



Build a supply chain design model risk management oriented

Consider disruption rates to select the best options as to minimize the entire Supply Chain disruption probability

Single sourcing/ Dual sourcing

Then implement it in the Graves model, with disruption rate as a supplementary option's parameter

#### Model

- ON/OFF cycles
- Each option characterized by the parameters  $(\lambda, \psi)$

- Expected duration of a ON cycle is 1/λ and OFF cycle 1/ ψ
- Duration of the cycles exponentially distributed



- Assumption: at most one option can be disrupted
- The Supply Chain thus becomes disrupted as well ( everything stops, no profit during this period)
- 1 option j selected for each stage i
- Functionnal equation:

$$P(SC=OFF) = P(\bigcup_{i} Xi = OFF)$$
$$= \sum_{i} P(Xi = OFF)$$

$$\min_{(\lambda i, \psi i)} \sum_{i} \frac{\lambda i}{\lambda i + \psi i}$$



- Assumption: at most one option can be disrupted
- The Supply Chain thus NEVER becomes disrupted ( as the other option of the stage will still be ON)
- 2 options (λi,ψi) and (αi,βi) selected for each stage i
- Functionnal equation:

$$P(SC=OFF) = 0$$

$$P(1 \ option = OFF) = P(\bigcup_{i} Xi = "OFF")$$

$$= \sum_{i} P(Xi = "OFF")$$

$$\min_{\substack{(\lambda i, \psi i) \\ (\alpha i, \beta i)}} \sum_{i} \frac{\lambda i}{\lambda i + \psi i} + \frac{\alpha i}{\alpha i + \beta i}$$



- <u>Assumption</u>: at most one node can be disrupted, which happens only when both options are disrupted
- The Supply Chain thus can be disrupted in this case ( minimize this probability)
- 2 options (λi,ψi) and (αi,βi) selected for each stage i
- 4 state Markov Chain, {00,01,10,11}

		option1	
		ON	OFF
o p t i o n	NO	11 ===================================	$\beta$ $\beta$ $0$ $\psi$
	OFF	01 -	$\beta$ 00

# Dual sourcing (more realistic)

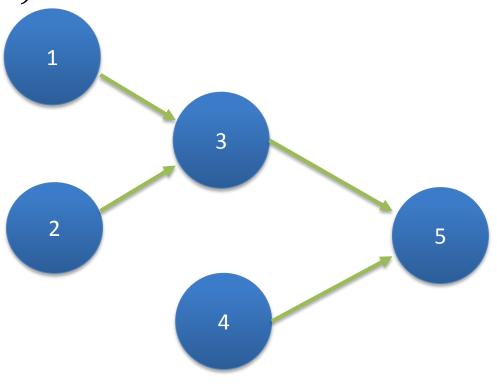
- Consider the probability that both options can be OFF for the node to be disrupted
- P(Xi = OFF) = P(01,00) \* P(11,01) + P(10,00) \* P(11,10)
- Functionnal equation:

$$P(SC=OFF) = P(\bigcup_{i} Xi = OFF)$$
$$= \sum_{i} P(Xi = OFF)$$

$$\min_{\substack{(\lambda i, \psi i) \\ (\alpha i, \beta i)}} \sum_{i} \alpha i \lambda i \left[ \frac{1}{(\alpha i + \psi i)(\lambda i + \psi i)} + \frac{1}{(\lambda i + \beta i)(\alpha i + \beta i)} \right]$$

### Simple Simulations

• Supply Chain network ( 5 nodes, 4 options at each)



## **Simple Simulations**



- Single sourcing P(SC = OFF) = 0.465557
- Dual sourcing P(SC = OFF) = 0 P(1 option is OFF) = 1.633458
- Dual sourcing (more realistic) P(SC = OFF) = 0.032104

#### Next Steps

• Consider disruption at supply chain design phase in Grave's model

Integrate disruption parameter in the options' choice

• Compare with Seiji's results (consider disruptions effect on the operational phase only)

