Pushdown Automata (PDA)

Input Tape:

 $\Sigma = \{a,b,cd\}$, String: aacdbab, Length: 6

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а	а	rd	l h	а	l h	ΙΛ.	ΙΛ	ΙΛ
u	u	Cu		u				

The START State:



The ACCEPT State:



The REJECT State:



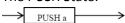
The READ State (Outgoing: Total alphabets+1):

$$\Sigma = \{a,b\}$$

$$READ$$

$$b$$

The PUSH State:



The POP State (Outgoing: Total alphabets+1):

$$\Sigma = \{a,b\}$$

$$\downarrow b$$

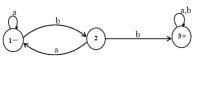
$$\downarrow b$$

$$\downarrow \Delta$$

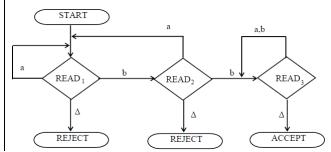
Note:

- START is connected to the initial state
- Final States are connected to ACCEPT through Δ
- \bullet $\;$ Non-Final States are connected to REJECT through Δ

FA: $\Sigma = \{a,b\}$ L = Containing bb



Using the new format:



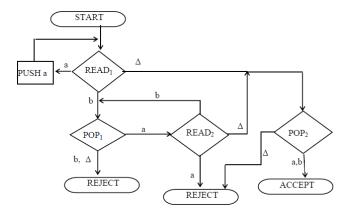
Tape: aaabb∆

State	Tape	New State
START	aaabb∆	READ1
READ1	<u>a</u> aabb∆	READ1
READ1	<mark>aa</mark> abb∆	READ1
READ1	<mark>aa<u>a</u>bb∆</mark>	READ1
READ1	<mark>aaa<u>b</u>b</mark> ∆	READ2
READ2	aaab <u>b</u> ∆	READ3
READ3	aaabb <u>∆</u>	ACCEPT

Tape: aab∆

State	Tape	New State
START	aab∆	READ1
READ1	<u>a</u> ab∆	READ1
READ1	<mark>a<u>a</u>b∆</mark>	READ1
READ1	aa <u>b</u> ∆	READ2
READ2	aab <u>∆</u>	REJECT

PDA:

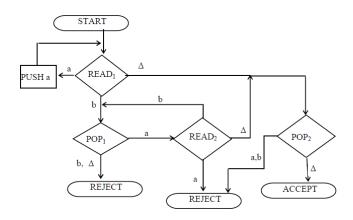


Tape: aaabbb∆

State Tape		Stack	New State
START	aaabbb∆	Δ	READ1
READ1	<u>a</u> aabbb∆	Push a into the stack: a∆	READ1
READ1	<mark>aa</mark> abbb∆	Push a into the stack: aa∆	READ1
READ1	aa <u>a</u> bbb∆	Push a into the stack: aaa∆	READ1
READ1	<mark>aaa</mark> <u>b</u> bb∆	POP1 a: aa∆	READ2
READ2	aaab<u>b</u> b∆	POP1 a: a∆	READ2

READ2	aaabb <u>b</u> ∆	POP1 a: Δ	READ2
READ2	aaabbb <u>∆</u>	POP2 Δ: Empty Stack	REJECT

PDA:



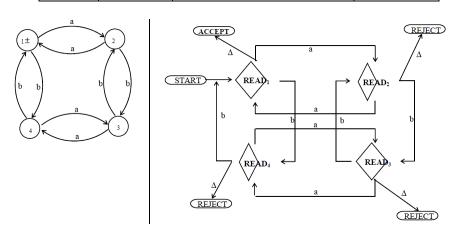
Tape: aaabbb∆

State	Tape	Stack	New State
START	aaabbb∆	Δ	READ1
READ1	<u>a</u> aabbb∆	Push a into the stack: a∆	READ1
READ1	<mark>a<u>a</u>abbb∆</mark>	Push a into the stack: aa∆	READ1
READ1	aa <u>a</u> bbb∆	Push a into the stack: aaa∆	READ1
READ1	<mark>aaa</mark> <u>b</u> bb∆	POP1 a: aa∆	READ2
READ2	aaab<u>b</u> b∆	POP1 a: a∆	READ2
READ2	aaabb <u>b</u> ∆	POP1 a: Δ	READ2
READ2	aaabbb <u>∆</u>	POP2 Δ: Empty Stack	ACCEPT

Tape: aab∆

State	Tape	Stack	New State
START	aab∆	Δ	READ1
READ1	<u>a</u> ab∆	Push a into the stack: a∆	READ1
READ1	<mark>aa</mark> b∆	Push a into the stack: aa∆	READ1
READ1	aa <u>b</u> ∆	POP1 a: a∆	READ2
READ2	aab <u>∆</u>	POP2 a: Δ	REJECT

FA:



Tape: aabbb Δ

State	Tape	New State
START	aabbb∆	READ1
READ1	<u>a</u> abbb∆	READ2
READ2	<mark>aa</mark> bbb∆	READ1
READ1	aa <u>b</u> bb∆	READ4
READ4	aab<u>b</u> b∆	READ1
READ1	aabb <u>b</u> ∆	READ4
READ4	aabbb <u>∆</u>	REJECT