Social network Graph Link Prediction - Facebook Challenge

September 12, 2018

Social network Graph Link Prediction - Facebook Challenge

0.0.1 Problem statement:

Given a directed social graph, have to predict missing links to recommend users (Link Prediction in graph)

0.0.2 Data Overview

Taken data from facebook's recruting challenge on kaggle https://www.kaggle.com/c/FacebookRecruiting data contains two columns source and destination eac edge in graph - Data columns (total 2 columns):

- source node int64
- destination_node int64

0.0.3 Mapping the problem into supervised learning problem:

- Generated training samples of good and bad links from given directed graph and for each
 link got some features like no of followers, is he followed back, page rank, katz score, adar
 index, some svd fetures of adj matrix, some weight features etc. and trained ml model based
 on these features to predict link.
- Some reference papers and videos:
 - https://www.cs.cornell.edu/home/kleinber/link-pred.pdf
 - https://www3.nd.edu/~dial/publications/lichtenwalter2010new.pdf
 - https://kaggle2.blob.core.windows.net/forum-message-attachments/2594/supervised_link_predictions.
 - https://www.youtube.com/watch?v=2M77Hgy17cg

0.0.4 Business objectives and constraints:

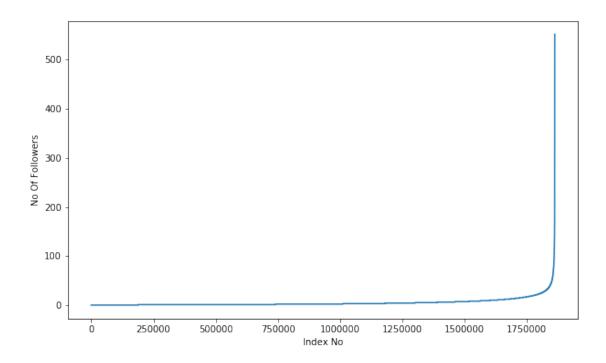
- No low-latency requirement.
- Probability of prediction is useful to recommend ighest probability links

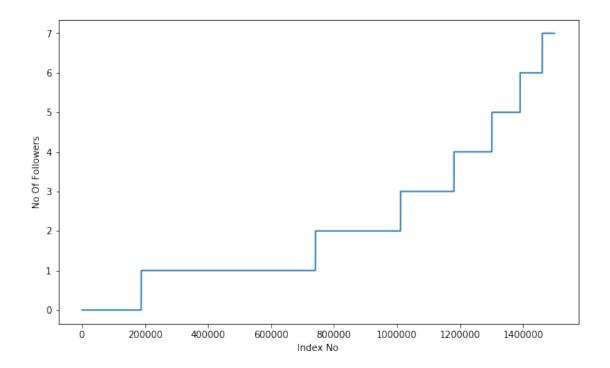
0.0.5 Performance metric for supervised learning:

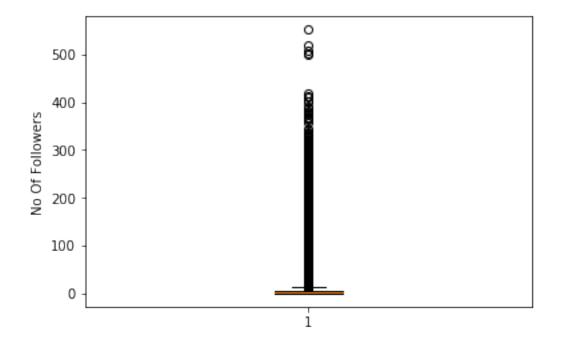
- Both precision and recall is important so F1 score is good choice
- Confusion matrix

```
In [1]: #Importing Libraries
        # please do go through this python notebook:
        import csv
        import pandas as pd#pandas to create small dataframes
        import datetime #Convert to unix time
        import time #Convert to unix time
        # if numpy is not installed already : pip3 install numpy
        import numpy as np#Do aritmetic operations on arrays
        # matplotlib: used to plot graphs
        import matplotlib
        import matplotlib.pylab as plt
        import seaborn as sns#Plots
        from matplotlib import rcParams#Size of plots
        from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        import math
        import pickle
        import os
        # to install xqboost: pip3 install xqboost
        import xgboost as xgb
        import warnings
        import networkx as nx
        import pdb
        import warnings
        warnings.filterwarnings("ignore")
In [2]: #reading df
       traincsv = pd.read_csv('train.csv')
In [3]: #chacking if any null values in given graph
       traincsv[traincsv.isna().any(1)]
Out[3]: Empty DataFrame
       Columns: [source_node, destination_node]
        Index: []
In [4]: #info of given data set
       traincsv.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 9437519 entries, 0 to 9437518
Data columns (total 2 columns):
source node
                    int64
destination node
                    int64
dtypes: int64(2)
memory usage: 144.0 MB
In [5]: #no of duplicates
        sum(traincsv.duplicated())
```

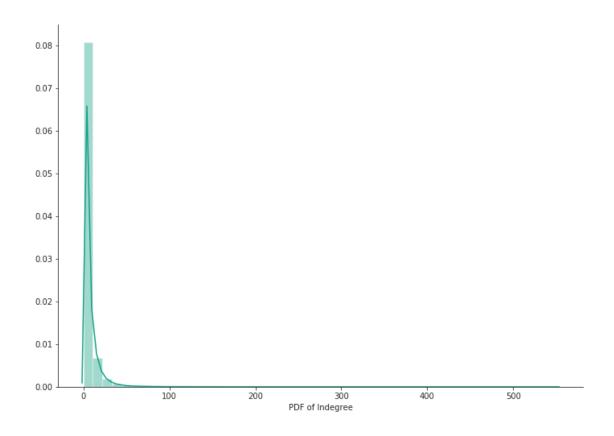
```
Out[5]: 0
In [6]: #removing header and saving
        traincsv.to_csv('train_woheader.csv',header=False,index=False)
In [2]: #Getting basic info from our data
       g=nx.read_edgelist('train_woheader.csv',delimiter=',',create_using=nx.DiGraph(),nodetype
        print(nx.info(g))
Name:
Type: DiGraph
Number of nodes: 1862220
Number of edges: 9437519
Average in degree:
                     5.0679
Average out degree:
                    5.0679
0.1 EDA
In [8]: # No of Unique persons
        len(g.nodes())
Out[8]: 1862220
   No of followers for each person
In [9]: indegree_dist = list(dict(g.in_degree()).values())
```



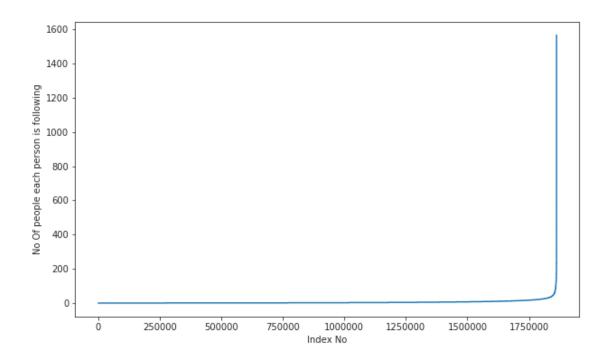


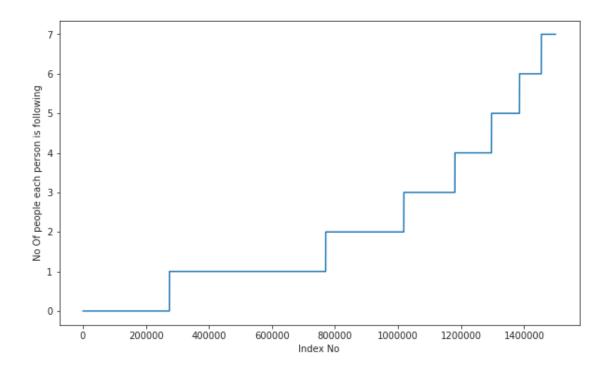


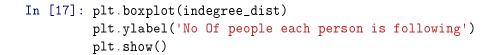
```
In [12]: ### 90-100 percentile
         for i in range(0,11):
             print(90+i, 'percentile value is', np.percentile(indegree_dist,90+i))
90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 552.0
   99% of data having followers of 40 only.
In [13]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is',np.percentile(indegree_dist,99+(i/100)))
99.1 percentile value is 42.0
99.2 percentile value is 44.0
99.3 percentile value is 47.0
99.4 percentile value is 50.0
99.5 percentile value is 55.0
99.6 percentile value is 61.0
99.7 percentile value is 70.0
99.8 percentile value is 84.0
99.9 percentile value is 112.0
100.0 percentile value is 552.0
In [14]: %matplotlib inline
         sns.set_style('ticks')
         fig, ax = plt.subplots()
         fig.set_size_inches(11.7, 8.27)
         sns.distplot(indegree_dist, color='#16A085')
         plt.xlabel('PDF of Indegree')
         sns.despine()
         #plt.show()
```

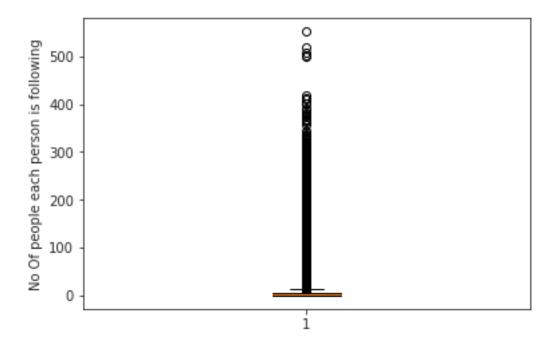


No of people each person is following

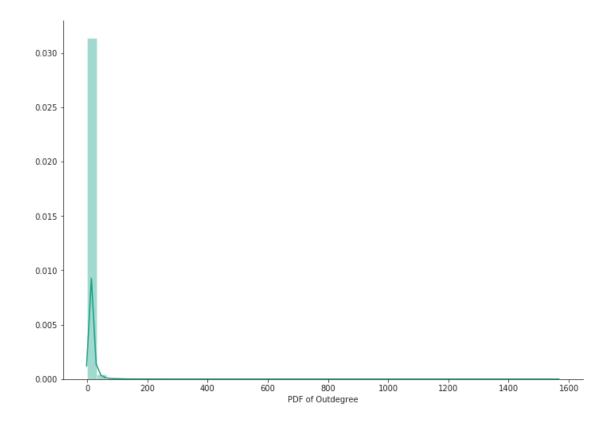








```
In [18]: ### 90-100 percentile
         for i in range(0,11):
             print(90+i, 'percentile value is', np.percentile(outdegree_dist,90+i))
90 percentile value is 12.0
91 percentile value is 13.0
92 percentile value is 14.0
93 percentile value is 15.0
94 percentile value is 17.0
95 percentile value is 19.0
96 percentile value is 21.0
97 percentile value is 24.0
98 percentile value is 29.0
99 percentile value is 40.0
100 percentile value is 1566.0
In [19]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is', np.percentile(outdegree_dist, 99+(i/100)))
99.1 percentile value is 42.0
99.2 percentile value is 45.0
99.3 percentile value is 48.0
99.4 percentile value is 52.0
99.5 percentile value is 56.0
99.6 percentile value is 63.0
99.7 percentile value is 73.0
99.8 percentile value is 90.0
99.9 percentile value is 123.0
100.0 percentile value is 1566.0
In [20]: sns.set_style('ticks')
         fig, ax = plt.subplots()
         fig.set_size_inches(11.7, 8.27)
         sns.distplot(outdegree_dist, color='#16A085')
         plt.xlabel('PDF of Outdegree')
         sns.despine()
```



In [21]: print('No of persons those are not following anyone are', sum(np.array(outdegree_dist)=

No of persons those are not not following anyone and also not having any followers are 0

both followers + following

```
In [24]: from collections import Counter
          dict_in = dict(g.in_degree())
          dict_out = dict(g.out_degree())
          d = Counter(dict_in) + Counter(dict_out)
          in_out_degree = np.array(list(d.values()))
In [25]: in_out_degree_sort = sorted(in_out_degree)
          plt.figure(figsize=(10,6))
          plt.plot(in_out_degree_sort)
          plt.xlabel('Index No')
          plt.ylabel('No Of people each person is following + followers')
          plt.show()
       1600
     No Of people each person is following + followers
       1400
       1200
       1000
        800
        600
        400
        200
          0
```

750000

1000000

Index No

1250000

250000

500000

1500000

1750000

```
In [27]: ### 90-100 percentile
         for i in range(0,11):
             print(90+i, 'percentile value is', np.percentile(in_out_degree_sort, 90+i))
90 percentile value is 24.0
91 percentile value is 26.0
92 percentile value is 28.0
93 percentile value is 31.0
94 percentile value is 33.0
95 percentile value is 37.0
96 percentile value is 41.0
97 percentile value is 48.0
98 percentile value is 58.0
99 percentile value is 79.0
100 percentile value is 1579.0
In [28]: ### 99-100 percentile
         for i in range(10,110,10):
             print(99+(i/100), 'percentile value is',np.percentile(in_out_degree_sort,99+(i/100))
99.1 percentile value is 83.0
99.2 percentile value is 87.0
99.3 percentile value is 93.0
99.4 percentile value is 99.0
```

```
99.5 percentile value is 108.0
99.6 percentile value is 120.0
99.7 percentile value is 138.0
99.8 percentile value is 168.0
99.9 percentile value is 221.0
100.0 percentile value is 1579.0
In [29]: print('Min of no of followers + following is',in_out_degree.min())
         print(np.sum(in_out_degree==in_out_degree.min()),' persons having minimum no of followed
Min of no of followers + following is 1
334291 persons having minimum no of followers + following
In [30]: print('Max of no of followers + following is',in_out_degree.max())
         print(np.sum(in_out_degree==in_out_degree.max()),' persons having maximum no of followed
Max of no of followers + following is 1579
1 persons having maximum no of followers + following
In [31]: print('No of persons having followers + following less than 10 are',np.sum(in_out_degre
No of persons having followers + following less than 10 are 1320326
In [32]: print('No of weakly connected components',len(list(nx.weakly_connected_components(g))))
         count=0
         for i in list(nx.weakly_connected_components(g)):
             if len(i)==2:
                 count+=1
         print('weakly connected components wit 2 nodes',count)
No of weakly connected components 45558
weakly connected components wit 2 nodes 32195
```

Generating some edges which are not present in graph for supervised learning Generated Bad links from graph which are not in graph and whose shortest path is greater than 2.

```
missing_edges = set([])
        while (len(missing_edges)<9437519):
            a=random.randint(1, 1862220)
            b=random.randint(1, 1862220)
            tmp = edges.get((a,b),-1)
            if tmp == -1 and a!=b:
                try:
                    if nx.shortest_path_length(g,source=a,target=b) > 2:
                        missing_edges.add((a,b))
                    else:
                         continue
                except:
                        missing_edges.add((a,b))
            else:
                continue
CPU times: user 2h 28min 24s, sys: 34.8 s, total: 2h 28min 59s
Wall time: 2h 28min 59s
In [7]: len(missing_edges)
Out[7]: 9437519
In [8]: import pickle
        pickle.dump(missing_edges,open('missing_edges_final.p','wb'))
In [45]: import pickle
         missing_edges = pickle.load(open('missing_edges_final.p','rb'))
Training and Test data split: Removed edges from Graph and used as test data and after remov-
ing used that graph for creating features for Train and test data
In [46]: #reading total data df
         df_pos = pd.read_csv('train.csv')
         df_neg = pd.DataFrame(list(missing_edges), columns=['source_node', 'destination_node'])
In [47]: #positive links i.e graph
         df_pos.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 9437519 entries, 0 to 9437518
Data columns (total 2 columns):
source node
                    int64
destination_node
                    int64
```

import random

dtypes: int64(2)

memory usage: 144.0 MB

```
In [48]: #negative links synthesized links
         df_neg.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 9437519 entries, 0 to 9437518
Data columns (total 2 columns):
source node
                    int64
destination_node
                    int64
dtypes: int64(2)
memory usage: 144.0 MB
In [49]: #Trian test split
         #Spiltted data into 80-20
         #positive links and negative links seperatly because we need positive training data onl
         #and for feature generation
         from sklearn.model_selection import train_test_split
         X_train_pos, X_test_pos, y_train_pos, y_test_pos = train_test_split(df_pos,np.ones(length))
         X_train_neg, X_test_neg, y_train_neg, y_test_neg = train_test_split(df_neg,np.zeros(leg))
In [50]: df_train_pos = pd.DataFrame(X_train_pos)
         #removing header and saving
         df_train_pos.to_csv('train_data.csv',header=False,index=False)
In [51]: #Graph from Traing data only
         g=nx.read_edgelist('train_data.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=in
         print(nx.info(g))
Name:
Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree:
                     4.2399
Average out degree:
                      4.2399
In [52]: #Graph of total data without splitting
         G=nx.read_edgelist('train_woheader.csv',delimiter=',',create_using=nx.DiGraph(),nodetyp
         print(nx.info(G))
Name:
Type: DiGraph
Number of nodes: 1862220
Number of edges: 9437519
Average in degree:
                     5.0679
Average out degree:
                      5.0679
In [53]: ###total nodes in train positive data
         train_nodes_pos = set(g.nodes())
```

```
###total nodes in total data
         total_nodes_pos = set(G.nodes())
         ###test nodes in pos data
         test_nodes_pos = set(X_test_pos.values.flatten())
In [11]: print('no of people common in train and test -- ',len(train_nodes_pos.intersection(test
         print('no of people present in train but not present in test -- ',len(train_nodes_pos -
         print('no of people present in test but not present in train -- ',len(test_nodes_pos -
no of people common in train and test -- 1063125
no of people present in train but not present in test -- 717597
no of people present in test but not present in train -- 81498
In [57]: print(' % of people not there in Train but exist in Test in total Test data are {} %'.\
                           format(len(test_nodes_pos - train_nodes_pos)/len(test_nodes_pos)*100)
\% of people not there in Train but exist in Test in total Test data are 7.1200735962845405 \%
  This will cause a cold start problem
In [13]: #final train and test data sets
         df_final_train = X_train_pos.append(X_train_neg,ignore_index=True)
         y_final_train = np.concatenate((y_train_pos,y_train_neg))
         df_final_test = X_test_pos.append(X_test_neg,ignore_index=True)
         y_final_test = np.concatenate((y_test_pos,y_test_neg))
In [14]: df_final_train.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 15100030 entries, 0 to 15100029
Data columns (total 2 columns):
source node
                    int64
destination_node
                    int64
dtypes: int64(2)
memory usage: 230.4 MB
In [15]: df_final_test.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 3775008 entries, 0 to 3775007
Data columns (total 2 columns):
source_node
                    int64
destination_node
                    int64
dtypes: int64(2)
memory usage: 57.6 MB
```

```
Adjacency_matrix https://en.wikipedia.org/wiki/Adjacency_matrix
```

0.2 Feature Engineering

0.2.1 SVD

```
In [9]: from scipy.sparse.linalg import svds, eigs
       U, s, V = svds(Adj,k = 6)
In [10]: U
Out[10]: array([[-2.06311438e-15, 4.86280646e-12, 4.32863386e-13,
                  6.34827889e-14, 1.18649118e-14, 1.85940576e-16],
                [-5.39810495e-14, 7.68601596e-13, 1.32207398e-11,
                  2.12945529e-13, 9.80313275e-13, 5.21376923e-16],
                [-1.03323961e-11, 2.77939874e-11, 1.56793759e-09,
                  2.35993376e-11, 3.87897382e-12, 6.99955573e-13],
                [-9.08926368e-15, 3.01073958e-14, 6.61712281e-13,
                  1.86989518e-13, 2.39751694e-12, 1.01911935e-14],
                [-4.04926290e-13, 1.66308893e-13, 1.36923604e-06,
                  6.08332634e-14, 1.84662990e-13, 1.79395445e-12],
                [-7.33024975e-15, 7.79261880e-15, 7.97714296e-14,
                  2.89269174e-16, 1.21312591e-15, 2.25623613e-16]])
In [11]: print('U Shape',U.shape)
         print('V Shape', V.shape)
         print('s Shape',s.shape)
U Shape (1780722, 6)
V Shape (6, 1780722)
s Shape (6,)
In [12]: del Adj
         del s
```

0.2.2 Similarity measures

Jaccard Distance:

$$j = \frac{|X \cap Y|}{|X \cup Y|} \tag{1}$$

```
In [21]: #for followees
         def jaccard_for_followees(a,b):
                  if len(set(g.successors(a))) == 0 | len(set(g.successors(b))) == 0:
                      return 0
                 sim = (len(set(g.successors(a)).intersection(set(g.successors(b)))))/
                                               (len(set(g.successors(a)).union(set(g.successors(b)
             except:
                 return 0
             return sim
In [22]: #one test case
         jaccard_for_followees(2,1615927)
Out[22]: 0.0
In [23]: #node 1635354 not in graph
         jaccard_for_followees(669354,1635354)
Out[23]: 0
In [24]: #for followers
         def jaccard_for_followers(a,b):
                 if len(set(g.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
                      return 0
                 sim = (len(set(g.predecessors(a)).intersection(set(g.predecessors(b)))))/\
                                            (len(set(g.predecessors(a)).union(set(g.predecessors(b)))
                 return sim
             except:
                 return 0
In [25]: jaccard_for_followers(2,470294)
Out[25]: 0.045454545454545456
In [26]: #node 1635354 not in graph
         jaccard_for_followees(669354,1635354)
Out[26]: 0
Cosine distance
                               CosineDistance = \frac{|X \cap Y|}{|X| \cdot |Y|}
                                                                                    (2)
In [27]: #for followees
         def cosine_for_followees(a,b):
             try:
                 if len(set(g.successors(a))) == 0 | len(set(g.successors(b))) == 0:
                      return 0
```

```
sim = (len(set(g.successors(a)).intersection(set(g.successors(b)))))/\
                                               (math.sqrt(len(set(g.successors(a)))*len((set(g.successors(a))))
                 return sim
             except:
                 return 0
In [28]: cosine_for_followees(2,470294)
Out [28]: 0.08944271909999159
In [29]: cosine_for_followees(669354,1635354)
Out[29]: 0
In [30]: def cosine_for_followers(a,b):
             try:
                 if len(set(g.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
                      return 0
                 sim = (len(set(g.predecessors(a)).intersection(set(g.predecessors(b)))))/
                                                (math.sqrt(len(set(g.predecessors(a))))*(len(set(g.predecessors(a))))
                 return sim
             except:
                 return 0
In [31]: cosine_for_followers(2,470294)
Out[31]: 0.02886751345948129
In [32]: cosine_for_followers(669354,1635354)
Out[32]: 0
0.2.3 Ranking Measures
https://en.wikipedia.org/wiki/PageRank
In [33]: pr = nx.pagerank(g, alpha=0.85)
In [34]: pickle.dump(pr,open('page_rank.p','wb'))
In [35]: len(pr)
Out[35]: 1780722
In [37]: pr = pickle.load(open('page_rank.p','rb'))
In [39]: print('min',pr[min(pr, key=pr.get)])
         print('max',pr[max(pr, key=pr.get)])
         print('mean',float(sum(pr.values())) / len(pr))
```

Shortest path: Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
In [8]: #if has direct edge then deleting that edge and calculating shortest path
        def compute_shortest_path_length(a,b):
            p = -1
            try:
                if g.has_edge(a,b):
                    g.remove_edge(a,b)
                    p= nx.shortest_path_length(g,source=a,target=b)
                    g.add_edge(a,b)
                    p= nx.shortest_path_length(g,source=a,target=b)
                return p
            except:
                return -1
In [9]: #testing
        compute_shortest_path_length(77697, 826021)
Out[9]: 10
In [10]: #testing
         compute_shortest_path_length(669354,1635354)
Out[10]: -1
Checking for same community
In [39]: #qetting weekly connected edges from graph
         wcc=list(nx.weakly_connected_components(g))
         def belongs_to_same_wcc(a,b):
             index = []
             if g.has_edge(b,a):
                 return 1
             if g.has_edge(a,b):
                     for i in wcc:
                         if a in i:
                             index= i
                             break
                     if (b in index):
```

```
g.remove_edge(a,b)
                           if compute_shortest_path_length(a,b)==-1:
                               g.add_edge(a,b)
                               return 0
                           else:
                               g.add_edge(a,b)
                               return 1
                      else:
                          return 0
             else:
                      for i in wcc:
                          if a in i:
                               index= i
                               break
                      if(b in index):
                          return 1
                      else:
                          return 0
In [40]: belongs_to_same_wcc(861, 1659750)
Out[40]: 0
In [41]: belongs_to_same_wcc(669354,1635354)
Out[41]: 0
Adamic/Adar Index
                                A = \sum_{u \in N(x) \cap N(y)} \frac{1}{\log |N(u)|}
                                                                                       (3)
In [42]: #adar index
         def calc_adar_in(a,b):
             sum=0
              try:
                  n=list(set(g.successors(a)).intersection(set(g.successors(b))))
                  if len(n)!=0:
                      for i in n:
                           sum=sum+(1/np.log10(len(list(g.predecessors(i)))))
                      return sum
                  else:
                      return 0
             except:
                  return 0
In [43]: calc_adar_in(1,189226)
Out[43]: 0
In [44]: calc_adar_in(669354,1635354)
Out[44]: 0
```

Is persion was following back:

```
In [45]: def follows_back(a,b):
             if g.has_edge(b,a):
                 return 1
             else:
                 return 0
In [46]: follows_back(1,189226)
Out[46]: 1
In [47]: follows_back(669354,1635354)
Out[47]: 0
Katz Centrality: https://en.wikipedia.org/wiki/Katz_centrality
In [119]: katz = nx.katz.katz_centrality(g,alpha=0.005,beta=1)
          #import pickle
          #katz = pickle.load(open('katz.p', 'rb'))
In [11]: import pickle
         katz = pickle.load(open('katz.p','rb'))
In [24]: type(katz)
Out [24]: dict
In [32]: print('min',katz[min(katz, key=katz.get)])
         print('max',katz[max(katz, key=katz.get)])
         print('mean',float(sum(katz.values())) / len(katz))
min 0.0007313532484065916
max 0.003394554981699122
mean 0.0007483800935562018
In [33]: mean_katz = float(sum(katz.values())) / len(katz)
Hits Score https://en.wikipedia.org/wiki/HITS_algorithm
In [40]: hits = nx.hits(g, max_iter=100, tol=1e-08, nstart=None, normalized=True)
         #hits = pickle.load(open('hits.p', 'rb'))
In [13]: hits = pickle.load(open('hits.p','rb'))
In [14]: len(hits)
Out[14]: 2
```

```
In [15]: len(hits[0])
Out[15]: 1780722
In [45]: print('min',hits[0][min(hits[0], key=hits[0].get)])
         print('max', hits[0][max(hits[0], key=hits[0].get)])
         print('mean',float(sum(hits[0].values())) / len(hits[0]))
min 0.0
max 0.004868653378780953
mean 5.615699699344123e-07
In [43]: import pickle
         pickle.dump(hits,open('hits.p','wb'))
   From all above scores preparing data set
In [54]: df_final_train.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 15100030 entries, 0 to 15100029
Data columns (total 2 columns):
                    int64
source node
destination_node
                    int64
dtypes: int64(2)
memory usage: 230.4 MB
In [55]: df_final_test.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 3775008 entries, 0 to 3775007
Data columns (total 2 columns):
source_node
                    int64
destination_node
                    int64
dtypes: int64(2)
memory usage: 57.6 MB
In [57]: #mapping jaccrd followers to train data
         df_final_train['jaccard_followers'] = df_final_train.apply(lambda row:
                                                  jaccard_for_followers(row['source_node'],row['d
In [59]: #mapping jaccrd followers to test data
         df_final_test['jaccard_followers'] = df_final_test.apply(lambda row:
                                                  jaccard_for_followers(row['source_node'],row['d
```

```
In [60]: #mapping jaccrd followees to train and test data
         df_final_train['jaccard_followees'] = df_final_train.apply(lambda row:
                                                  jaccard_for_followees(row['source_node'],row['d
         df_final_test['jaccard_followees'] = df_final_test.apply(lambda row:
                                                  jaccard_for_followees(row['source_node'],row['d
In [65]: #calculating no of followers followees for source and destination
         #calculating intersection of followers and followees for source and destination
         num_followers_s=[]
         num_followees_s=[]
         num_followers_d=[]
         num_followees_d=[]
         inter_followers=[]
         inter_followees=[]
         for i,row in df_final_train.iterrows():
             try:
                 s1=set(g.predecessors(row['source_node']))
                 s2=set(g.successors(row['source_node']))
             except:
                 s1 = set()
                 s2 = set()
             try:
                 d1=set(g.predecessors(row['destination_node']))
                 d2=set(g.successors(row['destination_node']))
             except:
                 d1 = set()
                 d2 = set()
             num_followers_s.append(len(s1))
             num_followees_s.append(len(s2))
             num_followers_d.append(len(d1))
             num_followees_d.append(len(d2))
             inter_followers.append(len(s1.intersection(d1)))
             inter_followees.append(len(s2.intersection(d2)))
In [66]: df_final_train['num_followers_s']=num_followers_s
         df_final_train['num_followees_s']=num_followees_s
         df_final_train['num_followers_d']=num_followers_d
         df_final_train['num_followees_d']=num_followees_d
         df_final_train['inter_followers']=inter_followers
         df_final_train['inter_followees']=inter_followees
In [67]: #For test data
         #calculating no of followers followees for source and destination
         #calculating intersection of followers and followees for source and destination
         num_followers_s=[]
         num_followees_s=[]
```

```
num_followers_d=[]
         num_followees_d=[]
         inter_followers=[]
         inter_followees=[]
         for i,row in df_final_test.iterrows():
             try:
                 s1=set(g.predecessors(row['source_node']))
                 s2=set(g.successors(row['source_node']))
             except:
                 s1 = set()
                 s2 = set()
                 d1=set(g.predecessors(row['destination_node']))
                 d2=set(g.successors(row['destination_node']))
             except:
                 d1 = set()
                 d2 = set()
             num_followers_s.append(len(s1))
             num_followees_s.append(len(s2))
             num_followers_d.append(len(d1))
             num_followees_d.append(len(d2))
             inter_followers.append(len(s1.intersection(d1)))
             inter_followees.append(len(s2.intersection(d2)))
In [68]: #assigning
         df_final_test['num_followers_s']=num_followers_s
         df_final_test['num_followees_s']=num_followees_s
         df_final_test['num_followers_d']=num_followers_d
         df_final_test['num_followees_d']=num_followees_d
         df_final_test['inter_followers']=inter_followers
         df_final_test['inter_followees']=inter_followees
In [69]: #saving to disk
         df_final_train.to_csv('df_final_train_some.csv',index=False)
         df_final_test.to_csv('df_final_test_some.csv',index=False)
In [71]: \#head\ of\ df
         df_final_train.head()
Out [71]:
            source_node destination_node jaccard_followers jaccard_followees \
                                  1505602
         0
                 273084
                                                     0.000000
                                                                        0.000000
                                  1678443
                                                                        0.058824
         1
                 912810
                                                     0.058824
         2
                 365429
                                  1523458
                                                     0.033058
                                                                        0.023077
                                                                        0.000000
         3
                 527014
                                  1605979
                                                     0.000000
                1228116
                                   471233
                                                     0.068966
                                                                        0.162162
            num_followers_s num_followees_s num_followers_d num_followees_d \
```

```
0
                                            15
                                                               6
                          11
                                                                                8
         1
                          10
                                            10
                                                              8
                                                                                8
         2
                          40
                                            49
                                                             85
                                                                               84
         3
                           0
                                            1
                                                              1
                                                                                0
         4
                          14
                                            23
                                                             48
                                                                               20
            inter_followers
                             inter_followees
         0
         1
                           1
                                            1
                           4
         2
                                            3
                                            0
         3
                           0
         4
In [72]: df_final_test.head()
Out [72]:
            source_node destination_node jaccard_followers jaccard_followees
         0
                 848424
                                    784690
                                                      0.052632
                                                                          0.000000
         1
                1248963
                                    444518
                                                      0.000000
                                                                          0.00000
         2
                 264224
                                    132395
                                                      0.375000
                                                                          0.400000
         3
                 549680
                                    326829
                                                      0.115385
                                                                          0.040000
                 875380
                                   1394902
                                                      0.190476
                                                                          0.184211
            num_followers_s num_followees_s num_followers_d num_followees_d \
         0
                           6
                                             6
                                                             14
                                                                                2
                           5
                                            8
                                                              1
         1
         2
                                            7
                                                              3
                                                                                7
                           8
         3
                          17
                                                             12
                                                                               15
                                            11
         4
                                                             29
                          21
                                            20
                                                                               25
            inter_followers
                              inter_followees
         0
                           0
                                            0
         1
         2
                           3
                                            4
         3
                           3
                           8
In [73]: #mapping adar index on train
         df_final_train['adar_index'] = df_final_train.apply(lambda row:
                                                   calc_adar_in(row['source_node'],row['destination
In [74]: #mapping adar index on test
         df_final_test['adar_index'] = df_final_test.apply(lambda row:
                                                   calc_adar_in(row['source_node'],row['destination
In [75]: #mapping followback or not on train
         df_final_train['follows_back'] = df_final_train.apply(lambda row:
                                                   follows_back(row['source_node'],row['destination
In [76]: #mapping followback or not on test
         df_final_test['follows_back'] = df_final_test.apply(lambda row:
                                                   follows_back(row['source_node'],row['destination
```

```
In [77]: ##mapping same component of wcc or not on train
         df_final_train['same_comp'] = df_final_train.apply(lambda row:
                                                 belongs_to_same_wcc(row['source_node'],row['des
In [78]: ##mapping same component of wcc or not on train
         df_final_test['same_comp'] = df_final_test.apply(lambda row:
                                                 belongs_to_same_wcc(row['source_node'],row['des
In [79]: #saving to disk beacuse above operation takes much time so at every check point saving
         df_final_train.to_csv('df_final_train_some1.csv',index=False)
         df_final_test.to_csv('df_final_test_some1.csv',index=False)
In [16]: df_final_train = pd.read_csv('df_final_train_some1.csv')
         df_final_test = pd.read_csv('df_final_test_some1.csv')
In [20]: #mapping shortest path on train
         df_final_train['shortest_path'] = df_final_train.apply(lambda row:
                                                 compute_shortest_path_length(row['source_node']
In [21]: #mapping shortest path on test
         df_final_test['shortest_path'] = df_final_test.apply(lambda row:
                                                 compute_shortest_path_length(row['source_node']
In [22]: df_final_train.to_csv('df_final_train_some2.csv',index=False)
         df_final_test.to_csv('df_final_test_some2.csv',index=False)
In [41]: #page rank for source and destination in Train
         #if anything not there in train graph then adding mean page rank
         df_final_train['page_rank_s'] = df_final_train.source_node.apply(lambda x:pr.get(x,mear
         df_final_train['page_rank_d'] = df_final_train.destination_node.apply(lambda x:pr.get(x
In [42]: #page rank for source and destination in Test
         #if anything not there in train graph then adding mean page rank
         df_final_test['page_rank_s'] = df_final_test.source_node.apply(lambda x:pr.get(x,mean_r
         df_final_test['page_rank_d'] = df_final_test.destination_node.apply(lambda x:pr.get(x,m))
In [43]: #Katz centrality score for source and destination in Train and test
         #if anything not there in train graph then adding mean katz score
         df_final_train['katz_s'] = df_final_train.source_node.apply(lambda x: katz.get(x,mean_k
         df_final_train['katz_d'] = df_final_train.destination_node.apply(lambda x: katz.get(x,m
         df_final_test['katz_s'] = df_final_test.source_node.apply(lambda x: katz.get(x,mean_kat
         df_final_test['katz_d'] = df_final_test.destination_node.apply(lambda x: katz.get(x,mea
In [46]: #Hits algorithm score for source and destination in Train
         #if anything not there in train graph then adding 0
         df_final_train['hubs_s'] = df_final_train.source_node.apply(lambda x: hits[0].get(x,0))
         df_final_train['hubs_d'] = df_final_train.destination_node.apply(lambda x: hits[0].get(
         df_final_train['authorities_s'] = df_final_train.source_node.apply(lambda x: hits[1].ge
         df_final_train['authorities_d'] = df_final_train.destination_node.apply(lambda x: hits[
```

```
In [47]: #Hits algorithm score for source and destination in Train
         \#if anything not there in train graph then adding 0
         df_final_test['hubs_s'] = df_final_test.source_node.apply(lambda x: hits[0].get(x,0))
         df_final_test['hubs_d'] = df_final_test.destination_node.apply(lambda x: hits[0].get(x,
         df_final_test['authorities_s'] = df_final_test.source_node.apply(lambda x: hits[1].get(
         df_final_test['authorities_d'] = df_final_test.destination_node.apply(lambda x: hits[1]
In [50]: #dependent varible i.e link exist or not
         df_final_train['indicator_link'] = y_final_train
         df_final_test['indicator_link'] = y_final_test
In [48]: #storing to db
         from pandas import HDFStore, DataFrame
         hdf = HDFStore('storage_temp.h5')
In [51]: hdf.put('train_df',df_final_train, format='table', data_columns=True)
In [52]: hdf.put('test_df',df_final_test, format='table', data_columns=True)
In [14]: del g
In [17]: #reading from db
         from pandas import read_hdf
         df_final_train = read_hdf('storage_temp.h5', 'train_df',mode='r')
         df_final_test = read_hdf('storage_temp.h5', 'test_df',mode='r')
Adding SVD Features:
In [13]: #for sud features to get feature vector creating a dict node val and inex in sud vector
         sadj_col = sorted(g.nodes())
         sadj_dict = { val:idx for idx,val in enumerate(sadj_col)}
         del sadj_col
In [20]: ##creating two df for U valuesfor train and test data with two columns source and destr
         #and each column will have a list of 6 svd features
         train_df_svd_u = pd.DataFrame()
         test_df_svd_u = pd.DataFrame()
         def svd_s(x):
             try:
                 z = sadj_dict[x]
                 return U[z]
             except:
                 return [0,0,0,0,0,0]
         train_df_svd_u['features_s'] = df_final_train.source_node.apply(lambda x: svd_s(x))
         train_df_svd_u['features_d'] = df_final_train.destination_node.apply(lambda x: svd_s(x)
         test_df_svd_u['features_s'] = df_final_test.source_node.apply(lambda x: svd_s(x))
         test_df_svd_u['features_d'] = df_final_test.destination_node.apply(lambda x: svd_s(x))
```

```
In [21]: ##creating two df for V valuesfor train and test data with two columns source and destr
         #and each column will have a list of 6 svd features
         train_df_svd_v = pd.DataFrame()
         test_df_svd_v = pd.DataFrame()
         def svd_v(x):
             try:
                 z = sadj_dict[x]
                 return V.T[z]
             except:
                 return [0,0,0,0,0,0]
         train_df_svd_v['features_s'] = df_final_train.source_node.apply(lambda x: svd_v(x))
         train_df_svd_v['features_d'] = df_final_train.destination_node.apply(lambda x: svd_v(x)
         test_df_svd_v['features_s'] = df_final_test.source_node.apply(lambda x: svd_v(x))
         test_df_svd_v['features_d'] = df_final_test.destination_node.apply(lambda x: svd_v(x))
In [22]: train_df_svd_u.index = df_final_train.index
         train_df_svd_v.index = df_final_train.index
         test_df_svd_u.index = df_final_test.index
         test_df_svd_v.index = df_final_test.index
In [23]: #Splitting those each one column into 6 features
         \#https://stackoverflow.com/questions/35491274/pandas-split-column-of-lists-into-multiplications
         df_final_train[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_
                                     pd.DataFrame(train_df_svd_u.features_s.values.tolist(), ind
         df_final_test[['svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5', 'svd_u_s
                                     pd.DataFrame(test_df_svd_u.features_s.values.tolist(), inde
         df_final_train[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_
                                     pd.DataFrame(train_df_svd_u.features_d.values.tolist(), ind
         df_final_test[['svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4', 'svd_u_d_5','svd_u_d
                                     pd.DataFrame(test_df_svd_u.features_d.values.tolist(), inde
In [24]: del train_df_svd_u
         del test_df_svd_u
In [25]: #Splitting those each one column into 6 features
         \#https://stackoverflow.com/questions/35491274/pandas-split-column-of-lists-into-multiplications
         df_final_train[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_
                                     pd.DataFrame(train_df_svd_v.features_s.values.tolist(), ind
         df_final_test[['svd_v_s_1','svd_v_s_2', 'svd_v_s_3', 'svd_v_s_4', 'svd_v_s_5', 'svd_v_s
                                     pd.DataFrame(test_df_svd_v.features_s.values.tolist(), inde
         df_final_train[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4','svd_v_d_5', 'svd_v_
                                     pd.DataFrame(train_df_svd_v.features_d.values.tolist(), ind
         df_final_test[['svd_v_d_1', 'svd_v_d_2', 'svd_v_d_3', 'svd_v_d_4','svd_v_d_5', 'svd_v_d
                                     pd.DataFrame(test_df_svd_v.features_d.values.tolist(), inde
In [26]: del train_df_svd_v
         del test_df_svd_v
         del U
```

```
del V
         del sadj_dict
In [28]: #data frame
         df final train columns
Out[28]: Index(['source_node', 'destination_node', 'jaccard_followers',
                'jaccard_followees', 'num_followers_s', 'num_followees_s',
                'num_followers_d', 'num_followees_d', 'inter_followers',
                'inter_followees', 'adar_index', 'follows_back', 'same_comp',
                'shortest_path', 'page_rank_s', 'page_rank_d', 'katz_s', 'katz_d',
                'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d', 'indicator_link',
                'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
                'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
                'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
                'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
                'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
               dtype='object')
  Storing data in HDF format
In [29]: from pandas import HDFStore,DataFrame
         hdf1 = HDFStore('storage_final_df.h5')
In [30]: hdf1.put('train_df',df_final_train, format='table', data_columns=True)
In [31]: hdf1.put('test_df',df_final_test, format='table', data_columns=True)
In [32]: hdf1.close()
In [2]: #reading
        from pandas import read_hdf
        df_final_train = read_hdf('storage_final_df.h5', 'train_df',mode='r')
        df_final_test = read_hdf('storage_final_df.h5', 'test_df',mode='r')
In [3]: df_final_train.columns
Out[3]: Index(['source_node', 'destination_node', 'jaccard_followers',
               'jaccard_followees', 'num_followers_s', 'num_followees_s',
               'num_followers_d', 'num_followees_d', 'inter_followers',
               'inter_followees', 'adar_index', 'follows_back', 'same_comp',
               'shortest_path', 'page_rank_s', 'page_rank_d', 'katz_s', 'katz_d',
               'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d', 'indicator_link',
               'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
               'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
               'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
               'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
               'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
              dtype='object')
```

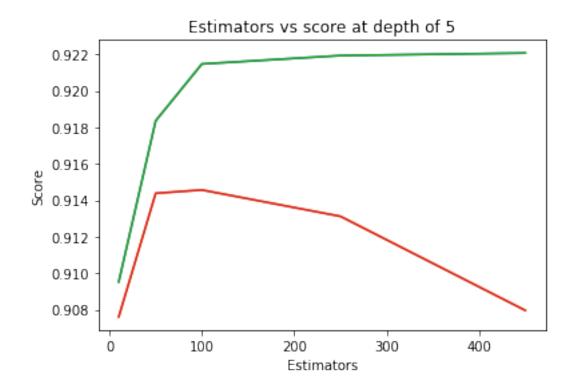
indicator_link is target varible.

```
In [4]: #dependent varible
       y_train = df_final_train.indicator_link
        y_test = df_final_test.indicator_link
In [5]: #dropping some columns
        df_final_train.drop(['source_node', 'destination_node','indicator_link'],axis=1,inplace=
        df_final_test.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,inplace=T
In [6]: df_final_train.columns
Out[6]: Index(['jaccard_followers', 'jaccard_followees', 'num_followers_s',
               'num_followees_s', 'num_followers_d', 'num_followees_d',
               'inter_followers', 'inter_followees', 'adar_index', 'follows_back',
               'same_comp', 'shortest_path', 'page_rank_s', 'page_rank_d', 'katz_s',
               'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
               'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
               'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
               'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
               'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
               'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
              dtype='object')
In [7]: df_final_test.columns
Out[7]: Index(['jaccard_followers', 'jaccard_followees', 'num_followers_s',
               'num_followees_s', 'num_followers_d', 'num_followees_d',
               'inter_followers', 'inter_followees', 'adar_index', 'follows_back',
               'same_comp', 'shortest_path', 'page_rank_s', 'page_rank_d', 'katz_s',
               'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
               'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
               'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
               'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
               'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
               'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6'],
              dtype='object')
In [8]: print('Train Shape', df_final_train.shape)
        print('Test Shape',df_final_test.shape)
Train Shape (15100030, 44)
Test Shape (3775008, 44)
0.2.4 Machine learning Models
In [9]: from sklearn.ensemble import RandomForestClassifier
```

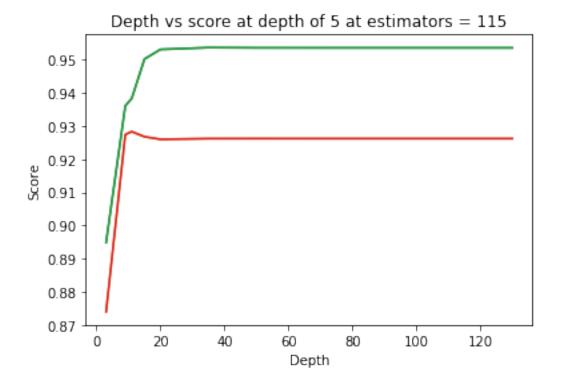
32

from sklearn.metrics import f1_score

```
In [54]: estimators = [10,50,100,250,450]
         train_scores = []
         test_scores = []
         for i in estimators:
             clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                     max_depth=5, max_features='auto', max_leaf_nodes=None,
                     min_impurity_decrease=0.0, min_impurity_split=None,
                     min_samples_leaf=52, min_samples_split=120,
                     min_weight_fraction_leaf=0.0, n_estimators=i, n_jobs=-1,random_state=25,ver
             clf.fit(df_final_train,y_train)
             train_sc = f1_score(y_train,clf.predict(df_final_train))
             test_sc = f1_score(y_test,clf.predict(df_final_test))
             test_scores.append(test_sc)
             train_scores.append(train_sc)
             print('Estimators = ',i,'Train Score',train_sc,'test Score',test_sc)
         plt.plot(estimators,train_scores,label='Train Score')
         plt.plot(estimators,test_scores,label='Test Score')
         plt.xlabel('Estimators')
         plt.ylabel('Score')
         plt.title('Estimators vs score at depth of 5')
Estimators = 10 Train Score 0.909522473891829 test Score 0.9076068019574423
Estimators = 50 Train Score 0.9183594774113881 test Score 0.9143837381083021
Estimators = 100 Train Score 0.9214777800537078 test Score 0.9145669218732931
Estimators = 250 Train Score 0.9219390207399591 test Score 0.9131197428892744
Estimators = 450 Train Score 0.922078108477195 test Score 0.9079599330754532
```



```
In [37]: depths = [3,9,11,15,20,35,50,70,130]
        train scores = []
        test_scores = []
        for i in depths:
            clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                     max_depth=i, max_features='auto', max_leaf_nodes=None,
                     min_impurity_decrease=0.0, min_impurity_split=None,
                     min_samples_leaf=52, min_samples_split=120,
                     min_weight_fraction_leaf=0.0, n_estimators=115, n_jobs=-1,random_state=25,v
            clf.fit(df_final_train,y_train)
             train_sc = f1_score(y_train,clf.predict(df_final_train))
             test_sc = f1_score(y_test,clf.predict(df_final_test))
             test_scores.append(test_sc)
             train_scores.append(train_sc)
             print('depth = ',i,'Train Score',train_sc,'test Score',test_sc)
         plt.plot(depths,train_scores,label='Train Score')
        plt.plot(depths,test_scores,label='Test Score')
        plt.xlabel('Depth')
        plt.ylabel('Score')
        plt.title('Depth vs score at depth of 5 at estimators = 115')
        plt.show()
depth = 3 Train Score 0.8949603900952848 test Score 0.8741052014942736
depth = 9 Train Score 0.9360254429127565 test Score 0.9273782435689065
depth = 11 Train Score 0.9382050540742228 test Score 0.9282749447838731
depth = 15 Train Score 0.9500877674602457 test Score 0.9267378494825711
depth = 20 Train Score 0.9529872894706812 test Score 0.9259543094148095
depth = 35 Train Score 0.9535361101001514 test Score 0.9261583609015455
depth = 50 Train Score 0.9534687885463979 test Score 0.9261677119534877
depth = 70 Train Score 0.9534623667394676 test Score 0.9261637624878941
depth = 130 Train Score 0.9534623667394676 test Score 0.9261637624878941
```

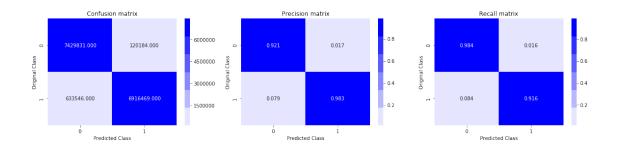


```
In [11]: from sklearn.metrics import f1_score
         from sklearn.ensemble import RandomForestClassifier
         from sklearn.metrics import f1_score
         from sklearn.model_selection import RandomizedSearchCV
         from scipy.stats import randint as sp_randint
         from scipy.stats import uniform
         param_dist = {"n_estimators":sp_randint(105,125),
                       "max_depth": sp_randint(10,15),
                       "min_samples_split": sp_randint(110,190),
                       "min_samples_leaf": sp_randint(25,65)}
         clf = RandomForestClassifier(random_state=25,n_jobs=-1)
         rf_random = RandomizedSearchCV(clf, param_distributions=param_dist,
                                            n_iter=5,cv=10,scoring='f1',random_state=25)
         rf_random.fit(df_final_train,y_train)
         import pickle
         pickle.dump(rf_random,open('rf_random_2.p','wb'))
In [12]: rf_random.grid_scores_
```

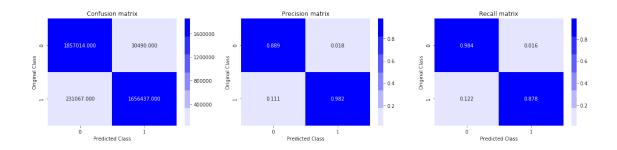
```
Out[12]: [mean: 0.94717, std: 0.00143, params: {'max_depth': 14, 'min_samples_leaf': 51, 'min_samples_
                                       mean: 0.94104, std: 0.00162, params: {'max_depth': 12, 'min_samples_leaf': 33, 'min_sa
                                       mean: 0.93796, std: 0.00125, params: {'max_depth': 11, 'min_samples_leaf': 56, 'min_sa
                                       mean: 0.94485, std: 0.00120, params: {'max_depth': 13, 'min_samples_leaf': 49, 'min_samples_leaf': 49,
                                       mean: 0.94772, std: 0.00114, params: {'max_depth': 14, 'min_samples_leaf': 28, 'min_samples_leaf': 28,
In [13]: print('mean test scores',rf_random.cv_results_['mean_test_score'])
                                    print('mean train scores',rf_random.cv_results_['mean_train_score'])
mean test scores [0.94716991 0.94103944 0.93796448 0.94485387 0.94772461]
mean train scores [0.94719986 0.94105021 0.93797457 0.94487586 0.94775144]
In [14]: #best estimator
                                   rf_random.best_estimator_
Out[14]: RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                                                                                   max_depth=14, max_features='auto', max_leaf_nodes=None,
                                                                                   min_impurity_decrease=0.0, min_impurity_split=None,
                                                                                   min_samples_leaf=28, min_samples_split=111,
                                                                                   min_weight_fraction_leaf=0.0, n_estimators=121, n_jobs=-1,
                                                                                   oob_score=False, random_state=25, verbose=0, warm_start=False)
In [15]: clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                                                                                   max_depth=14, max_features='auto', max_leaf_nodes=None,
                                                                                   min_impurity_decrease=0.0, min_impurity_split=None,
                                                                                   min_samples_leaf=28, min_samples_split=111,
                                                                                   min_weight_fraction_leaf=0.0, n_estimators=121, n_jobs=-1,
                                                                                   oob_score=False, random_state=25, verbose=0, warm_start=False)
                                   clf.fit(df_final_train,y_train)
                                   import pickle
                                   pickle.dump(clf,open('clf_rf.p','wb'))
In [22]: print('Train f1 score',f1_score(y_train,y_pred_train))
                                   print('Test f1 score',f1_score(y_test,y_pred_test))
Train f1 score 0.9483274727305785
Test f1 score 0.926825556291337
In [18]: from sklearn.metrics import confusion_matrix
                                    def plot_confusion_matrix(test_y, predict_y):
                                                   C = confusion_matrix(test_y, predict_y)
                                                   A = (((C.T)/(C.sum(axis=1))).T)
                                                   B = (C/C.sum(axis=0))
                                                    plt.figure(figsize=(20,4))
```

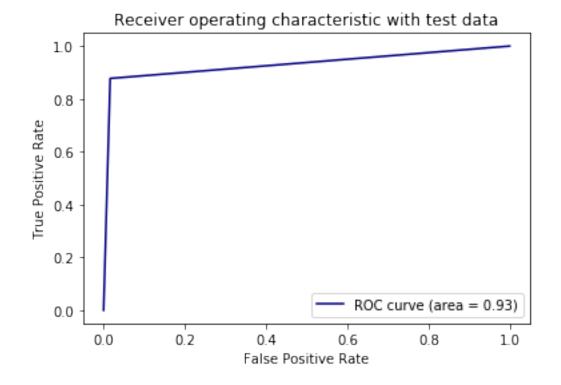
```
labels = [0,1]
             # representing A in heatmap format
             cmap=sns.light_palette("blue")
             plt.subplot(1, 3, 1)
             sns.heatmap(C, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=la
             plt.xlabel('Predicted Class')
             plt.ylabel('Original Class')
             plt.title("Confusion matrix")
             plt.subplot(1, 3, 2)
             sns.heatmap(B, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=la
             plt.xlabel('Predicted Class')
             plt.ylabel('Original Class')
             plt.title("Precision matrix")
             plt.subplot(1, 3, 3)
             # representing B in heatmap format
             sns.heatmap(A, annot=True, cmap=cmap, fmt=".3f", xticklabels=labels, yticklabels=la
             plt.xlabel('Predicted Class')
             plt.ylabel('Original Class')
             plt.title("Recall matrix")
             plt.show()
In [18]: y_pred_train = clf.predict(df_final_train)
         y_pred_test = clf.predict(df_final_test)
         print('Train confusion_matrix')
         plot_confusion_matrix(y_train,y_pred_train)
         print('Test confusion_matrix')
         plot_confusion_matrix(y_test,y_pred_test)
```

Train confusion_matrix

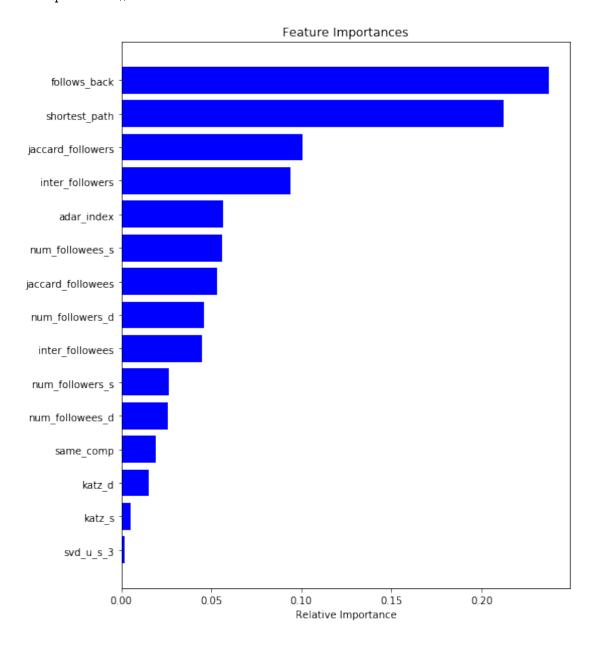


Test confusion_matrix





```
indices = (np.argsort(importances))[-15:]
plt.figure(figsize=(8,10))
plt.title('Feature Importances')
plt.barh(range(len(indices)), importances[indices], color='b', align='center')
plt.yticks(range(len(indices)), [features[i] for i in indices])
plt.xlabel('Relative Importance')
plt.show()
```



Some other features:

Weight Features In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other. credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

```
In [2]: ##reading data
        from pandas import read_hdf
        df_final_train = read_hdf('storage_final_df.h5', 'train_df',mode='r')
        df_final_test = read_hdf('storage_final_df.h5', 'test_df',mode='r')
In [38]: #Getting basic info from our data
         g=nx.read_edgelist('train_data.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=in
         print(nx.info(g))
Name:
Type: DiGraph
Number of nodes: 1780722
Number of edges: 7550015
Average in degree:
                      4.2399
Average out degree:
                       4.2399
In [39]: from tqdm import tqdm
                                    W = \frac{1}{\sqrt{1 + |X|}}
                                                                                    (4)
```

it is directed graph so calculated Weighted in and Weighted out differently

```
In [40]: #weight for source and destination of each link
    Weight_in = []
    Weight_out = []
    for i in tqdm(g.nodes()):
        s1=set(g.predecessors(i))
        w_in = 1.0/(np.sqrt(1+len(s1)))
        s2=set(g.successors(i))
        w_out = 1.0/(np.sqrt(1+len(s2)))
        Weight_in.append((i,w_in))
        Weight_out.append((i,w_out))

100%|| 1780722/1780722 [00:14<00:00, 122313.55it/s]

In [42]: #converting as dict to map DataFrame
        Weight_in_dict = dict(Weight_in)
        Weight_out_dict = dict(Weight_out)</pre>
```

```
In [45]: #saving to disk
         import pickle
         pickle.dump(Weight_in_dict,open('Weight_in_dict.p','wb'))
         pickle.dump(Weight_out_dict,open('Weight_out_dict.p','wb'))
In [6]: import pickle
        Weight_in_dict = pickle.load(open('Weight_in_dict.p','rb'))
        Weight_out_dict = pickle.load(open('Weight_out_dict.p','rb'))
In [7]: #for imputing
       mean_weight_in = np.mean(list(Weight_in_dict.values()))
        mean_weight_out = np.mean(list(Weight_out_dict.values()))
In [8]: #mapping to pandas train
        df_final_train['Weight_in'] = df_final_train.destination_node.apply(lambda x: Weight_in_
        df_final_train['Weight_out'] = df_final_train.source_node.apply(lambda x: Weight_out_dic
        #mapping to pandas test
        df_final_test['Weight_in'] = df_final_test.destination_node.apply(lambda x: Weight_in_di
        df_final_test['Weight_out'] = df_final_test.source_node.apply(lambda x: Weight_out_dict.
  From above derived some other features
In [9]: #some features engineerings on tose in and out weigts
        df_final_train['Weight_f1'] = df_final_train.Weight_in + df_final_train.Weight_out
        df_final_train['Weight_f2'] = df_final_train.Weight_in * df_final_train.Weight_out
        df_final_train['Weight_f3'] = (2*df_final_train.Weight_in + 1*df_final_train.Weight_out)
        df_final_train['Weight_f4'] = (1*df_final_train.Weight_in + 2*df_final_train.Weight_out)
        #some features engineerings on tose in and out weigts
        df_final_test['Weight_f1'] = df_final_test.Weight_in + df_final_test.Weight_out
        df_final_test['Weight_f2'] = df_final_test.Weight_in * df_final_test.Weight_out
        df_final_test['Weight_f3'] = (2*df_final_test.Weight_in + 1*df_final_test.Weight_out)
        df_final_test['Weight_f4'] = (1*df_final_test.Weight_in + 2*df_final_test.Weight_out)
In [11]: df_final_train.columns
Out[11]: Index(['source_node', 'destination_node', 'jaccard_followers',
                'jaccard_followees', 'num_followers_s', 'num_followees_s',
                'num_followers_d', 'num_followees_d', 'inter_followers',
                'inter_followees', 'adar_index', 'follows_back', 'same_comp',
                'shortest_path', 'page_rank_s', 'page_rank_d', 'katz_s', 'katz_d',
                'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d', 'indicator_link',
                'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
                'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
                'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
                'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
                'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6', 'Weight_in',
                'Weight_out', 'Weight_f1', 'Weight_f2', 'Weight_f3', 'Weight_f4'],
               dtype='object')
In [13]: del Weight_in_dict
         del Weight_out_dict
```

Some Other SVD Features:

```
In [14]: #adj matrix
         g=nx.read_edgelist('train_data.csv',delimiter=',',create_using=nx.DiGraph(),nodetype=in
         Adj = nx.adjacency_matrix(g,nodelist=sorted(g.nodes()))
         Adj = Adj.asfptype()
         Adj
Out[14]: <1780722x1780722 sparse matrix of type '<class 'numpy.float64'>'
                 with 7550015 stored elements in Compressed Sparse Row format>
In [15]: #nodes list sorted
         nodes_list = list(g.nodes())
         nodes_list = sorted(nodes_list)
         #node and index as key value pairs, i need it because getting index from list is O(n)
         # but from dict its O(1)
         nodes_list_dict = {k:v for v,k in enumerate(nodes_list)}
In [16]: # deleting because of sapce constraint
         del g
         del nodes_list
In [17]: ### sud decomposition
         from sklearn.decomposition import TruncatedSVD
         svd = TruncatedSVD(n_components=200, n_iter=7, random_state=42)
         svd_mat = svd.fit_transform(Adj)
In [18]: # deleting because of sapce constraint
         del Adj
In [19]: import pickle
         pickle.dump(svd_mat,open('svd_mat.p','wb'))
         pickle.dump(nodes_list_dict,open('nodes_list_dict.p','wb'))
In [5]: import pickle
        svd_mat = pickle.load(open('svd_mat.p','rb'))
        nodes_list_dict = pickle.load(open('nodes_list_dict.p','rb'))
In [21]: #for Train
         \textit{### SVD dot product of source and destination vectores}
         ### SVD mean of source and destination vector
         from tqdm import tqdm
         svd_dot = []
         svd_mean_dest = []
         svd_mean_source = []
         for idx,temp_series in tqdm(df_final_train.iterrows(),total=df_final_train.shape[0]):
             in_idx = nodes_list_dict.get(temp_series.destination_node,'X')
             out_idx = nodes_list_dict.get(temp_series.source_node,'X')
             if in_idx != 'X':
```

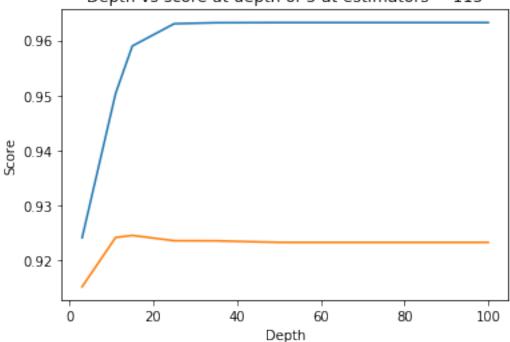
```
#mean of total svd vector
                 svd_mean_dest.append(np.squeeze(np.mean(svd_mat[in_idx,:])))
             else:
                 svd_mean_dest.append(0)
             if out_idx != 'X':
                 #mean of total sud vector
                 svd_mean_source.append(np.squeeze(np.mean(svd_mat[out_idx,:])))
             else:
                 svd_mean_source.append(0)
             if ( in_idx != 'X' and out_idx != 'X' ):
                 #dot product of sud vector of Source and destination
                 svd_temp = np.dot(svd_mat[in_idx,:],svd_mat[out_idx,:])
                 svd_dot.append(svd_temp)
             else:
                 svd_dot.append(0)
100%|| 15100030/15100030 [16:53<00:00, 14894.68it/s]
In [22]: import pickle
         pickle.dump(svd_dot,open('svd_dot_train.p','wb'))
         pickle.dump(svd_mean_source,open('svd_mean_source_train.p','wb'))
         pickle.dump(svd_mean_dest,open('svd_mean_dest_train.p','wb'))
In [23]: ###mappng above features into
         df_final_train['svd_dot'] = svd_dot
         df_final_train['svd_mean_s'] = svd_mean_source
         df_final_train['svd_mean_d'] = svd_mean_dest
In [24]: del svd_dot
         del svd_mean_dest
         del svd_mean_source
In [25]: ###for test
         ### SVD dot product of source and destination vectores
         ### SVD mean of source and destination vector
         from tqdm import tqdm
         svd_dot = []
         svd_mean_dest = []
         svd_mean_source = []
         for idx, temp_series in tqdm(df_final_test.iterrows(),total=df_final_test.shape[0]):
             in_idx = nodes_list_dict.get(temp_series.destination_node, 'X')
             out_idx = nodes_list_dict.get(temp_series.source_node,'X')
             if in_idx != 'X':
                 svd_mean_dest.append(np.squeeze(np.mean(svd_mat[in_idx,:])))
             else:
                 svd_mean_dest.append(0)
```

```
if out_idx != 'X':
                 svd_mean_source.append(np.squeeze(np.mean(svd_mat[out_idx,:])))
             else:
                 svd_mean_source.append(0)
             if ( in_idx != 'X' and out_idx != 'X' ):
                 svd_temp = np.dot(svd_mat[in_idx,:],svd_mat[out_idx,:])
                 svd_dot.append(svd_temp)
             else:
                 svd_dot.append(0)
100%|| 3775008/3775008 [04:14<00:00, 14830.45it/s]
In [26]: import pickle
         pickle.dump(svd_dot,open('svd_dot_test.p','wb'))
         pickle.dump(svd_mean_source,open('svd_mean_source_test.p','wb'))
         pickle.dump(svd_mean_dest,open('svd_mean_dest_test.p','wb'))
In [27]: ###mappng above features into
         df_final_test['svd_dot'] = svd_dot
         df_final_test['svd_mean_s'] = svd_mean_source
         df_final_test['svd_mean_d'] = svd_mean_dest
In [28]: del svd_dot
         del svd_mean_dest
         del svd_mean_source
         del nodes_list_dict
In [32]: #saving to db
         from pandas import HDFStore, DataFrame
         hdf2 = HDFStore('storage_all_features.h5')
In [33]: #saving to disk
         hdf2.put('train_df',df_final_train, format='table', data_columns=True)
In [34]: #saving to disk
         hdf2.put('test_df',df_final_test, format='table', data_columns=True)
In [35]: hdf2.close()
In [2]: ## reading
        from pandas import read_hdf
        df_final_train = read_hdf('storage_all_features.h5', 'train_df',mode='r')
       df_final_test = read_hdf('storage_all_features.h5', 'test_df',mode='r')
In [3]: #dependent varible
        y_train = df_final_train.indicator_link
        y_test = df_final_test.indicator_link
```

```
In [4]: #dropping some columns
        df_final_train.drop(['source_node', 'destination_node', 'indicator_link'],axis=1,inplace=
        df_final_test.drop(['source_node', 'destination_node', 'indicator_link'], axis=1,inplace=T
In [5]: df_final_train.columns
Out[5]: Index(['jaccard_followers', 'jaccard_followees', 'num_followers_s',
               'num_followees_s', 'num_followers_d', 'num_followees_d',
               'inter_followers', 'inter_followees', 'adar_index', 'follows_back',
               'same_comp', 'shortest_path', 'page_rank_s', 'page_rank_d', 'katz_s',
               'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
               'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
               'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
               'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
               'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
               'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6', 'Weight_in',
               'Weight_out', 'Weight_f1', 'Weight_f2', 'Weight_f3', 'Weight_f4',
               'svd_dot', 'svd_mean_s', 'svd_mean_d'],
              dtype='object')
In [6]: df final test columns
Out[6]: Index(['jaccard_followers', 'jaccard_followees', 'num_followers_s',
               'num_followees_s', 'num_followers_d', 'num_followees_d',
               'inter_followers', 'inter_followees', 'adar_index', 'follows_back',
               'same_comp', 'shortest_path', 'page_rank_s', 'page_rank_d', 'katz_s',
               'katz_d', 'hubs_s', 'hubs_d', 'authorities_s', 'authorities_d',
               'svd_u_s_1', 'svd_u_s_2', 'svd_u_s_3', 'svd_u_s_4', 'svd_u_s_5',
               'svd_u_s_6', 'svd_u_d_1', 'svd_u_d_2', 'svd_u_d_3', 'svd_u_d_4',
               'svd_u_d_5', 'svd_u_d_6', 'svd_v_s_1', 'svd_v_s_2', 'svd_v_s_3',
               'svd_v_s_4', 'svd_v_s_5', 'svd_v_s_6', 'svd_v_d_1', 'svd_v_d_2',
               'svd_v_d_3', 'svd_v_d_4', 'svd_v_d_5', 'svd_v_d_6', 'Weight_in',
               'Weight_out', 'Weight_f1', 'Weight_f2', 'Weight_f3', 'Weight_f4',
               'svd_dot', 'svd_mean_s', 'svd_mean_d'],
              dtype='object')
In [7]: depths = [3,11,15,25,35,50,100]
        train scores = []
        test_scores = []
        for i in depths:
            clf = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                    max_depth=i, max_features=11, max_leaf_nodes=None,
                    min_impurity_decrease=0.0, min_impurity_split=None,
                    min_samples_leaf=52, min_samples_split=120,
                    min_weight_fraction_leaf=0.0, n_estimators=115, n_jobs=-1,random_state=25,ve
            clf.fit(df_final_train,y_train)
            train_sc = f1_score(y_train,clf.predict(df_final_train))
            test_sc = f1_score(y_test,clf.predict(df_final_test))
```

```
test_scores.append(test_sc)
            train_scores.append(train_sc)
            print('depth = ',i,'Train Score',train_sc,'test Score',test_sc)
        plt.plot(depths,train_scores,label='Train Score')
        plt.plot(depths,test_scores,label='Test Score')
        plt.xlabel('Depth')
        plt.ylabel('Score')
        plt.title('Depth vs score at depth of 5 at estimators = 115')
        plt.show()
depth = 3 Train Score 0.924170984571304 test Score 0.9152763777461715
depth = 11 Train Score 0.9503796519459076 test Score 0.924220959419516
depth = 15 Train Score 0.9590027669458241 test Score 0.9245986302407551
depth = 25 Train Score 0.9630456634334905 test Score 0.9236317354926886
depth = 35 Train Score 0.9632218097809785 test Score 0.9236077277146334
depth = 50 Train Score 0.9632496325083799 test Score 0.9233378118527031
depth = 100 Train Score 0.9632496325083799 test Score 0.9233378118527031
```

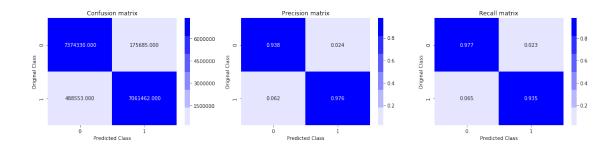
Depth vs score at depth of 5 at estimators = 115



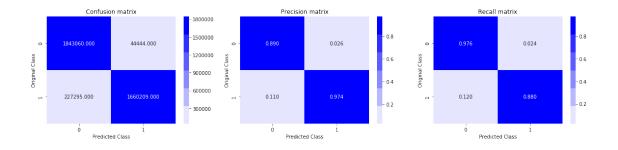
```
clf = RandomForestClassifier(random_state=25,n_jobs=-1)
        rf_random = RandomizedSearchCV(clf,param_distributions=param_dist,
                                           n_iter=5,cv=10,scoring='f1',random_state=25)
       rf_random.fit(df_final_train,y_train)
        print(rf_random.grid_scores_)
        print()
        print(rf_random.cv_results_)
        import pickle
        pickle.dump(rf_random,open('rf_random_final.p','wb'))
In [10]: rf_random.grid_scores_
Out[10]: [mean: 0.95251, std: 0.00109, params: {'max_depth': 14, 'max_features': 'auto', 'min_sa
         mean: 0.95499, std: 0.00083, params: {'max_depth': 12, 'max_features': 11, 'min_sample
         mean: 0.95229, std: 0.00054, params: {'max_depth': 11, 'max_features': 11, 'min_sample
         mean: 0.95015, std: 0.00092, params: {'max_depth': 13, 'max_features': 'auto', 'min_sa
         mean: 0.94129, std: 0.00128, params: {'max_depth': 11, 'max_features': 'auto', 'min_sa
In [11]: print('mean test scores',rf_random.cv_results_['mean_test_score'])
         print('mean train scores',rf_random.cv_results_['mean_train_score'])
mean test scores [0.95250539 0.95498837 0.95228519 0.95015108 0.94129217]
mean train scores [0.95258963 0.95503648 0.95233589 0.95022736 0.94129525]
In [12]: rf_random.best_estimator_
Out[12]: RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                     max_depth=12, max_features=11, max_leaf_nodes=None,
                     min_impurity_decrease=0.0, min_impurity_split=None,
                     min_samples_leaf=33, min_samples_split=138,
                     min_weight_fraction_leaf=0.0, n_estimators=109, n_jobs=-1,
                     oob_score=False, random_state=25, verbose=0, warm_start=False)
In [13]: clf_1 = RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
                     max_depth=12, max_features=11, max_leaf_nodes=None,
                     min_impurity_decrease=0.0, min_impurity_split=None,
                     min_samples_leaf=33, min_samples_split=138,
                     min_weight_fraction_leaf=0.0, n_estimators=109, n_jobs=-1,
                     oob_score=False, random_state=25, verbose=0, warm_start=False)
         clf_1.fit(df_final_train,y_train)
         import pickle
         pickle.dump(clf_1,open('clf2_1.p','wb'))
```

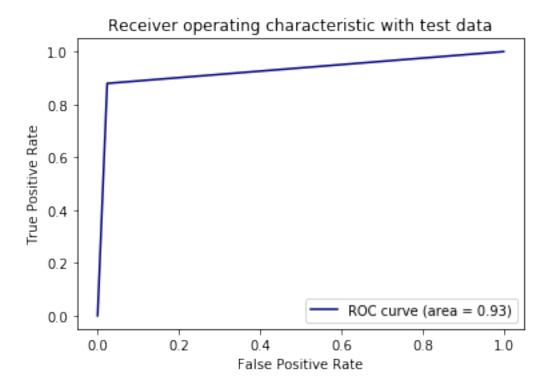
```
In [6]: clf_1 = pickle.load(open('/home/u19292/clf2_1.p','rb'))
In [7]: y_train_pred1 = clf_1.predict(df_final_train)
        y_test_pred1 = clf_1.predict(df_final_test)
In [29]: from sklearn.metrics import f1_score
         print('Train f1 score',f1_score(y_train,y_train_pred1))
         print('Test f1 score',f1_score(y_test,y_test_pred1))
Train f1 score 0.9550800890664483
Test f1 score 0.9243521371699511
In [8]: df_final_test1 = read_hdf('storage_all_features.h5', 'test_df',mode='r')
In [9]: train_nodes_pos = pickle.load(open('train_nodes_pos.p','rb'))
In [32]: from tqdm import tqdm
         count_error = 0
         count_cold_err = 0
         total_cold_nodes = 0
         for i,row in tqdm(df_final_test1.iterrows(),total=df_final_test1.shape[0]):
             if row['source_node'] not in train_nodes_pos or row['destination_node'] not in trai
                 total_cold_nodes = total_cold_nodes + 1
                 if y_test.values[i] != y_test_pred1[i]:
                     count_error = count_error + 1
                     count_cold_err = count_cold_err + 1
             else:
                 if y_test.values[i] != y_test_pred1[i]:
                     count_error = count_error + 1
100%|| 3775008/3775008 [02:07<00:00, 29524.56it/s]
In [35]: print('Length of Total Test data',len(df_final_test1))
         print('Total no of errors in test data',count_error)
         print('Leghth of test data where any one of nodes are not there in Train',total_cold_no
         print('Total no of error Where any one of nodes are not there in Train',count_cold_err)
Length of Total Test data 3775008
Total no of errors in test data 271739
Leghth of test data where any one of nodes are not there in Train 253173
Total no of error Where any one of nodes are not there in Train 91728
In [41]: print('Total Error is {}%'.format(count_error/len(df_final_test1)*100))
         print('Error Where nodes not in Train Data is {}%'.format(count_cold_err/len(df_final_t
Total Error is 7.198368851138859%
Error Where nodes not in Train Data is 2.429875645296646%
```

Train confusion_matrix

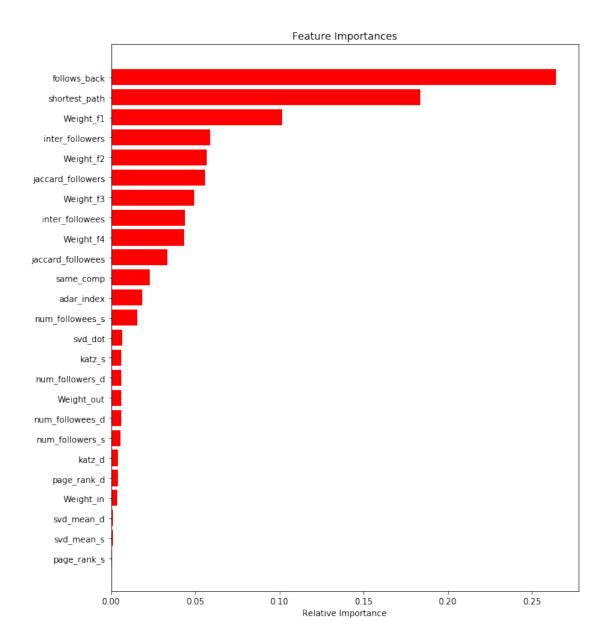


Test confusion_matrix





```
In [32]: features = df_final_train.columns
    importances = clf_1.feature_importances_
    indices = (np.argsort(importances))[-25:]
    plt.figure(figsize=(10,12))
    plt.title('Feature Importances')
    plt.barh(range(len(indices)), importances[indices], color='r', align='center')
    plt.yticks(range(len(indices)), [features[i] for i in indices])
    plt.xlabel('Relative Importance')
    plt.show()
```



improved some score and we can observe that Weight features and svd dot produts is somewhat better features than so many features.

1.838595e-01

1.016269e-01

5.900783e-02

shortest_path

inter_followers

Weight_f1

TT : 1 + CO	F 704000 00
Weight_f2	5.704880e-02
jaccard_followers	5.575706e-02
Weight_f3	4.926787e-02
inter_followees	4.368723e-02
Weight_f4	4.320862e-02
jaccard_followees	3.365333e-02
same_comp	2.304795e-02
adar_index	1.836028e-02
num_followees_s	1.532252e-02
svd_dot	6.457175e-03
katz_s	6.271872e-03
num_followers_d	6.163456e-03
Weight_out	6.068274e-03
num_followees_d	5.916338e-03
num_followers_s	5.488586e-03
katz_d	4.136551e-03
page_rank_d	4.104543e-03
Weight_in	3.734412e-03
svd_mean_d	1.305648e-03
svd_mean_s	1.046256e-03
page_rank_s	4.384363e-04
svd_v_d_3	1.556681e-04
svd_u_s_3	1.194442e-04
svd_u_d_3	1.100387e-04
svd_v_s_3	5.851178e-05
	2.462293e-05
svd_u_s_6	1.759360e-05
svd_v_s_6	
svd_v_d_6	1.725545e-05 1.137179e-05
svd_u_d_6	
hubs_s	5.677168e-06
svd_u_s_2	3.717209e-06
svd_v_s_2	3.399203e-06
authorities_s	2.399581e-06
authorities_d	2.198454e-06
hubs_d	1.640633e-06
svd_v_d_2	1.500757e-06
svd_v_s_1	1.477797e-06
svd_u_d_2	1.179593e-06
svd_u_s_5	5.564461e-07
svd_v_s_5	5.549624e-07
svd_u_s_4	4.290664e-07
svd_u_s_1	4.018964e-07
svd_u_d_5	1.630302e-07
svd_v_d_5	1.376959e-07
svd_v_d_4	1.319796e-07
svd_v_s_4	7.132748e-08
svd_u_d_4	3.841453e-08
svd_u_d_1	3.704987e-09

svd_v_d_1 0.000000e+00