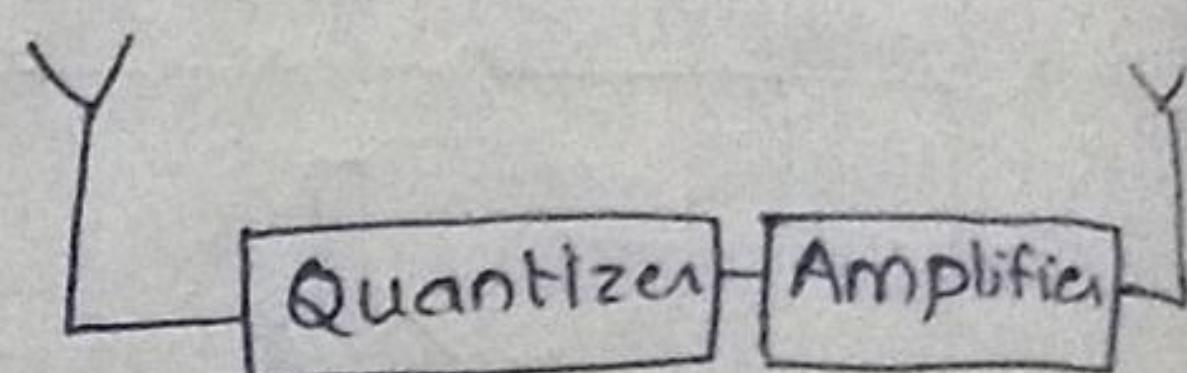


→ Problems (2) {4, 5}

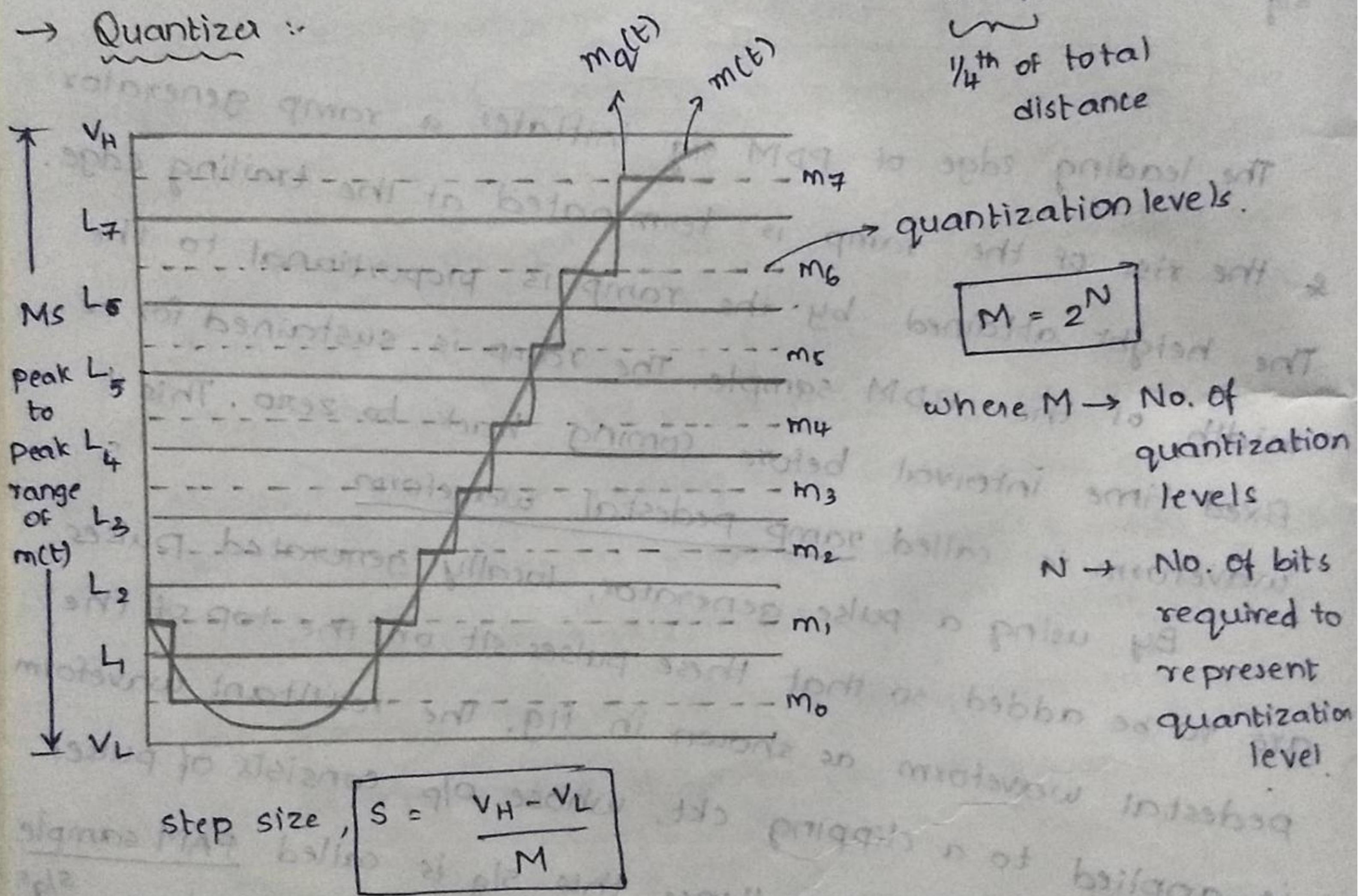
→ Repeater : Repeater is used to improve S/N ratio.

Quantizer is used to reduce the noise of small amplitudes. Thus finally, the repeater can increase sig power or sig strength.



Hardware of repeater

→ Quantizer :



$$e^2(t) = \frac{s^2}{12} \quad \text{where } m(t) \text{ is original sig} \\ m_q(t) \text{ is quantized sig}$$

For uniform quantizer, mean square quantization error is

$$\overline{e^2(t)} = \frac{s^2}{12}$$

$$\left\{ N_q \times e(t) \approx s \times \frac{1}{M} \right\}$$

∴ In order to reduce the error, the step size 's' should be reduced, so that we have to select large value of M.

$$\left\{ e \downarrow \Rightarrow s \downarrow \Rightarrow M \uparrow \right\}$$

→ Quantization error derivation.

→ Problems (3) { repeater calculation. }

→ Note: As long as the noise has an instantaneous amplitude $< S/2$, the noise will not appear at the o/p. But if this noise exceeds $S/2$, an error in level will occur.

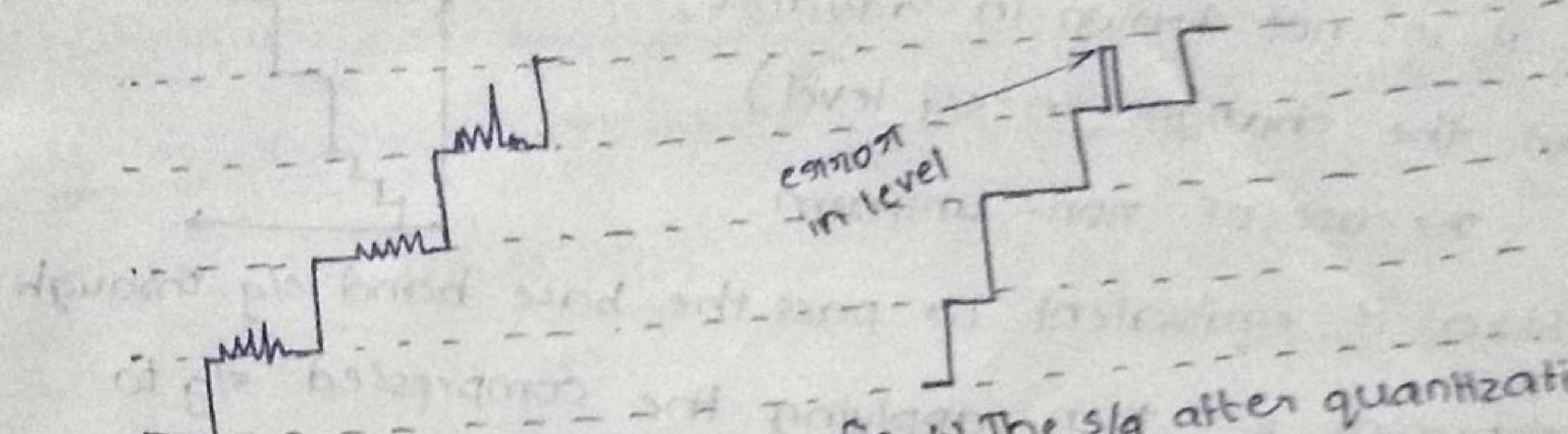


fig a) A quantized sig with added noise.

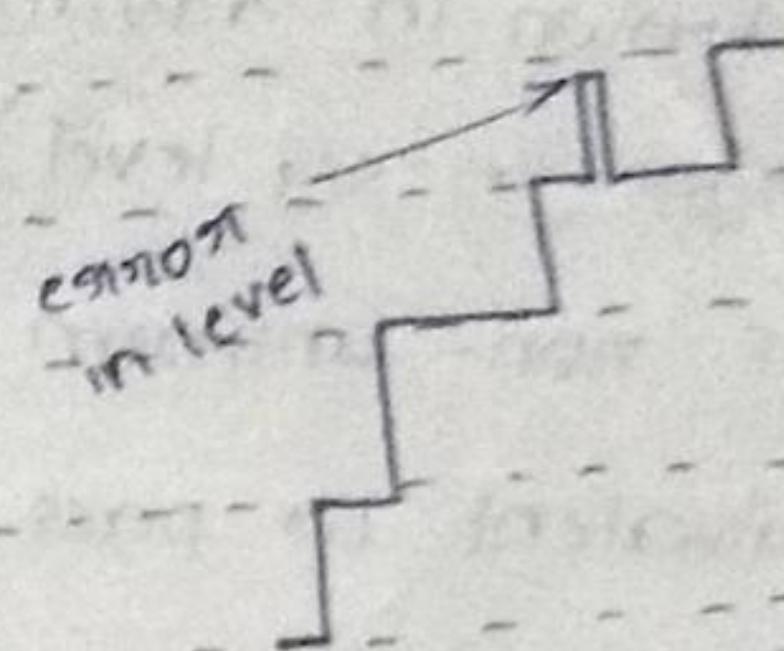


fig b) The sig after quantization, one instance is recorded in which the noise level is so large that an error results.

→ Quantization error

→ Companding "

The difference b/w the original sig & quantized sig may be viewed as quantization noise & is called quantization error.

$$e(t) = m(t) - m_q(t)$$

Mean-square quantization error :- $\overline{e^2(t)} = \frac{s^2}{12}$

This error results in quantization noise (N_q)

$\therefore N_q \propto s$ where s is step size. Therefore in order to reduce the quantization error, the step size must be as low as possible. This can be achieved by increasing no. of quantization levels 'M'.

In most cases, volume of human speech is very low & in very rare cases, the volume is high. The range of voltages covered by voice sigs from the peak of loud sigs to the peak of weak sigs is in the order of 1000 to 1.

By using a uniform quantizer, since the step size is fixed, N_q is same for every quantized sig level which gives rise to low avg SNR. So in order to improve avg SNR, we use non-uniform quantizer which increases

the step size for s/gs of large amplitude, while it decreases the step size for s/gs of small amplitudes. But in practice, it is difficult to implement the non-uniform quantizer (since it is not known in advance, about the changes in s/g level)

The use of non-uniform

quantizer is equivalent to pass the base band s/g through a compressor & then applying the compressed s/g to a uniform quantizer.

This compressed & quantized

s/g is fixed through a channel &

this compression produces s/g

distortion. To undo this distortion

at the Rxer, the recovered s/g

is passed through an expander

n/w. An expander n/w has an

i/p - o/p characteristic which

is the reverse characteristic

of compressor. Finally, an o/p

s/g is generated without distortion due to this reverse

characteristics of compressor & expander.

Thus the compression of s/g at the Txer & expansion at Rxer is called companding.

From fig 2), for small amplitude s/gs there

is great improvement

in SNR, but for large

amp s/gs over a slight range

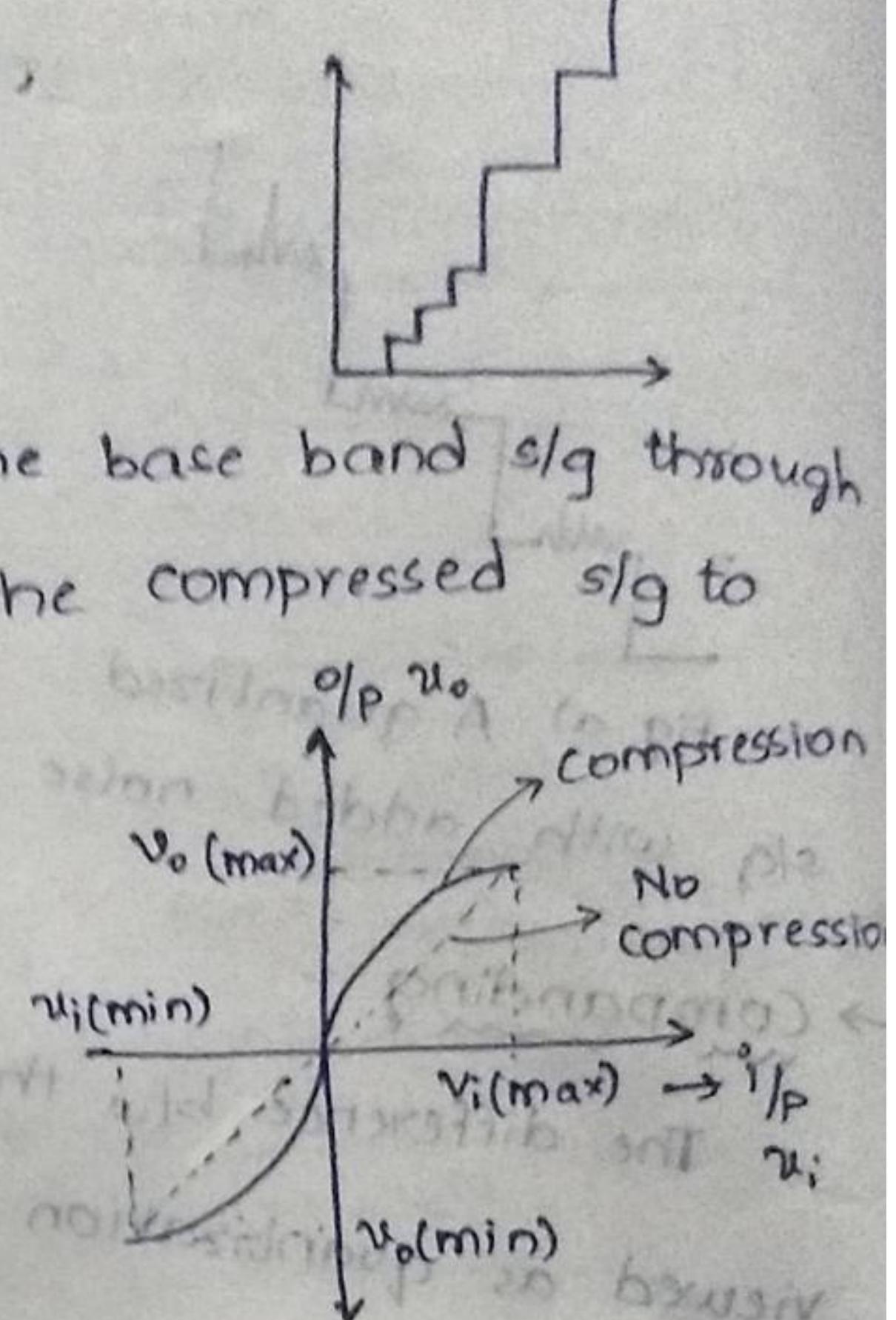


fig.. An i/p - o/p characteristic which provides compression.

From above fig., slope is larger at low amps than at larger amplitudes.

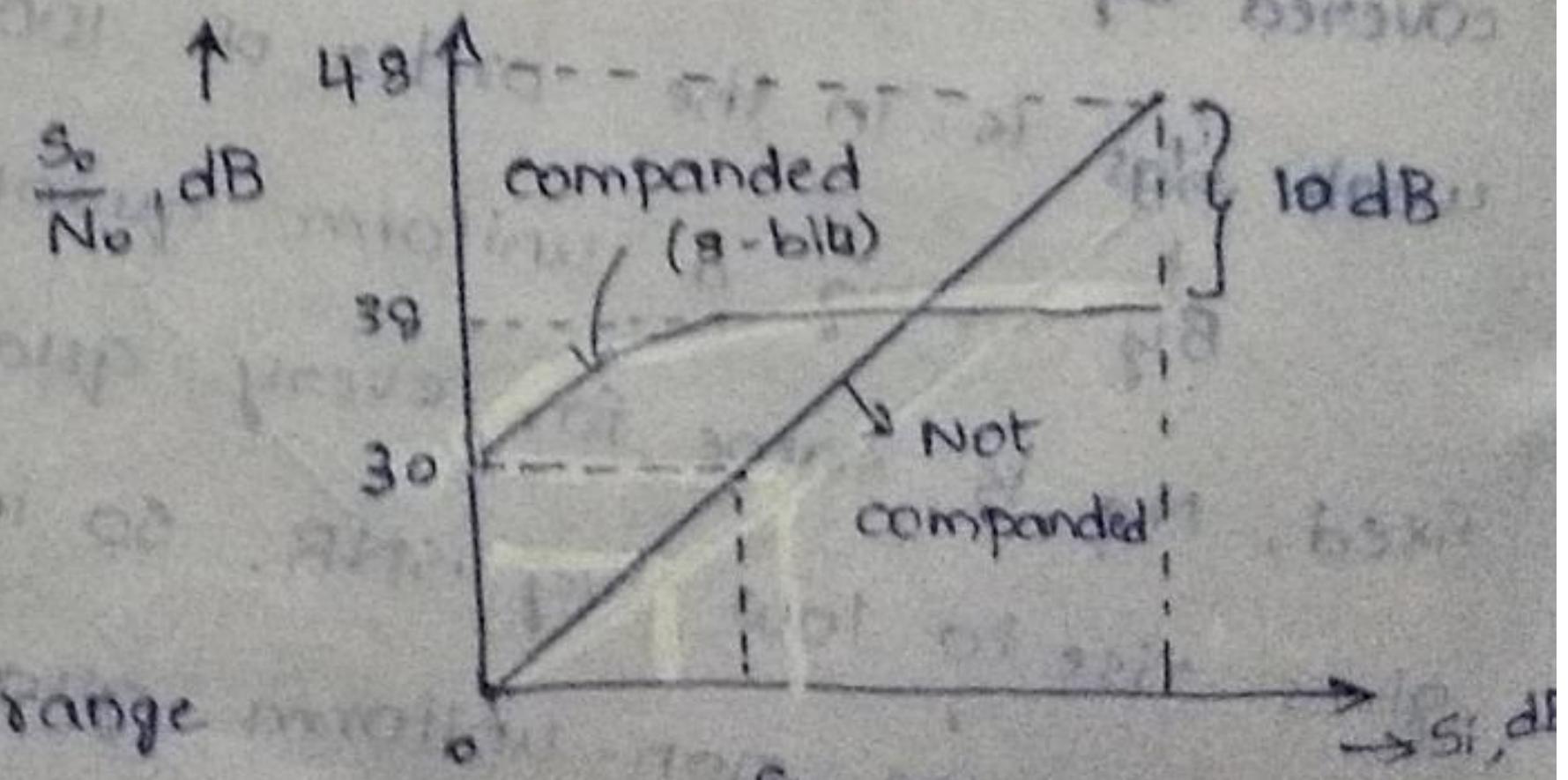


fig. 2)

at peak sigs, a slight reduction in SNR is observed.

A particular form of compression laws are in use, the following expressions specifies μ -law & A-law compression techniques.

μ -law (U.S., Canada, Japan)

$$|v_o| = \frac{\log(1 + \mu|v_i|)}{\log(1 + \mu)}$$

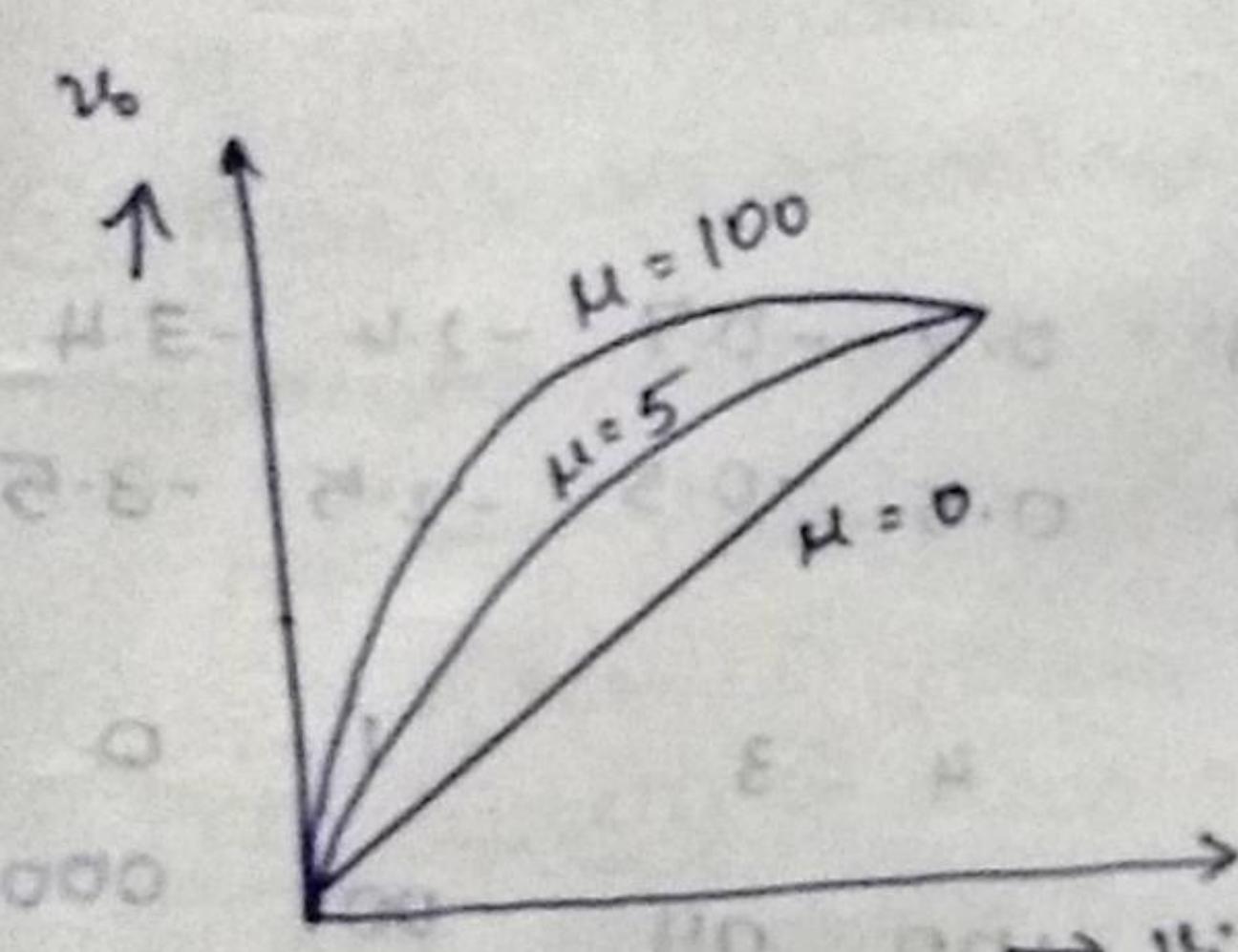


fig :- compressor characteristic of μ -Law compressor.

This law is used in US, Canada, Japan.

If the sig is compressed at

Txer, then it is expanded at the Rxer. Then the combination of compression & expansion is called companding.

A-law (rest of world)

$$|v_o| = A|v_i| ; 0 \leq |v_i| \leq \frac{1}{A}$$

$$= \frac{1 + \log(A|v_i|)}{1 + \log A} ; \frac{1}{A} \leq |v_i| \leq 1$$

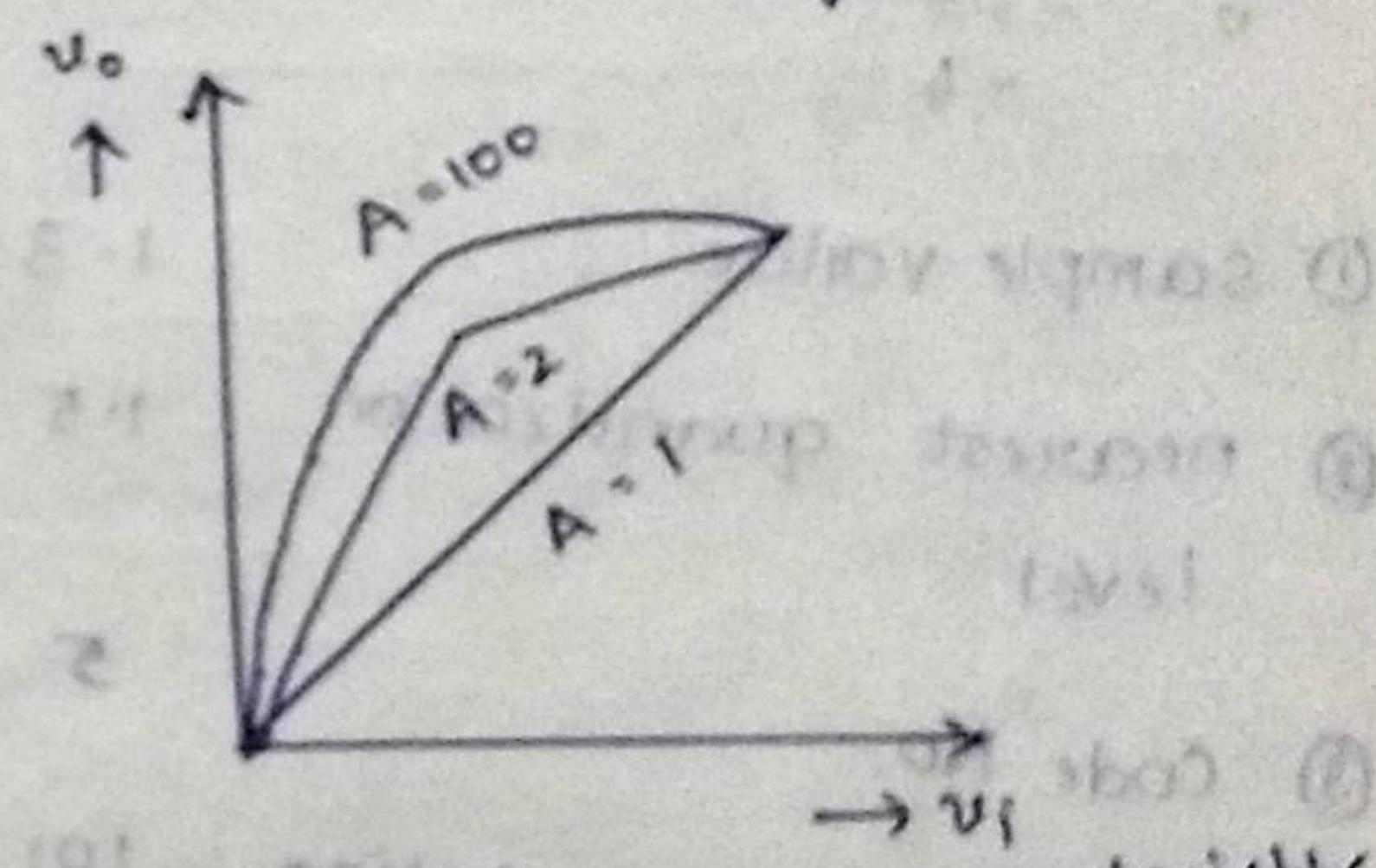


fig :- compressor characteristic of A-law compressor

This law is not used in US, Japan & Canada & used in rest of the world.