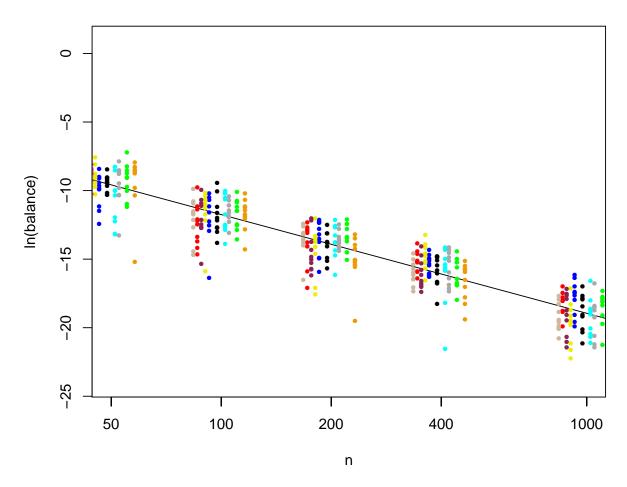
Simulation Result Report

Adam Kapelner

Sunday $15^{\rm th}$ February, 2015, 16:48

1 Results for each Run

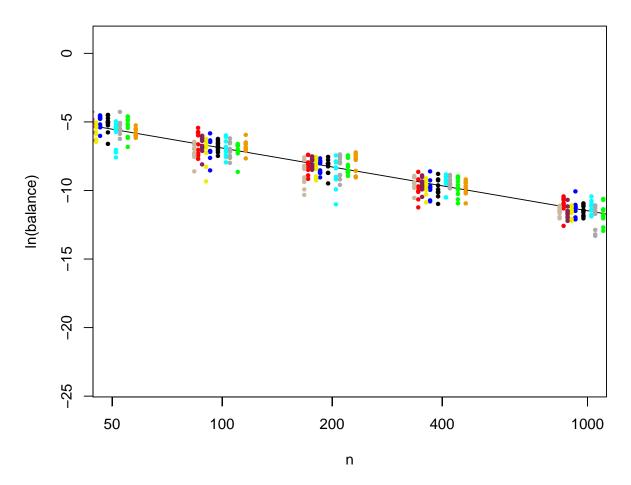
p = 1 max_iters = Inf



```
## p = 1 max iters = Inf
##
##
## examine log-log linear regression
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.648 0.32724 8.092 4.538e-15
```

```
## lnx -3.126 0.06011 -52.008 2.093e-203
## ensure log-law relationship
## Analysis of Variance Table
## Model 1: lny ~ poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 983
## 2 495 970 3 12.5 2.12 0.096 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 983
## 2 489 942 9 40.6 2.34 0.014 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 983
## 2 480 879 18 104 3.17 1.4e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

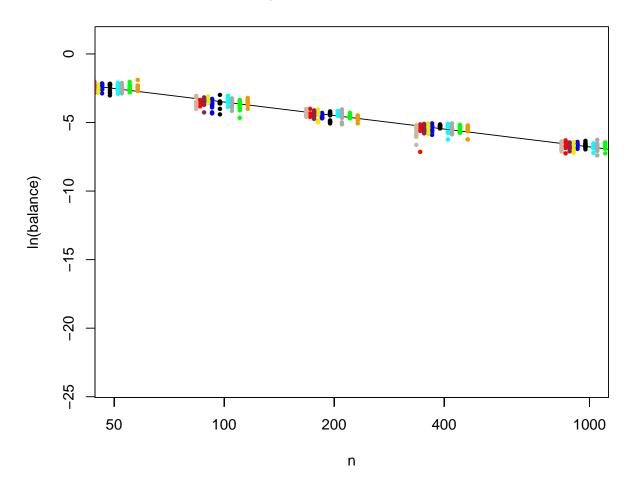
p = 2 max_iters = Inf



```
## p = 2 \max iters = Inf
##
##
## examine log-log linear regression
              Estimate Std. Error t value Pr(>|t|)
                        0.1476 15.18 4.707e-43
## (Intercept)
                 2.240
                           0.0271 -73.27 6.995e-269
                -1.986
## ensure log-law relationship
## Analysis of Variance Table
##
## Model 1: lny \sim poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
  Res.Df RSS Df Sum of Sq F Pr(>F)
## 1
       498 200
       495 199 3
                      0.553 0.46 0.71
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny \sim lnx
```

```
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1    498 200
## 2    489 195 9    4.56 1.27    0.25
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1    498 200
## 2    480 188 18    12.2 1.73    0.031 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

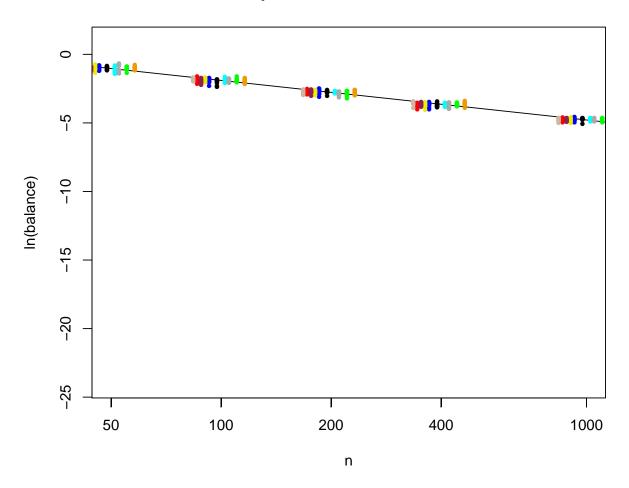
p = 5 max_iters = Inf



```
## p = 5 max iters = Inf
##
##
## examine log-log linear regression
## Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept) 3.041 0.06357 47.84 2.432e-188
## lnx -1.421 0.01168 -121.74 0.000e+00
## ensure log-law relationship
## Analysis of Variance Table
##
## Model 1: lny \sim poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 37.1
## 2 495 35.8 3 1.32 6.07 0.00046 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny \sim lnx
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 37.1
## 2 489 36.2 9 0.853 1.28 0.25
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 37.1
## 2 480 35.6 18 1.46 1.09 0.36
```

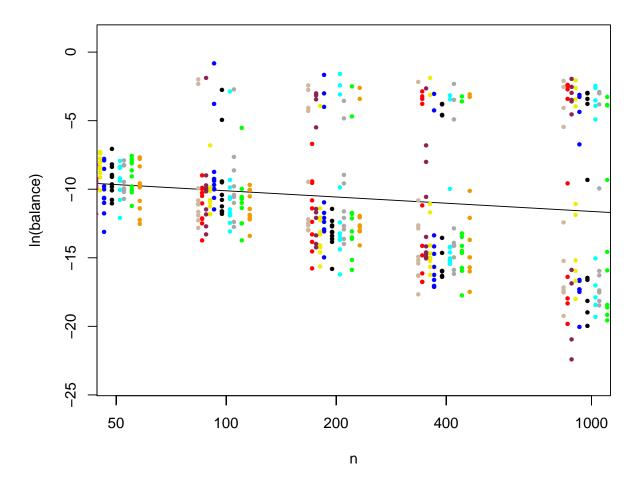
p = 10 max_iters = Inf



```
## p = 10 \max iters = Inf
##
##
## examine log-log linear regression
              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 3.864 0.032841
                                   117.7
                -1.252
                        0.006032 -207.6
## ensure log-law relationship
## Analysis of Variance Table
##
## Model 1: lny \sim poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
   Res.Df RSS Df Sum of Sq
                                F Pr(>F)
## 1
       498 9.90
       495 9.81 3
                      0.0948 1.59
                                   0.19
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny \sim lnx
```

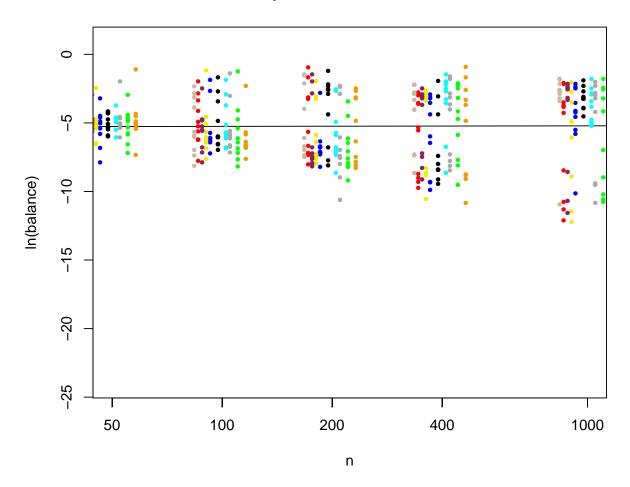
```
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 9.90
## 2 489 9.68 9 0.224 1.26 0.26
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 9.90
## 2 480 9.53 18 0.367 1.03 0.43
```

p = 1 max_iters = 2



```
## ensure log-law relationship
## Analysis of Variance Table
## Model 1: lny ~ poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 10316
## 2 495 10163 3 153 2.48 0.06 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 10316
## 2 489 10260 9 56.6 0.3 0.97
## Analysis of Variance Table
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 10316
## 2 480 10135 18 182 0.48 0.97
```

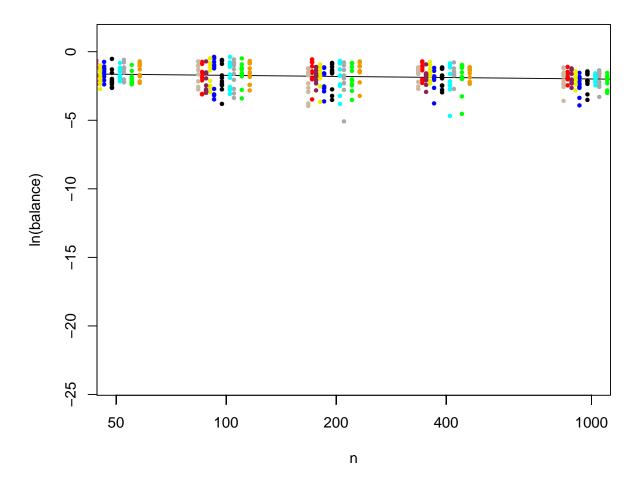
$p = 2 max_iters = 2$



```
## p = 2 \max iters = 2
##
##
## examine log-log linear regression
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.33102
                       0.5592 -9.5338 6.686e-20
                          0.1027 0.1653 8.687e-01
               0.01698
## ensure log-law relationship
## Analysis of Variance Table
##
## Model 1: lny \sim poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
  Res.Df RSS Df Sum of Sq F Pr(>F)
## 1
       498 2870
## 2
       495 2831 3
                     39.1 2.28 0.079 .
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## ensure no dataset effect
## Analysis of Variance Table
```

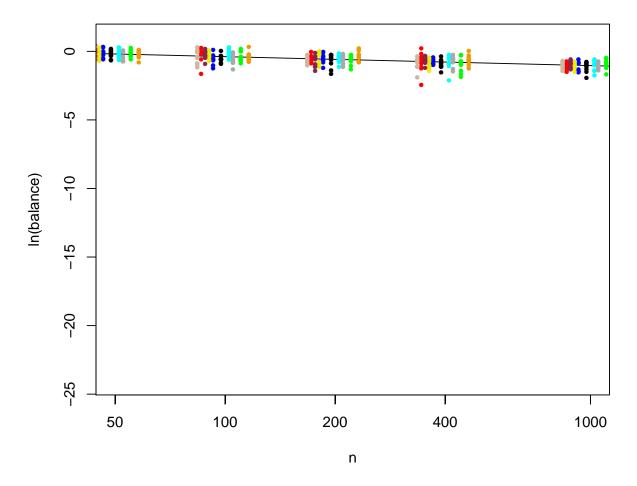
```
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
      498 2870
## 2
       489 2783 9
                    87.3 1.7 0.085 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Analysis of Variance Table
## Model 1: lny \sim lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1
     498 2870
      480 2697 18 173 1.71 0.034 *
## 2
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

$p = 5 max_iters = 2$



```
## p = 5 \max iters = 2
##
## examine log-log linear regression
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) -1.1958 0.17517 -6.827 2.537e-11
## lnx -0.1145 0.03218 -3.560 4.065e-04
## ensure log-law relationship
## Analysis of Variance Table
## Model 1: lny ~ poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 282
## 2 495 280 3 1.59 0.94 0.42
## ensure no dataset effect
## Analysis of Variance Table
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 282
## 2 489 273 9 8.21 1.63 0.1
## Analysis of Variance Table
## Model 1: lny \sim lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 282
## 2 480 270 18 11.9 1.18 0.27
```

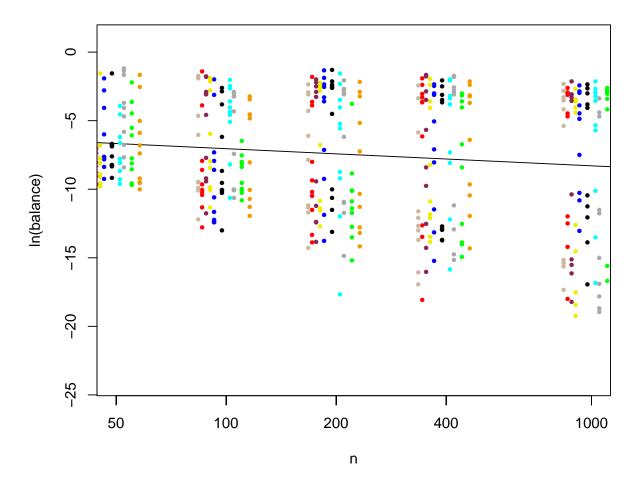
p = 10 max_iters = 2



```
## p = 10 \max iters = 2
##
##
## examine log-log linear regression
              Estimate Std. Error t value Pr(>|t|)
                        0.08125 11.34 1.141e-26
## (Intercept)
               0.9213
                          0.01492 -19.02 4.686e-61
               -0.2839
## ensure log-law relationship
## Analysis of Variance Table
##
## Model 1: lny \sim poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
   Res.Df RSS Df Sum of Sq
                              F Pr(>F)
## 1
       498 60.6
       495 60.5 3
                       0.123 0.34
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny \sim lnx
```

```
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 60.6
## 2 489 59.3 9 1.24 1.14 0.33
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 60.6
## 2 480 58.6 18 2.02 0.92 0.55
```

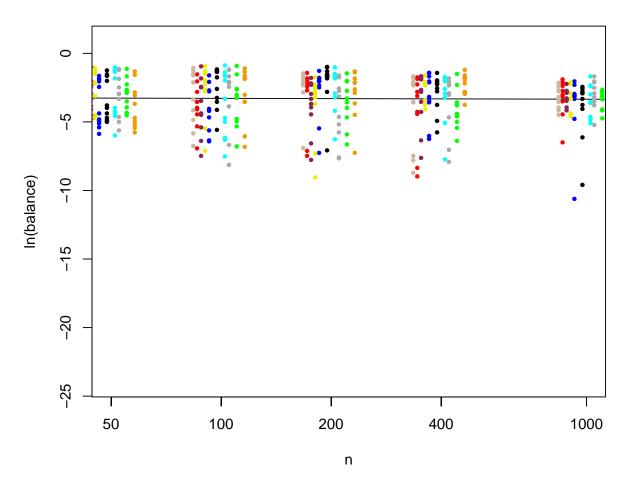
p = 1 max_iters = 1



```
## p = 1 max iters = 1
##
##
## examine log-log linear regression
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) -4.542    1.045 -4.345 1.692e-05
## lnx    -0.543    0.192 -2.828 4.879e-03
```

```
## ensure log-law relationship
## Analysis of Variance Table
## Model 1: lny ~ poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 10032
## 2 495 10028 3 4.01 0.07 0.98
## ensure no dataset effect
## Analysis of Variance Table
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 10032
## 2 489 9914 9 118 0.65 0.76
## Analysis of Variance Table
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 10032
## 2 480 9616 18 416 1.15 0.3
```

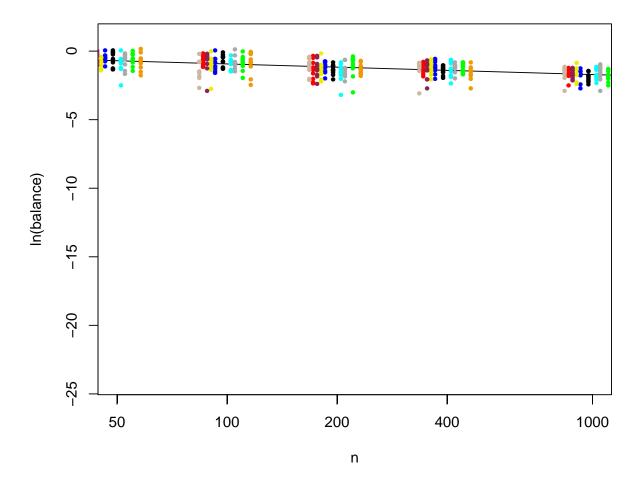
p = 2 max_iters = 1



```
## p = 2 \max iters = 1
##
##
## examine log-log linear regression
              Estimate Std. Error t value Pr(>|t|)
                        0.40802 -7.7452 5.383e-14
## (Intercept) -3.16015
               -0.02654
                          0.07494 -0.3541 7.234e-01
## ensure log-law relationship
## Analysis of Variance Table
##
## Model 1: lny \tilde{} poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
  Res.Df RSS Df Sum of Sq
                               F Pr(>F)
## 1
       498 1528
       495 1525 3
                         3.05 0.33
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny \sim lnx
```

```
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 1528
## 2 489 1506 9 21.6 0.78 0.64
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 1528
## 2 480 1489 18 39.3 0.7 0.81
```

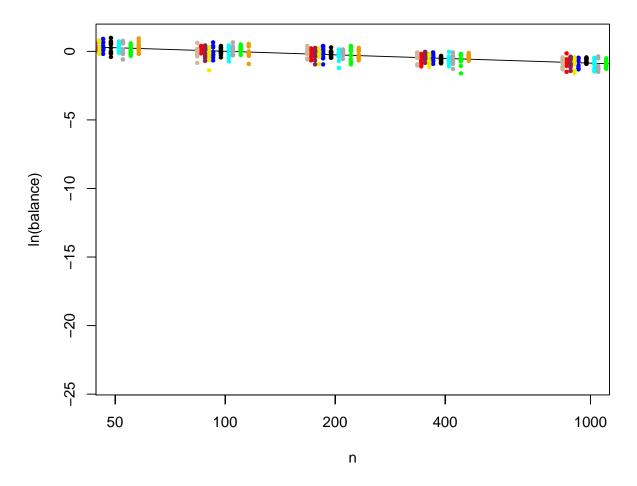
p = 5 max_iters = 1



```
## p = 5 max iters = 1
##
##
## examine log-log linear regression
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 0.6113 0.12485 4.896 1.322e-06
## lnx -0.3361 0.02293 -14.656 1.082e-40
```

```
## ensure log-law relationship
## Analysis of Variance Table
## Model 1: lny ~ poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 143
## 2 495 140 3 2.75 3.23 0.022 *
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 143
## 2 489 141 9 2.33 0.9 0.53
## Analysis of Variance Table
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1 498 143
## 2 480 137 18 6.27 1.22 0.24
```

p = 10 max_iters = 1



```
## p = 10 \max iters = 1
##
##
## examine log-log linear regression
              Estimate Std. Error t value Pr(>|t|)
                          0.07628 22.76 3.777e-79
## (Intercept)
               1.7364
                -0.3757
                          0.01401 -26.81 1.131e-98
## ensure log-law relationship
## Analysis of Variance Table
##
## Model 1: lny \sim poly(lnx, 1)
## Model 2: lny ~ poly(lnx, 4)
   Res.Df RSS Df Sum of Sq
                                F Pr(>F)
## 1
       498 53.4
       495 52.9 3
                       0.498 1.55
## ensure no dataset effect
## Analysis of Variance Table
##
## Model 1: lny \sim lnx
```

```
## Model 2: lny ~ lnx + dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1    498 53.4
## 2    489 52.1 9    1.35 1.41    0.18
## Analysis of Variance Table
##
## Model 1: lny ~ lnx
## Model 2: lny ~ lnx * dataset
## Res.Df RSS Df Sum of Sq F Pr(>F)
## 1    498 53.4
## 2    480 51.5 18    1.95 1.01    0.45
```

2 Multiple and Rate Results over all Runs

	p	max_iters	int	slope
1	1.0000	Inf	2.6479	-3.1261
2	2.0000	Inf	2.2401	-1.9860
3	5.0000	Inf	3.0409	-1.4215
4	10.0000	Inf	3.8644	-1.2522
5	1.0000	2.0000	-7.1018	-0.6540
6	2.0000	2.0000	-5.3310	0.0170
7	5.0000	2.0000	-1.1958	-0.1145
8	10.0000	2.0000	0.9213	-0.2839
9	1.0000	1.0000	-4.5420	-0.5430
10	2.0000	1.0000	-3.1601	-0.0265
11	5.0000	1.0000	0.6113	-0.3361
12	10.0000	1.0000	1.7364	-0.3757

