## **Implement a Heap Data Structure**

You have been provided with a partial implementation of a heap data structure code. The code already has the following functions implemented:

- initialize (int v[], int n) Initialize the heap to store vertices in array v with all their keys set to  $\infty$ .
- heapify(int i) This operation is required to re-store heap property for implementing certain operations, such as removeMin operation, and updateKey operation. This function is already implemented in given sample skeleton.
- $getKey(int \ data)$  This operation returns the key value of the given data in the heap.
- *emtpy()* Returns *true* if the heap is empty, otherwise returns false.
- *printHeap()* Prints the heap.

Your job is to complete the implementation that support the following heap operations:

- buHeapify(int i) This operation is called when key value of an existing node is decreased or a new item is inserted at the end of the heap. For example, when the key value of a data item at node index i is decreased, the node may be required to move up the tree so that heap property (parent's key less than or equal to childs' key) remains correct. This may be implemented as a recursive function or in iterative manner that starts swapping of nodes at node number i, then may call recursively at parent of i. In the worse case, the function will end at the root of the tree (all nodes from i up-to the root will be swapped).
- *void insertItem*(*int data*, *int key*) This function inserts a new (*data*, *key*) pair in the heap. The new item is first inserted at the end of the heap which may violate heap property. So *buHeapify* operation is executed to ensure that heap property is restored. In the worst case, the inserted node may end up moving at the root node of the heap.
- HeapItem removeMin() This operation will return the heap node that has the minimum key value. Must restore heap property by calling heapify after removal.
- updateKey(int data, float key) This operation updates the key value of the given data to the given key. The function first searches for given data in the heap and then updates the key value.
  After update, it may happen that the new key violates min-heap property. Hence, after update, a call to heapify or buheapify is required.

Note the following-

-You must extend this class to implement your own Heap class. You cannot write your own class.

- -Note that a special array map is kept in this MinHeap class to keep track of where each data value is currently stored inside the heap. This is required for searching in the updateKey(data, key) operation, because we need to know in which node the input data is stored.
- -Without keeping this map array, you may find where data is stored by a linear search through all heap nodes which will require O(n) time (n is the number of nodes in heap). In this case, updateKey will also require O(n) time which is prohibited.
- -However, keeping a map array does the data search in constant time, which gives the overall time of O(logn) for the updateKey operation. This is very much important for certain algorithms such as Prim's MST algorithm or Dijkstra's shortest path algorithm to ensure their optimal running time.
- -The *map* array also helps us for *getKey* operation to return the *key* value of a vertex in constant time without keeping additional storage.