

# hw1\_37810\_weidi

## Section 4.1.1

### Exercise 2

(a)

```
Fibonacci <- numeric(30)
Fibonacci[1] <- Fibonacci[2] <- 1
for (i in 3:30) Fibonacci[i] <- Fibonacci[i - 2] + Fibonacci[i - 1]
print(Fibonacci)

## [1] 1 1 2 3 5 8 13 21 34 55
## [11] 89 144 233 377 610 987 1597 2584 4181 6765
## [21] 10946 17711 28657 46368 75025 121393 196418 317811 514229 832040

#Compute f(n)/f(n-1)

print(Fibonacci[2:30]/Fibonacci[1:29])

## [1] 1.000000 2.000000 1.500000 1.666667 1.600000 1.625000 1.615385
## [8] 1.619048 1.617647 1.618182 1.617978 1.618056 1.618026 1.618037
## [15] 1.618033 1.618034 1.618034 1.618034 1.618034 1.618034 1.618034
## [22] 1.618034 1.618034 1.618034 1.618034 1.618034 1.618034 1.618034
## [29] 1.618034
```

Yes, the sequence appears to be converging to 1.618034.

(b)

```
(1+sqrt(5))/2

## [1] 1.618034
```

Yes, the sequence is converging to this ratio. Proof:  $f(n) = f(n-2) + f(n-1)$   $f(n)/f(n-1) = f(n-2)/f(n-1) + 1$   
 $\lim f(n)/f(n-1) = \lim f(n-2)/f(n-1) + 1$   $L = 1/L + 1$   $L^2 - L - 1 = 0$   $L = (1+\sqrt{5})/2$

### Exercise 3

(a)

The final value of answer should be  $1+2+3+4+5 = 15$

```
answer <- 0
for (j in 1:5) answer <- answer + j
answer
```

```
## [1] 15
```

(b)

The final value of answer should be  $c(1,2,3,4,5)$

```
answer <- NULL
for (j in 1:5) answer <- c(answer, j)
answer
```

```
## [1] 1 2 3 4 5
```

(c)

The final value of answer should be  $c(0,1,2,3,4,5)$

```
answer <- 0
for (j in 1:5) answer <- c(answer, j)
answer
```

```
## [1] 0 1 2 3 4 5
```

(d)

The final value of answer should be  $12345 = 120$

```
answer <- 1
for (j in 1:5) answer <- answer * j
answer
```

```
## [1] 120
```

(e)

The final value of answer should be 3

```
answer <- 3
for (j in 1:15) answer <- c(answer, (7 * answer[j]) %% 31)
answer
```

```
## [1] 3 21 23 6 11 15 12 22 30 24 13 29 17 26 27 3
```

## Section 4.1.2

### Exercise 4

```
# p is the initial investment amount, n is the number of interest periods
compInterest <- function(p,n) {
  if(n<=3) i<-0.04 else i<-0.05
  interest = p*((1+i)^n-1)
  return (interest)
}
```

### Exercise 5

```
#function to calculate a monthly mortgage payment R where i is an interest rate (compounded monthly),P
compPayment <- function(n,p,openTerm) {
  if(openTerm==TRUE) i <- 0.005 else i<-0.004
  payment = p*i/(1-(1+i)^(-n))
  return (payment)
}
```

## Section 4.1.3

### Exercise 2

```
Fibonacci <- c(1, 1)
while (max(Fibonacci) < 300) {
  n = length(Fibonacci)
  Fibonacci <- c(Fibonacci, Fibonacci[n-1]+Fibonacci[n])
}
```

```
Fibonacci
```

```
## [1] 1 1 2 3 5 8 13 21 34 55 89 144 233 377
```

#### Exercise 4

```
i <- 0.006
i2 <- (1 - (1 + i)^(-20)) / 19

while (abs(i-i2) > 0.000001) {
  i <- i2
  i2 <- (1 - (1 + i2)^(-20)) / 19
}
i2
```

```
## [1] 0.004954139
```

If we try other starting guesses of  $i$ , such as  $i = 0.1$

```
i <- 0.1
i2 <- (1 - (1 + i)^(-20)) / 19

while (abs(i-i2) > 0.000001) {
  i <- i2
  i2 <- (1 - (1 + i2)^(-20)) / 19
}
i2
```

```
## [1] 0.004953499
```

The final values of  $i$  are very close regardless of the starting guesses.

#### Exercise 5

```
i <- 0.006
i2 <- (1 - (1 + i)^(-20)) / 19
n_iter = 1

while (abs(i-i2) > 0.000001) {
  i <- i2
  i2 <- (1 - (1 + i2)^(-20)) / 19
  n_iter = n_iter + 1
}
i2
```

```
## [1] 0.004954139
```

```
paste('The number of iterations needed is ',n_iter)
```

```
## [1] "The number of iterations needed is 74"
```

### Section 4.1.5

#### Exercise 2

Once  $p \geq \sqrt{n}$ , all the factors of the composite numbers have been exhausted, thus all remaining entries in sieve are prime

```

Eratosthenes <- function(n) {
  # Print prime numbers up to n (based on the sieve of Eratosthenes)
  if (n >= 2) {
    sieve <- seq(2, n)
    primes <- c()
    while (length(sieve) > 0) {
      p <- sieve[1]
      primes <- c(primes, p)
      sieve <- sieve[(sieve %% p) != 0]
      if(p>=sqrt(n)) return(c(primes,sieve))
    }
    return(primes)
  } else {
    stop("Input value of n should be at least 2.")
  }
}

```

```
Eratosthenes(30)
```

```
## [1]  2  3  5  7 11 13 17 19 23 29
```

## Section 4.2.1

### Exercise 2

(a)

```

compound.interest <- function(p,i,n) {
  fv = p*(1+i)^n
  return(fv)
}

```

(b)

```

#how much will Mr. Ng have in the bank at the end of 30 months, if he deposits $1000, and the interest
compound.interest(1000,0.01,30)

```

```
## [1] 1347.849
```

### Exercise 3

```

bisection <- function(f, x1, x2) {
  repeat{

    x3 <- (x1 + x2)/2

    if(f(x3) == 0) {
      return(x3)
    }

    if (f(x3)*f(x1) > 0) {
      x1 <- x3
    } else {
      x2 <- x3
    }
  }
}

```

```

    }

    if (abs(x1 - x2) < 1e-15) {
      return((x1 + x2)/2)
    }
  }
}

```

```
bisection(function(x) x^2-4,1,3)
```

```
## [1] 2
```

## Section 4.4.1

### Exercise 1

```

mergesort <- function (x, decreasing=FALSE) {
  len <- length(x)
  if (len<2) result<-x
  else {
    y <- x[1:(len%/%2)]
    z <- x[(len%/%2+1):len]
    y <- mergesort(y,decreasing)
    z <- mergesort(z,decreasing)
    result <- c()
    while (min(length(y),length(z)) > 0) {
      if ((!decreasing && y[1]<z[1]) || (decreasing && y[1]>z[1])) {
        result <- c(result,y[1])
        y <- y[-1]
      } else {
        result <- c(result,z[1])
        z <- z[-1]
      }
    }

    if (length(y) > 0)
      result <- c(result,y)
    else
      result <- c(result,z)
  }
  return(result)
}

```

```
mergesort(c(1,4,2,7,3,5),TRUE)
```

```
## [1] 7 5 4 3 2 1
```

```
mergesort(c(1,4,2,7,3,5))
```

```
## [1] 1 2 3 4 5 7
```

### Section 4.4.3 (2016 edition, not required)

#### Exercise 1

```
factorial(10)
```

```
## [1] 3628800
```

```
factorial(50)
```

```
## [1] 3.041409e+64
```

```
factorial(1000)
```

```
## Warning in factorial(1000): value out of range in 'gammafn'
```

```
## [1] Inf
```

#### Exercise 2

(a)

```
binom <- function(n,m) {  
  return(factorial(n)/(factorial(n-m)*factorial(m)))  
}
```

(b)

```
binom(4,2)
```

```
## [1] 6
```

```
binom(50,20)
```

```
## [1] 4.712921e+13
```

```
binom(5000,2000)
```

```
## Warning in factorial(n): value out of range in 'gammafn'
```

```
## Warning in factorial(n - m): value out of range in 'gammafn'
```

```
## Warning in factorial(m): value out of range in 'gammafn'
```

```
## [1] NaN
```

(c)

```
binom_new <- function(n,m) {  
  return(exp(sum(log(1:n))-sum(log(1:(n-m)))-sum(log(1:m))))  
}
```

(d)

```
binom_new(4,2)
```

```
## [1] 6
```

```
binom_new(50,20)
```

```
## [1] 4.712921e+13
```

```
binom_new(5000,2000)
```

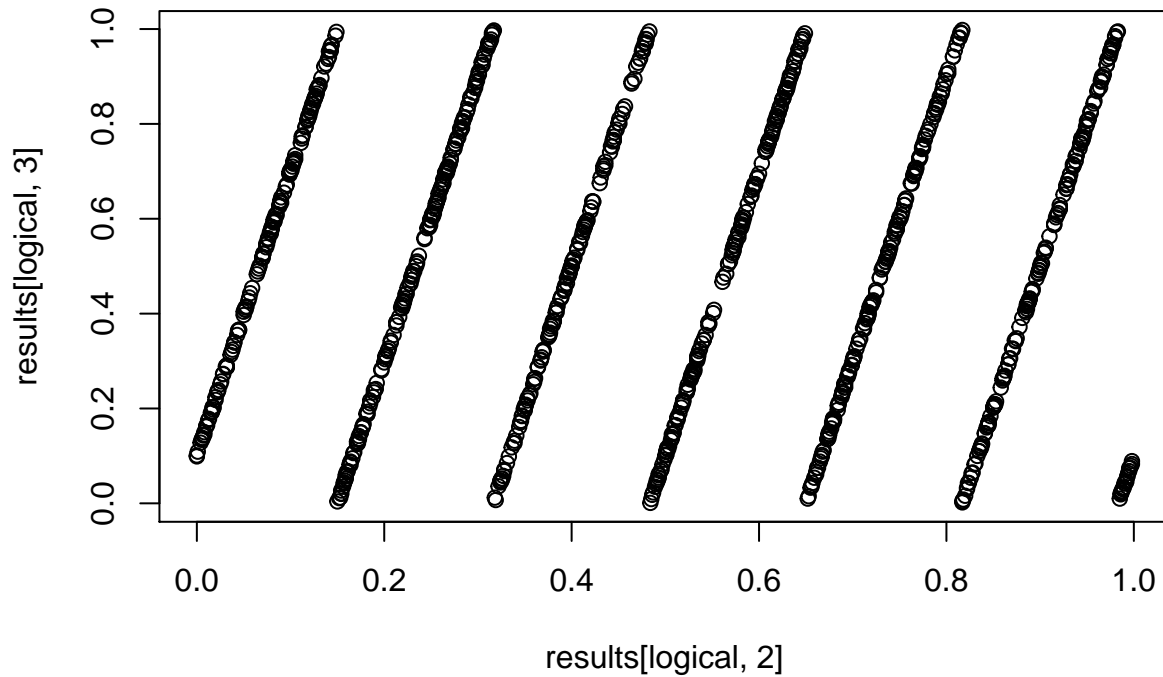
```
## [1] Inf
```

## Chapter 4 (2016 edition)

### Exercise 1

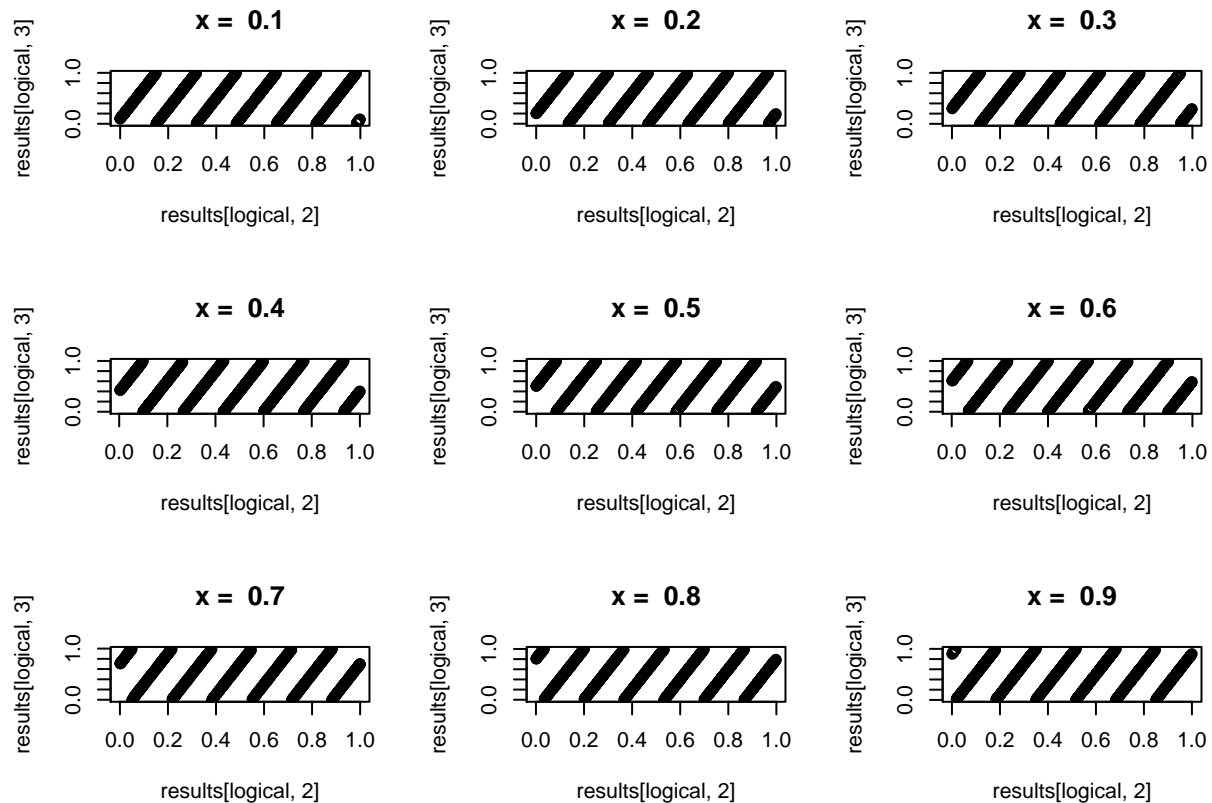
```
results <- numeric(3000000)
x4 <- 123
for (i in 1:3000000) {
  x4 <- (65539*x4) %% (2^31)
  results[i] <- x4 / (2^31)
}
results <- matrix(round(results, 3), ncol = 3, byrow = TRUE)

logical<-results[,1]==0.1
plot(results[logical,2],results[logical,3])
```



```
par(mfrow = c(3, 3))

for (i in seq(0.1,0.9,0.1)) {
  logical<-results[,1]==round(i,3)
  plot(results[logical,2],results[logical,3],main=paste("x = ",i))
}
```



## Exercise 2

```
directpoly <- function(x, coeff){
  n <- length(coeff)
  y <- 0
  for(i in 1:n) {
    y <- y + coeff[i]*x^(n-i)
  }
  return(y)
}
```

```
directpoly(2,1:3)
```

```
## [1] 11
```

## Exercise 3

```
hornerpoly <- function(x, coeff){
  n <- length(coeff)
  a <- rep(coeff[1], length(x))
  for (i in (n-1):1) {
    a <- a*x + coeff[n-i+1]
  }
  return(a)
}
```

```
hornerpoly(2,1:3)
```

```
## [1] 11
```