Online Retail Data Clustering

February 19, 2026

1 IMPORTING THE REQUIRED LIBRARIES

[1]:
```
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns

from sklearn.cluster import KMeans
from sklearn.metrics import silhouette_score
from sklearn.preprocessing import StandardScaler

# Setting to make numbers easier to read on display
pd.options.display.float_format = '{:20.2f}'.format

# Show all columns on output
pd.set_option('display.max_columns', 999)
```

[2]:
```
df = pd.read_excel("online_retail_II.xlsx", sheet_name=0)

df.head(10)
```

[2]:

	Invoice	StockCode	Description	Quantity	InvoiceDate	Price	Customer ID
0	489434	85048	15CM CHRISTMAS GLASS BALL 20 LIGHTS	12	2009-12-01 07:45:00	6.95	13085.00
1	489434	79323P	PINK CHERRY LIGHTS	12	2009-12-01 07:45:00	6.75	13085.00
2	489434	79323W	WHITE CHERRY LIGHTS	12	2009-12-01 07:45:00	6.75	13085.00
3	489434	22041	RECORD FRAME 7" SINGLE SIZE	48	2009-12-01 07:45:00	2.10	13085.00
4	489434	21232	STRAWBERRY CERAMIC TRINKET BOX	24			
5	489434	22064	PINK DOUGHNUT TRINKET POT	24			
6	489434	21871	SAVE THE PLANET MUG	24			
7	489434	21523	FANCY FONT HOME SWEET HOME DOORMAT	10			
8	489435	22350	CAT BOWL	12			
9	489435	22349	DOG BOWL , CHASING BALL DESIGN	12			

```
4 2009-12-01 07:45:00                1.25             13085.00
5 2009-12-01 07:45:00                1.65             13085.00
6 2009-12-01 07:45:00                1.25             13085.00
7 2009-12-01 07:45:00                5.95             13085.00
8 2009-12-01 07:46:00                2.55             13085.00
9 2009-12-01 07:46:00                3.75             13085.00

          Country
0  United Kingdom
1  United Kingdom
2  United Kingdom
3  United Kingdom
4  United Kingdom
5  United Kingdom
6  United Kingdom
7  United Kingdom
8  United Kingdom
9  United Kingdom
```

2 EXPLORATORY DATA ANALYSIS

[3]:
```
df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 525461 entries, 0 to 525460
Data columns (total 8 columns):
 #   Column       Non-Null Count   Dtype
---  ------       --------------   -----
 0   Invoice      525461 non-null  object
 1   StockCode    525461 non-null  object
 2   Description  522533 non-null  object
 3   Quantity     525461 non-null  int64
 4   InvoiceDate  525461 non-null  datetime64[ns]
 5   Price        525461 non-null  float64
 6   Customer ID  417534 non-null  float64
 7   Country      525461 non-null  object
dtypes: datetime64[ns](1), float64(2), int64(1), object(4)
memory usage: 32.1+ MB
```

[4]:
```
df.describe()
```

[4]:
```
                 Quantity                    InvoiceDate  \
count          525461.00                         525461
mean               10.34  2010-06-28 11:37:36.845017856
min             -9600.00            2009-12-01 07:45:00
25%                 1.00            2010-03-21 12:20:00
50%                 3.00            2010-07-06 09:51:00
```

```
75%                  10.00            2010-10-15 12:45:00
max                19152.00            2010-12-09 20:01:00
std                  107.42                            NaN

                       Price          Customer ID
count             525461.00            417534.00
mean                   4.69             15360.65
min                -53594.36             12346.00
25%                    1.25             13983.00
50%                    2.10             15311.00
75%                    4.21             16799.00
max                25111.09             18287.00
std                  146.13              1680.81
```

[9]:
```
df.describe(include="O")
```

[9]:
```
        Invoice StockCode                         Description         Country
count    525461    525461                              522533          525461
unique    28816      4632                                4681              40
top      537434    85123A  WHITE HANGING HEART T-LIGHT HOLDER  United Kingdom
freq        675      3516                                3549          485852
```

[10]:
```
df[df["Customer ID"].isna()].head(10)
```

[10]:
```
     Invoice StockCode                      Description  Quantity  \
263   489464     21733                85123a mixed         -96
283   489463     71477                       short         -240
284   489467    85123A                21733 mixed         -192
470   489521     21646                         NaN         -50
577   489525    85226C     BLUE PULL BACK RACING CAR           1
578   489525     85227   SET/6 3D KIT CARDS FOR KIDS           1
1055  489548     22271          FELTCRAFT DOLL ROSIE           1
1056  489548     22254          FELT TOADSTOOL LARGE          12
1057  489548     22273          FELTCRAFT DOLL MOLLY           3
1058  489548     22195  LARGE HEART MEASURING SPOONS           1

              InvoiceDate  Price  Customer ID         Country
263   2009-12-01 10:52:00   0.00          NaN  United Kingdom
283   2009-12-01 10:52:00   0.00          NaN  United Kingdom
284   2009-12-01 10:53:00   0.00          NaN  United Kingdom
470   2009-12-01 11:44:00   0.00          NaN  United Kingdom
577   2009-12-01 11:49:00   0.55          NaN  United Kingdom
578   2009-12-01 11:49:00   0.85          NaN  United Kingdom
1055  2009-12-01 12:32:00   2.95          NaN  United Kingdom
1056  2009-12-01 12:32:00   1.25          NaN  United Kingdom
1057  2009-12-01 12:32:00   2.95          NaN  United Kingdom
1058  2009-12-01 12:32:00   1.65          NaN  United Kingdom
```

[11]:
```
df[df["Quantity"]<0].head(10)
```

[11]:

	Invoice	StockCode	Description	Quantity	\
178	C489449	22087	PAPER BUNTING WHITE LACE	-12	
179	C489449	85206A	CREAM FELT EASTER EGG BASKET	-6	
180	C489449	21895	POTTING SHED SOW 'N' GROW SET	-4	
181	C489449	21896	POTTING SHED TWINE	-6	
182	C489449	22083	PAPER CHAIN KIT RETRO SPOT	-12	
183	C489449	21871	SAVE THE PLANET MUG	-12	
184	C489449	84946	ANTIQUE SILVER TEA GLASS ETCHED	-12	
185	C489449	84970S	HANGING HEART ZINC T-LIGHT HOLDER	-24	
186	C489449	22090	PAPER BUNTING RETRO SPOTS	-12	
196	C489459	90200A	PURPLE SWEETHEART BRACELET	-3	

	InvoiceDate	Price	Customer ID	\
178	2009-12-01 10:33:00	2.95	16321.00	
179	2009-12-01 10:33:00	1.65	16321.00	
180	2009-12-01 10:33:00	4.25	16321.00	
181	2009-12-01 10:33:00	2.10	16321.00	
182	2009-12-01 10:33:00	2.95	16321.00	
183	2009-12-01 10:33:00	1.25	16321.00	
184	2009-12-01 10:33:00	1.25	16321.00	
185	2009-12-01 10:33:00	0.85	16321.00	
186	2009-12-01 10:33:00	2.95	16321.00	
196	2009-12-01 10:44:00	4.25	17592.00	

	Country
178	Australia
179	Australia
180	Australia
181	Australia
182	Australia
183	Australia
184	Australia
185	Australia
186	Australia
196	United Kingdom

[13]:
```
df["Invoice"]=df["Invoice"].astype("str")
df[df["Invoice"].str.match("\\d{6}$") == False]
```

[13]:

	Invoice	StockCode	Description	Quantity	\
178	C489449	22087	PAPER BUNTING WHITE LACE	-12	
179	C489449	85206A	CREAM FELT EASTER EGG BASKET	-6	
180	C489449	21895	POTTING SHED SOW 'N' GROW SET	-4	
181	C489449	21896	POTTING SHED TWINE	-6	
182	C489449	22083	PAPER CHAIN KIT RETRO SPOT	-12	

```
…          …       …                                    …        …
524695  C538123     22956          36 FOIL HEART CAKE CASES        -2
524696  C538124         M                           Manual        -4
524697  C538124     22699  ROSES REGENCY TEACUP AND SAUCER         -1
524698  C538124     22423           REGENCY CAKESTAND 3 TIER        -1
525282  C538164    35004B       SET OF 3 BLACK FLYING DUCKS        -1

                InvoiceDate                Price          Customer ID  \
178     2009-12-01 10:33:00                 2.95             16321.00
179     2009-12-01 10:33:00                 1.65             16321.00
180     2009-12-01 10:33:00                 4.25             16321.00
181     2009-12-01 10:33:00                 2.10             16321.00
182     2009-12-01 10:33:00                 2.95             16321.00
…                       …                  …                   …
524695 2010-12-09 15:41:00                 2.10             12605.00
524696 2010-12-09 15:43:00                 0.50             15329.00
524697 2010-12-09 15:43:00                 2.95             15329.00
524698 2010-12-09 15:43:00                12.75             15329.00
525282 2010-12-09 17:32:00                 1.95             14031.00

                Country
178           Australia
179           Australia
180           Australia
181           Australia
182           Australia
…                   …
524695          Germany
524696   United Kingdom
524697   United Kingdom
524698   United Kingdom
525282   United Kingdom

[10209 rows x 8 columns]
```

[14]:
```
df["Invoice"].str.replace("[0-9]","",regex=True).unique()
```

[14]:
```
array(['', 'C', 'A'], dtype=object)
```

[16]:
```
df[df["Invoice"].str.startswith("A")]
```

[16]:
```
        Invoice StockCode      Description  Quantity         InvoiceDate  \
179403  A506401         B  Adjust bad debt         1 2010-04-29 13:36:00
276274  A516228         B  Adjust bad debt         1 2010-07-19 11:24:00
403472  A528059         B  Adjust bad debt         1 2010-10-20 12:04:00

                      Price  Customer ID         Country
```

```
179403            -53594.36          NaN  United Kingdom
276274            -44031.79          NaN  United Kingdom
403472            -38925.87          NaN  United Kingdom
```

[21]:
```
df["StockCode"]=df["StockCode"].astype("str")
df[(df["StockCode"].str.match("^\\d{5}$") == False) & (df["StockCode"].str.
  ↪match("^\\d{5}[a-zA-Z]+$") == False)]["StockCode"].unique()
```

[21]:
```
array(['POST', 'D', 'DCGS0058', 'DCGS0068', 'DOT', 'M', 'DCGS0004',
       'DCGS0076', 'C2', 'BANK CHARGES', 'DCGS0003', 'TEST001',
       'gift_0001_80', 'DCGS0072', 'gift_0001_20', 'DCGS0044', 'TEST002',
       'gift_0001_10', 'gift_0001_50', 'DCGS0066N', 'gift_0001_30',
       'PADS', 'ADJUST', 'gift_0001_40', 'gift_0001_60', 'gift_0001_70',
       'gift_0001_90', 'DCGSSGIRL', 'DCGS0006', 'DCGS0016', 'DCGS0027',
       'DCGS0036', 'DCGS0039', 'DCGS0060', 'DCGS0056', 'DCGS0059', 'GIFT',
       'DCGSLBOY', 'm', 'DCGS0053', 'DCGS0062', 'DCGS0037', 'DCGSSBOY',
       'DCGSLGIRL', 'S', 'DCGS0069', 'DCGS0070', 'DCGS0075', 'B',
       'DCGS0041', 'ADJUST2', '47503J ', 'C3', 'SP1002', 'AMAZONFEE'],
      dtype=object)
```

[22]:
```
df[df["StockCode"].str.contains("^DOT")]
```

[22]:
```
       Invoice StockCode     Description  Quantity         InvoiceDate  \
2379    489597       DOT  DOTCOM POSTAGE         1 2009-12-01 14:28:00
2539    489600       DOT  DOTCOM POSTAGE         1 2009-12-01 14:43:00
2551    489601       DOT  DOTCOM POSTAGE         1 2009-12-01 14:44:00
2571    489602       DOT  DOTCOM POSTAGE         1 2009-12-01 14:45:00
2619    489603       DOT  DOTCOM POSTAGE         1 2009-12-01 14:46:00
…         …       …              …       …                 …
524272  538071       DOT  DOTCOM POSTAGE         1 2010-12-09 14:09:00
524887  538148       DOT  DOTCOM POSTAGE         1 2010-12-09 16:26:00
525000  538149       DOT  DOTCOM POSTAGE         1 2010-12-09 16:27:00
525126  538153       DOT  DOTCOM POSTAGE         1 2010-12-09 16:31:00
525147  538154       DOT  DOTCOM POSTAGE         1 2010-12-09 16:35:00

                     Price  Customer ID         Country
2379                647.19          NaN  United Kingdom
2539                 55.96          NaN  United Kingdom
2551                 68.39          NaN  United Kingdom
2571                 59.35          NaN  United Kingdom
2619                 42.39          NaN  United Kingdom
…                      …          …             …
524272              885.94          NaN  United Kingdom
524887              547.32          NaN  United Kingdom
525000              620.68          NaN  United Kingdom
525126              822.94          NaN  United Kingdom
525147               85.79          NaN  United Kingdom
```

[736 rows x 8 columns]

3 DATA CLEANING

[23]:
```
cleaned_df = df.copy()
```

[24]:
```
cleaned_df["Invoice"]= cleaned_df["Invoice"].astype("str")
mask = (
    cleaned_df["Invoice"].str.match("^\\d{6}$")==True
)
cleaned_df = cleaned_df[mask]
cleaned_df
```

[24]:

	Invoice	StockCode	Description	Quantity	\
0	489434	85048	15CM CHRISTMAS GLASS BALL 20 LIGHTS	12	
1	489434	79323P	PINK CHERRY LIGHTS	12	
2	489434	79323W	WHITE CHERRY LIGHTS	12	
3	489434	22041	RECORD FRAME 7" SINGLE SIZE	48	
4	489434	21232	STRAWBERRY CERAMIC TRINKET BOX	24	
…	…	…	…	…	
525456	538171	22271	FELTCRAFT DOLL ROSIE	2	
525457	538171	22750	FELTCRAFT PRINCESS LOLA DOLL	1	
525458	538171	22751	FELTCRAFT PRINCESS OLIVIA DOLL	1	
525459	538171	20970	PINK FLORAL FELTCRAFT SHOULDER BAG	2	
525460	538171	21931	JUMBO STORAGE BAG SUKI	2	

	InvoiceDate	Price	Customer ID	\
0	2009-12-01 07:45:00	6.95	13085.00	
1	2009-12-01 07:45:00	6.75	13085.00	
2	2009-12-01 07:45:00	6.75	13085.00	
3	2009-12-01 07:45:00	2.10	13085.00	
4	2009-12-01 07:45:00	1.25	13085.00	
…	…	…	…	
525456	2010-12-09 20:01:00	2.95	17530.00	
525457	2010-12-09 20:01:00	3.75	17530.00	
525458	2010-12-09 20:01:00	3.75	17530.00	
525459	2010-12-09 20:01:00	3.75	17530.00	
525460	2010-12-09 20:01:00	1.95	17530.00	

	Country
0	United Kingdom
1	United Kingdom
2	United Kingdom
3	United Kingdom
4	United Kingdom
…	…

```
525456  United Kingdom
525457  United Kingdom
525458  United Kingdom
525459  United Kingdom
525460  United Kingdom

[515252 rows x 8 columns]
```

[26]:
```
cleaned_df["StockCode"]= cleaned_df["StockCode"].astype("str")
mask = (
    (cleaned_df["StockCode"].str.match("^\\d{5}$")==True)
    | (cleaned_df["StockCode"].str.match("^\\d{5}[a-zA-Z]+$")==True)
    | (cleaned_df["StockCode"].str.match("^PADS$") == True)
)

cleaned_df = cleaned_df[mask]
cleaned_df
```

```
C:\Users\udayd\AppData\Local\Temp\ipykernel_8468\3378931196.py:1:
SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
  cleaned_df["StockCode"]= cleaned_df["StockCode"].astype("str")
```

[26]:

	Invoice	StockCode	Description	Quantity	\
0	489434	85048	15CM CHRISTMAS GLASS BALL 20 LIGHTS	12	
1	489434	79323P	PINK CHERRY LIGHTS	12	
2	489434	79323W	WHITE CHERRY LIGHTS	12	
3	489434	22041	RECORD FRAME 7" SINGLE SIZE	48	
4	489434	21232	STRAWBERRY CERAMIC TRINKET BOX	24	
…	…	…	…	…	
525456	538171	22271	FELTCRAFT DOLL ROSIE	2	
525457	538171	22750	FELTCRAFT PRINCESS LOLA DOLL	1	
525458	538171	22751	FELTCRAFT PRINCESS OLIVIA DOLL	1	
525459	538171	20970	PINK FLORAL FELTCRAFT SHOULDER BAG	2	
525460	538171	21931	JUMBO STORAGE BAG SUKI	2	

	InvoiceDate	Price	Customer ID	\
0	2009-12-01 07:45:00	6.95	13085.00	
1	2009-12-01 07:45:00	6.75	13085.00	
2	2009-12-01 07:45:00	6.75	13085.00	
3	2009-12-01 07:45:00	2.10	13085.00	
4	2009-12-01 07:45:00	1.25	13085.00	
…	…	…	…	
525456	2010-12-09 20:01:00	2.95	17530.00	

```
525457 2010-12-09 20:01:00                3.75             17530.00
525458 2010-12-09 20:01:00                3.75             17530.00
525459 2010-12-09 20:01:00                3.75             17530.00
525460 2010-12-09 20:01:00                1.95             17530.00

                Country
0        United Kingdom
1        United Kingdom
2        United Kingdom
3        United Kingdom
4        United Kingdom
…                  …
525456   United Kingdom
525457   United Kingdom
525458   United Kingdom
525459   United Kingdom
525460   United Kingdom

[512796 rows x 8 columns]
```

[28]:
```
cleaned_df.dropna(subset = ["Customer ID"],inplace = True)
```

```
C:\Users\udayd\AppData\Local\Temp\ipykernel_8468\2119709935.py:1:
SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
  cleaned_df.dropna(subset = ["Customer ID"],inplace = True)
```

[29]:
```
cleaned_df.describe()
```

[29]:
```
                  Quantity                    InvoiceDate  \
count             406337.00                         406337
mean                  13.62  2010-07-01 10:11:06.543288320
min                    1.00            2009-12-01 07:45:00
25%                    2.00            2010-03-26 14:01:00
50%                    5.00            2010-07-09 15:48:00
75%                   12.00            2010-10-14 17:09:00
max                 19152.00            2010-12-09 20:01:00
std                    97.00                            NaN

                      Price          Customer ID
count             406337.00            406337.00
mean                   2.99             15373.63
min                    0.00             12346.00
25%                    1.25             14004.00
50%                    1.95             15326.00
```

```
75%                   3.75             16814.00
max                 295.00             18287.00
std                   4.29              1677.37
```

[31]:
```
len(cleaned_df[cleaned_df["Price"] == 0])
```

[31]:
```
28
```

[34]:
```
cleaned_df = cleaned_df[cleaned_df["Price"]> 0.0]
```

[35]:
```
cleaned_df.describe()
```

[35]:
```
                 Quantity                    InvoiceDate  \
count          406309.00                         406309
mean               13.62  2010-07-01 10:14:25.869572352
min                 1.00            2009-12-01 07:45:00
25%                 2.00            2010-03-26 14:01:00
50%                 5.00            2010-07-09 15:48:00
75%                12.00            2010-10-14 17:09:00
max             19152.00            2010-12-09 20:01:00
std                97.00                            NaN

                    Price          Customer ID
count          406309.00            406309.00
mean                2.99             15373.72
min                 0.00             12346.00
25%                 1.25             14006.00
50%                 1.95             15326.00
75%                 3.75             16814.00
max               295.00             18287.00
std                 4.29              1677.33
```

[36]:
```
cleaned_df["Price"].min()
```

[36]:
```
0.001
```

[37]:
```
len(cleaned_df)/len(df)
```

[37]:
```
0.7732429238325965
```

Dropped about 23% of records.

4 FEATURE ENGINEERING

[38]:
```
cleaned_df["SalesLineTotal"] = cleaned_df["Quantity"] * cleaned_df["Price"]

cleaned_df
```

[38]:
```
       Invoice StockCode                          Description  Quantity  \
0       489434     85048  15CM CHRISTMAS GLASS BALL 20 LIGHTS        12
1       489434    79323P                   PINK CHERRY LIGHTS        12
2       489434    79323W                  WHITE CHERRY LIGHTS        12
3       489434     22041         RECORD FRAME 7" SINGLE SIZE         48
4       489434     21232       STRAWBERRY CERAMIC TRINKET BOX        24
…          …       …                                     …       …
525456  538171     22271                 FELTCRAFT DOLL ROSIE         2
525457  538171     22750         FELTCRAFT PRINCESS LOLA DOLL         1
525458  538171     22751       FELTCRAFT PRINCESS OLIVIA DOLL         1
525459  538171     20970   PINK FLORAL FELTCRAFT SHOULDER BAG         2
525460  538171     21931               JUMBO STORAGE BAG SUKI         2

                InvoiceDate                 Price          Customer ID  \
0       2009-12-01 07:45:00                  6.95            13085.00
1       2009-12-01 07:45:00                  6.75            13085.00
2       2009-12-01 07:45:00                  6.75            13085.00
3       2009-12-01 07:45:00                  2.10            13085.00
4       2009-12-01 07:45:00                  1.25            13085.00
…                       …                    …                 …
525456 2010-12-09 20:01:00                  2.95            17530.00
525457 2010-12-09 20:01:00                  3.75            17530.00
525458 2010-12-09 20:01:00                  3.75            17530.00
525459 2010-12-09 20:01:00                  3.75            17530.00
525460 2010-12-09 20:01:00                  1.95            17530.00

                Country       SalesLineTotal
0        United Kingdom                83.40
1        United Kingdom                81.00
2        United Kingdom                81.00
3        United Kingdom               100.80
4        United Kingdom                30.00
…                   …                    …
525456   United Kingdom                 5.90
525457   United Kingdom                 3.75
525458   United Kingdom                 3.75
525459   United Kingdom                 7.50
525460   United Kingdom                 3.90

[406309 rows x 9 columns]
```

[39]:
```
aggregated_df = cleaned_df.groupby(by="Customer ID", as_index=False) \
    .agg(
        MonetaryValue=("SalesLineTotal", "sum"),
        Frequency=("Invoice", "nunique"),
        LastInvoiceDate=("InvoiceDate", "max")
    )
```

```
aggregated_df.head(5)
```

[39]:

	Customer ID	MonetaryValue	Frequency	LastInvoiceDate
0	12346.00	169.36	2	2010-06-28 13:53:00
1	12347.00	1323.32	2	2010-12-07 14:57:00
2	12348.00	221.16	1	2010-09-27 14:59:00
3	12349.00	2221.14	2	2010-10-28 08:23:00
4	12351.00	300.93	1	2010-11-29 15:23:00

[40]:
```
max_invoice_date = aggregated_df["LastInvoiceDate"].max()

aggregated_df["Recency"] = (max_invoice_date -␣
 ↪aggregated_df["LastInvoiceDate"]).dt.days

aggregated_df.head(5)
```

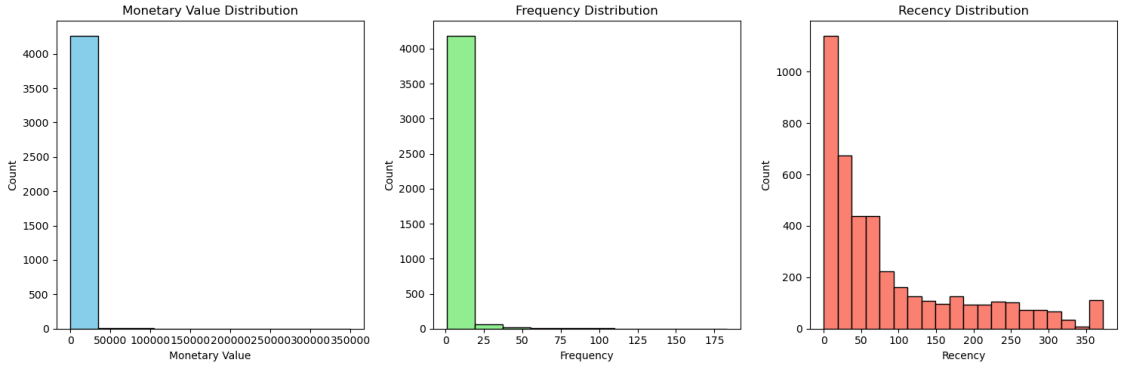
[40]:

	Customer ID	MonetaryValue	Frequency	LastInvoiceDate	\
0	12346.00	169.36	2	2010-06-28 13:53:00	
1	12347.00	1323.32	2	2010-12-07 14:57:00	
2	12348.00	221.16	1	2010-09-27 14:59:00	
3	12349.00	2221.14	2	2010-10-28 08:23:00	
4	12351.00	300.93	1	2010-11-29 15:23:00	

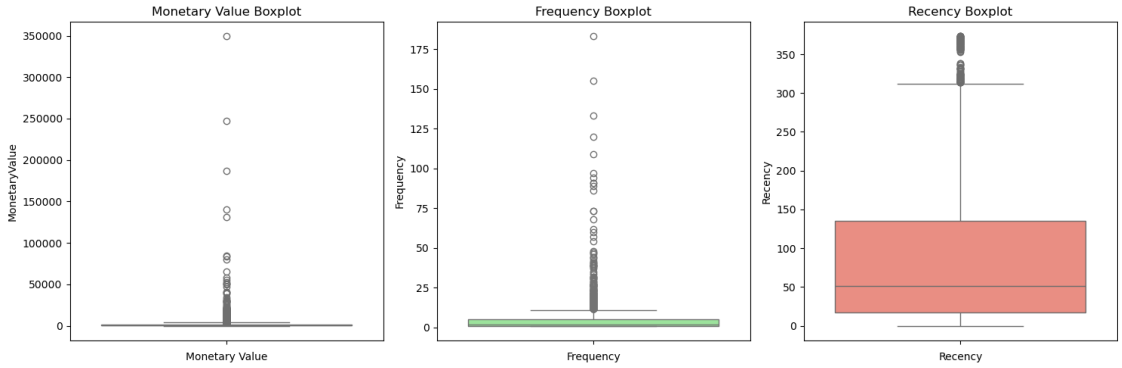
	Recency
0	164
1	2
2	73
3	42
4	10

[41]:
```
plt.figure(figsize=(15, 5))

plt.subplot(1, 3, 1)
plt.hist(aggregated_df['MonetaryValue'], bins=10, color='skyblue',␣
 ↪edgecolor='black')
plt.title('Monetary Value Distribution')
plt.xlabel('Monetary Value')
plt.ylabel('Count')

plt.subplot(1, 3, 2)
plt.hist(aggregated_df['Frequency'], bins=10, color='lightgreen',␣
 ↪edgecolor='black')
plt.title('Frequency Distribution')
plt.xlabel('Frequency')
plt.ylabel('Count')
```

```
plt.subplot(1, 3, 3)
plt.hist(aggregated_df['Recency'], bins=20, color='salmon', edgecolor='black')
plt.title('Recency Distribution')
plt.xlabel('Recency')
plt.ylabel('Count')

plt.tight_layout()
plt.show()
```



[42]:
```
plt.figure(figsize=(15, 5))

plt.subplot(1, 3, 1)
sns.boxplot(data=aggregated_df['MonetaryValue'], color='skyblue')
plt.title('Monetary Value Boxplot')
plt.xlabel('Monetary Value')

plt.subplot(1, 3, 2)
sns.boxplot(data=aggregated_df['Frequency'], color='lightgreen')
plt.title('Frequency Boxplot')
plt.xlabel('Frequency')

plt.subplot(1, 3, 3)
sns.boxplot(data=aggregated_df['Recency'], color='salmon')
plt.title('Recency Boxplot')
plt.xlabel('Recency')

plt.tight_layout()
plt.show()
```



[43]:
```
M_Q1 = aggregated_df["MonetaryValue"].quantile(0.25)
M_Q3 = aggregated_df["MonetaryValue"].quantile(0.75)
M_IQR = M_Q3 - M_Q1

monetary_outliers_df = aggregated_df[(aggregated_df["MonetaryValue"] > (M_Q3 +␣
↪1.5 * M_IQR)) | (aggregated_df["MonetaryValue"] < (M_Q1 - 1.5 * M_IQR))].
↪copy()

monetary_outliers_df.describe()
```

[43]:

	Customer ID	MonetaryValue	Frequency	\
count	423.00	423.00	423.00	
mean	15103.04	12188.10	17.17	
min	12357.00	3802.04	1.00	
25%	13622.00	4605.94	8.00	
50%	14961.00	6191.32	12.00	
75%	16692.00	10273.24	18.00	
max	18260.00	349164.35	183.00	
std	1728.66	25830.85	19.73	

	LastInvoiceDate	Recency
count	423	423.00
mean	2010-11-09 12:26:02.978723328	30.04
min	2009-12-10 18:03:00	0.00
25%	2010-11-08 13:17:30	3.00
50%	2010-11-26 12:19:00	13.00
75%	2010-12-06 10:34:30	31.00
max	2010-12-09 19:32:00	364.00
std	NaN	51.54

[44]:
```
F_Q1 = aggregated_df['Frequency'].quantile(0.25)
F_Q3 = aggregated_df['Frequency'].quantile(0.75)
F_IQR = F_Q3 - F_Q1
```

```
frequency_outliers_df = aggregated_df[(aggregated_df['Frequency'] > (F_Q3 + 1.5␣
↪* F_IQR)) | (aggregated_df['Frequency'] < (F_Q1 - 1.5 * F_IQR))].copy()

frequency_outliers_df.describe()
```

[44]:

	Customer ID	MonetaryValue	Frequency	\
count	279.00	279.00	279.00	
mean	15352.66	14409.71	23.81	
min	12437.00	1094.39	12.00	
25%	13800.00	4331.56	13.00	
50%	15465.00	6615.77	17.00	
75%	16828.50	11692.41	23.00	
max	18260.00	349164.35	183.00	
std	1748.43	31381.74	21.93	

	LastInvoiceDate	Recency
count	279	279.00
mean	2010-11-23 11:06:20.645161216	16.09
min	2010-05-12 16:51:00	0.00
25%	2010-11-20 13:14:30	2.00
50%	2010-12-02 10:46:00	7.00
75%	2010-12-07 11:08:30	19.00
max	2010-12-09 19:32:00	211.00
std	NaN	26.59

[47]:
```
non_outliers_df = aggregated_df[(~aggregated_df.index.isin(monetary_outliers_df.
↪index)) & (~aggregated_df.index.isin(frequency_outliers_df.index))]

non_outliers_df.describe()
```

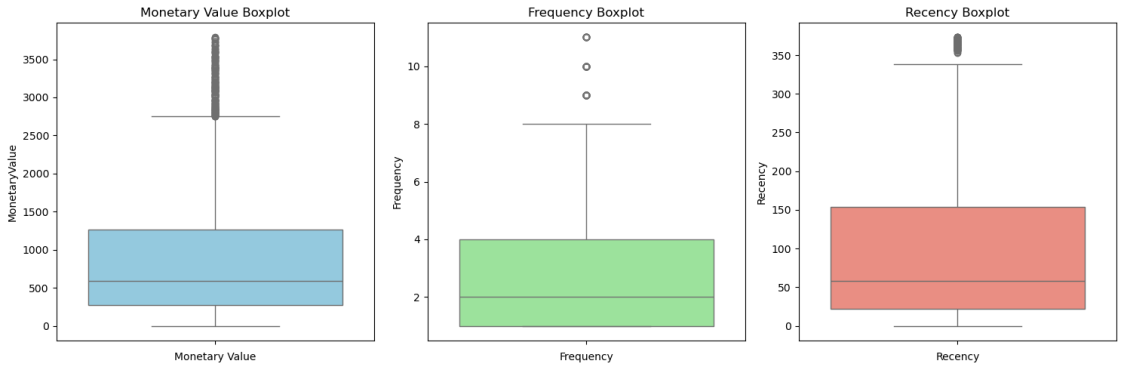
[47]:

	Customer ID	MonetaryValue	Frequency	\
count	3809.00	3809.00	3809.00	
mean	15376.48	885.50	2.86	
min	12346.00	1.55	1.00	
25%	13912.00	279.91	1.00	
50%	15389.00	588.05	2.00	
75%	16854.00	1269.05	4.00	
max	18287.00	3788.21	11.00	
std	1693.20	817.67	2.24	

	LastInvoiceDate	Recency
count	3809	3809.00
mean	2010-09-03 11:16:46.516146176	97.08
min	2009-12-01 10:49:00	0.00
25%	2010-07-08 14:48:00	22.00
50%	2010-10-12 16:25:00	58.00
75%	2010-11-17 13:14:00	154.00

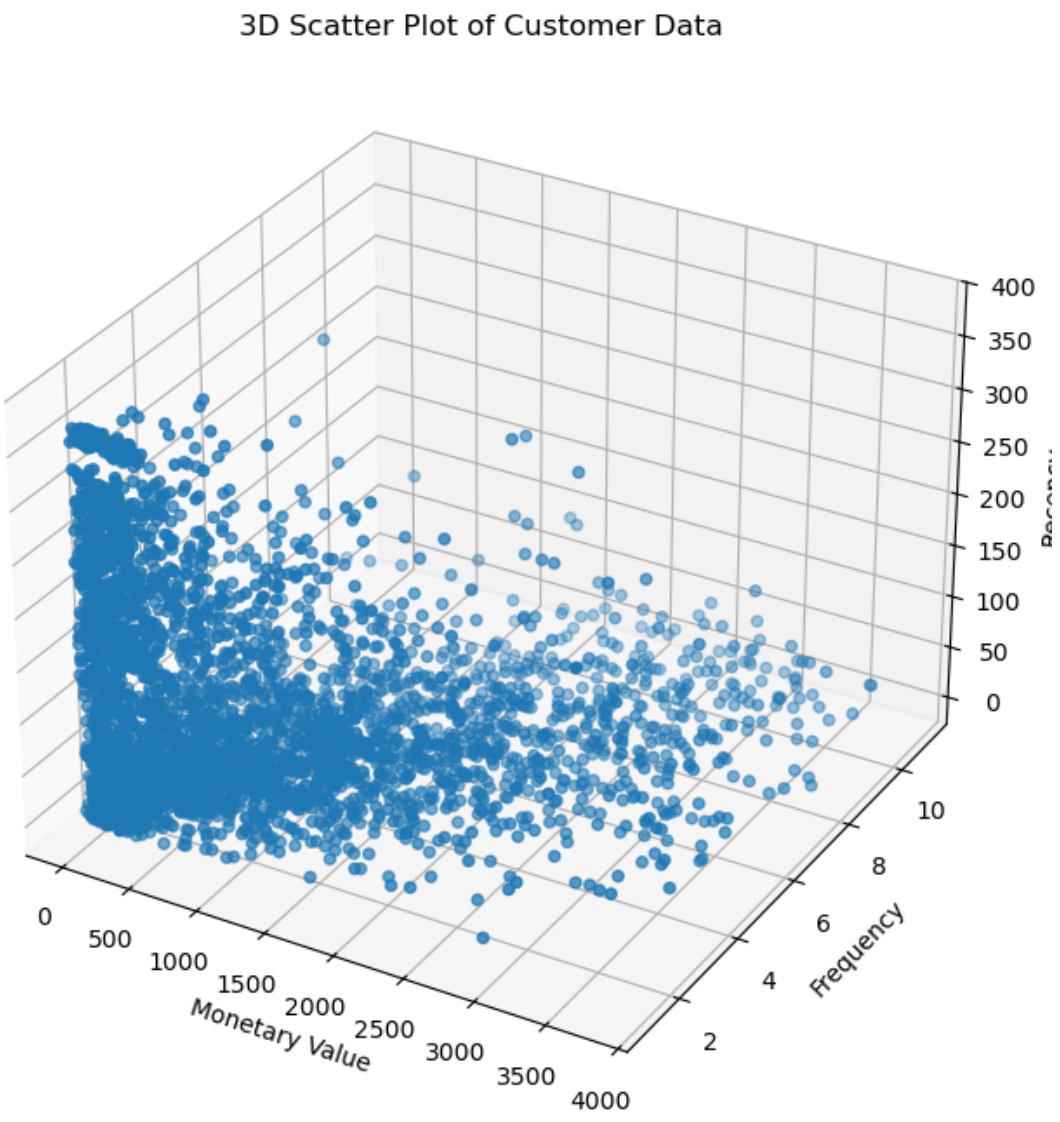
```
max              2010-12-09 20:01:00              373.00
std                              NaN               98.11
```

[48]:
```
plt.figure(figsize=(15, 5))

plt.subplot(1, 3, 1)
sns.boxplot(data=non_outliers_df['MonetaryValue'], color='skyblue')
plt.title('Monetary Value Boxplot')
plt.xlabel('Monetary Value')

plt.subplot(1, 3, 2)
sns.boxplot(data=non_outliers_df['Frequency'], color='lightgreen')
plt.title('Frequency Boxplot')
plt.xlabel('Frequency')

plt.subplot(1, 3, 3)
sns.boxplot(data=non_outliers_df['Recency'], color='salmon')
plt.title('Recency Boxplot')
plt.xlabel('Recency')

plt.tight_layout()
plt.show()
```



[49]:
```
fig = plt.figure(figsize=(8, 8))

ax = fig.add_subplot(projection="3d")

scatter = ax.scatter(non_outliers_df["MonetaryValue"],␣
 ↪non_outliers_df["Frequency"], non_outliers_df["Recency"])

ax.set_xlabel('Monetary Value')
ax.set_ylabel('Frequency')
ax.set_zlabel('Recency')
```

```
ax.set_title('3D Scatter Plot of Customer Data')

plt.show()
```



[50]:
```
scaler = StandardScaler()

scaled_data = scaler.fit_transform(non_outliers_df[["MonetaryValue",␣
↪"Frequency", "Recency"]])

scaled_data
```

[50]:
```
array([[-0.87594534, -0.38488934,  0.68214853],
       [ 0.5355144 , -0.38488934, -0.96925093],
       [-0.81258645, -0.83063076, -0.24548944],
       …,
       [-0.62197163, -0.83063076,  2.01753946],
       [ 0.44146683, -0.38488934,  0.14187587],
       [ 1.72488781,  0.50659348, -0.81634357]])
```

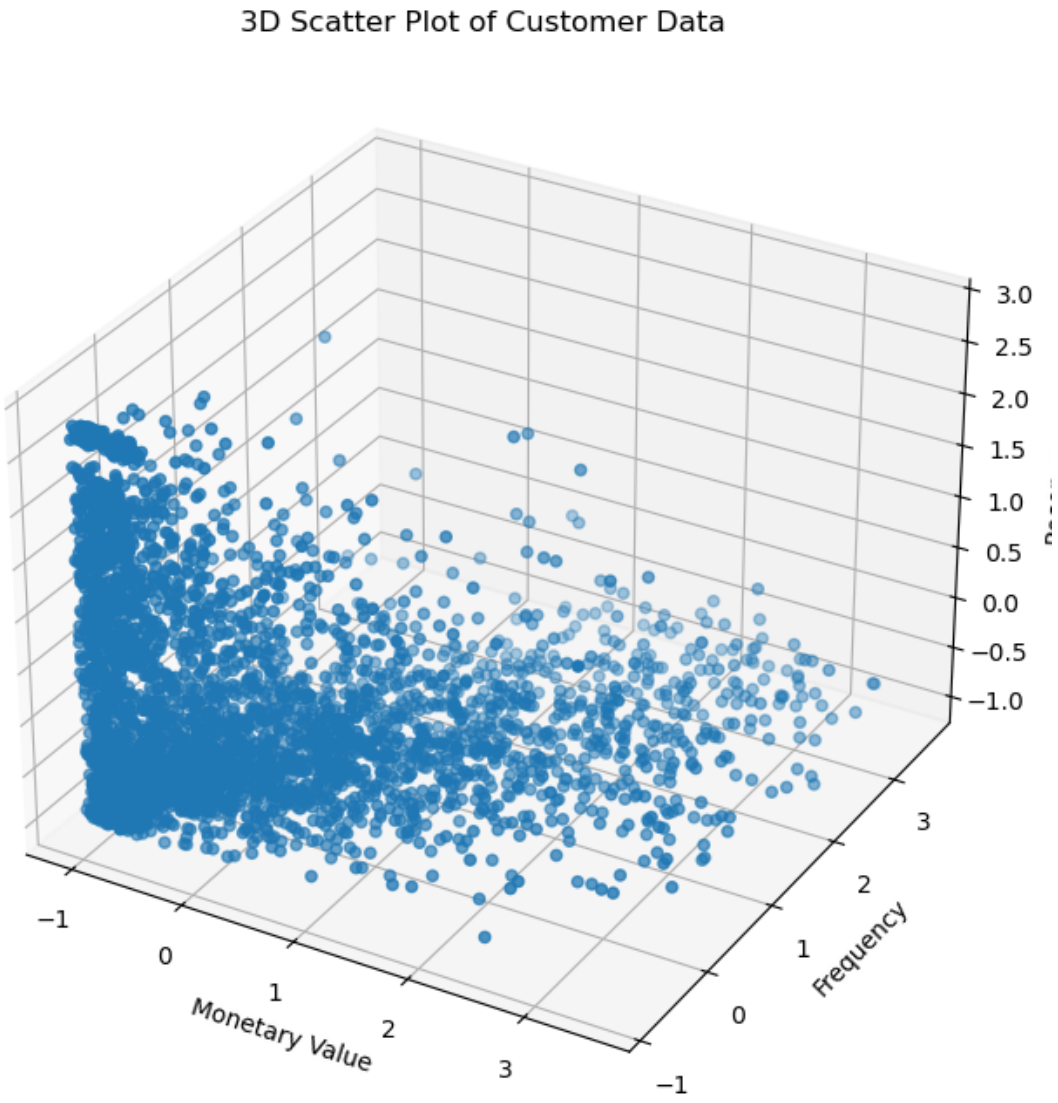
[51]:
```
scaled_data_df = pd.DataFrame(scaled_data, index=non_outliers_df.index,␣
 ↪columns=("MonetaryValue", "Frequency", "Recency"))

scaled_data_df
```

[51]:

	MonetaryValue	Frequency	Recency
0	-0.88	-0.38	0.68
1	0.54	-0.38	-0.97
2	-0.81	-0.83	-0.25
3	1.63	-0.38	-0.56
4	-0.72	-0.83	-0.89
…	…	…	…
4280	-0.30	1.40	-0.82
4281	-0.58	-0.83	-0.32
4282	-0.62	-0.83	2.02
4283	0.44	-0.38	0.14
4284	1.72	0.51	-0.82

[3809 rows x 3 columns]

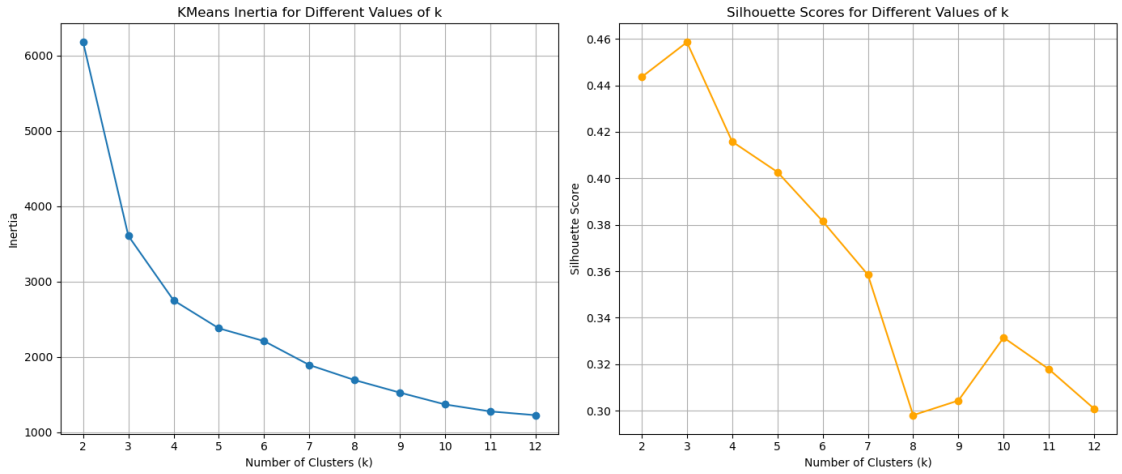
[52]:
```
fig = plt.figure(figsize=(8, 8))

ax = fig.add_subplot(projection="3d")

scatter = ax.scatter(scaled_data_df["MonetaryValue"],␣
 ↪scaled_data_df["Frequency"], scaled_data_df["Recency"])

ax.set_xlabel('Monetary Value')
ax.set_ylabel('Frequency')
ax.set_zlabel('Recency')

ax.set_title('3D Scatter Plot of Customer Data')

plt.show()
```



5 KMEANS CLUSTERING

[53]:
```
max_k = 12

inertia = []
silhoutte_scores = []
k_values = range(2, max_k + 1)

for k in k_values:

    kmeans = KMeans(n_clusters=k, random_state=42, max_iter=1000)
```

```
    cluster_labels = kmeans.fit_predict(scaled_data_df)

    sil_score = silhouette_score(scaled_data_df, cluster_labels)

    silhoutte_scores.append(sil_score)

    inertia.append(kmeans.inertia_)

plt.figure(figsize=(14, 6))

plt.subplot(1, 2, 1)
plt.plot(k_values, inertia, marker='o')
plt.title('KMeans Inertia for Different Values of k')
plt.xlabel('Number of Clusters (k)')
plt.ylabel('Inertia')
plt.xticks(k_values)
plt.grid(True)

plt.subplot(1, 2, 2)
plt.plot(k_values, silhoutte_scores, marker='o', color='orange')
plt.title('Silhouette Scores for Different Values of k')
plt.xlabel('Number of Clusters (k)')
plt.ylabel('Silhouette Score')
plt.xticks(k_values)
plt.grid(True)

plt.tight_layout()
plt.show()
```



[54]:
```
kmeans = KMeans(n_clusters=4, random_state=42, max_iter=1000)

cluster_labels = kmeans.fit_predict(scaled_data_df)

cluster_labels
```

[54]:
```
array([1, 0, 2, …, 1, 0, 0], dtype=int32)
```

[55]:
```
non_outliers_df["Cluster"] = cluster_labels

non_outliers_df
```

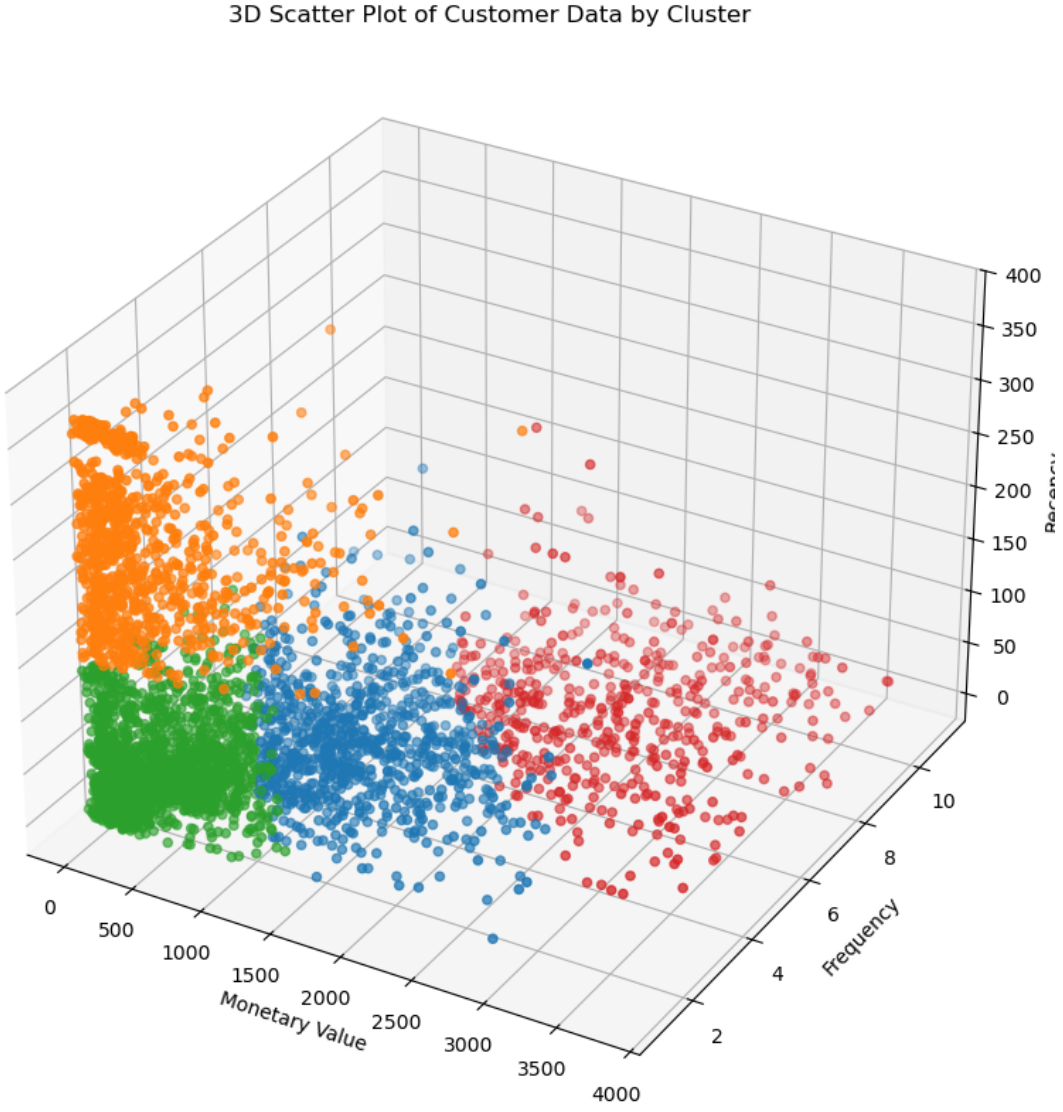
```
C:\Users\udayd\AppData\Local\Temp\ipykernel_8468\3577770544.py:1:
SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-
docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
  non_outliers_df["Cluster"] = cluster_labels
```

[55]:

	Customer ID	MonetaryValue	Frequency	LastInvoiceDate	Recency	Cluster
0	12346.00	169.36	2	2010-06-28 13:53:00	164	1
1	12347.00	1323.32	2	2010-12-07 14:57:00	2	0
2	12348.00	221.16	1	2010-09-27 14:59:00	73	2
3	12349.00	2221.14	2	2010-10-28 08:23:00	42	0
4	12351.00	300.93	1	2010-11-29 15:23:00	10	2
…	…	…	…	…	…	…
4280	18283.00	641.77	6	2010-11-22 15:30:00	17	0
4281	18284.00	411.68	1	2010-10-04 11:33:00	66	2
4282	18285.00	377.00	1	2010-02-17 10:24:00	295	1
4283	18286.00	1246.43	2	2010-08-20 11:57:00	111	0
4284	18287.00	2295.71	4	2010-11-22 11:51:00	17	0

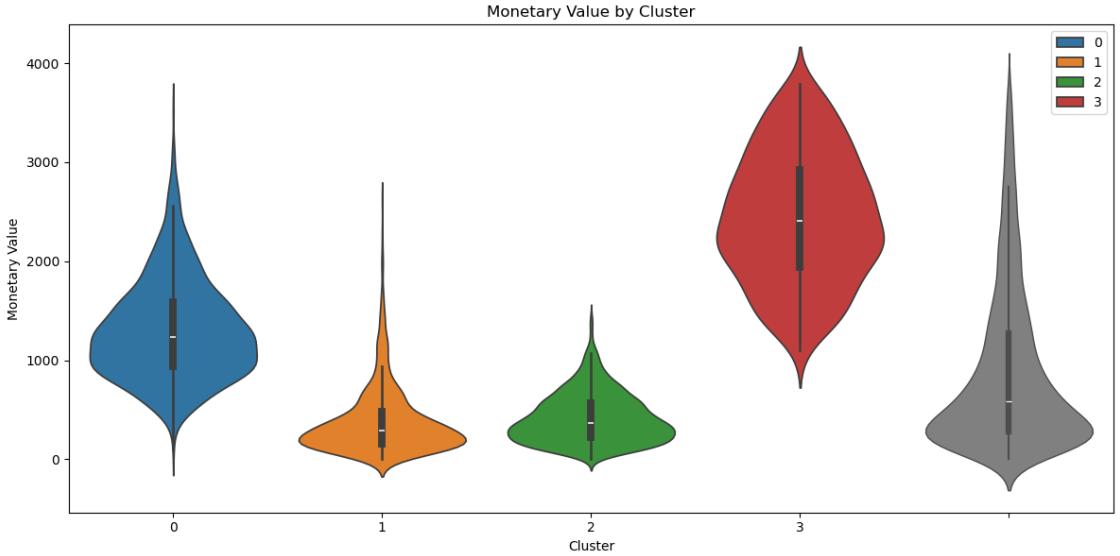
[3809 rows x 6 columns]

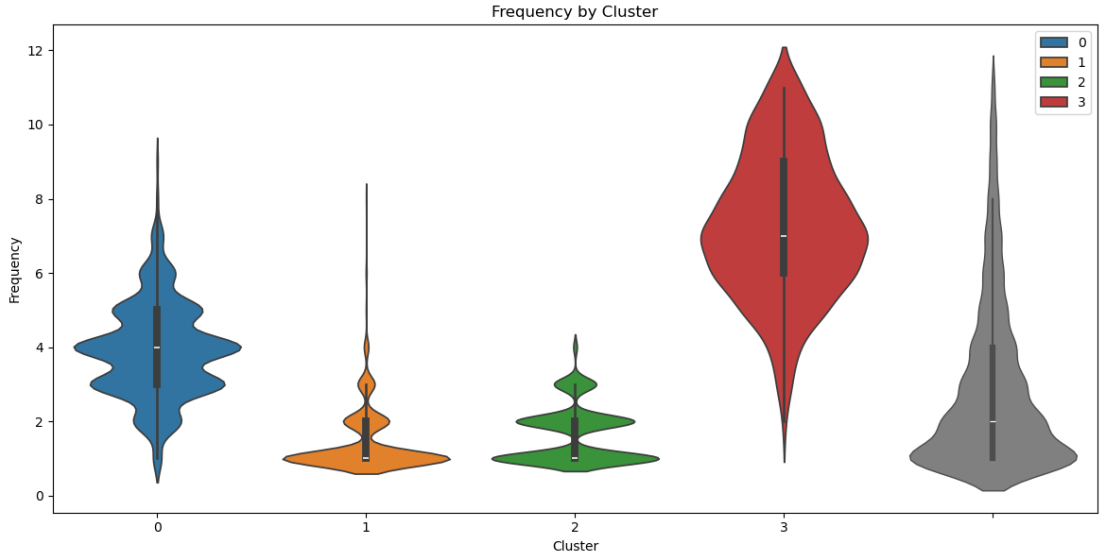
[56]:
```
cluster_colors = {0: '#1f77b4',  # Blue
                  1: '#ff7f0e',  # Orange
                  2: '#2ca02c',  # Green
                  3: '#d62728'}  # Red

colors = non_outliers_df['Cluster'].map(cluster_colors)

fig = plt.figure(figsize=(10, 10))
ax = fig.add_subplot(projection='3d')

scatter = ax.scatter(non_outliers_df['MonetaryValue'],
                     non_outliers_df['Frequency'],
                     non_outliers_df['Recency'],
                     c=colors,  # Use mapped solid colors
                     marker='o')

ax.set_xlabel('Monetary Value')
ax.set_ylabel('Frequency')
ax.set_zlabel('Recency')

ax.set_title('3D Scatter Plot of Customer Data by Cluster')

plt.show()
```

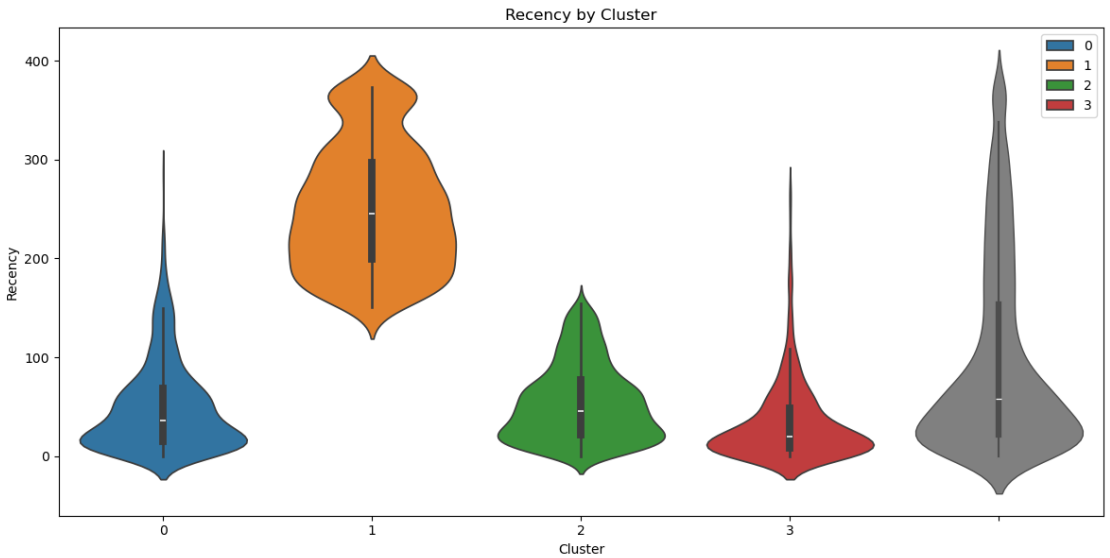


[57]:
```
plt.figure(figsize=(12, 18))

plt.subplot(3, 1, 1)
sns.violinplot(x=non_outliers_df['Cluster'],␣
↪y=non_outliers_df['MonetaryValue'], palette=cluster_colors,␣
↪hue=non_outliers_df["Cluster"])
sns.violinplot(y=non_outliers_df['MonetaryValue'], color='gray', linewidth=1.0)
plt.title('Monetary Value by Cluster')
plt.ylabel('Monetary Value')

plt.subplot(3, 1, 2)
```

```
sns.violinplot(x=non_outliers_df['Cluster'], y=non_outliers_df['Frequency'],␣
 ↪palette=cluster_colors, hue=non_outliers_df["Cluster"])
sns.violinplot(y=non_outliers_df['Frequency'], color='gray', linewidth=1.0)
plt.title('Frequency by Cluster')
plt.ylabel('Frequency')


plt.subplot(3, 1, 3)
sns.violinplot(x=non_outliers_df['Cluster'], y=non_outliers_df['Recency'],␣
 ↪palette=cluster_colors, hue=non_outliers_df["Cluster"])
sns.violinplot(y=non_outliers_df['Recency'], color='gray', linewidth=1.0)
plt.title('Recency by Cluster')
plt.ylabel('Recency')

plt.tight_layout()
plt.show()
```


Monetary Value by Cluster
Monetary Value
Cluster
0
1
2
3
4000
3000
2000
1000
0


Frequency by Cluster
Frequency
Cluster
0
1
2
3
12
10
8
6
4
2
0


Recency by Cluster
Recency
Cluster
0
1
2
3
400
300
200
100
0

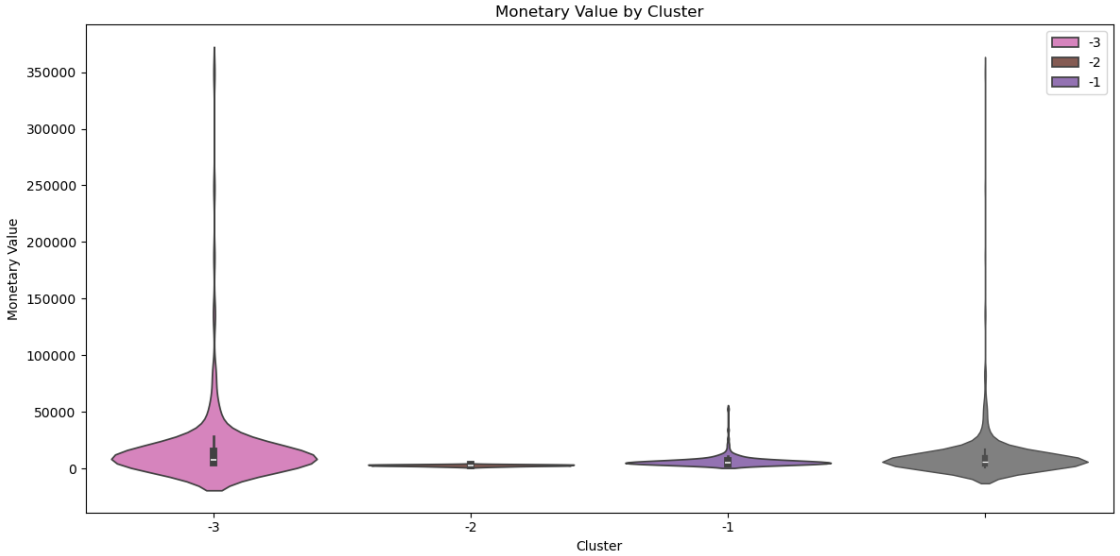
[58]:
```
overlap_indices = monetary_outliers_df.index.intersection(frequency_outliers_df.
 ↪index)

monetary_only_outliers = monetary_outliers_df.drop(overlap_indices)
frequency_only_outliers = frequency_outliers_df.drop(overlap_indices)
monetary_and_frequency_outliers = monetary_outliers_df.loc[overlap_indices]

monetary_only_outliers["Cluster"] = -1
frequency_only_outliers["Cluster"] = -2
monetary_and_frequency_outliers["Cluster"] = -3

outlier_clusters_df = pd.concat([monetary_only_outliers,␣
 ↪frequency_only_outliers, monetary_and_frequency_outliers])

outlier_clusters_df
```

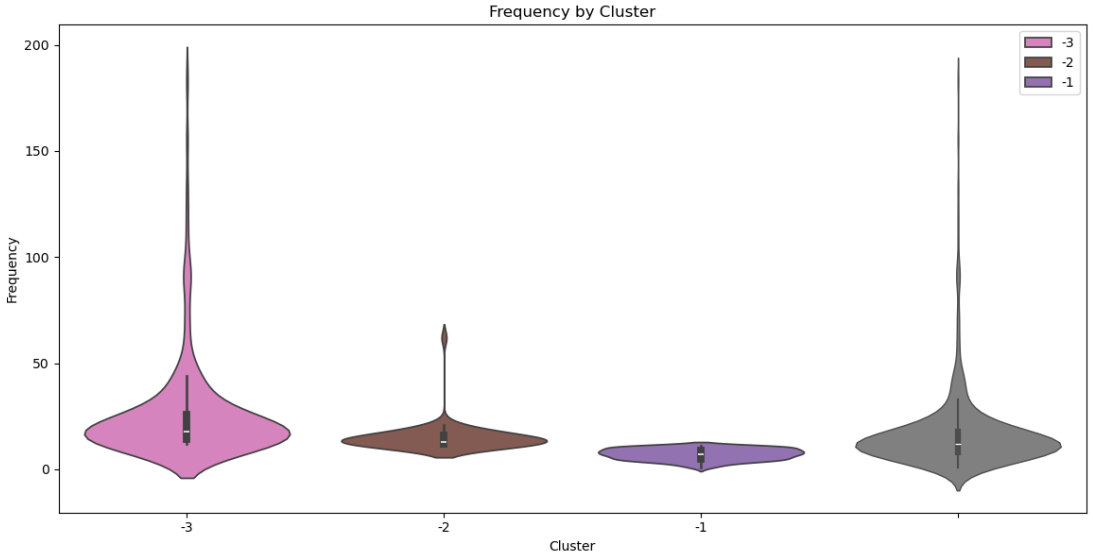
[58]:

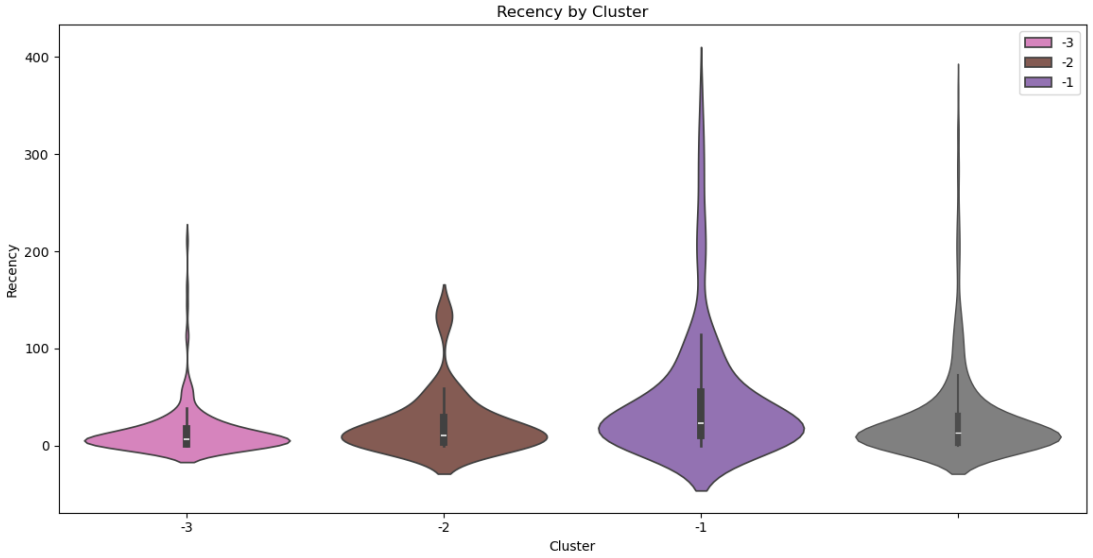
	Customer ID	MonetaryValue	Frequency	LastInvoiceDate	Recency	Cluster
9	12357.00	11229.99	1	2010-11-16 10:05:00	23	-1
25	12380.00	4782.84	4	2010-08-31 14:54:00	100	-1
42	12409.00	12346.62	4	2010-10-15 10:24:00	55	-1
48	12415.00	19468.84	4	2010-11-29 15:07:00	10	-1
61	12431.00	4145.52	11	2010-12-01 10:03:00	8	-1
…	…	…	…	…	…	…
4235	18223.00	7516.31	12	2010-11-17 12:20:00	22	-3
4236	18225.00	7545.14	15	2010-12-09 15:46:00	0	-3
4237	18226.00	6650.83	15	2010-11-26 15:51:00	13	-3
4241	18231.00	4791.80	23	2010-10-29 14:17:00	41	-3
4262	18260.00	7318.91	17	2010-11-30 12:25:00	9	-3

[476 rows x 6 columns]

[59]:
```
cluster_colors = {-1: '#9467bd',
                  -2: '#8c564b',
                  -3: '#e377c2'}

plt.figure(figsize=(12, 18))

plt.subplot(3, 1, 1)
sns.violinplot(x=outlier_clusters_df['Cluster'],␣
 ↪y=outlier_clusters_df['MonetaryValue'], palette=cluster_colors,␣
 ↪hue=outlier_clusters_df["Cluster"])
sns.violinplot(y=outlier_clusters_df['MonetaryValue'], color='gray',␣
 ↪linewidth=1.0)
plt.title('Monetary Value by Cluster')
plt.ylabel('Monetary Value')

plt.subplot(3, 1, 2)
sns.violinplot(x=outlier_clusters_df['Cluster'],␣
 ↪y=outlier_clusters_df['Frequency'], palette=cluster_colors,␣
 ↪hue=outlier_clusters_df["Cluster"])
sns.violinplot(y=outlier_clusters_df['Frequency'], color='gray', linewidth=1.0)
plt.title('Frequency by Cluster')
plt.ylabel('Frequency')

plt.subplot(3, 1, 3)
sns.violinplot(x=outlier_clusters_df['Cluster'],␣
 ↪y=outlier_clusters_df['Recency'], palette=cluster_colors,␣
 ↪hue=outlier_clusters_df["Cluster"])
sns.violinplot(y=outlier_clusters_df['Recency'], color='gray', linewidth=1.0)
plt.title('Recency by Cluster')
plt.ylabel('Recency')

plt.tight_layout()
plt.show()
```


Monetary Value by Cluster
Monetary Value
350000
300000
250000
200000
150000
100000
50000
0
-3
-2
-1
Cluster


Frequency by Cluster
Frequency
200
150
100
50
0
-3
-2
-1
Cluster


Recency by Cluster
Recency
400
300
200
100
0
-3
-2
-1
Cluster

[61]:
```
cluster_labels = {
    0: "RETAIN",
    1: "RE-ENGAGE",
    2: "NURTURE",
    3: "REWARD",
    -1: "PAMPER",
    -2: "UPSELL",
    -3: "DELIGHT"
}
```

[62]:
```
full_clustering_df = pd.concat([non_outliers_df, outlier_clusters_df])
full_clustering_df
```

[62]:
```
              Customer ID        MonetaryValue  Frequency     LastInvoiceDate  \
0                 12346.00               169.36          2 2010-06-28 13:53:00
1                 12347.00              1323.32          2 2010-12-07 14:57:00
2                 12348.00               221.16          1 2010-09-27 14:59:00
3                 12349.00              2221.14          2 2010-10-28 08:23:00
4                 12351.00               300.93          1 2010-11-29 15:23:00
…                      …                    …          …                   …
4235              18223.00              7516.31         12 2010-11-17 12:20:00
4236              18225.00              7545.14         15 2010-12-09 15:46:00
4237              18226.00              6650.83         15 2010-11-26 15:51:00
4241              18231.00              4791.80         23 2010-10-29 14:17:00
4262              18260.00              7318.91         17 2010-11-30 12:25:00

      Recency  Cluster
0         164        1
1           2        0
2          73        2
3          42        0
4          10        2
…       …       …
4235       22       -3
4236        0       -3
4237       13       -3
4241       41       -3
4262        9       -3

[4285 rows x 6 columns]
```

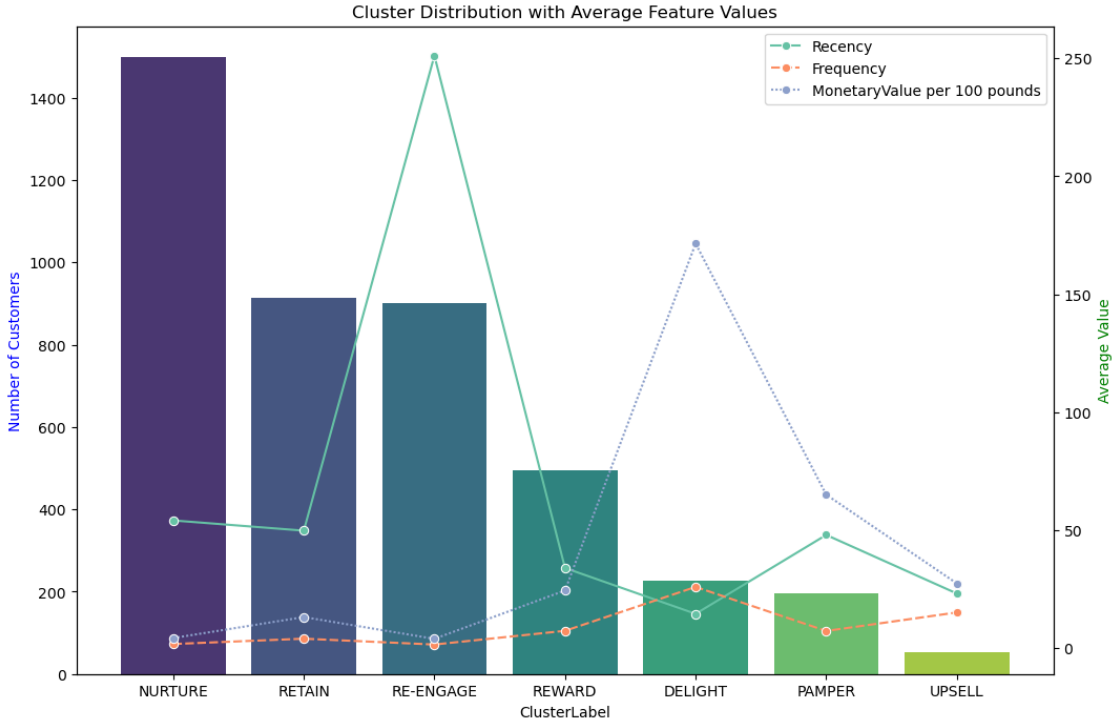
[63]:
```
full_clustering_df["ClusterLabel"] = full_clustering_df["Cluster"].
  ↪map(cluster_labels)
full_clustering_df
```

[63]:
```
              Customer ID        MonetaryValue  Frequency     LastInvoiceDate  \
0                12346.00               169.36          2 2010-06-28 13:53:00
1                12347.00              1323.32          2 2010-12-07 14:57:00
2                12348.00               221.16          1 2010-09-27 14:59:00
3                12349.00              2221.14          2 2010-10-28 08:23:00
4                12351.00               300.93          1 2010-11-29 15:23:00
…                     …                    …          …                   …
4235             18223.00              7516.31         12 2010-11-17 12:20:00
4236             18225.00              7545.14         15 2010-12-09 15:46:00
4237             18226.00              6650.83         15 2010-11-26 15:51:00
4241             18231.00              4791.80         23 2010-10-29 14:17:00
4262             18260.00              7318.91         17 2010-11-30 12:25:00

      Recency  Cluster ClusterLabel
0         164        1    RE-ENGAGE
1           2        0       RETAIN
2          73        2      NURTURE
3          42        0       RETAIN
4          10        2      NURTURE
…       …       …           …
4235       22       -3      DELIGHT
4236        0       -3      DELIGHT
4237       13       -3      DELIGHT
4241       41       -3      DELIGHT
4262        9       -3      DELIGHT

[4285 rows x 7 columns]
```

6 VISUALISATION

[64]:
```
cluster_counts = full_clustering_df['ClusterLabel'].value_counts()
full_clustering_df["MonetaryValue per 100 pounds"] =␣
 ↪full_clustering_df["MonetaryValue"] / 100.00
feature_means = full_clustering_df.groupby('ClusterLabel')[['Recency',␣
 ↪'Frequency', 'MonetaryValue per 100 pounds']].mean()

fig, ax1 = plt.subplots(figsize=(12, 8))

sns.barplot(x=cluster_counts.index, y=cluster_counts.values, ax=ax1,␣
 ↪palette='viridis', hue=cluster_counts.index)
ax1.set_ylabel('Number of Customers', color='b')
ax1.set_title('Cluster Distribution with Average Feature Values')

ax2 = ax1.twinx()

sns.lineplot(data=feature_means, ax=ax2, palette='Set2', marker='o')
```

```
ax2.set_ylabel('Average Value', color='g')

plt.show()
```



[ ]: