

# PAPER REVIEW

Presented By: Udochukwu Nweke  
CS734: Introduction to Information Retrieval  
Dr. Michael Nelson

October 12, 2017

# Paper 1

## Extension of Zipf's Law to Words and Phrases

Le Quan Ha, E. I. Sicilia-Garcia, Ji Ming, F. J. Smith  
School Computer Science  
Queen's University of Belfast Belfast  
BT7 1NN, Northern Ireland  
Date: 2002

## **Paper 2**

# **A Comparison of Document, Sentence, and Term Event Spaces**

Catherine Blake

School of Information and Library Science

University of North Carolina at Chapel Hill

North Carolina, NC 27599-3360

Date : 2006

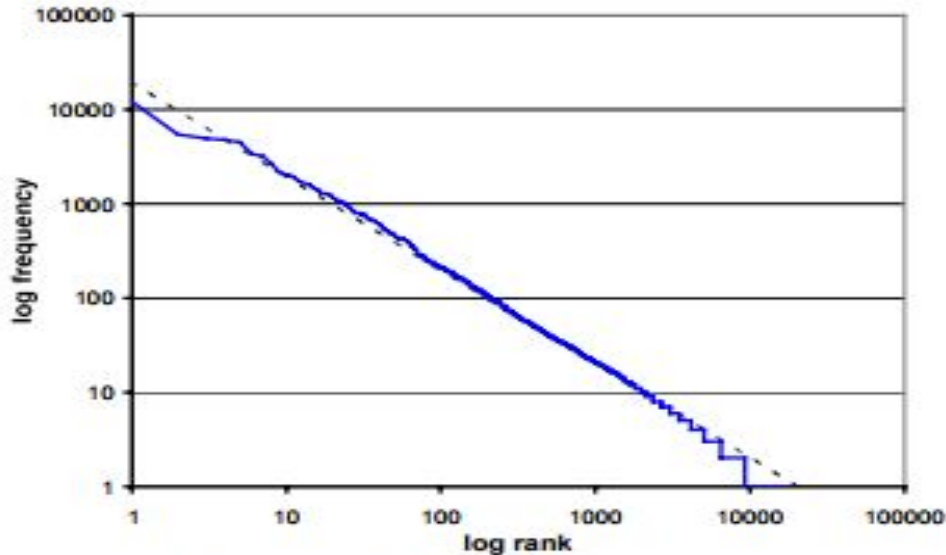
# Zipf's Law

- Observation: frequent words and rare words
- In English, in a random piece of text: “of” and “the” make up 10% of all occurrences
- A Word like “aardvark” is extremely rare
- Zipf's law states that the frequency of word tokens in a large corpus of natural language is inversely proportional to the rank.

$$f = \frac{k}{r}$$

Where  $f$  is the frequency of word in a corpus,  $r$  is the rank, and  $k$  is the constant for the corpus

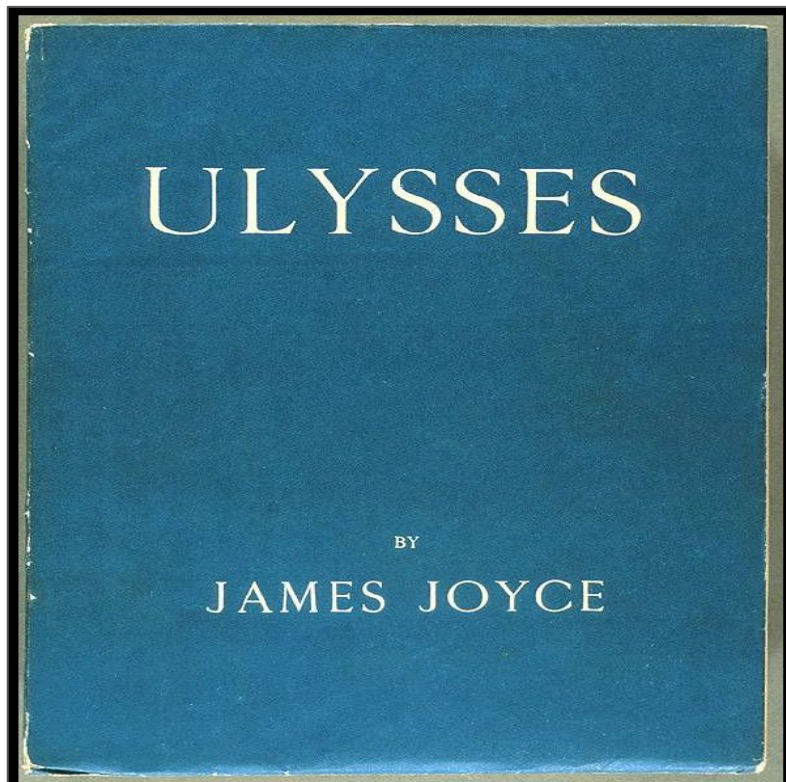
# Zipf's Curve



**Figure 1 Zipf curve for the unigrams extracted from a 250,000 word tokens corpus**

- After computing the frequencies and sorting the frequencies by rank
- Zipf's curve is a straight line with a slope of -1.

# Zipf's Law Discovery



- Zipf discovered the law by manually analyzing the frequency of words in the novel “Ulysses”
- The novel contains 29, 899 different word types associated with 260,430 word tokens

# Zipf's Law For Larger Corpora

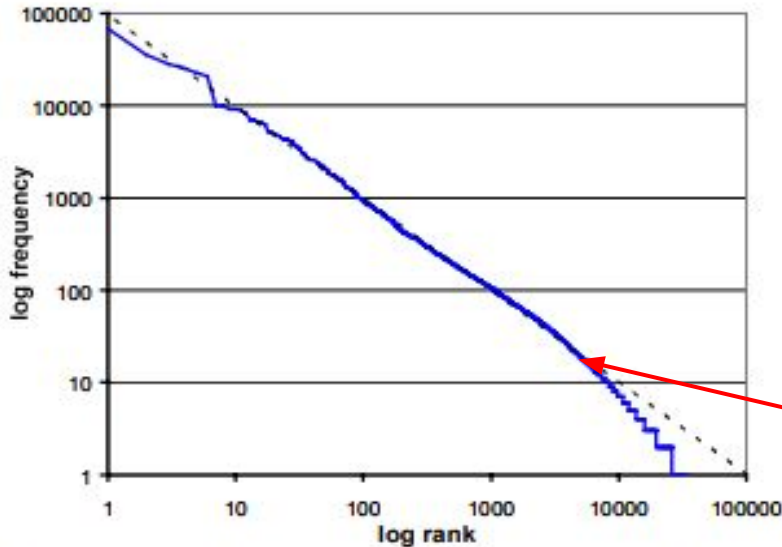
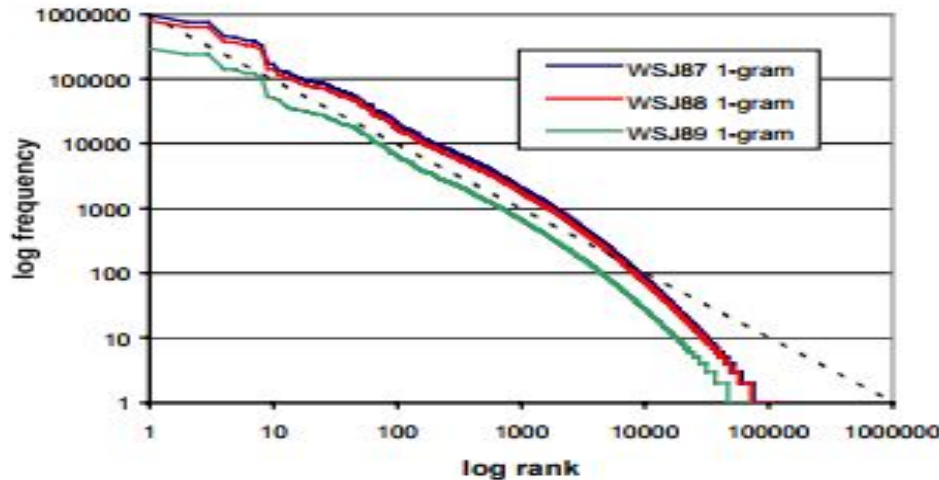


Figure 2 Zipf curve for the unigrams extracted from the 1 million words of the Brown corpus

After the development of more advanced PCs in 1980, a larger corpora of over a million word was processed and when Zipf's curve was drawn, it was found to drop below the zipf straight line with a slope of -1 for  $r > 5000$ .

# Exploring the Invalidity of Zipf's Law for Larger Corpora In Two Languages (Paper 1)



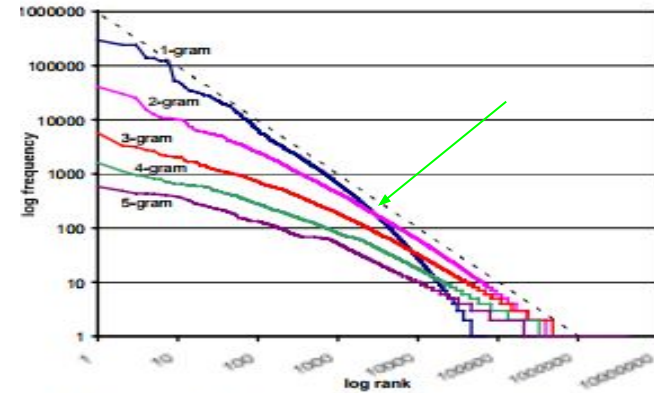
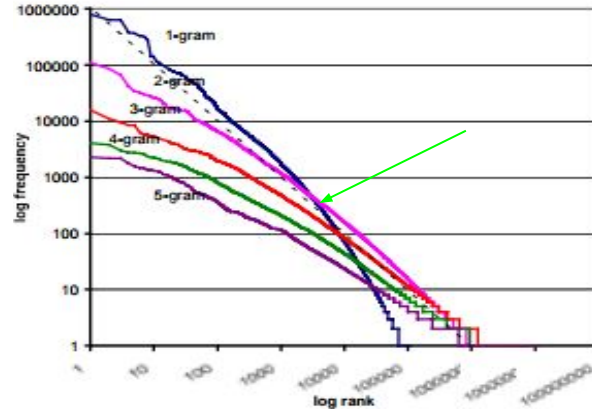
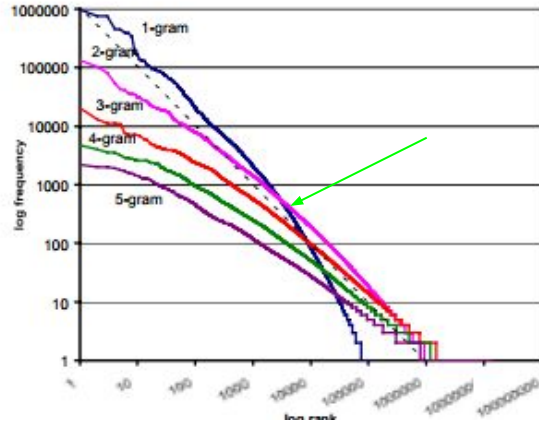
The English corpora used for these experiments were taken from the Wall Street journal (Paul & Baker, 1992) for 1987, 1988, 1989, with sizes approximately 19 million, 16 million and 6 million tokens respectively.



# English Corpora

- Documents are not made of individual words but also consist of phrases of 2, 3 and more word, usually called n grams.
- In order to draw Zipf's curve for  $n = 2$  to 5 grams, the frequency of n-gram in each corpus is computed and placed in a rank order.

# Zipf's curve for WSJ Corpus (n=1, 2, 3, 4 and 5 grams)



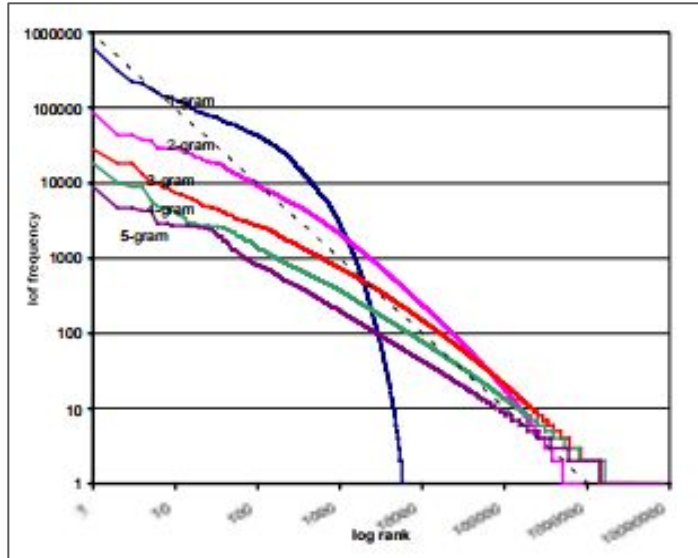
Although the Zipf's curves for the WSJ corpora follow a straight line, the unigram curves crosses the bigram when the rank is approximately 3,000 in all 3 cases

# Mandarin Corpora

The Mandarin corpus used in for experiments is the TREC Corpus. It was obtained from the People's Daily Newspaper from 01/1991 to 12/1993 and from the Xinhua News Agency for 04/1994 to 09/1995 from the Linguistic Data Consortium (<http://www ldc.upenn.edu>).

Note: The Mandarin language is a syllable-class language in which each syllable is the same time a word and a chinese character.

# Zipf's Curve For TREC Mandarin Corpus

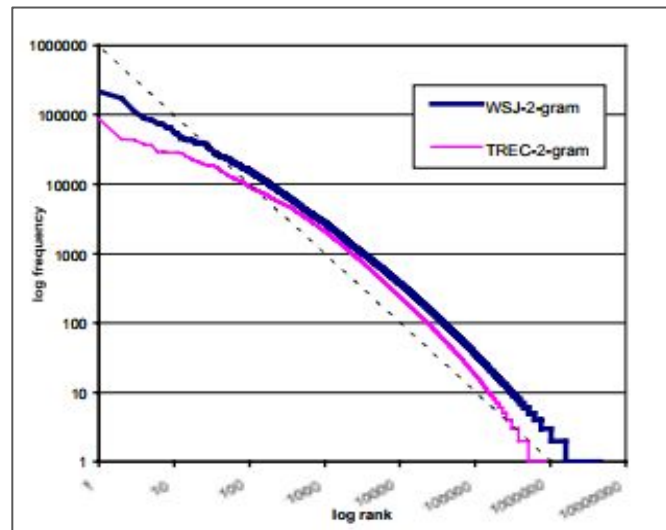
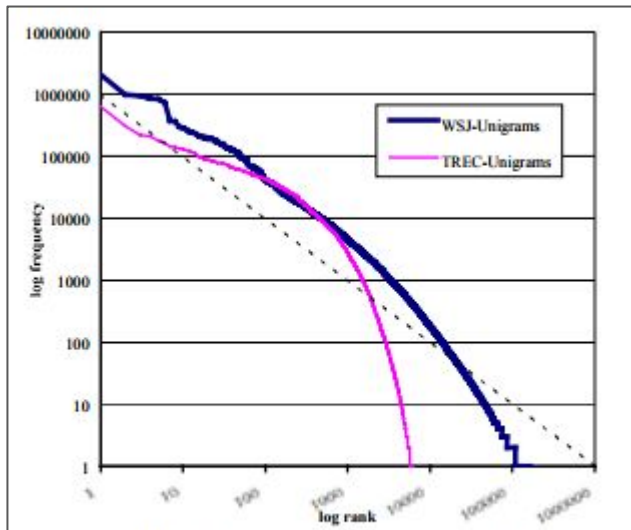


## Observations:

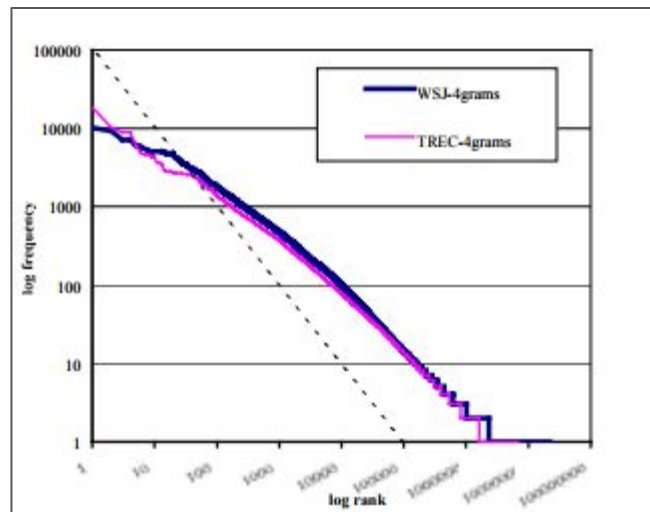
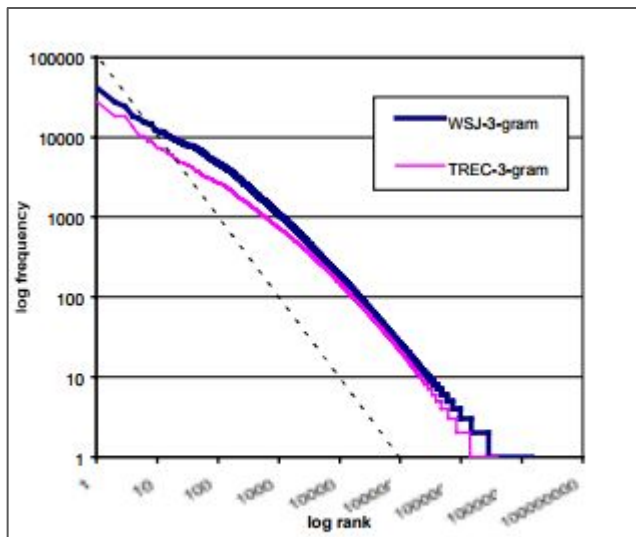
- The bigram curve in the mandarin is more curved than the bigram curve in English Corpora.
- The shapes of the other TREC n-gram Zipfian curves are similar to but not the same for those in the English Corpora.

# Comparing Unigrams and 2-grams For The WSJ English And TREC Mandarin Corpora

The English curves are for the 3 WSJ corpora joined together making 40 million word corpus.



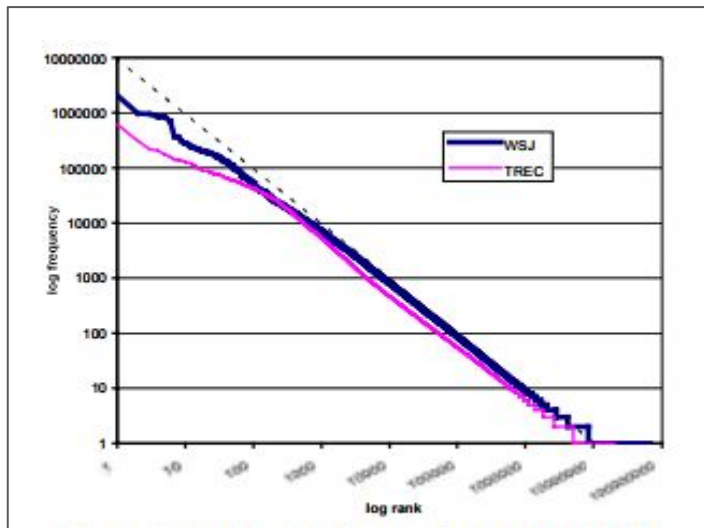
# Comparing Trigram and 4-grams For The WSJ English And TREC Mandarin Corpora



# Why Zipf's Law Is Invalid for Large Corpora

- Zipf's law derivation was solely based on single words and it failed for English when the number of word types was greater than 5000 words
- In Mandarin, it failed almost immediately for unigrams
- Probably combining Mandarin compound words in bigram, trigram and higher n-gram statistics wouldn't have failed Zipf's law

# Combined n-grams Will Give A Better Zipf Curve



Zipf's curve for all unigram and n-gram together with their frequencies, sorted on frequency and put in a rank.

The combined n-gram curve follows Zipf's straight line with slope close to -1



# Findings

- The combined curve for both languages are straight line with slope close to -1 for all ranks  $> 100$ .
- The result has been found to be remarkable for 3 other natural languages: Irish, Latin and Vietnamese, in preliminary experiment.

## **Paper 2**

# **A Comparison of Document, Sentence, and Term Event Spaces**

Catherine Blake

School of Information and Library Science

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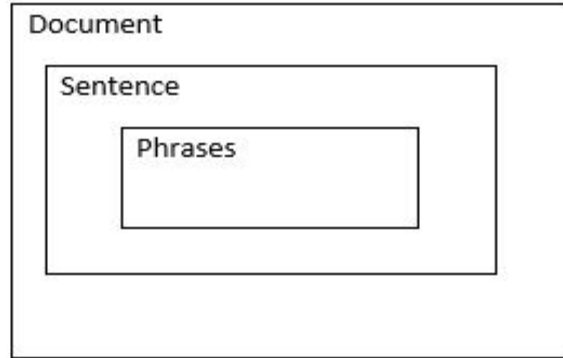
North Carolina, NC 27599-3360

Date: 2006

# Identifying Relevant Documents In Terms of IDF

- In Information retrieval, relevant documents are identified by comparing query terms with terms from a document corpus
- The most common corpus weighting scheme is term frequency (TF) x inverse document frequency (IDF)
- $IDF = \frac{\text{Number of Document}(N)}{\text{Number of Document}(n_i) \text{ with term}(t_i)}$
- N is the total number of corpus documents;  $n_i$  is the number of documents that contain at least one occurrence of the term  $t_i$ ; and  $t_i$  is a term, which is typically stemmed.

# IDF Should Not Be The Only Corpus Weighting Scheme



- Information retrieval systems trends from document to sub-document retrieval
- Sentence for summarization
- Words or Phrases for question answering system
- IDF should be replaced with ISF and ITF when sub-documents are retrieved

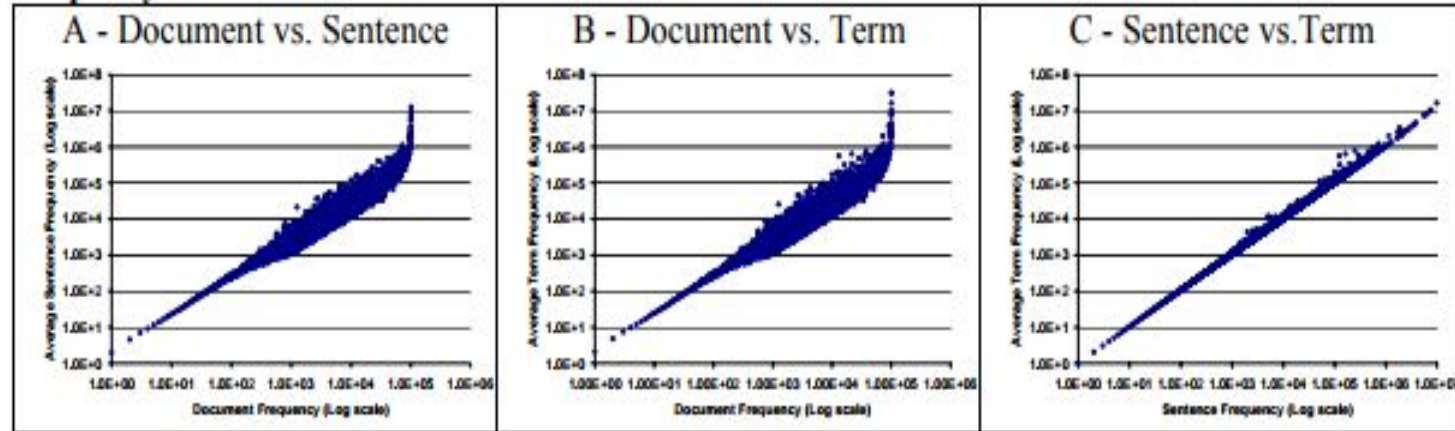
$$\text{ISF} = \frac{\text{Number of Sentence}(N)}{\text{Number of Sentence}(n_i) \text{ with term}(t_i)}$$

# ISF and ITF Challenges

- The challenge is that although document language models (IDF) has had unprecedented empirical success, language models based on a sentence or term do not appear to work well (Robertson, 2004).
- The goal is to uncover why IDF is the best weighting scheme using different metrics

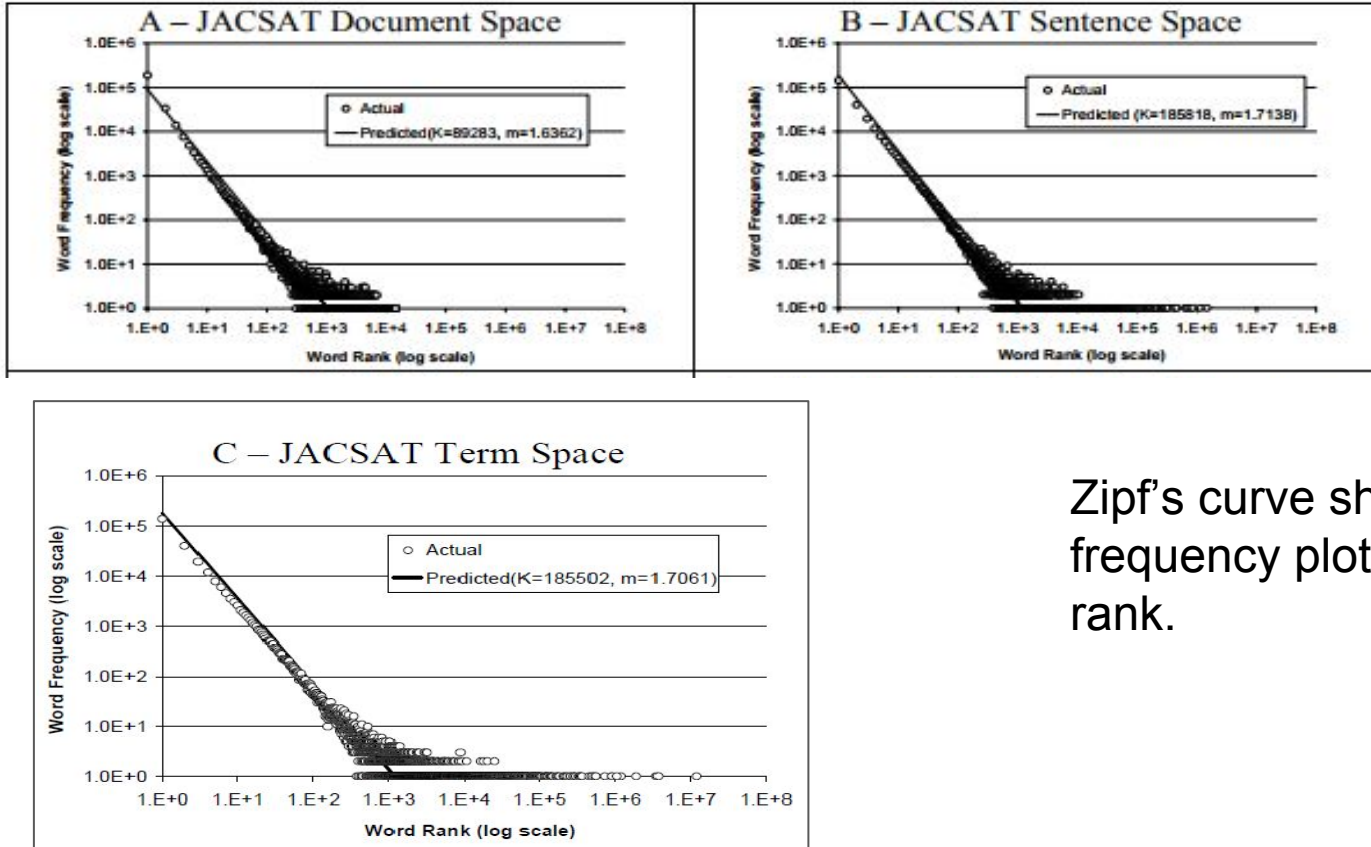
# Raw Term Comparison

## Frequency



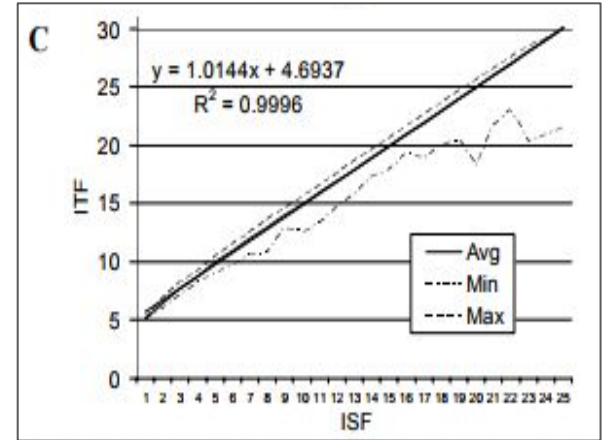
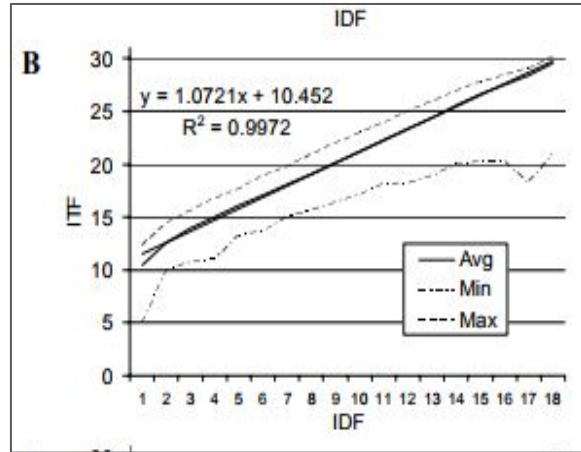
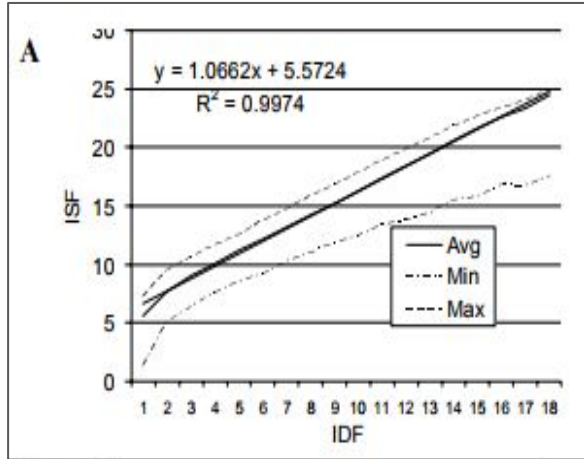
- A compares the document and the average term frequency
- B compares the the document and the average term frequency
- C shows the sentence frequency and average term frequency, demonstrating that sentence and term are highly correlated, unlike A and B

# Zipf Law Holds For All Event Spaces



Zipf's curve showing word frequency plot against rank.

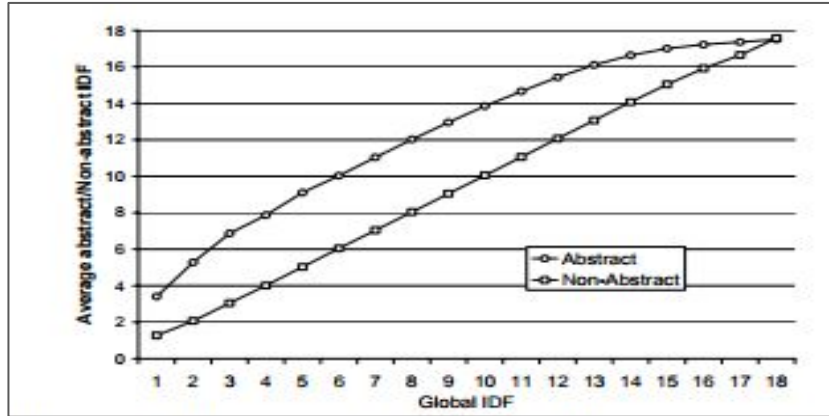
# Direct IDF, ISF, and ITF Comparisons



- A shows the average, minimum and maximum ISF for each rounded IDF value. Although the graph shows a correlation for A and B, the average ISF and ITF values are 5.57 and 10.45 times greater than the corresponding IDF respectively.
- Although C shows a stronger correlation between ITF and ISF, the ITF values are higher than the equivalent ISF values



# Abstract Versus Full-Text Comparison



The graph explains that the weight assigned to stemmed terms in abstract were higher than the weight assigned to terms in the body of a document.

# IDF, ISF And ITF Values of Abstract and Main Text

| Word        | Document (IDF) |        |        | Sentence (ISF) |        |        | Term (ITF) |        |        |
|-------------|----------------|--------|--------|----------------|--------|--------|------------|--------|--------|
|             | Abs            | NonAbs | All    | Abs            | NonAbs | All    | Abs        | NonAbs | All    |
| the         | 1.014          | 1.004  | 1.001  | 1.342          | 1.364  | 1.373  | 4.604      | 9.404  | 5.164  |
| chemist     | 11.074         | 5.957  | 5.734  | 13.635         | 12.820 | 12.553 | 22.838     | 17.592 | 17.615 |
| synthesis   | 14.331         | 11.197 | 10.827 | 17.123         | 18.000 | 17.604 | 26.382     | 22.632 | 22.545 |
| electrochem | 17.501         | 15.251 | 15.036 | 20.293         | 22.561 | 22.394 | 29.552     | 26.965 | 27.507 |

The Table shows IDF, ISF and ITF values for abstract and non abstract documents. ITF assigned the highest weights followed by ISF and IDF has the least value.

# Findings

- A linear transformation between document to sub document will be difficult because there is no direct correlation between document and sub documents.
- Although IDF, ISF and ITF are highly correlated, replacing IDF with ISF or ITF will result in a weighting scheme where corpus weight dominated the weight assigned to a query and document terms.

# Relationship Between Paper 1 and Paper 2

Zipf's law based solely on single term failed for large corpora when the number of word type approached 5000.

Both papers use Zipf's law to understand the distribution of words in a corpus. Paper 1 shows that different corpora follow the Zipf's law, but when the size of a corpus grows, some of the curves deviated from Zipf's straight line curve.

Paper 2 shows that Zipf's law is applicable to multiple event spaces such as Document (IDF), Sentence (ISF), and term (ITF).

Zipf's law was a better fit when term space comprised of both word and phrases