_h_s, sim_length) %>%
  do(stability_measures = get_stability_measures(.$ss_res[[1]]))
stab_data1 <- unnest(stab_data1, cols = c(stability_measures))</pre>
saveRDS(stab_data1, here("experiments/experiment 1/data/stab_data_80000.RDS"))
## sim length 1'000'000, 20 x 20 factorial, reference maximum diversity
var expt2 <- readRDS(here("experiments/experiment 1/data/ss data 1000000 20factorial.RDS")) %>%
 mutate(sim_length = 1000000)
stab_data2 <- var_expt2 %>%
  group_by(CB_var_gmax_s, CB_var_h_s,
           SB_var_gmax_s, SB_var_h_s,
           PB_var_gmax_s, PB_var_h_s, sim_length) %>%
  do(stability_measures = get_stability_measures(.$ss_res[[1]]))
stab_data2 <- unnest(stab_data2, cols = c(stability_measures))</pre>
saveRDS(stab_data2, here("experiments/experiment 1/data/stab_data_1000000_20factorial.RDS"))
## sim length 1'000'000, 20 SBPBgrad, 5x maximum diversity
var_expt3 <- readRDS(here("experiments/experiment 1/data/ss_data_1e6_noCB_5xSBPB_.RDS")) %>%
 mutate(sim length = 1000000)
stab_data3 <- var_expt3 %>%
  group_by(CB_var_gmax_s, CB_var_h_s,
           SB_var_gmax_s, SB_var_h_s,
           PB_var_gmax_s, PB_var_h_s, sim_length) %>%
  do(stability_measures = get_stability_measures(.$ss_res[[1]]))
```

```
stab_data3 <- unnest(stab_data3, cols = c(stability_measures))</pre>
saveRDS(stab_data3, here("experiments/experiment 1/data/stab_data_1e6_noCB_5xSBPB .RDS"))
## sim length 300'000, 20 SBPBgrad, reference maximum diversity
var_expt4 <- readRDS(here("experiments/experiment 1/data/ss_data_300000_small.RDS")) %>%
 mutate(sim_length = 300000)
stab data4 <- var expt4 %>%
  group_by(CB_var_gmax_s, CB_var_h_s,
           SB_var_gmax_s, SB_var_h_s,
           PB_var_gmax_s, PB_var_h_s, sim_length) %>%
 do(stability_measures = get_stability_measures(.$ss_res[[1]]))
stab_data4 <- unnest(stab_data4, cols = c(stability_measures))</pre>
saveRDS(stab_data4, here("experiments/experiment 1/data/stab_data_300000.RDS"))
## sim length 1'000'000, 20 SBPBgrad, 2xCB variation, 6xSBPB variation
var_expt5 <- readRDS(here("experiments/experiment 1/data/ss_data_1e6_x2x6_factorial.RDS")) %%</pre>
 mutate(sim_length = 1000000)
stab_data5 <- var_expt5 %>%
  group_by(CB_var_gmax_s, CB_var_h_s,
           SB_var_gmax_s, SB_var_h_s,
           PB_var_gmax_s, PB_var_h_s, sim_length) %>%
  do(stability_measures = get_stability_measures(.$ss_res[[1]]))
stab_data5 <- unnest(stab_data5, cols = c(stability_measures))</pre>
saveRDS(stab_data5, here("experiments/experiment 1/data/stab_data_1e6_x2x6_factorial.RDS"))
```

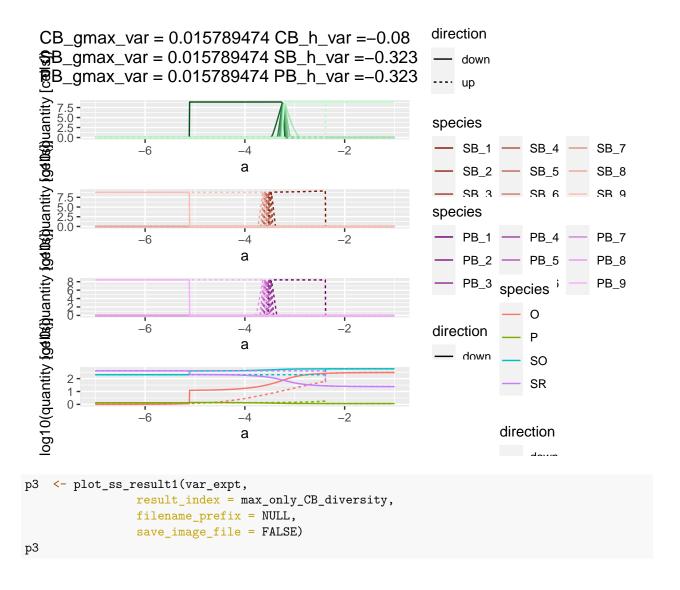
SS, no diversity, all diversity, CB only, and SBPB only

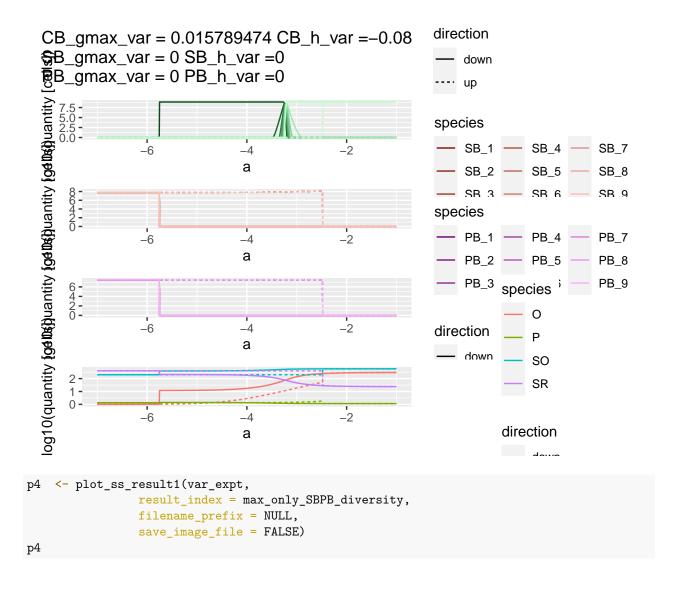
```
## find various combinations of diversity
var_expt <- readRDS(here("experiments/experiment 1/data/ss_data_1000000_20factorial.RDS"))</pre>
var_expt_levels <- var_expt[,1:6]</pre>
no_diversity <- which(rowSums(abs(var_expt_levels))==0)</pre>
max_diversty_all <- which(max(rowSums(abs(var_expt_levels))) ==</pre>
                             rowSums(abs(var_expt_levels)))
max_only_CB_diversity <- which(max(rowSums(abs(var_expt_levels[,1:2]))) ==</pre>
                             rowSums(abs(var_expt_levels[,1:2])) &
                               rowSums(abs(var expt levels[,3:6]))==0)
#var_expt_levels[381,]
max_only_SBPB_diversity <- which(max(rowSums(abs(var_expt_levels[,3:6]))) ==</pre>
                             rowSums(abs(var expt levels[,3:6])) &
                               rowSums(abs(var_expt_levels[,1:2]))==0)
#var_expt_levels[20,]
p1 <- plot_ss_result1(var_expt,</pre>
                result_index = no_diversity,
                 filename prefix = NULL,
                 save_image_file = FALSE)
```

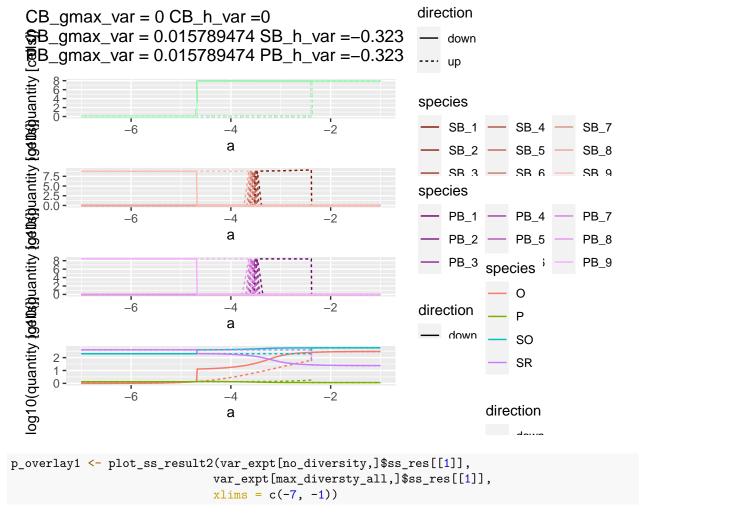
p1



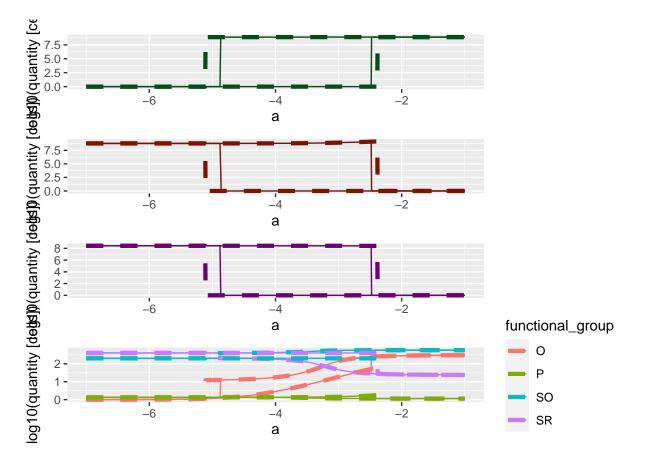
#junk1 <- var_expt[no_diversity,]\$ss_res[[1]]</pre>



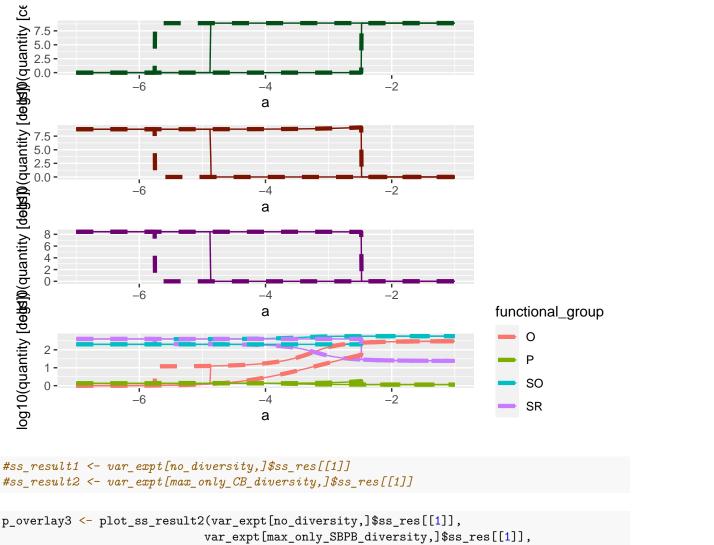




```
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
```

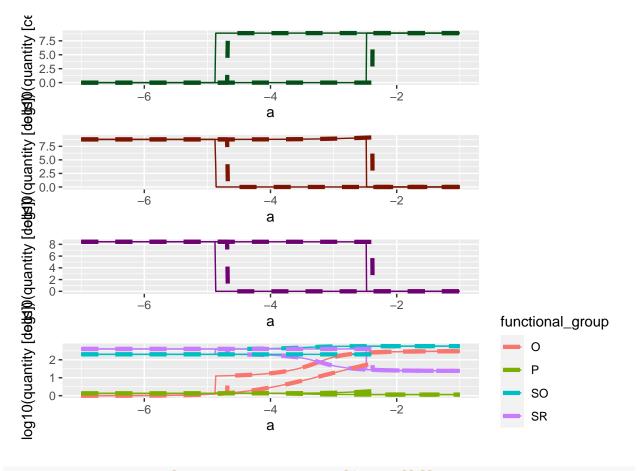


```
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
```



```
p_overlay3 <- plot_ss_result2(var_expt[no_diversity,]$ss_res[[1]],</pre>
                               xlims = c(-7, -1))
```

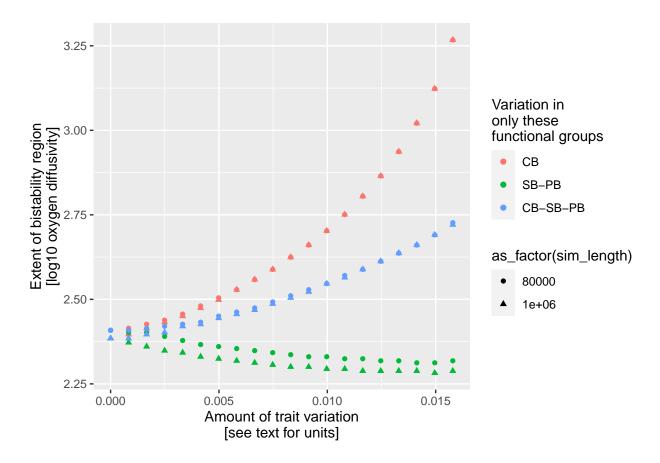
```
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
```



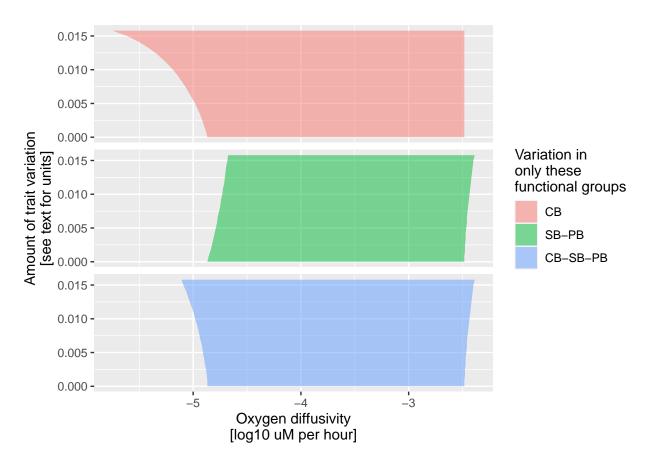
#ss_result3 <- var_expt[max_only_SBPB_diversity,]\$ss_res[[1]]</pre>

Look at stability measures

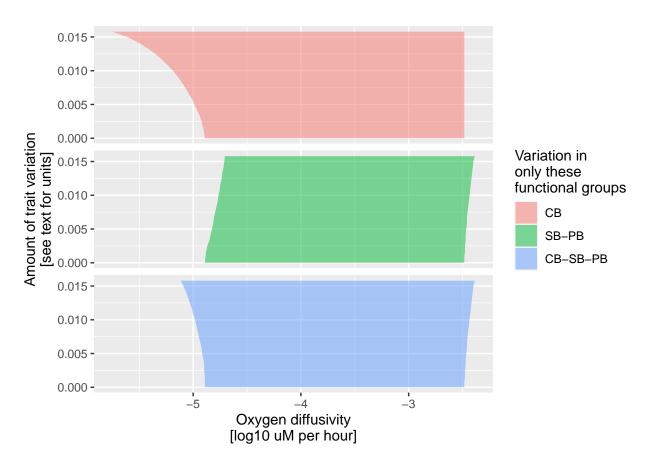
```
CBSBPB_stab_data <- stab_data %>%
  right_join(for_join) %>%
  mutate(var_treat = "CB-SB-PB",
         var_gmax = CB_var_gmax_s)
## Joining, by = c("CB_var_gmax_s", "SB_var_gmax_s")
all_stab_results <- CB_stab_data %>%
 bind rows(SBPB stab data) %>%
# bind_rows(results3) %>%
# bind rows(results4) %>%
 bind_rows(CBSBPB_stab_data)
all_stab_results<- all_stab_results %>%
   mutate(var_treat = forcats::fct_relevel(var_treat, levels = c("CB", "SB-PB", "CB-SB-PB")))
## Warning: Outer names are only allowed for unnamed scalar atomic inputs
#saveRDS(all_stab_results, here("experiments/experiment summary/all_stab.RDS"))
#all_stab_results <- readRDS(here("experiments/experiment summary/all_stab.RDS"))</pre>
all_stab_results %>%
 filter(Species == "0") %>%
 ggplot(aes(x = var_gmax, y = hyst_range, col=var_treat, shape = as_factor(sim_length))) +
 geom_point() +
  xlab("Amount of trait variation\n[see text for units]") +
  ylab("Extent of bistability region\n[log10 oxygen diffusivity]") +
  labs(col = "Variation in\nonly these\nfunctional groups")
```

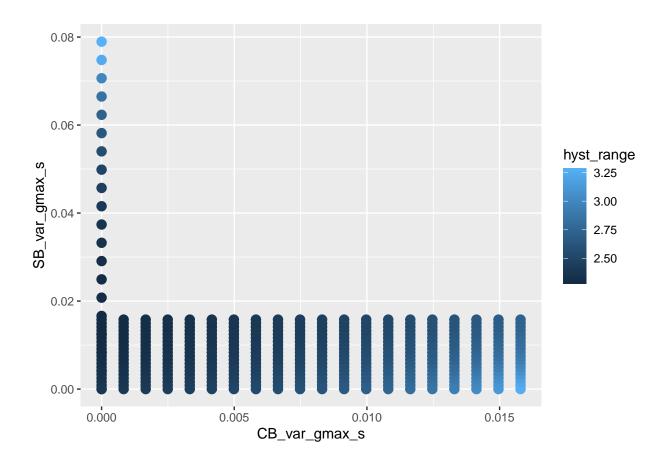


```
##ggsave("manuscript/figures/extent_of_bistab1.pdf", height = 4)
all_stab_results %>%
  #filter(var_treat == "CB") %>%
  filter(Species == "0",
         sim_length == 1e6) %>%
  ggplot(aes(x = var_gmax,
             ymin = hyst_min,
             ymax = hyst_max,
            fill=var_treat)) +
  geom_ribbon(alpha = 0.5) +
  facet_wrap( ~ var_treat, nrow = 3) +
  xlab("Amount of trait variation\n[see text for units]") +
  ylab("Oxygen diffusivity\n[log10 uM per hour]") +
  labs(fill = "Variation in\nonly these\nfunctional groups") +
  coord_flip() +
  theme(
    strip.background = element_blank(),
    strip.text.x = element_blank()
```

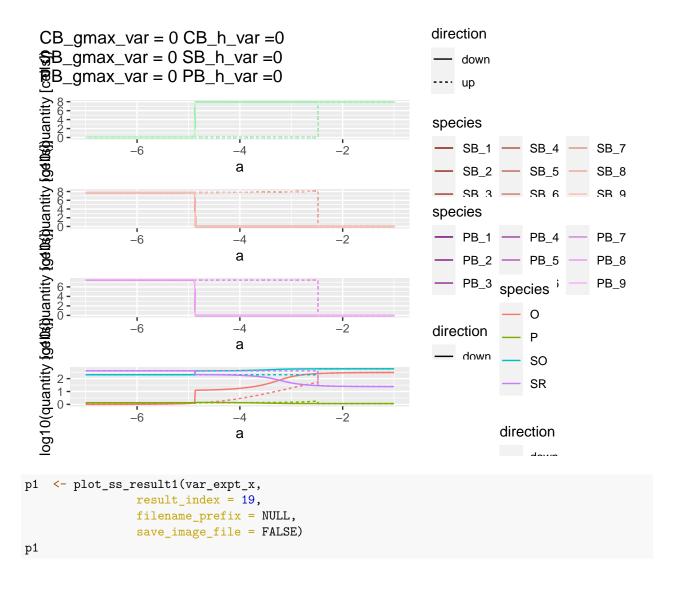


```
all_stab_results %>%
  #filter(var_treat == "CB") %>%
  filter(Species == "0",
         sim_length == 8e4) \%%
  ggplot(aes(x = var_gmax,
            ymin = hyst_min,
             ymax = hyst_max,
             fill=var_treat)) +
  geom_ribbon(alpha = 0.5) +
 facet_wrap( ~ var_treat, nrow = 3) +
 xlab("Amount of trait variation \n[see text for units]") +
  ylab("Oxygen diffusivity\n[log10 uM per hour]") +
  labs(fill = "Variation in\nonly these\nfunctional groups") +
  coord_flip() +
 theme(
    strip.background = element_blank(),
   strip.text.x = element_blank()
```

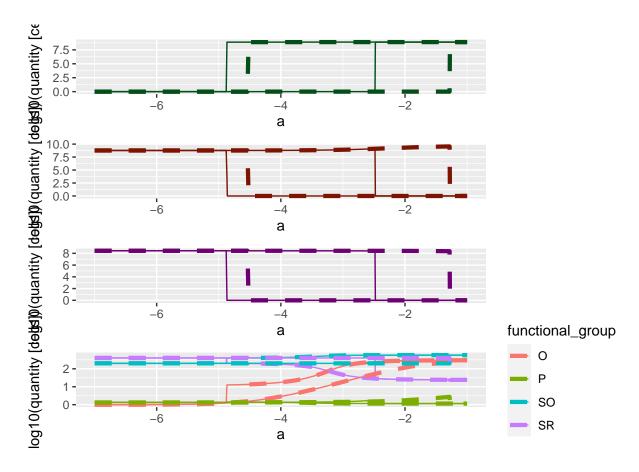




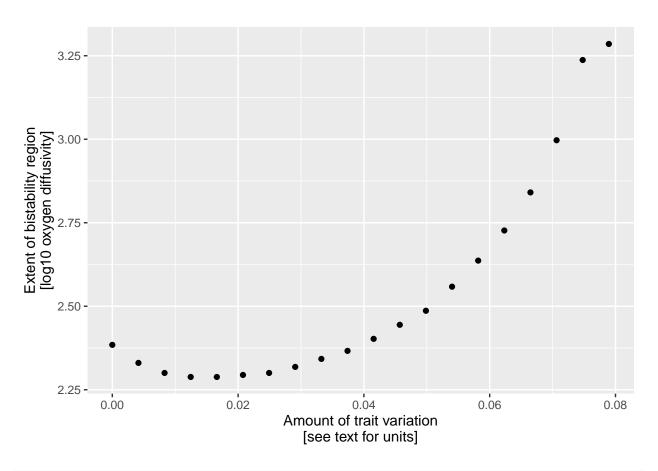
Extra SBPB diversity

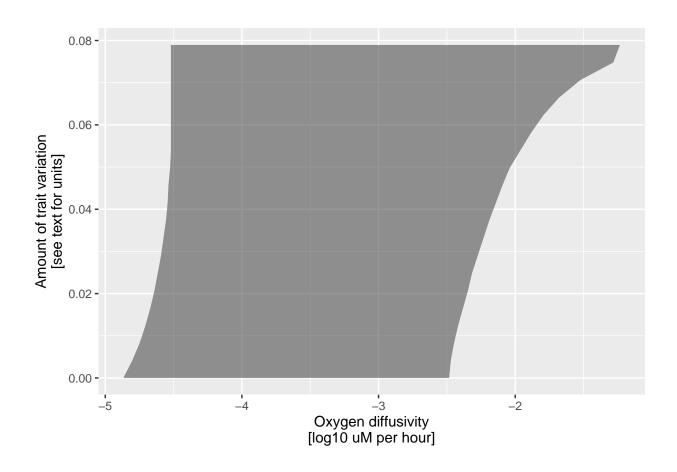


```
direction
  CB_gmax_var = 0 CB_h_var =0
  $B_gmax_var = 0.0747922452631579 SB_h_var = -1.56wn
  BB_gmax_var = 0.0747922452631579 PB_h_var =-1.53
 log10(quantity {gd0k}}uantity {gd0k}}uantity {
                                                              species
                                                              — SB_1 — SB_4 —
                                                                                      SB_7
                  -6
                                                -2
                                 а
                                                                          - SB_5
                                                                                      SB<sub>8</sub>
                                                                  SB 3 -
                                                                          - SB 6
                                                                                      SR 9
                                                              species
                                                                 PB_1
                                                                          - PB_4
                                                                                      PB_7
                  -6
                                               -2
                                 а
                                                                  PB_2
                                                                                      PB_8
                                                                            PB_5
                                                                  PB_3
                                                                                      PB_9
                                                                        species ;
                                                -2
                  -6
                                                              direction
                                 а
                                                                down
                                                                            SO
                                                                            SR
                  -6
                                               -
2
                                 -4
                                                                        direction
                                 а
p_overlay1 <- plot_ss_result2(var_expt_x[1,]$ss_res[[1]],</pre>
                              var_expt_x[19,]$ss_res[[1]],
                              xlims = c(-7, -1))
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
```

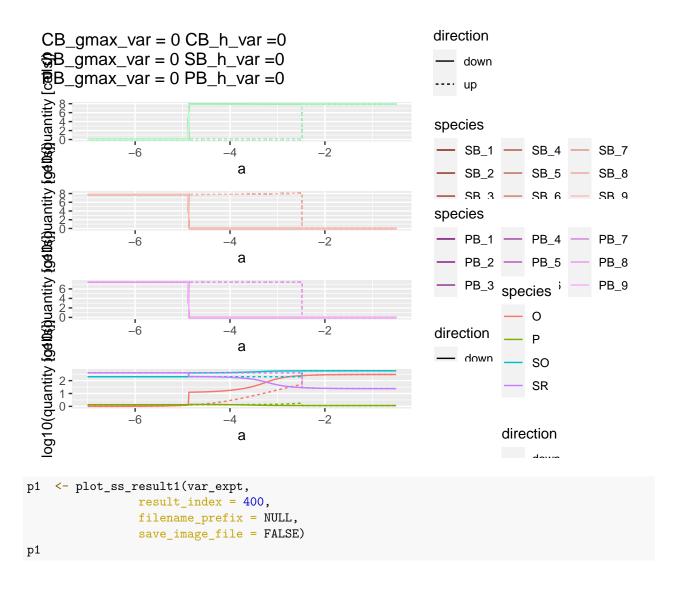


```
stab_data_x %>%
  filter(Species == "0") %>%
  ggplot(aes(x = SB_var_gmax_s, y = hyst_range)) +
  geom_point() +
  xlab("Amount of trait variation\n[see text for units]") +
  ylab("Extent of bistability region\n[log10 oxygen diffusivity]") +
  labs(col = "Variation in\nonly these\nfunctional groups")
```

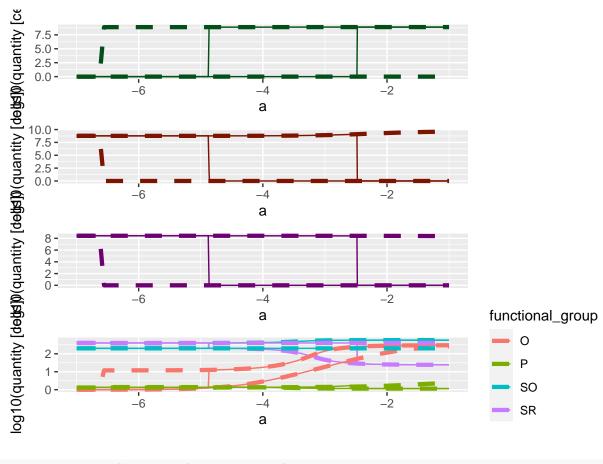




2x CB, 6xSBPB diversity



```
direction
  CB_gmax_var = 0.031578948 CB_h_var = -0.16
  $B_gmax_var = 0.094736844 SB_h_var =-1.938
                                                                down
  B_gmax_var = 0.094736844 PB_h_var =-1.938
  log10(quantity {ge/0k})uantity {ge/0k})uantity {ge/0k}
     7.5 - 5.0 - 2.5 - 0.0 -
                                                              species
                                                                SB_1 — SB_4 —
                                                                                       SB 7
                 -6
                               -4
                                             -2
                                                                           - SB_5
                                                                                        SB<sub>8</sub>
                                                                   SB 3 -
                                                                           - SB 6
                                                                                       SR 9
                                                              species
                                                                  PB_1
                                                                             PB_4
                                                                                       PB 7
                 -6
                                             -2
                               -4
                                 а
                                                                   PB 2
                                                                             PB 5
                                                                                        PB 8
                                                                                        PB<sub>9</sub>
                                                                   PB_3
                                                                         species '
                  -6
                                             -2
                                                              direction
                                 а
                                                                 down
                                                                             SO
                                                                             SR
                  -6
                                -4
                                             -2
                                                                         direction
                                 а
p_overlay1 <- plot_ss_result2(var_expt[1,]$ss_res[[1]],</pre>
                               var_expt[400,]$ss_res[[1]],
                               xlims = c(-7, -1))
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
## 'summarise()' has grouped output by 'a', 'direction', 'var_type'. You can override using the '.group
p_overlay1
## Warning: Removed 154 row(s) containing missing values (geom_path).
## Warning: Removed 154 row(s) containing missing values (geom_path).
## Warning: Removed 154 row(s) containing missing values (geom_path).
## Warning: Removed 154 row(s) containing missing values (geom_path).
## Warning: Removed 154 row(s) containing missing values (geom_path).
## Warning: Removed 154 row(s) containing missing values (geom_path).
## Warning: Removed 616 row(s) containing missing values (geom_path).
## Warning: Removed 616 row(s) containing missing values (geom_path).
```



```
CB_vars <- unique(stab_data$CB_var_gmax_s)</pre>
SB_vars <- unique(stab_data$SB_var_gmax_s)</pre>
CB_stab_data <- stab_data %>%
  filter(SB_var_gmax_s == 0) %>%
  mutate(var_treat = "CB",
         var_gmax = CB_var_gmax_s)
SBPB_stab_data <- stab_data %>%
  filter(CB_var_gmax_s == 0) %>%
  mutate(var_treat = "SB-PB",
         var_gmax = SB_var_gmax_s)
for_join <- tibble(CB_var_gmax_s = CB_vars,</pre>
                      SB_var_gmax_s = SB_vars)
CBSBPB_stab_data <- stab_data %>%
  right_join(for_join) %>%
  mutate(var_treat = "CB-SB-PB",
         var_gmax = CB_var_gmax_s)
```

Joining, by = c("CB_var_gmax_s", "SB_var_gmax_s")

```
# bind_rows(results4) %>%
bind_rows(CBSBPB_stab_data)

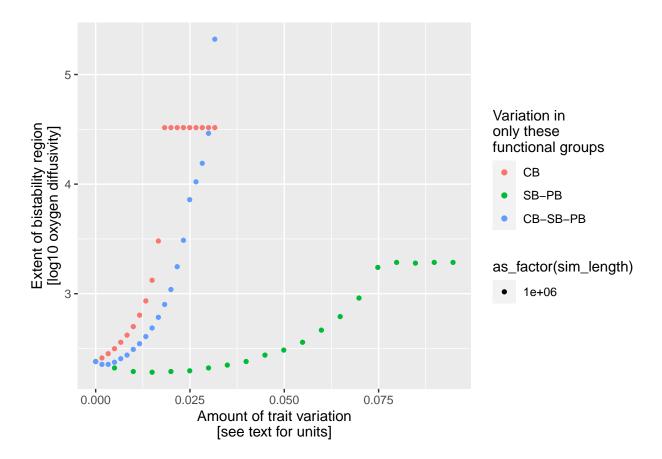
all_stab_results<- all_stab_results %>%
    mutate(var_treat = forcats::fct_relevel(var_treat, levels = c("CB", "SB-PB", "CB-SB-PB")))
```

Warning: Outer names are only allowed for unnamed scalar atomic inputs

```
#saveRDS(all_stab_results, here("experiments/experiment summary/all_stab.RDS"))

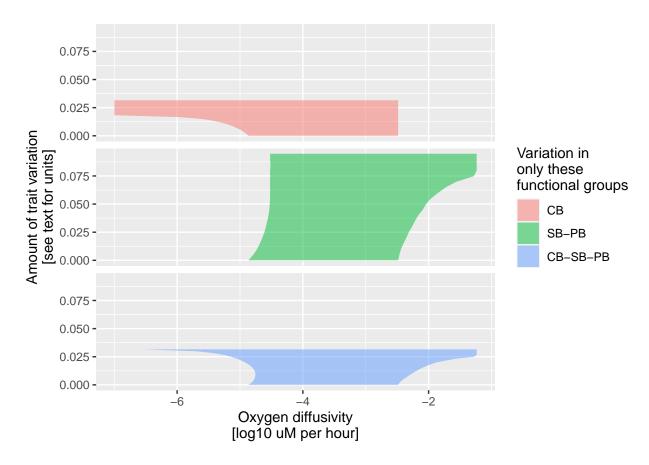
#all_stab_results <- readRDS(here("experiments/experiment summary/all_stab.RDS"))

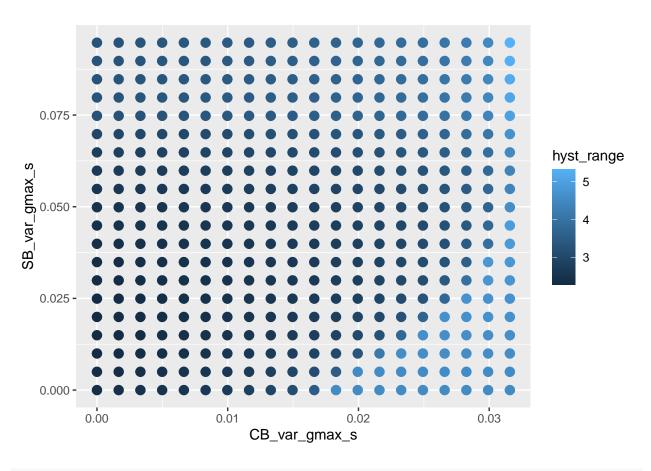
all_stab_results %>%
   filter(Species == "0") %>%
   ggplot(aes(x = var_gmax, y = hyst_range, col=var_treat, shape = as_factor(sim_length))) +
   geom_point() +
   xlab("Amount of trait variation\n[see text for units]") +
   ylab("Extent of bistability region\n[log10 oxygen diffusivity]") +
   labs(col = "Variation in\nonly these\nfunctional groups")
```

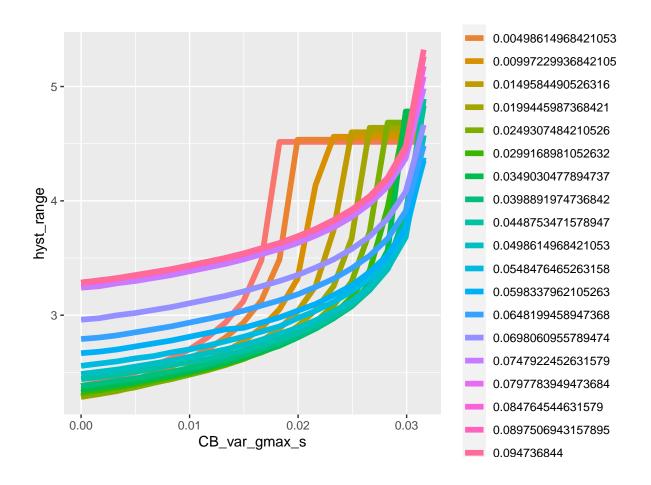


```
##ggsave("manuscript/figures/extent_of_bistab1.pdf", height = 4)
all_stab_results %>%
```

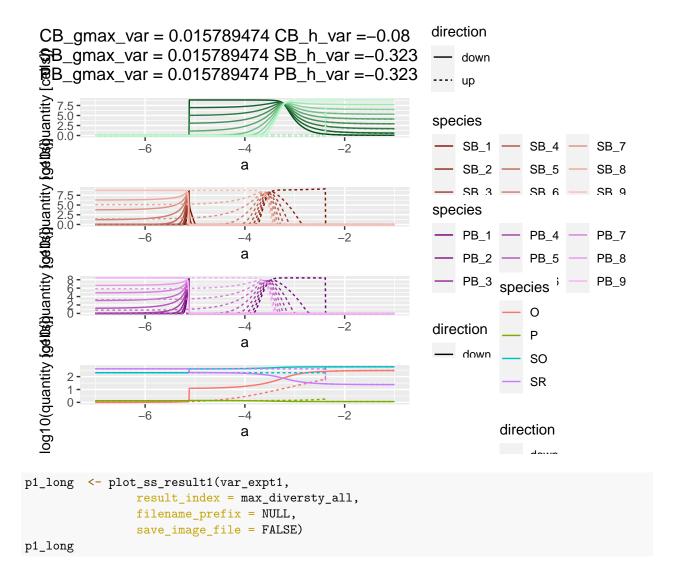
```
#filter(var_treat == "CB") %>%
filter(Species == "0",
       sim_length == 1e6) %>%
ggplot(aes(x = var_gmax,
           ymin = hyst_min,
           ymax = hyst_max,
           fill=var_treat)) +
geom_ribbon(alpha = 0.5) +
facet_wrap( ~ var_treat, nrow = 3) +
xlab("Amount of trait variation\n[see text for units]") +
ylab("Oxygen diffusivity\n[log10 uM per hour]") +
labs(fill = "Variation in\nonly these\nfunctional groups") +
coord_flip() +
theme(
  strip.background = element_blank(),
  strip.text.x = element_blank()
```

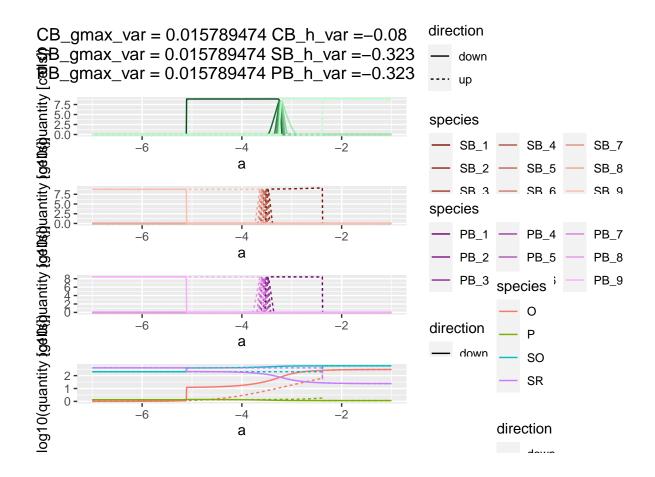






What effect of changing the length of the simulations

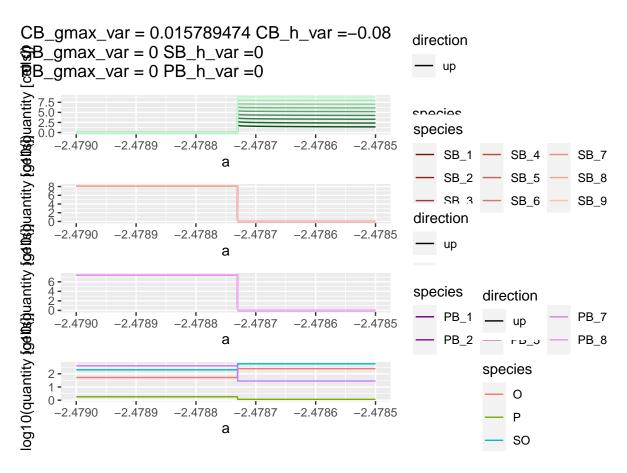




Zoom in on SS

```
a_0s <- 10^seq(-2.479, -2.4785, length=grid_num_a) ## sequence of a_0 values
initial_CBs <- 1#10^seq(0, 0, length=grid_num_N) ## sequence of N values
initial_PBs <- 1e8 ## not varied</pre>
initial_SBs <- 1e8 ## not varied</pre>
# next line creates all possible combinations
ss_expt <- expand.grid(N_CB = initial_CBs,</pre>
                       N_PB = initial_PBs,
                       N_SB = initial_SBs,
                       a_0 = a_0s
var_expt_master <- var_expt</pre>
var_expt <- var_expt_master[381,]</pre>
#var_expt <- run_ss_var_experiment()</pre>
#saveRDS(var_expt, here("experiments/experiment 1/data/ss_data_zoom.RDS"))
library(here)
zoom <- readRDS(here("experiments/experiment 1/data/ss_data_zoom.RDS"))</pre>
p1 <- plot_ss_result1(zoom,</pre>
                 result_index = 1,
```

```
filename_prefix = NULL,
    save_image_file = FALSE)
p1
```



Negative abundance investigation

I (Owen) found that the sampling interval had an effect on the stability of the simulation. If the sampling interval was long, then in some rare cases (see below) the odesolver failed, with negative abundances occurring. I think this is due to abundances becoming very small, and then the computer having trouble with precision. I guess that when a sample is taken, the abundance is somehow altered if it is very low, probably by some rounding.

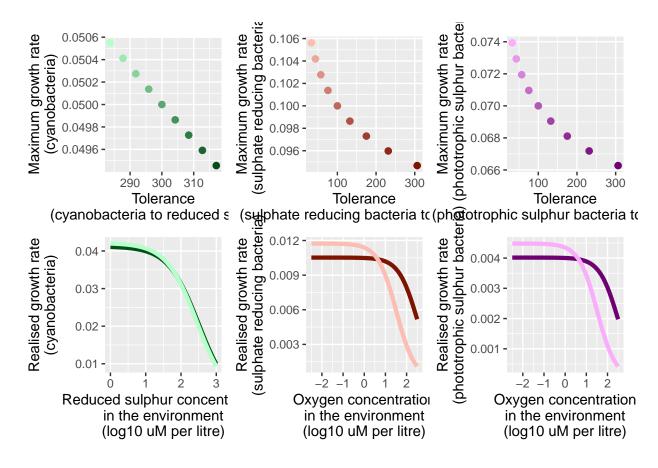
```
var_expt$pars[[1]]
dd <- var_expt$ss_res[[1]]
dd1 <- filter(dd, PB_1<(-0.0001))
dd1$a_0

ss_expt_master <- ss_expt
ss_expt <- ss_expt_master[abs(ss_expt_master$a_0 - 1.336984e-05)<1e-10,]

var_expt_master <- var_expt
#var_expt <- var_expt[1,]
var_expt_test <- run_ss_var_experiment()</pre>
```

```
res <- var_expt_test$ss_res[[1]]
test1 <- ss_by_a_N(ss_expt, var_expt$pars[[1]])</pre>
x \leftarrow ss expt[2,]
param <- var_expt$pars[[1]]</pre>
get_final_states_a_N(x, param)
ssfind_parameters <- param</pre>
ssfind simulation sampling interval <- 1000
## now run inside the function "get_final_states_a_N"
simres1 <- simres
ssfind_simulation_sampling_interval <- 5000
## now run inside the function "get_final_states_a_N"
simres2 <- simres # this fails</pre>
## now run inside the function "get_final_states_a_N"
plot_dynamics(simres2)
ggplot() +
  geom_line(data = simres1$result,
              mapping = aes(x = time, y = log10(PB_1))) +
  geom_point(data = simres2$result,
              mapping = aes(x = time, y = log10(PB_1))) +
  xlim(c(0, 250000))
ccc <- simres2$result</pre>
simres2$result$PB 1
simres2$result$time
log10_a <- log10(ss_expt$a_0[1]) ## very slowly goes anoxic</pre>
\#loq10_a \leftarrow loq10(a_0s[354]) \# very slowly goes anoxic
\#log10_a \leftarrow log10(a_0s[356]) \# very very very slowly goes anoxic
\#log10_a \leftarrow log10(a_0s[357]) \#\# does not go anoxic
default_dynamic_model <- bushplus_dynamic_model</pre>
default_event_definition <- event_definition_1</pre>
default_event_interval <- ssfind_simulation_duration</pre>
default_noise_sigma <- 0</pre>
default_minimum_abundances <- ssfind_minimum_abundances</pre>
default sim duration <- ssfind simulation duration
default_sim_sample_interval <- ssfind_simulation_duration</pre>
#initial_pars_from <- "bush_ssfig3"</pre>
default_log10a_series <- c(log10_a, log10_a)</pre>
initial_state <- new_initial_state(num_CB_strains,</pre>
                                      num_PB_strains,
                                      num_SB_strains,
                                      values = "bush_ssfig3")
initial_state[grep("CB_", names(initial_state))] <- 10^10/num_CB_strains
```

Understand about relative and absolute variation in traits



```
## [1] 0.03266455
```

[1] 0.01063672

[1] 0.004061293

With the CB diversity multiplier set at 1 and the SB/PB multiplier set at 5 the range of realised growth rates of CB is 0.0326645, range of SB is 0.0106367, and range of PB is 0.0040613.