

Accuracy Report

Weidi Pan

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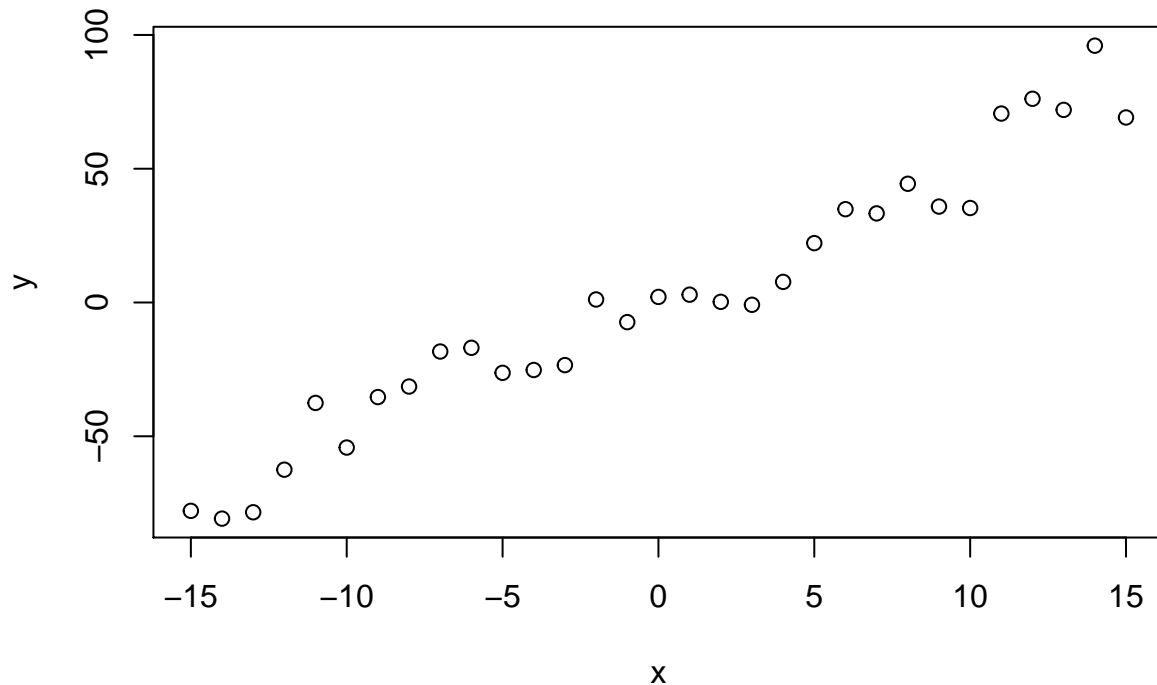
```
source("functions.R")

trueA <- 5   #true slope
trueB <- 0   #true intercept
trueSd <- 10 #true standard deviation of error
sampleSize <- 31 #sample size

# create independent x-values
x <- (-(sampleSize-1)/2):((sampleSize-1)/2) # n=sampleSize
# create dependent values according to  $ax + b + N(0, sd)$ 
y <- trueA * x + trueB + rnorm(n=sampleSize, mean=0, sd=trueSd)

plot(x, y, main="Test Data")
```

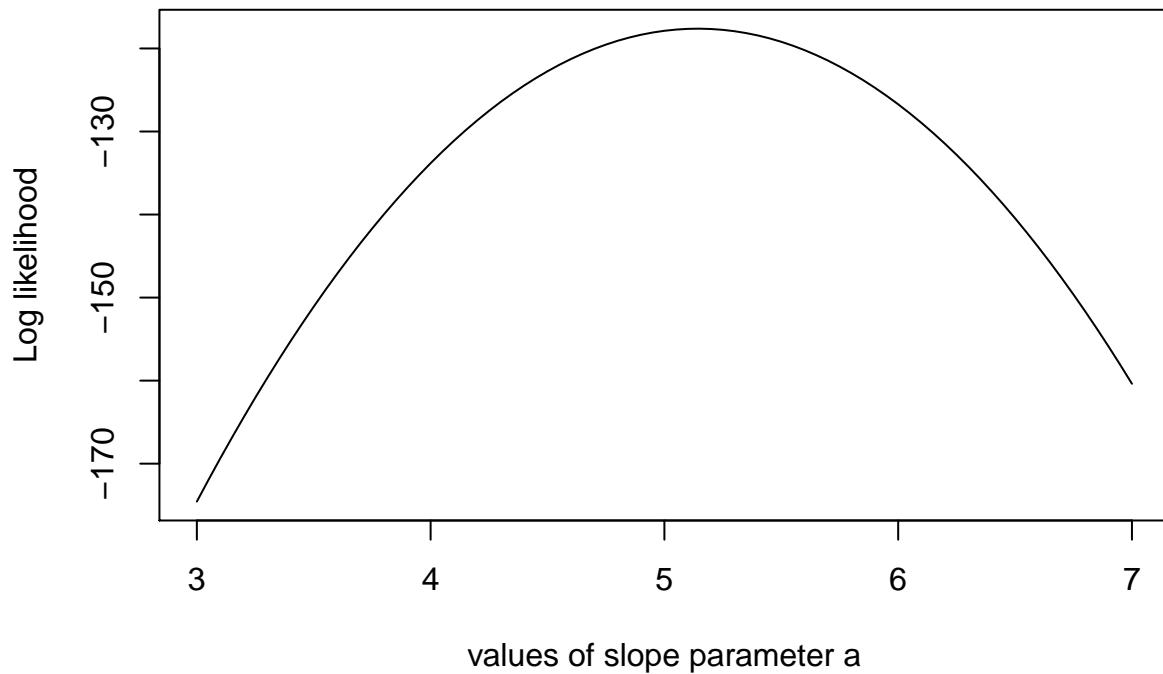
Test Data



```
#balanced x values around zero to "de-correlate" slope and intercept
#a scatterplot of test data
```

```
# Example: plot the likelihood profile of the slope a
```

```
slopelikelihoods <- lapply(seq(3, 7, by=.05), slopevalues) #applies the function on a vector of slopes
plot (seq(3, 7, by=.05), slopelikelihoods , type="l", xlab = "values of slope parameter a", ylab = "Log
```



#plot log likelihoods against different values of slope parameter a

Metropolis algorithm

startvalue = c(4,0,10) *#starting value of the procedure*

chain = run_metropolis_MCMC(startvalue, 10000) *#inputs startvalue and number of iterations, outputs matrix*

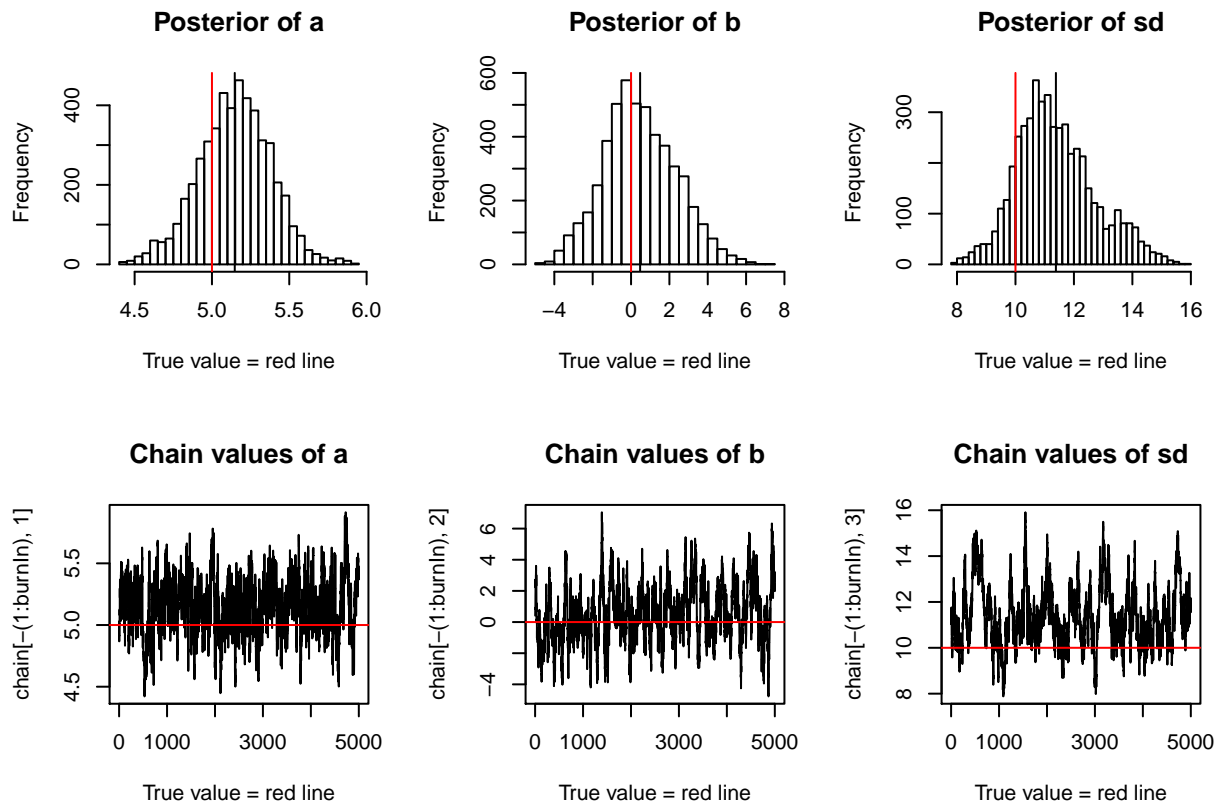
burnIn = 5000

*#The first steps of the algorithm may be biased by the initial value,
#and are therefore usually discarded for the further analysis (burn-in time)*

acceptance = 1-mean(duplicated(chain[-(1:burnIn),])) *# acceptance rate*

Summary:

graph_summary(chain,burnIn,trueA,trueB,trueSd)



for comparison:

```
summary(lm(y~x))
```

```
##
## Call:
## lm(formula = y ~ x)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -17.169  -8.864  -1.667   9.449  23.104
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   0.8846     1.9803   0.447   0.658
## x             5.1430     0.2214  23.229 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 11.03 on 29 degrees of freedom
## Multiple R-squared:  0.949, Adjusted R-squared:  0.9472
## F-statistic: 539.6 on 1 and 29 DF, p-value: < 2.2e-16
```

#compare this procedure MCMC with linear regression

```
source("functions.R")
```

*#compare_outcomes, that takes as input an iteration number
 #for instance 1000, 10000, or 100000. Your function should loop 10 times; each
 #time, it should initialize the MCMC chain with randomly selected start values
 #for a, b, and sd and then run to completion after the required number of*

*#iterations. After each loop, the function should compute the mean and std
#of the values in the chain for a, and it should print these out. Test your
#function for 1,000, 10,000, and 100,000 iterations.*

```
compare_outcomes <- function(iterations) {  
  for (i in 1:10) {  
    a = runif(1, min=0, max=10)  
    b = rnorm(1, 0, 5)  
    sd = runif(1, min=0, max=30)  
    startvalue=c(a,b,sd)  
    chain = run_metropolis_MCMC(startvalue,iterations)  
    print(c(mean(chain[,1]),sd(chain[,1])))  
  }  
}
```

```
compare_outcomes(1000)
```

```
## [1] 4.9001116 0.7271469  
## [1] 5.0374254 0.4500609  
## [1] 5.1968695 0.3936781  
## [1] 5.3269349 0.8176538  
## [1] 5.4014838 0.8390039  
## [1] 5.0619177 0.2668544  
## [1] 4.987807 0.291718  
## [1] 4.9603720 0.7515964  
## [1] 5.1491683 0.2466659  
## [1] 4.7369434 0.9857535
```

```
compare_outcomes(10000)
```

```
## [1] 5.170628 0.346492  
## [1] 5.1881224 0.4359597  
## [1] 5.1543642 0.2726847  
## [1] 5.1409152 0.2273817  
## [1] 5.1706545 0.3764299  
## [1] 5.1534378 0.3296608  
## [1] 5.1337848 0.2318604  
## [1] 5.1383639 0.2209119  
## [1] 5.1631443 0.2889778  
## [1] 5.1493873 0.2520079
```

```
compare_outcomes(100000)
```

```
## [1] 5.1404316 0.2385761  
## [1] 5.146323 0.232953  
## [1] 5.1408837 0.2438869  
## [1] 5.1495599 0.2316727  
## [1] 5.1415549 0.2364506  
## [1] 5.1358966 0.2411718  
## [1] 5.1525921 0.2592225  
## [1] 5.1384591 0.2433755  
## [1] 5.1457031 0.2410367  
## [1] 5.1445782 0.2461923
```

From the outputs above, we can see that as iterations grow larger, the values of mean of A are more stable,

and standard deviations become smaller.

$n = 1000$, mean ranges from 4.60 to 5.16, sd ranges from 0.19 to 1.03 $n = 10000$, mean ranges from 4.82 to 4.88, sd ranges from 0.19 to 0.44 $n = 100000$, mean ranges from 4.85 to 4.87, sd ranges from 0.20 to 0.25

Thus, the accuracy of this algorithm in finding A increases as iterations grow; accordingly, the time to process also increases