

BFS

DFS

- 1) BFS finds the shortest path to the destination.
 - 2) The full form of BFS is Breadth first search.
 - 3) It uses a queue to keep track of the next location to visit.
 - 4) BFS traverse according to tree level.
 - 5) It is implemented using FIFO list.
 - 6) It requires more memory as compare to DFS.
 - 7) This algorithm gives the shallowest path solution.
 - 8) There is no need to backtracking in BFS.
 - 9) You can never be trapped into infinite loop.
- 1) DFS goes to the bottom of a subtree, then back tracks.
 - 2) The full form of DFS is Depth First search.
 - 3) It uses a stack to keep track of the next location to visit.
 - 4) DFS traverses according to tree depth.
 - 5) It is implemented using LIFO list.
 - 6) It require less memory as compare to BFS.
 - 7) This algorithm doesn't guarantee the shallowest path solⁿ.
 - 8) There is need of backtracking in DFS.
 - 9) You can be trapped into infinite loops.

1) If you do not find any goal, you may need to expand many nodes before the solⁿ is found.

2) If you do not find any goal the leaf node backtracking may occur.

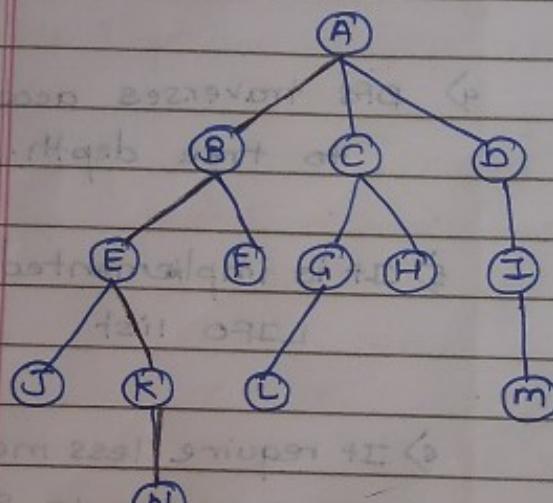
Q 2 Uninformed Search -

Q 2 a) Breadth First Search -

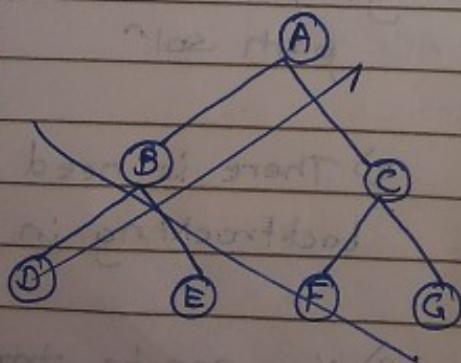
- uninformed search technique.

- It uses FIFO method

- It moves level by level



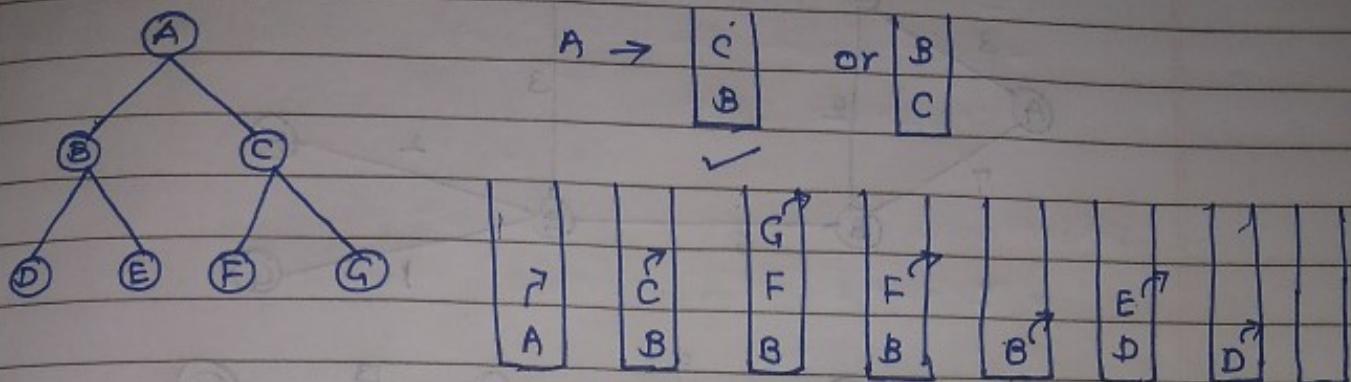
A
A
BCD
CDEF
CDEFGH
CEFGHI
FGHIJK
GHIJK
HIJKL
IJKL
IJKLM
JKLM
KLM
KMN
MN
N



A	C	G
B	F	B

② Depth First Search

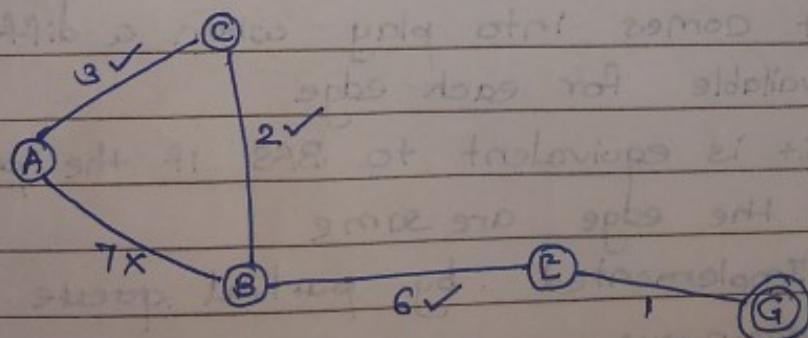
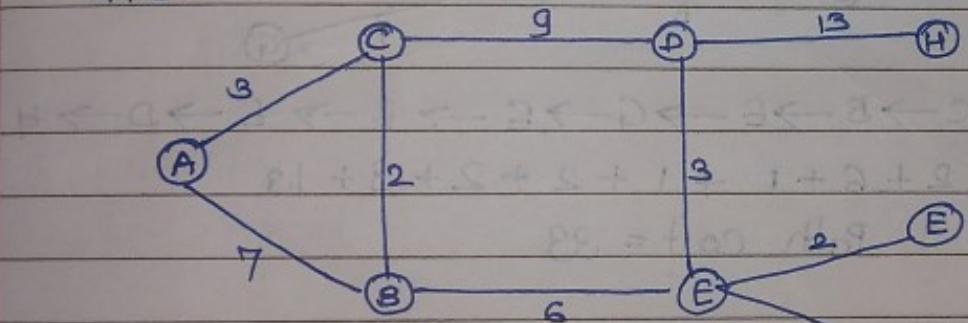
Ex.



Final path = ACGFBED

③ Uniform Cost Search

Ex 1 -

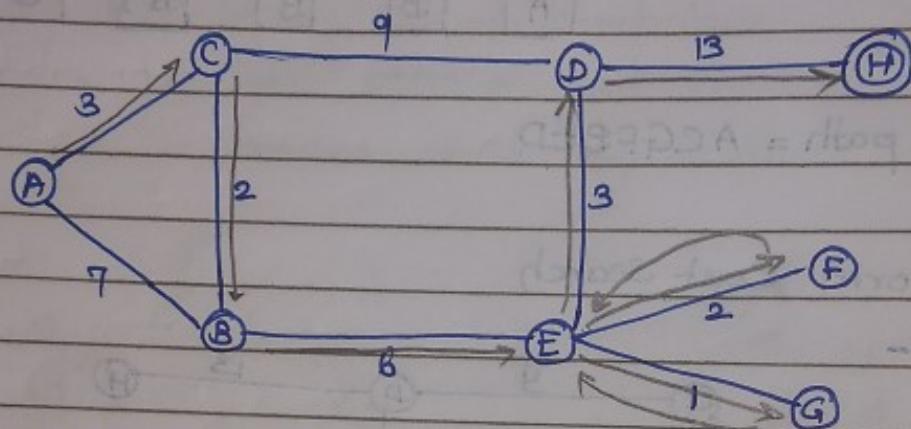
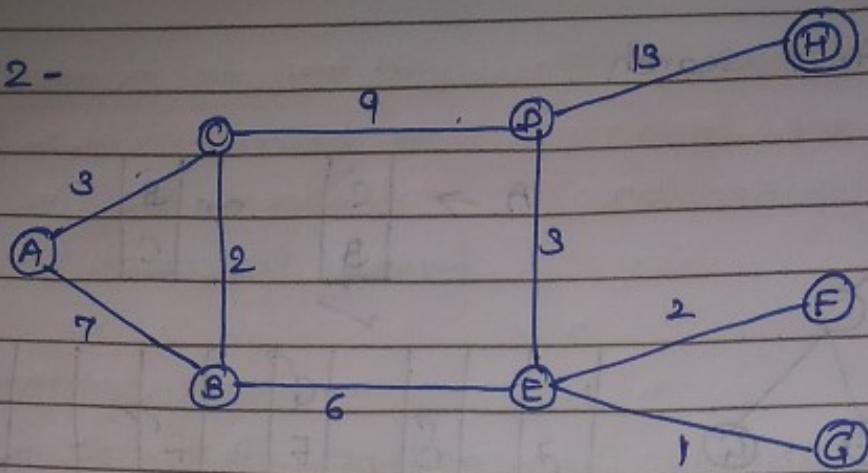


$A \rightarrow C \rightarrow B \rightarrow E \rightarrow G$

$$3 + 2 + 6 + 1 = 12$$

Path cost = 12

EX 2 -



$A \rightarrow C \rightarrow B \rightarrow E \rightarrow G \rightarrow F \rightarrow E \rightarrow D \rightarrow H$

$$3 + 2 + 6 + 1 + 1 + 2 + 2 + 3 + 13$$

Path Cost = 33

- It is used for traversing a weighted tree or graph
- It comes into play when a diff cost is available for each edge
- It is equivalent to BFS if the path cost of all the edges are same
- Implemented by partial queue . priority queue
- Used to solve any graph or tree
- Highest priority to minimum cost backtracking is there

Informed Search--

④ Bidirectional Search

> Two diff. searches run simultaneously

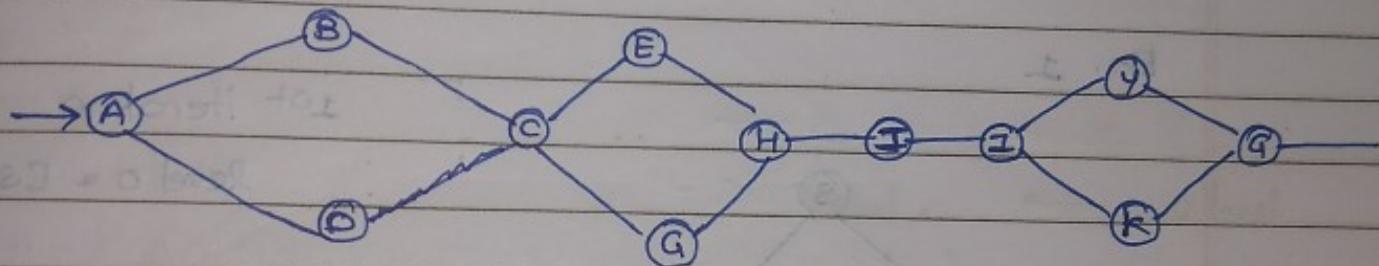
 > Forward Search

 > Backward Search

> Single search graph replaced with two small graphs.

> Any search technique can be used (BFS, DFS)

> Search stop condition (when graph intersect with each other)



Forward

A

ABD

ABDC

ABDCEF

Backward

G

GKY

GK~~Y~~I

G~~K~~YII

ABDCEF~~H~~

G~~K~~YII~~H~~

~~A→B→D→C→E→F→H→I→J→K→G~~

5) Iterative deepening search

> It is combination of both BFS & DFS

> Best depth limit is found out by gradually increasing limit

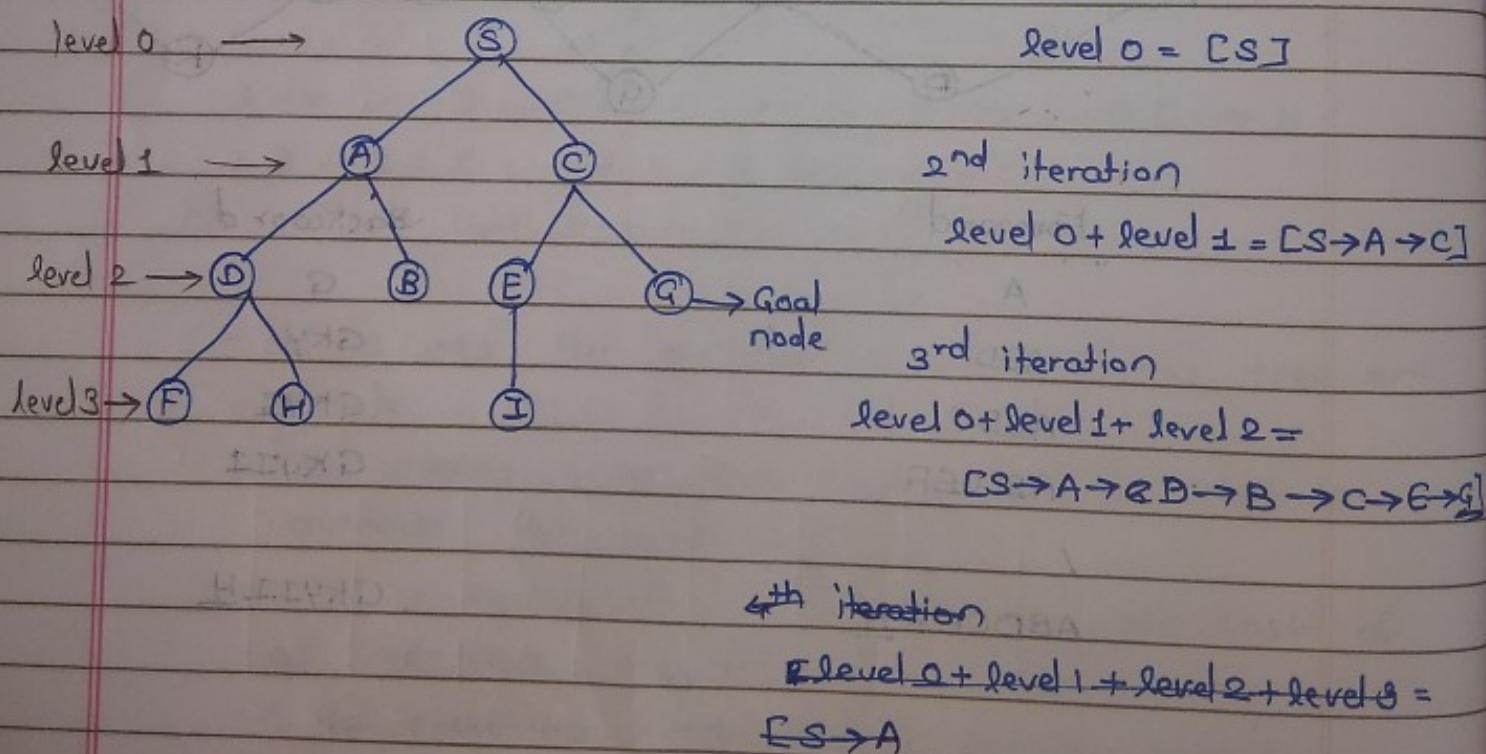
Advantages

> Fast & less memory requires.

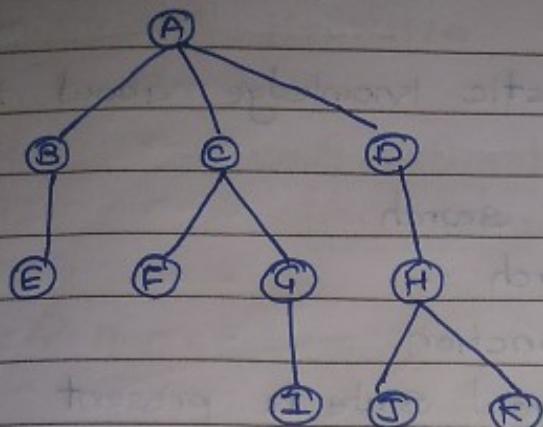
Disadvantages

> Repeat the work / process

Ex. 1



Ex 2.

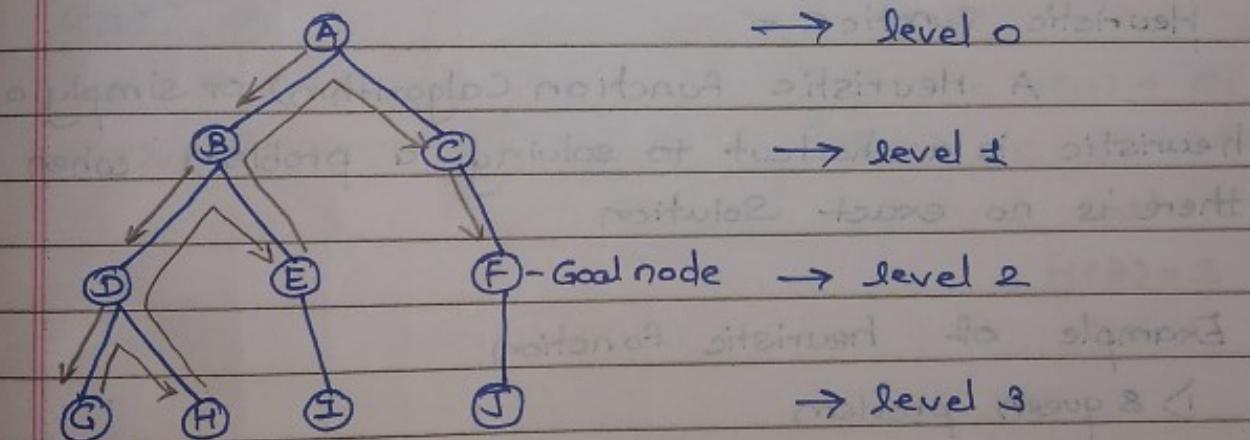


Depth level
0 → A
1 → ABCD
2 → ABECFGDH
3 → ABECFGIDHJK

Goal Node = K

→ Depth Limited Search is a non-linear search

Ex 1



Path = A → B → D → G → H → E → C → F

Depth limit = 2

- Depth limited search algorithm is similar to depth-first search with a predetermined limit
- Depth limited search is memory efficient.
- Depth limited search also has disadvantage of incompleteness.
- It is not optimal if the problem has more than one sol?

Informed Search

> Here we use heuristic knowledge about this problem.

> Types of Informed search

1. Heuristic search

2. Heuristic Function

> Information about goal state is present

> Find optimal or good sol?

Heuristic search form optimize path

Heuristic function a function which will give us a sol

→ Best first search

Heuristic function -

A Heuristic Function (Algorithm) or simply a heuristic is a shortcut to solving a problem when there is no exact solution

Example of heuristic function

→ 8 queen problem

7	2	4		1	2	
5		6		3	4	5
8	3	1		6	7	8

$$h_1 = \text{Total moves} = 8$$

$$h_2 = 3 + 1 + 2 + 2 + 2 + 3 + 3 + 2 = 18$$

$$\text{Total moves} = 18 + 8 = 26$$

Types of Heuristic

> Admissible

- underestimate cost

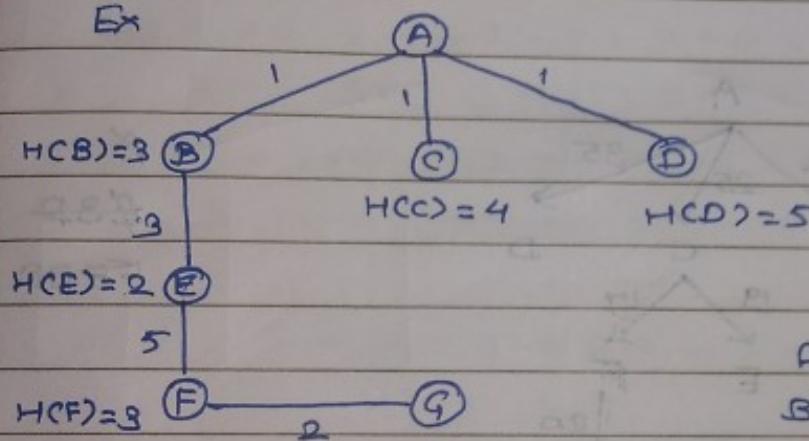
$$H(n) \leq H'(n)$$

> non-Admissible

- Overestimated cost

$$H(n) > H'(n)$$

Ex



Heuristic value of B

$$HCB = 3$$

Cost value of A to B = 1

$$P(n) = H(n) + G(n)$$

$$B = 4, C = 5, D = 6$$

$$\text{Actual cost} = 11$$

$$H(B) = 3$$

$$3 < 11$$

> Best First Search

- It always selects the path which appears best

at that movement

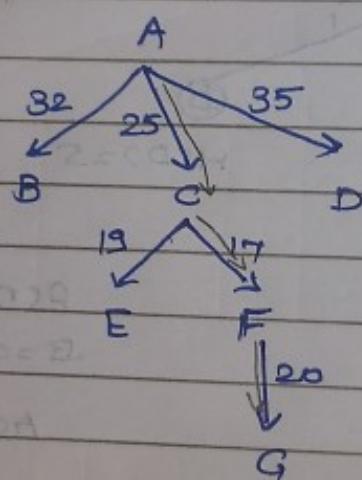
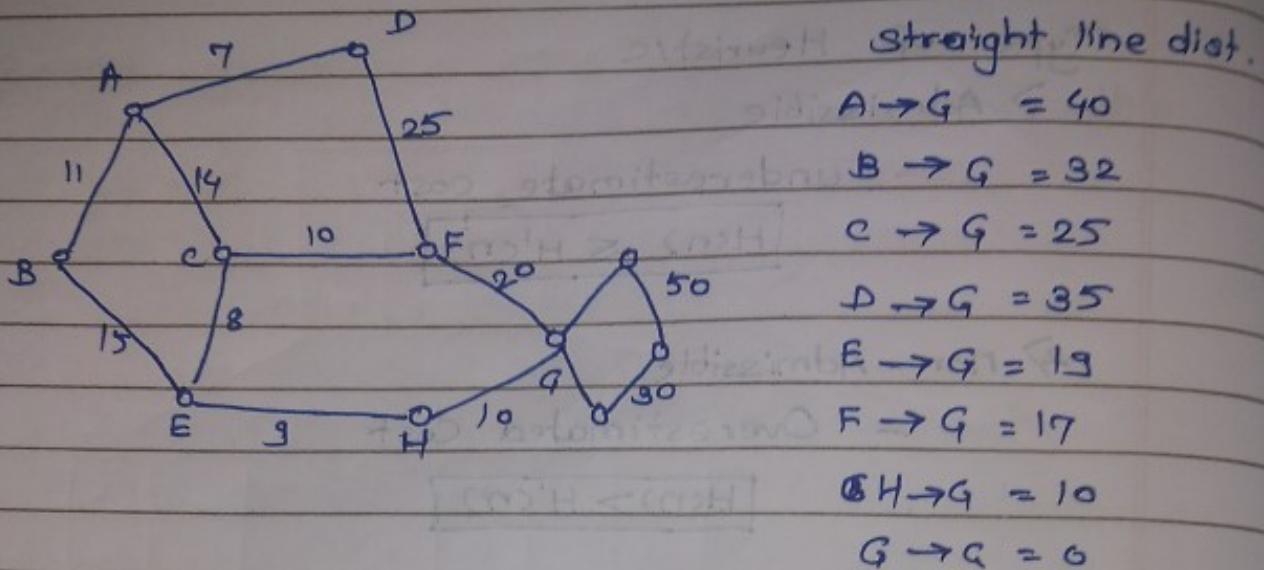
- Combination of Both DFS & BFS

- It uses heuristic function $h(n) \leq h^*(n)$

$h(n)$ = heuristic cost

$h^*(n)$ = estimated cost

- The greedy best first algorithm implemented by priority queue.



Final path = ACFG

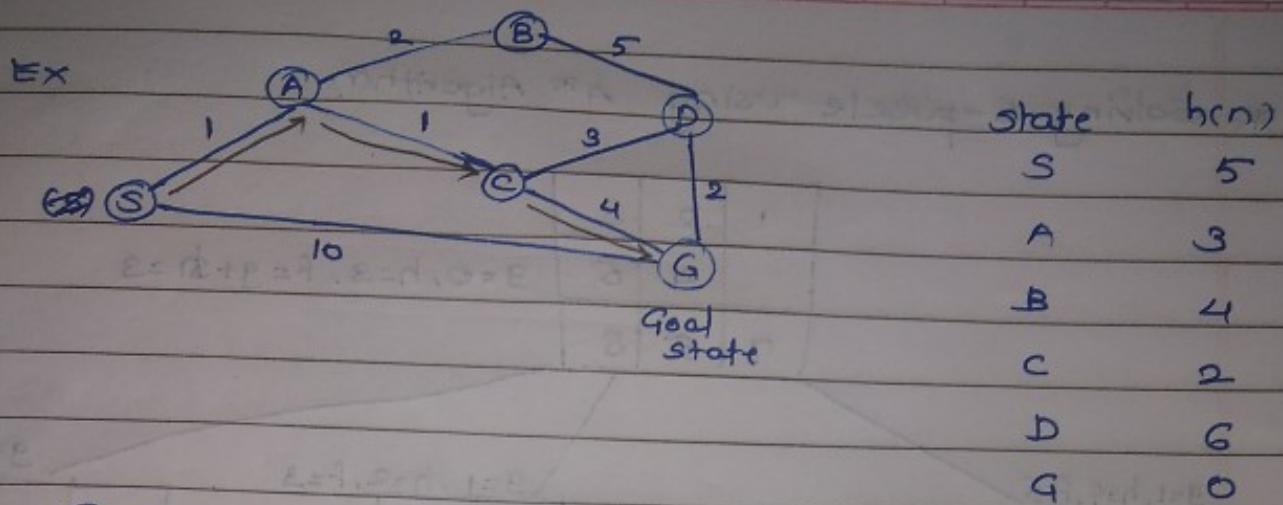
⇒ A* search

$$f(n) = g(n) + h(n)$$

$g(n)$ = actual cost from start node to n

$h(n)$ = estimation cost from n to goal node

⇒ A* search is both optimal & complete



$$\textcircled{1} \quad S \rightarrow A \Rightarrow f(n) = g(n) + h(n) = 1 + 3 = 4 \quad \checkmark$$

$$S \rightarrow G = f(n) = 10 + 0 = 10$$

$$\textcircled{2} \quad S \rightarrow A \rightarrow B \Rightarrow f(n) = 3 + 4 = 7$$

$$S \rightarrow A \rightarrow B \rightarrow C \Rightarrow f(n) = 2 + 2 = 4 \quad \checkmark$$

$$\textcircled{3} \quad S \rightarrow A \rightarrow C \rightarrow D \Rightarrow f(n) = 5 + 6 = 11$$

$$S \rightarrow A \rightarrow C \rightarrow G \Rightarrow f(n) = 6 + 0 = 6 \quad \checkmark$$

$$S \rightarrow A \rightarrow C \rightarrow G = 1 + 1 + 4 = 6$$

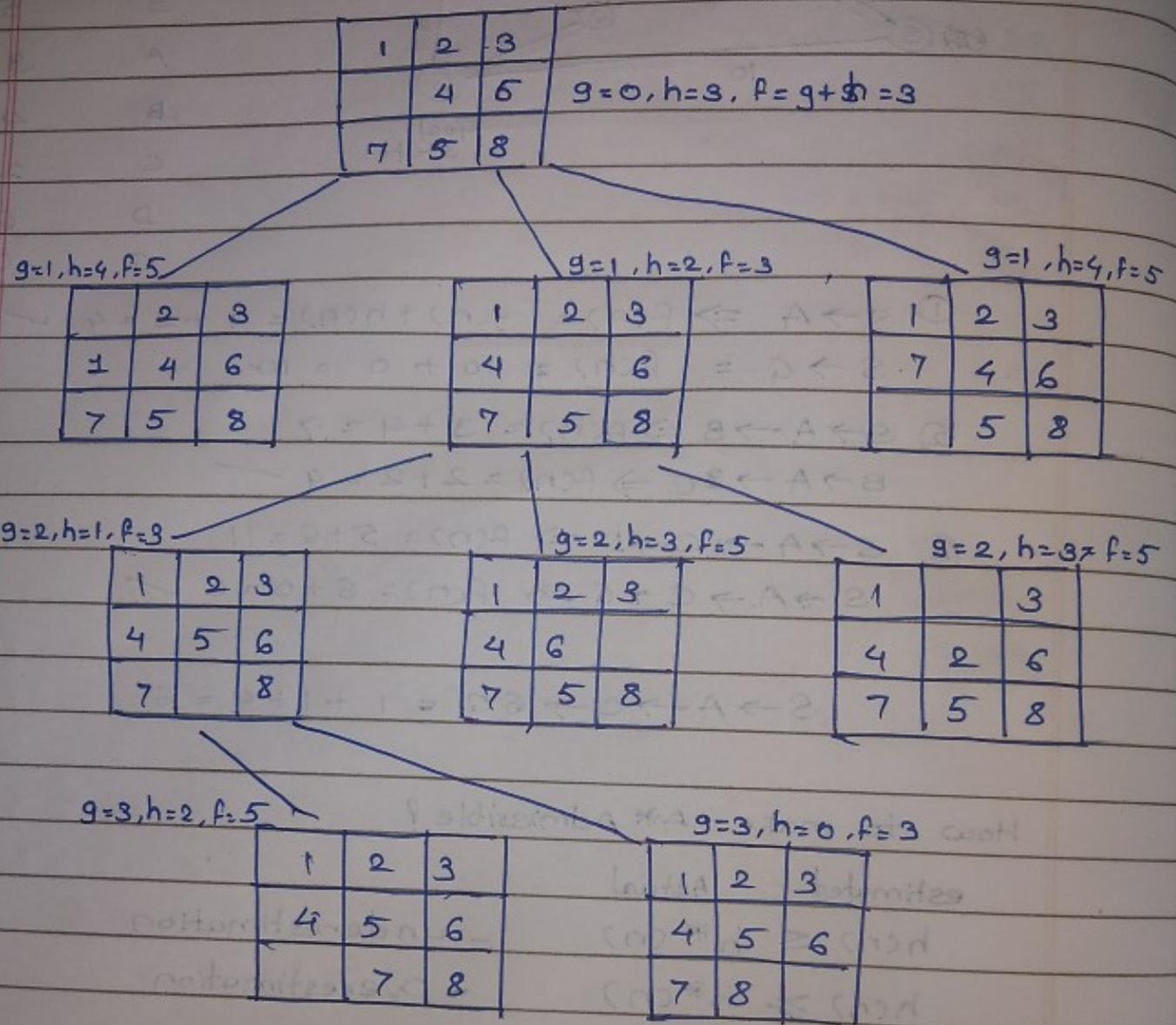
How to make A* Admissible?

estimated Actual

$h(n) \leq h^*(n)$ - underestimation

$h(n) \geq h^*(n)$ - overestimation

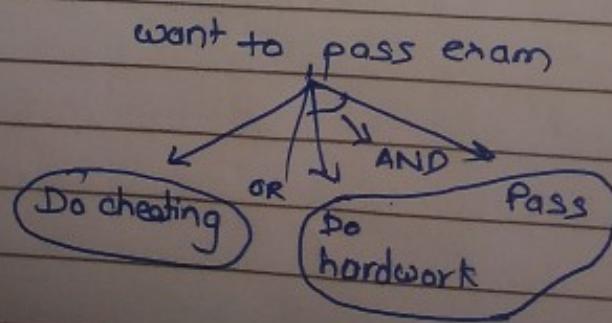
* Solving 8-puzzle using A* Algorithm



⇒ AO* Algorithm -

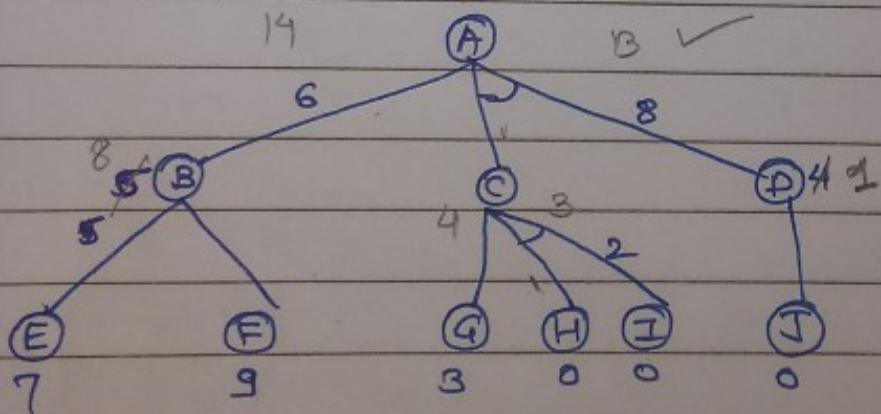
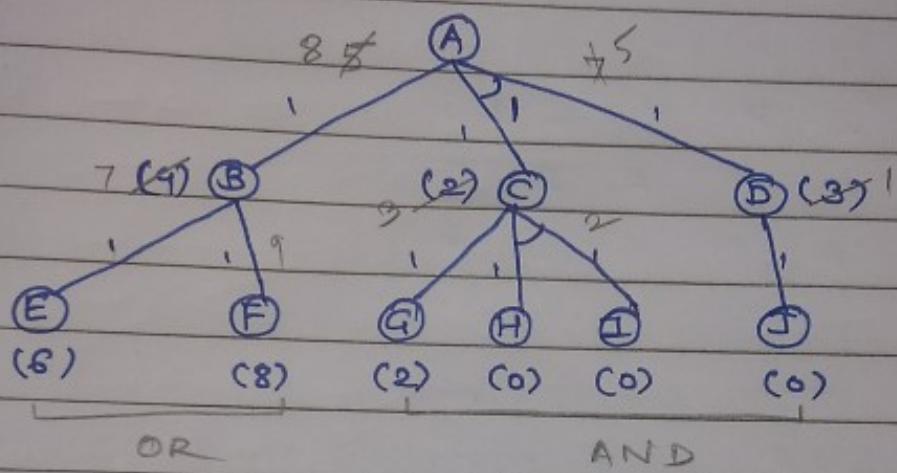
AND/OR - special graph →

- Problem Decomposition (Breakdown into small pieces)



- It the basis of heuristic value we find the optimal solution
- informed search technique.
- guaranteed optimal soln

Ex



* Solve the following crypt arithmetic problem

$$\begin{array}{r} \text{C R O S S} \\ + \text{R O A D S} \\ \hline \text{D A N G E R} \end{array}$$

→

$$\begin{array}{ccccc} c_5 & c_4 & c_3 & c_2 & c_1 \\ * & \text{C} & \text{R} & \text{O} & \text{S} \text{ } \text{S} \\ + & \text{R} & \text{O} & \text{A} & \text{D} \text{ } \text{S} \\ \hline & \text{D} & \text{A} & \text{N} & \text{G} \text{ } \text{E} \text{ } \text{R} \end{array}$$

$c_5 = 1$ becoz c_5 is carry

$S+S=R$ so R must be even no so possibility
 $\{0, 2, 4, 6, 8\}$

Q. If we take 0 is value so

$$S+S=R$$

$$0+0=0$$

S & R value must be same so it create conflict

If we take 2 is value then

$$S+S=R$$

$$(2+2=4)$$

But then the conflict occur with A & R

If we take 8 is value $R=6$, $S=3$

$$S+S=R$$

$$3+3=6$$

$$\begin{array}{r} \boxed{c} \boxed{9} \quad \boxed{R} \boxed{6} \quad \boxed{0} \boxed{2} \quad \boxed{s} \boxed{3} \quad \boxed{s} \boxed{3} \\ + \quad \boxed{R} \boxed{6} \quad \boxed{0} \boxed{2} \quad \boxed{A} \boxed{5} \quad \boxed{D} \boxed{1} \quad \boxed{s} \boxed{3} \\ \hline \boxed{D} \boxed{1} \quad \boxed{A} \boxed{5} \quad \boxed{N} \boxed{8} \quad \boxed{G} \boxed{7} \quad \boxed{E} \boxed{4} \quad \boxed{R} \boxed{6} \end{array}$$

* Solve the following crypt Arithmetic problems

$$\begin{array}{r} S \ A \ S \ E \\ + B \ A \ L \ L \\ \hline G \ A \ M \ E \ S \end{array}$$

→

$$E + L = S \rightarrow (a) \text{ [no carry]}$$

$$S + L = E + 10 \rightarrow (b) \text{ [Carry]}$$

$$\hookrightarrow E = S - L + 10$$

$$S + L = E \downarrow$$

$$S + L = S - L + 10$$

$$\text{or } 2L = 10$$

$$L = 5$$

$$\text{so } E + L = S$$

$$5 = S - E$$

so we find the combination of $S \& E$ $\text{① } (5,0) \times$ assing value L

$(6,1) \times 9$

$(7,2)$

$(8,3)$

$(9,4)$

$$B + B = A + \text{Carry}$$

value of B must be $5, 6, 7, 8, 9$

Let $(S, E) = (7, 2) \& B = 6 \quad B + B = 12 \xrightarrow{A} \rightarrow c \text{ value already assign}$

Let $(S, E) = (8, 3) \& B = 7 \quad B + B = 14$

$$\begin{array}{r} \boxed{B \ 7} \quad \boxed{A \ 4} \quad \boxed{S \ 8} \quad \boxed{E \ 3} \\ + \quad \boxed{B \ 7} \quad \boxed{A \ 4} \quad \boxed{L \ 5} \quad \boxed{L \ 5} \\ \hline \boxed{G \ 1} \quad \boxed{A \ 4} \quad \boxed{M \ 9} \quad \boxed{E \ 3} \end{array}$$

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