Asymptotic notations are the mathematical notations used to describe the running time of an algorithm when the input tends towards a particular value or a limiting value. There are mainly three asymptotic notations:

• Big-O notation: It represents the upper bound of the running time of an algorithm. The following expression can be described as a function f(n) belongs to the set O(g(n)) if there exists a positive constant c such that it lies between 0 and cg(n), for sufficiently large n.

 $O(g(n)) = \{f(n): \text{ there exist positive constants } c \text{ and } n_0 \}$ such that $0 \le f(n) \le cg(n)$ for all $n \ge n_0\}$

• Omega notation: It represents the lower bound of the running time of an algorithm. The following expression can be described as a function f(n) belongs to the set $\Omega(g(n))$ if there exists a positive constant c such that it lies above cg(n), for sufficiently large n.

 $\Omega(g(n)) = \{f(n): \text{ there exist positive constants } c \text{ and } n_0 \}$ such that $0 \le cg(n) \le f(n)$ for all $n \ge n_0\}$

• Theta notation: It represents the upper and the lower bound of the running time of an algorithm. The following expression can be described as a function f(n) belongs to the set O(g(n)) if there exist positive constants c_1 and c_2 such that it can be sandwiched between $c_1g(n)$ and $c_2g(n)$, for sufficiently large n.

 $\Theta(g(n)) = \{f(n): \text{ there exist positive constants } c_1, c_2 \text{ and } n_0 \}$ such that $0 \le c_1 g(n) \le f(n) \le c_2 g(n) \text{ for all } n \ge n_0 \}$





