

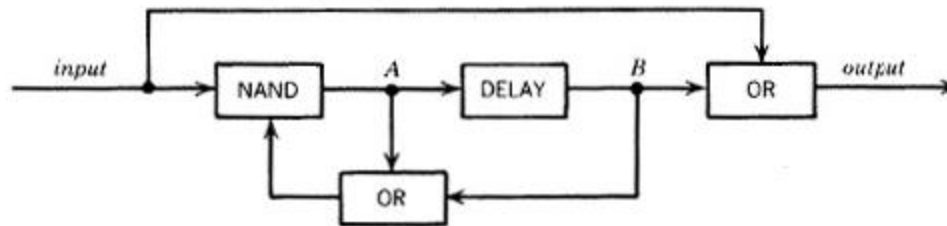
CSC 2204 Finite Automata Theory and Formal Languages



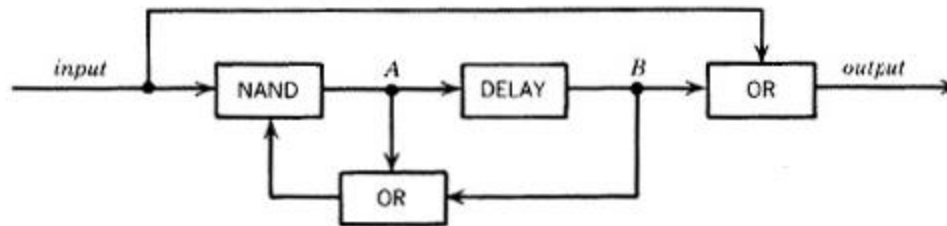
Department of Computer Science
SZABIST (Islamabad Campus)

Week 9 (Week 2)

Example 2

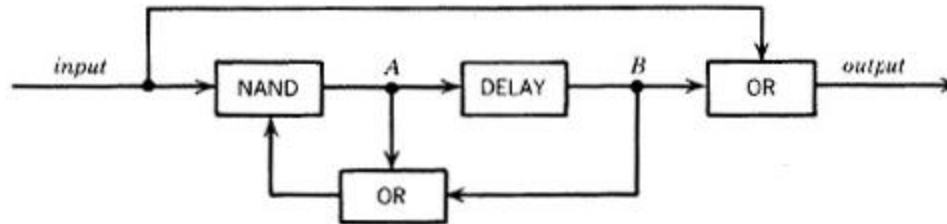


Example 2



q_0 is $A = 0$,	$B = 0$
q_1 is $A = 0$,	$B = 1$
q_2 is $A = 1$,	$B = 0$
q_3 is $A = 1$,	$B = 1$

Example 2



q_0 is $A = 0,$	$B = 0$
q_1 is $A = 0,$	$B = 1$
q_2 is $A = 1,$	$B = 0$
q_3 is $A = 1,$	$B = 1$

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New $B = \text{old } A$

New $A = (\text{input}) \text{ NAND } (\text{old } A \text{ OR old } B)$

Output = (input) OR (old B)



Example 2

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New B = old A

New A = (input) NAND (old A OR old B)

Output = (input) OR (old B)



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$$\text{New } B = \text{old } A$$

$$\text{New } A = (\text{input}) \text{ NAND } (\text{old } A \text{ OR old } B)$$

$$\text{Output} = (\text{input}) \text{ OR } (\text{old } B)$$

Suppose we are in state q_0 and we receive the input 0:

$$\text{New } B = \text{old } A = 0$$

$$\begin{aligned}\text{New } A &= (\text{input}) \text{ NAND } (\text{old } A \text{ OR old } B) \\ &= (0) \text{ NAND } (0 \text{ OR } 0) \\ &= 0 \text{ NAND } 0 \\ &= 1\end{aligned}$$

$$\text{Output} = 0 \text{ OR } 0 = 0$$

The new state is q_2 (because new $A = 1$, new $B = 0$).



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$$\text{New } B = \text{old } A$$

$$\text{New } A = (\text{input}) \text{ NAND } (\text{old } A \text{ OR old } B)$$

$$\text{Output} = (\text{input}) \text{ OR } (\text{old } B)$$

Suppose we are in state q_0 and we receive the input 0:

$$\text{New } B = \text{old } A = 0$$

$$\begin{aligned}\text{New } A &= (\text{input}) \text{ NAND } (\text{old } A \text{ OR old } B) \\ &= (0) \text{ NAND } (0 \text{ OR } 0) \\ &= 0 \text{ NAND } 0 \\ &= 1\end{aligned}$$

$$\text{Output} = 0 \text{ OR } 0 = 0$$

The new state is q_2 (because new $A = 1$, new $B = 0$).

If we are in state q_0 and we receive the input 1,

$$\text{New } B = \text{old } A = 0$$

$$\text{New } A = 1 \text{ NAND } (0 \text{ OR } 0) = 1$$

$$\text{Output} = 1 \text{ OR } 0 = 1$$

The new state is q_2 (because the new $A = 1$ and the new $B = 0$).



Example 2

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New B = old A

New A = (input) NAND (old A OR old B)

Output = (input) OR (old B)

If we are in q_1 and we receive the input 0:

New B = old A = 0

New A = 0 NAND (0 OR 1) = 1

Output = 0 OR 1 = 1

The new state is q_2 .



Example 2

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New B = old A

New A = (input) NAND (old A OR old B)

Output = (input) OR (old B)

If we are in q_1 and we receive the input 0:

New B = old A = 0

New A = 0 NAND (0 OR 1) = 1

Output = 0 OR 1 = 1

The new state is q_2 .

If we are in q_1 and we receive the input 1,

New B = old A = 0

New A = 1 NAND (0 OR 1) = 0

Output = 1 OR 1 = 1

The new state is q_1



Example 2

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New B = old A

New A = (input) NAND (old A OR old B)

Output = (input) OR (old B)

If we are in state q_2 and we receive the input 0,

New B = old A = 1

New A = 0 NAND (1 OR 0) = 1

Output = 0 OR 0 = 0

The new state is q_3 .



Example 2

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New B = old A

New A = (input) NAND (old A OR old B)

Output = (input) OR (old B)

If we are in state q_2 and we receive the input 0,

New B = old A = 1

New A = $0 \text{ NAND } (1 \text{ OR } 0) = 1$

Output = $0 \text{ OR } 0 = 0$

The new state is q_3 .

If we are in q_2 and we receive the input 1,

New B = old A = 1

New A = $1 \text{ NAND } (1 \text{ OR } 0) = 0$

Output = $1 \text{ OR } 0 = 1$

The new state is q_1



Example 2

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New B = old A

New A = (input) NAND (old A OR old B)

Output = (input) OR (old B)

If we are in q_3 and we receive the input 0,

New B = old A = 1

New A = 0 NAND (1 OR 1) = 1

Output = 0 OR 1 = 1

The new state is q_3



Example 2

The operation of this circuit is such that after an input of 0 or 1, the state changes according to the following rules:

New B = old A

New A = (input) NAND (old A OR old B)

Output = (input) OR (old B)

If we are in q_3 and we receive the input 0,

New B = old A = 1

New A = 0 NAND (1 OR 1) = 1

Output = 0 OR 1 = 1

The new state is q_3

If we are in q_3 and we receive the input 1,

New B = old A = 1

New A = 1 NAND (1 OR 1) = 0

Output = 1 OR 1 = 1

The new state is q_1 .



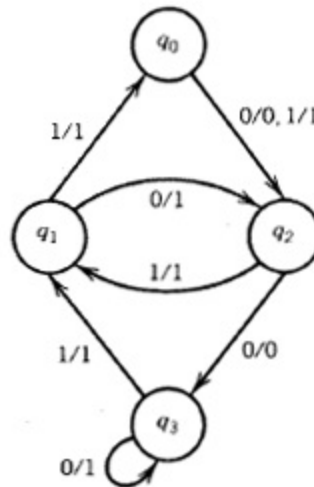
Example 2

Old State	After Input 0		After Input 1	
	New State	Output	New State	Output
q_0	q_2	0	q_2	1
q_1	q_2	1	q_0	1
q_2	q_3	0	q_1	1
q_3	q_3	1	q_1	1

Example 2

Old State	After Input 0		After Input 1	
	New State	Output	New State	Output
q_0	q_2	0	q_2	1
q_1	q_2	1	q_0	1
q_2	q_3	0	q_1	1
q_3	q_3	1	q_1	1

input string 011011



Example 2

Old State	After Input 0		After Input 1	
	New State	Output	New State	Output
q_0	q_2	0	q_2	1
q_1	q_2	1	q_0	1
q_2	q_3	0	q_1	1
q_3	q_3	1	q_1	1

input string 011011
output sequence 111011

