

CSC 3201 Compiler Construction



Department of Computer Science
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Week 6 (Lecture 2)



LL(1) Parsing

- The 1st L represents that the scanning of the Input will be done from Left to Right manner.
- The 2nd L shows that Left most Derivation will be used.
- The number 1 represents the number of look ahead.
 - Look Ahead means how many symbols will be seen to make a decision.



LL(1) Parsing Table

- Two functions:
 - First(): The beginning Terminal Symbol if from a variable all strings are derived.
 - Follow(): The Terminal Symbol which follows a variable in the process of derivation.
- After computing the First and Follow set for each Non-Terminal symbol we have to construct the Parsing table.
 - Rows contain the NTs.
 - Column contain the Ts.



LL(1) Parsing Table

- Example 1:

$$E \rightarrow TE'$$
$$E' \rightarrow +TE' \mid \varepsilon$$
$$T \rightarrow FT'$$
$$T' \rightarrow *FT' \mid \varepsilon$$
$$F \rightarrow id \mid (E)$$



LL(1) Parsing Table

Production	First	Follow
$E \rightarrow TE'$	{ id, (}	{ \$,) }
$E' \rightarrow +TE' \mid \epsilon$	{ +, ϵ }	{ \$,) }
$T \rightarrow FT'$	{ id, (}	{ +, \$,) }
$T' \rightarrow *FT' \mid \epsilon$	{ *, ϵ }	{ +, \$,) }
$F \rightarrow id \mid (E)$	{ id, (}	{ *, +, \$,) }

LL(1) Parsing Table

	First	Follow	Production No
$E \rightarrow TE'$	$\{id, (\}$	$\{ \$,) \}$	1
$E' \rightarrow +TE' \mid \epsilon$	$\{ +, \epsilon \}$	$\{ \$,) \}$	2
$T \rightarrow FT'$	$\{id, (\}$	$\{ +,), \$ \}$	3
$T' \rightarrow *FT' \mid \epsilon$	$\{ *, \epsilon \}$	$\{ +,), \$ \}$	4
$F \rightarrow id(E)$	$\{id, (\}$	$\{ *, +,), \$ \}$	5

LL(1) Parsing Table

- Check First(LHS) in the production
- If it is ϵ then check Follow(LHS)

	id	+	*	()	\$
E	1			1		
E'		2a			2b	2b
T	3			3		
T'		4b	4a		4b	4b
F	5a			5b		

LL(1) Parsing Table

NON - TERMINAL	INPUT SYMBOL					
	id	+	*	()	\$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
F	$F \rightarrow \text{id}$			$F \rightarrow (E)$		



LL(1) Parsing Table

- NOTE:
 - LL(1) Table cannot be constructed for left recursive and non-deterministic grammars.
 - Remove left recursion.
 - Ensure left factoring.
 - Sometimes valid grammars may not have LL(1) table. Example:
 - $A \rightarrow \text{Multiple-Options}$ (More than one productions go to the same cell).



LL(1) Parsing Table

- Example 2:

$S \rightarrow A \mid a$

$A \rightarrow a$



LL(1) Parsing Table

- Example 2:

$$S \rightarrow A \mid a$$
$$A \rightarrow a$$

Production	First	Follow
$S \rightarrow A \mid a$	{a}	{ \$ }
$A \rightarrow a$	{a}	{ \$ }



LL(1) Parsing Table

Production	First	Follow
$S \rightarrow A \mid a$	{a}	{ $\$$ }
$A \rightarrow a$	{a}	{ $\$$ }

	A	\$
S	$S \rightarrow A$ $S \rightarrow a$	
A	$A \rightarrow a$	

- Language is not LL(1)



LL(1) Parsing Table

Production	First	Follow
$S \rightarrow A \mid a$	{a}	{ $\$$ }
$A \rightarrow a$	{a}	{ $\$$ }



LL(1) Parsing Table

- Example 3:

$E \rightarrow ABC$

$A \rightarrow a \mid Cb \mid \epsilon$

$B \rightarrow c \mid xA \mid \epsilon$

$C \rightarrow y \mid z$



LL(1) Parsing Table

$\text{First}(E) = \{a, y, z, \epsilon\}$

$\text{First}(A) = \{a, y, z, \epsilon\}$

$\text{First}(B) = \{c, x, \epsilon\}$

$\text{First}(C) = \{y, z\}$

$\text{Follow}(E) = \{\$ \}$

$\text{Follow}(A) = \{c, x, y, z\}$

$\text{Follow}(B) = \{y, z\}$

$\text{Follow}(C) = \{b, \$ \}$



LL(1) Parsing Table

	x	a	b	c	y	z	\$
E		ABC			ABC	ABC	ϵ
A	ϵ	a		ϵ	Cb	Cb	
B	xA			c	ϵ	ϵ	
C					y	z	

LL(1)?

$$\begin{aligned} S &\rightarrow aSbS \\ &\mid bSaS \\ &\mid \epsilon \end{aligned}$$
$$\begin{aligned} S &\rightarrow A \mid a \\ A &\rightarrow a \end{aligned}$$
$$\begin{aligned} S &\rightarrow aABb \\ A &\rightarrow c \mid \epsilon \\ B &\rightarrow d \mid \epsilon \end{aligned}$$
$$\begin{aligned} S &\rightarrow aB \mid \epsilon \\ B &\rightarrow bC \mid \epsilon \\ C &\rightarrow cS \mid \epsilon \end{aligned}$$

LL(1)?

x $S \rightarrow aSbS$
| $bSaS$
| ϵ

x $S \rightarrow A|a$
 $A \rightarrow a$
 $\{a\} \cap \{a\}$

✓ $S \rightarrow aABb$
 $A \rightarrow c|\epsilon$
 $B \rightarrow d|\epsilon$

✓ $S \rightarrow aB|\epsilon$
 $B \rightarrow bC|\epsilon$
 $C \rightarrow cS|\epsilon$

LL(1)?

$S \rightarrow AB$

$A \rightarrow a/\epsilon$

$B \rightarrow b/\epsilon$

$S \rightarrow aSA/\epsilon$

$A \rightarrow c/\epsilon$

$S \rightarrow iEtSS'/a$

$S' \rightarrow eS/\epsilon$

$E \rightarrow b$

LL(1)?

✓ $S \rightarrow AB$
 $A \rightarrow a/\epsilon$
 $B \rightarrow b/\epsilon$

x $S \rightarrow aSA/\epsilon$
 $A \rightarrow c/\epsilon$

x $S \rightarrow iEtSS'/a$
 $S' \rightarrow eS/\epsilon$
 $E \rightarrow b$
 $\{e\} \cap \{e\}$



LL(1)?

$S \rightarrow A$

$A \rightarrow Bb \mid Cd$

$B \rightarrow aB \mid \epsilon$

$C \rightarrow cC \mid \epsilon$

$S \rightarrow aAa \mid \epsilon$

$A \rightarrow abS \mid \epsilon$



LL(1)?

✓ $S \rightarrow A$
 $A \rightarrow Bb | Cd$
 $B \rightarrow aB | \epsilon$
 $C \rightarrow cC | \epsilon$

x $S \rightarrow aAa | \epsilon$
 $A \rightarrow abS | \epsilon$