



Exponential distribution

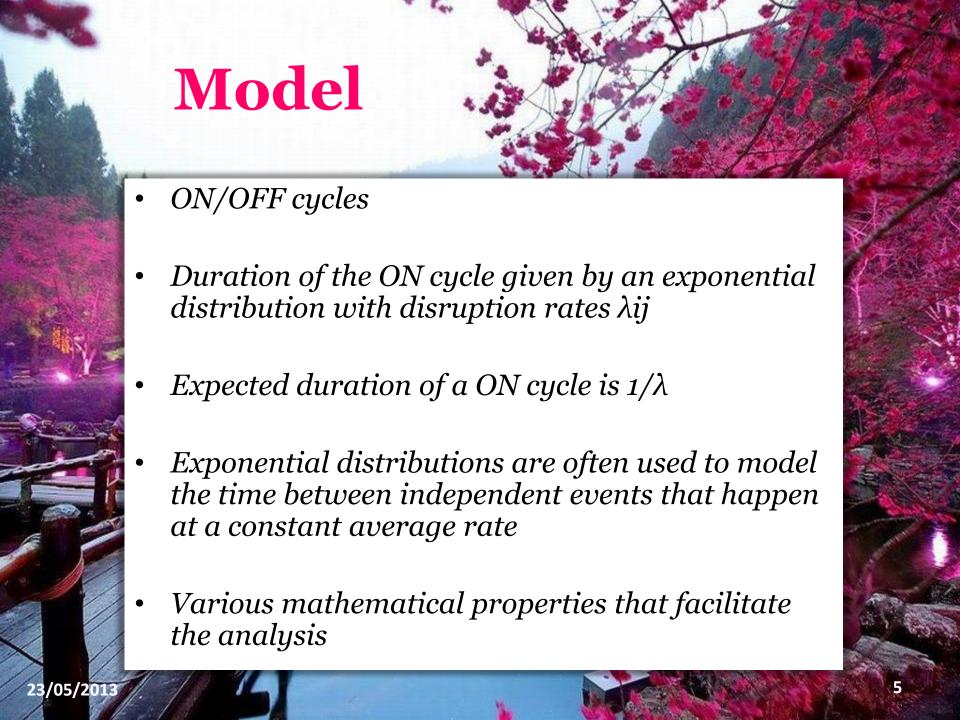
- Family of continuous probability distributions
- Describes the time between events in a Poisson process

$$f(x;\lambda) = \begin{cases} \lambda e^{-\lambda x}, & x \ge 0, \\ 0, & x < 0. \end{cases}$$

$$E[X] = \frac{1}{\lambda}.$$

$$\operatorname{Var}[X] = \frac{1}{\lambda^2}.$$

$$\Pr(T > s + t \mid T > s) = \Pr(T > t)$$
 for all $s, t \ge 0$.



Model

- Let Xi be the exponentially distributed variable that represents the ON cycle duration of node I
- Then the duration of the ON cycle of the total supply chain is also exponentially distributed with rate

$$\lambda = \lambda_1 + \cdots + \lambda_n$$
.

$$\Pr\left(\min\{X_1,\ldots,X_n\}>x\right)=\Pr\left(X_1>x \text{ and } \ldots \text{ and } X_n>x\right)$$

$$= \prod_{i=1}^{n} \Pr(X_i > x) = \prod_{i=1}^{n} \exp(-x\lambda_i) = \exp\left(-x\sum_{i=1}^{n} \lambda_i\right)$$

