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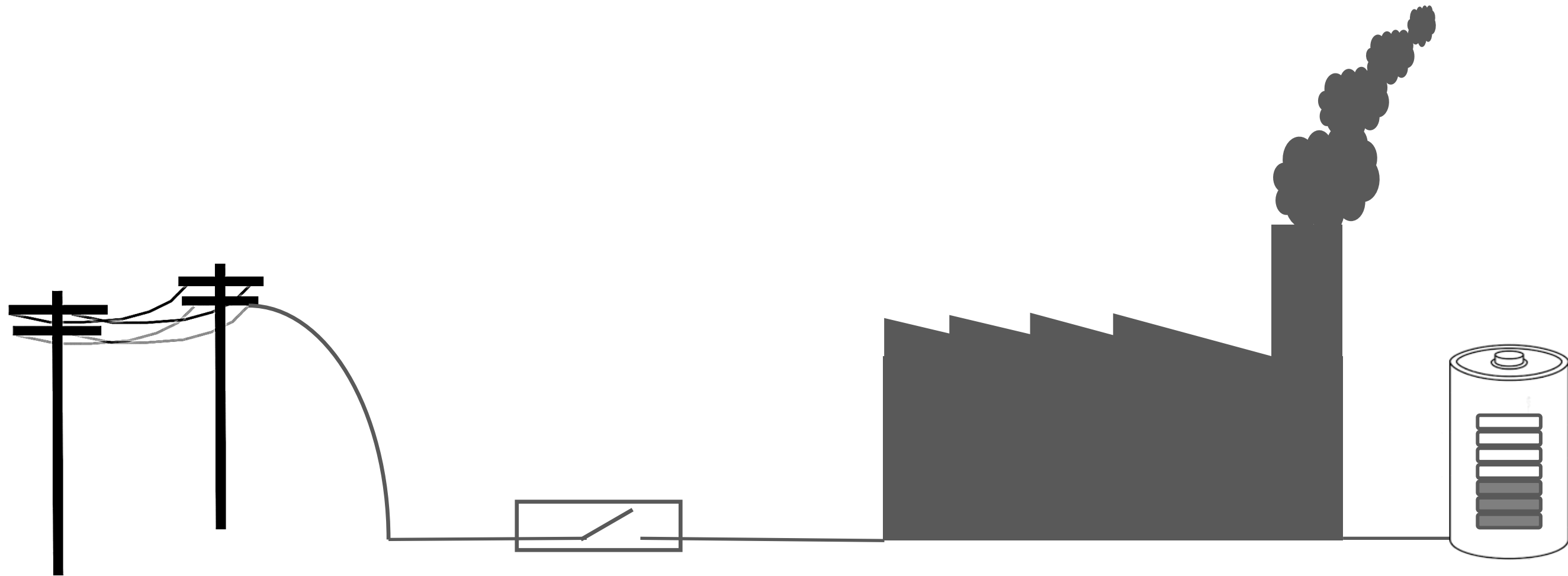
PHYSICS-INFORMED RECURRENT NEURAL NETWORKS

for the identification of a generic energy buffer system

Manu Lahariya¹, **Farzaneh Karami**², Chris Develder¹, Guillaume Crevecoeur²

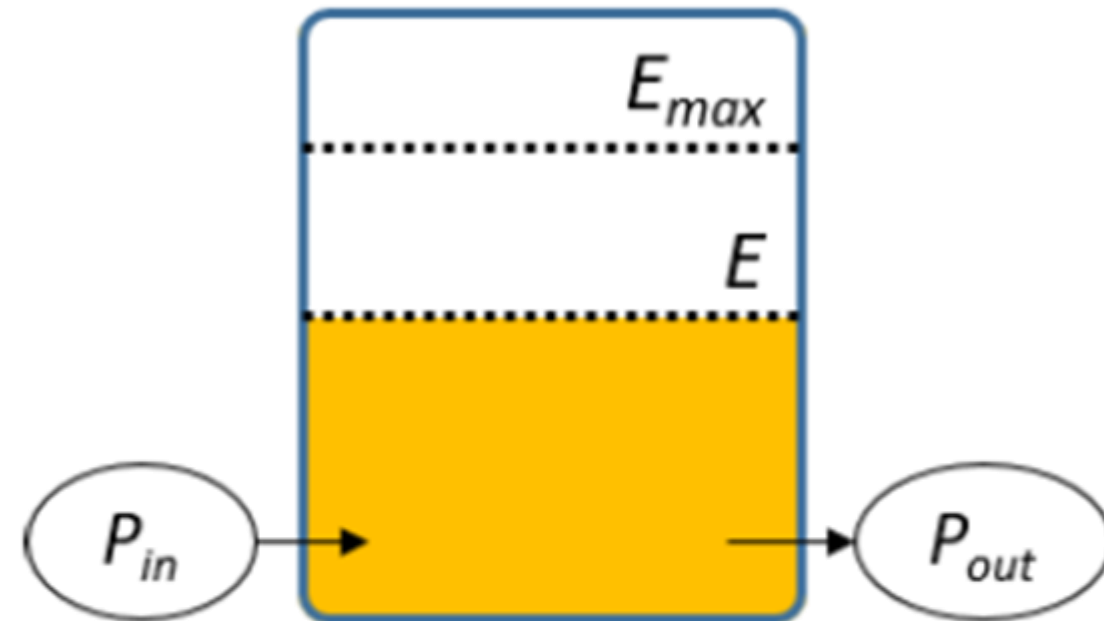
1.IDLab, Ghent University – imec

2.EEDT-DC lab, Ghent University, Flanders Make



1. Physic rules: white-box model
2. Data-driven approaches: black-box model
3. Combination (1 and 2): grey-box model



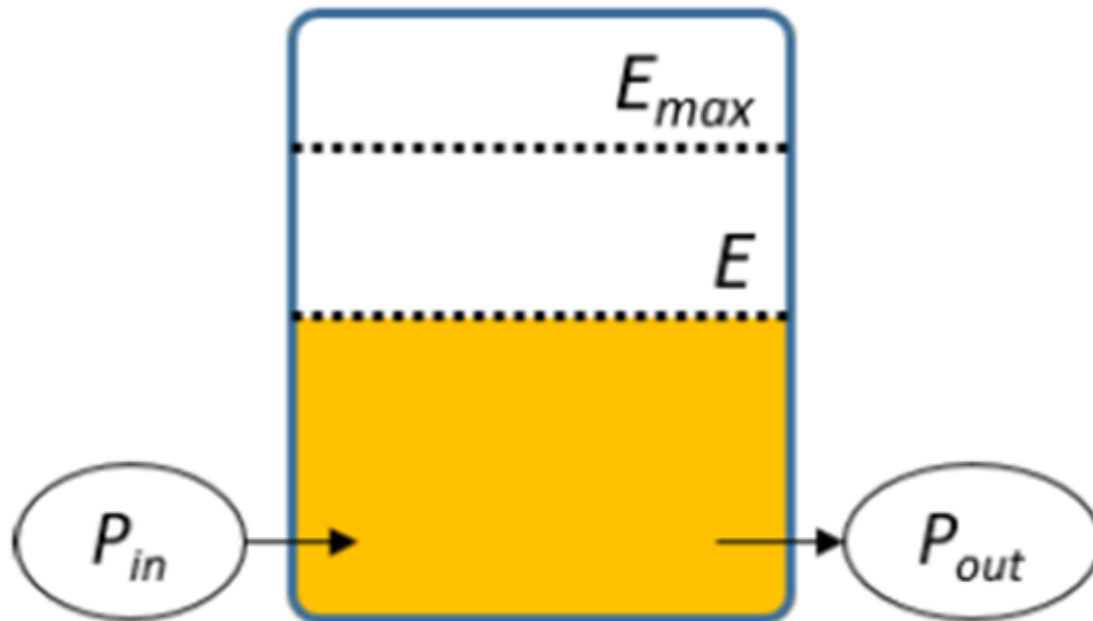


Generic buffer
(Used to represent
industrial processes in
form of virtual battery)

$$\frac{\partial m}{\partial t} = K(P_{out} - P_{in})$$

$$E = \frac{m - m_{min}}{K}$$

$$E_{min} \leq E \leq E_{max}$$

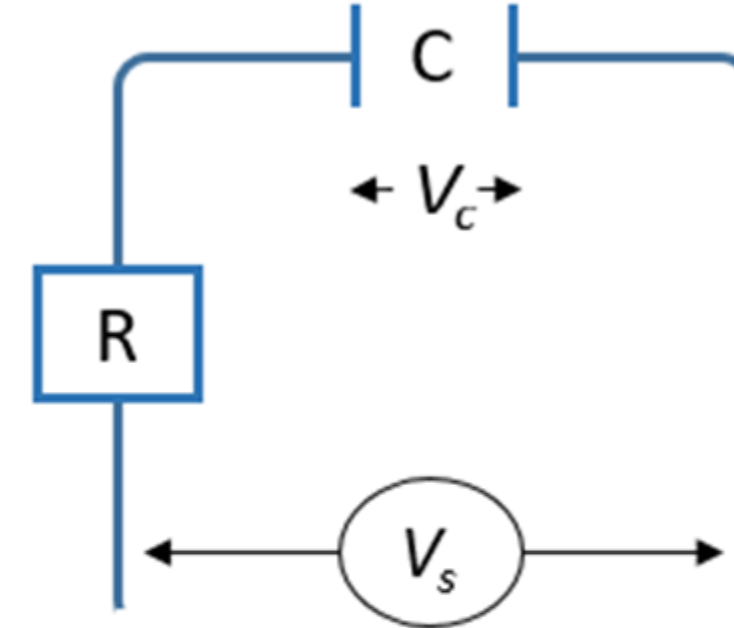


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RC-circuit as a virtual
battery
(V_s : Input voltage,
 V_c : Capacitor voltage)

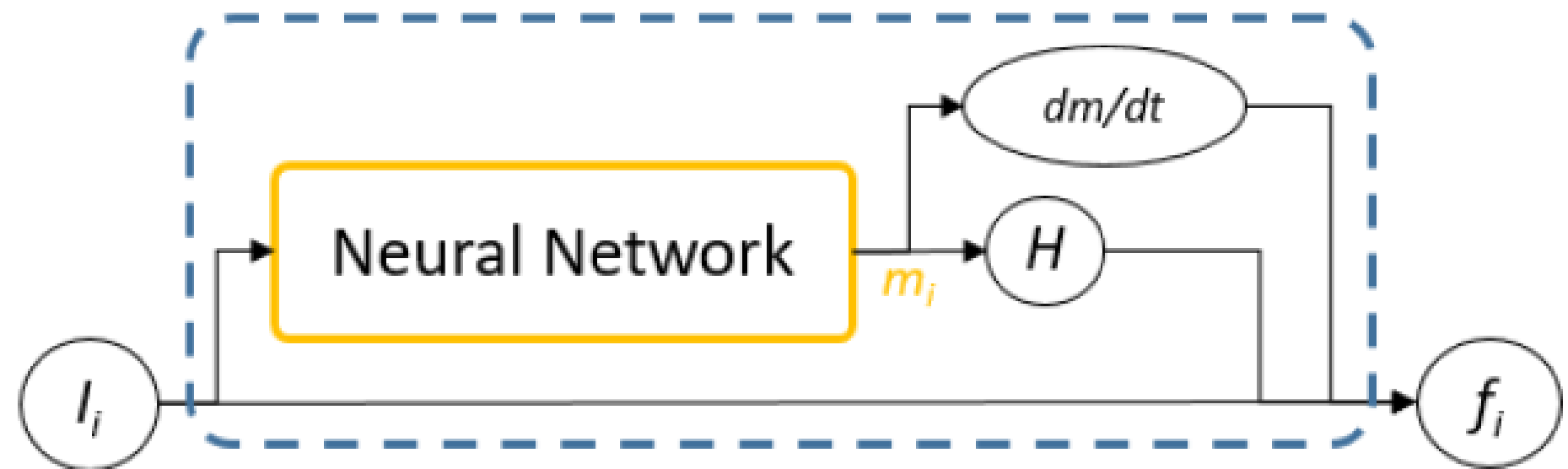
$$\frac{\partial V_c}{\partial t} = \frac{V_s - V_c}{RC}$$

PyNN: physics-informed neural networks

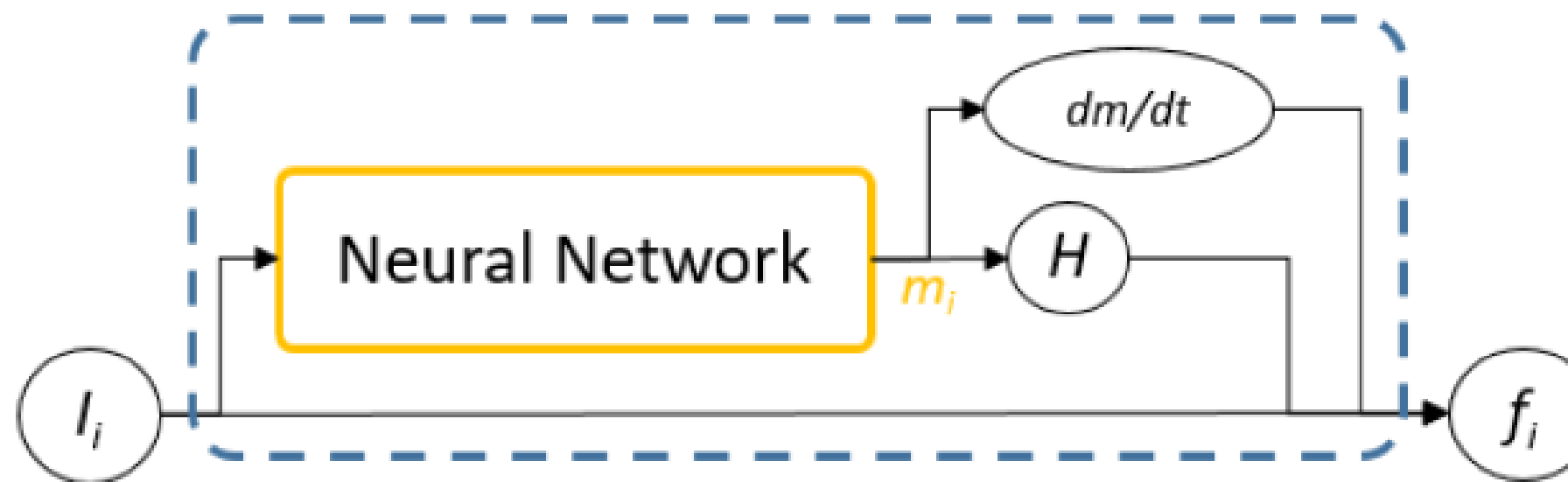
$$\frac{\partial m}{\partial t} + H(m; \lambda) = 0$$

$$f = \frac{\partial m}{\partial t} + H(m; \lambda)$$

$$f = \frac{\partial V_c}{\partial t} - \frac{V_s - V_c}{RC}$$



PyNN: physics-informed neural networks

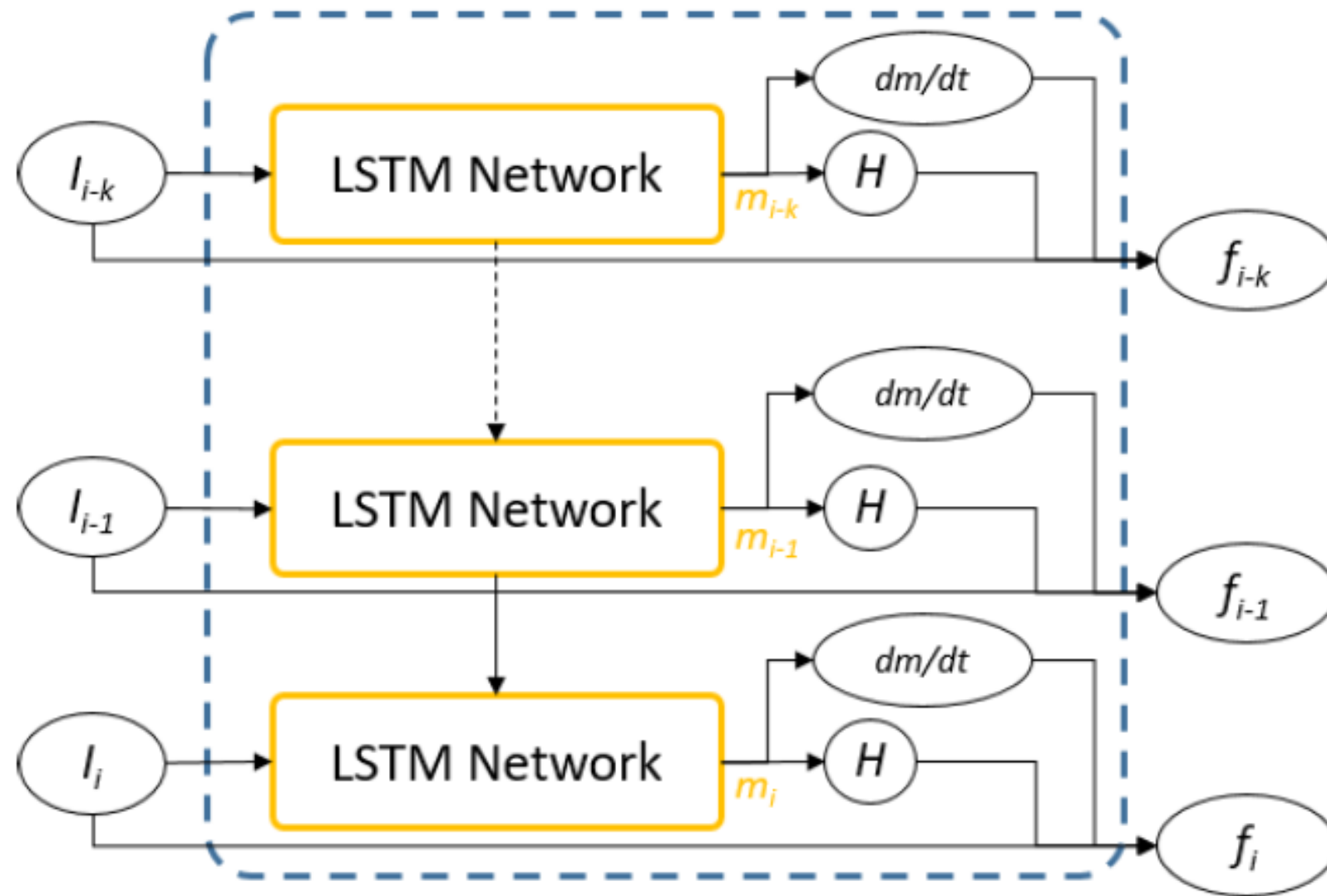


$$\hat{m}_i^{PyNN} = PyNN(I_i; \theta)$$

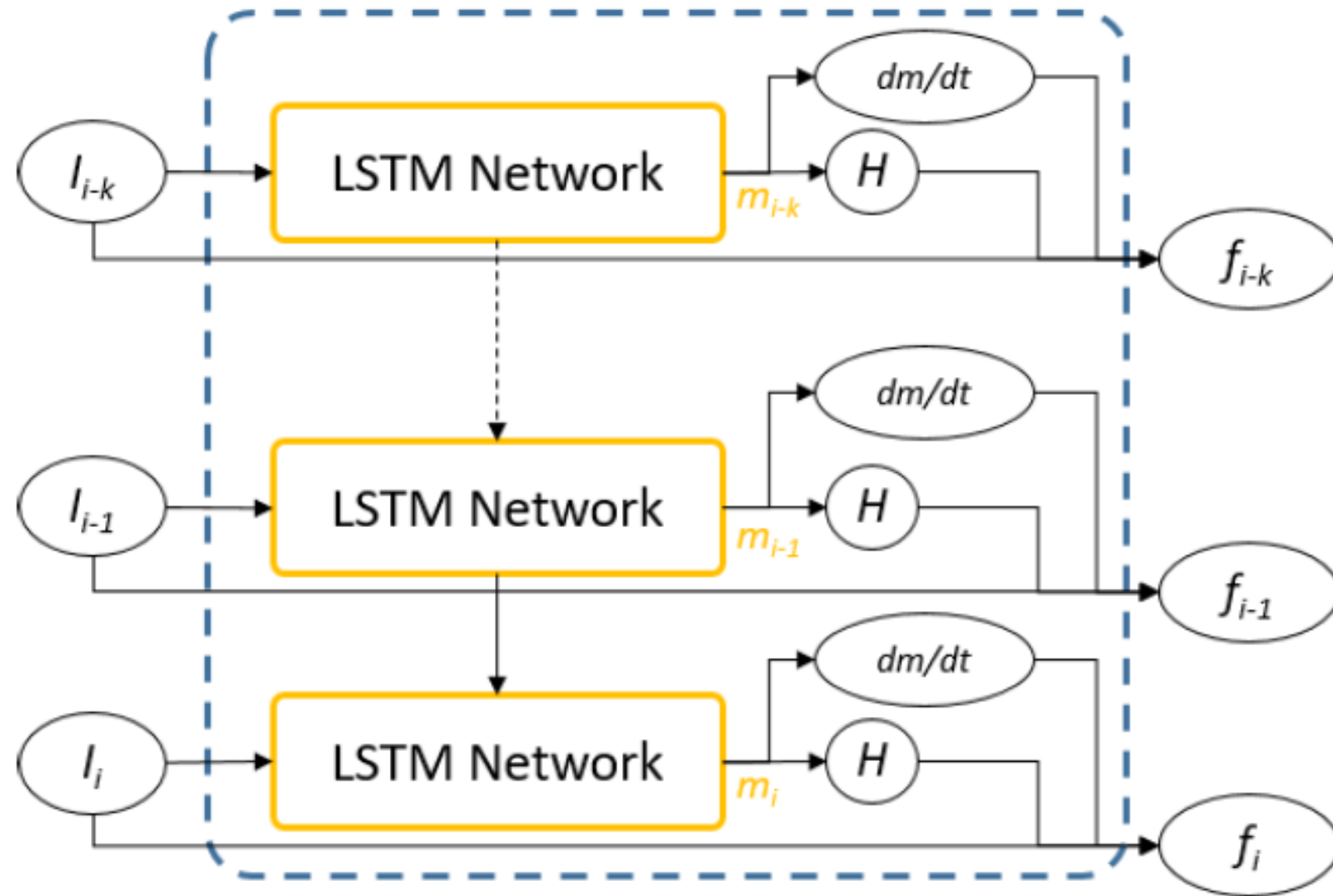
$$\hat{V}_{c,i}^{PyNN} = PyNN(R_i, C_i, V_{s,i}, t_i; \theta)$$

$$\hat{f}_i^{PyNN} = \left(\frac{\partial \hat{V}_c^{PyNN}}{\partial t} \right)_i - \frac{V_{s,i} - \hat{V}_{c,i}^{PyNN}}{R_i C_i}$$

PyLSTM: physics-informed long short-term memory networks



PyLSTM: physics-informed long short-term memory networks



$$\hat{m}_i^{PyLSTM} = PyLSTM(I_i, I_{i-1}, \dots, I_{i-k}; \theta)$$

$$\hat{V}_{c,i}^{PyLSTM} = PyLSTM(R_i, C_i, V_{s,i}, t_i, \dots, R_{i-k}, C_{i-k}, V_{s,i-k}, t_{i-k}; \theta)$$

- Training

$$\begin{aligned} L(W) &= MSE_m + MSE_f + \Omega(W) \\ &= \frac{1}{N} \sum_{i=1}^N (e_{m,i}^2 + e_{f,i}^2 + \lambda |W_i|^2) \end{aligned}$$

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- Data simulation

- ☐ Identifying voltage across the capacitor (V_c)
- ☐ Data is simulated for 5000 seconds (100 observations/second) based on randomly chosen values

$$V_s \in \{0, 1, 2, 3\}V; R \in \{1, 2, 3\}\Omega; C \in \{1, 2, 3\}F$$

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- Model configuration

- ☐ Both architectures are fully connected networks with two hidden layers with 16 neurons in each layer.
- ☐ We build a PyLSTM with the length $k = 50$ steps to make predictions for the next step. Two hidden layers of 16 LSTM cells each are utilized.
- ☐ The 'teacher-forcing' training is used to train the LSTM network at each step.
- ☐ Prediction with PyLSTM: the data id feed for the last k steps to make the prediction.

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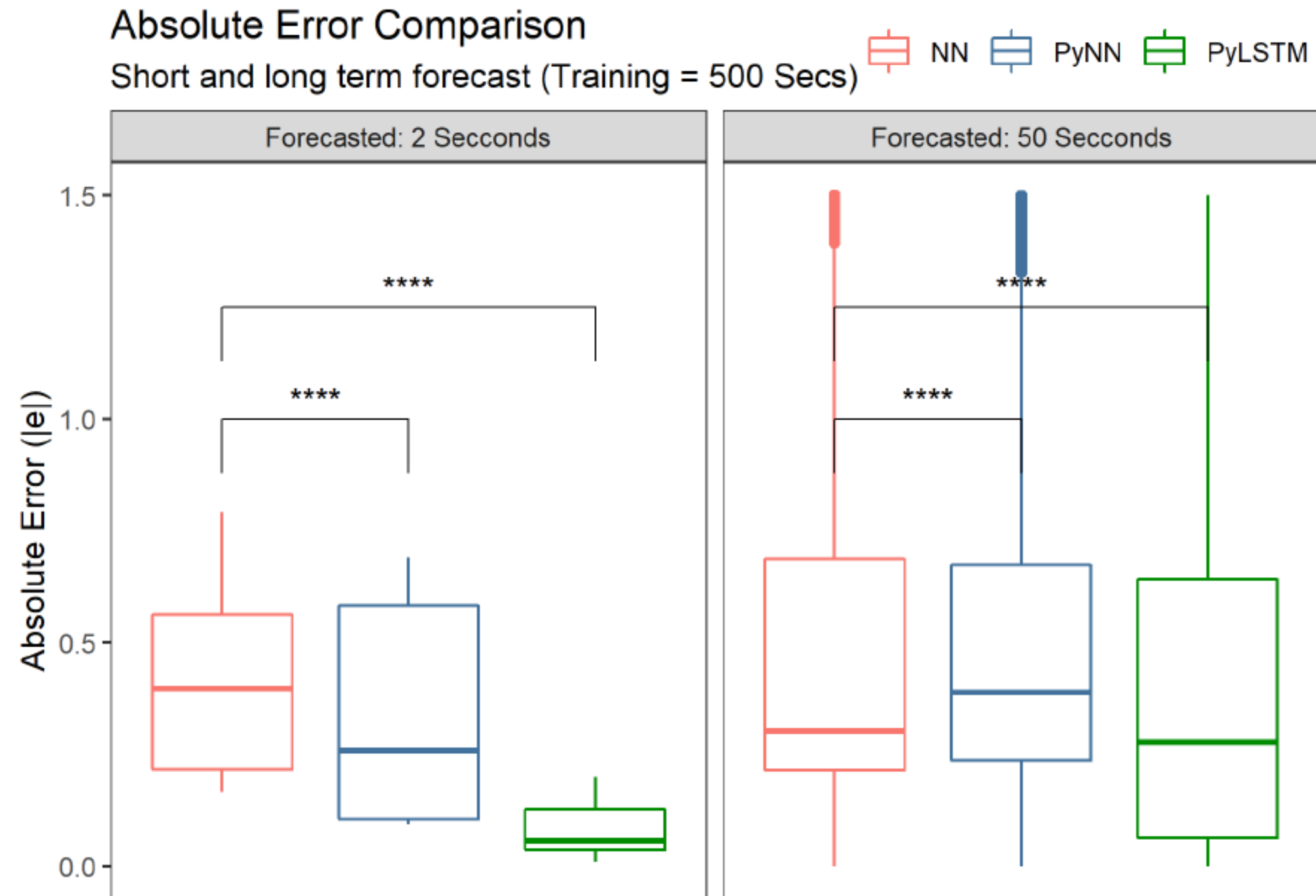
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- Evaluation

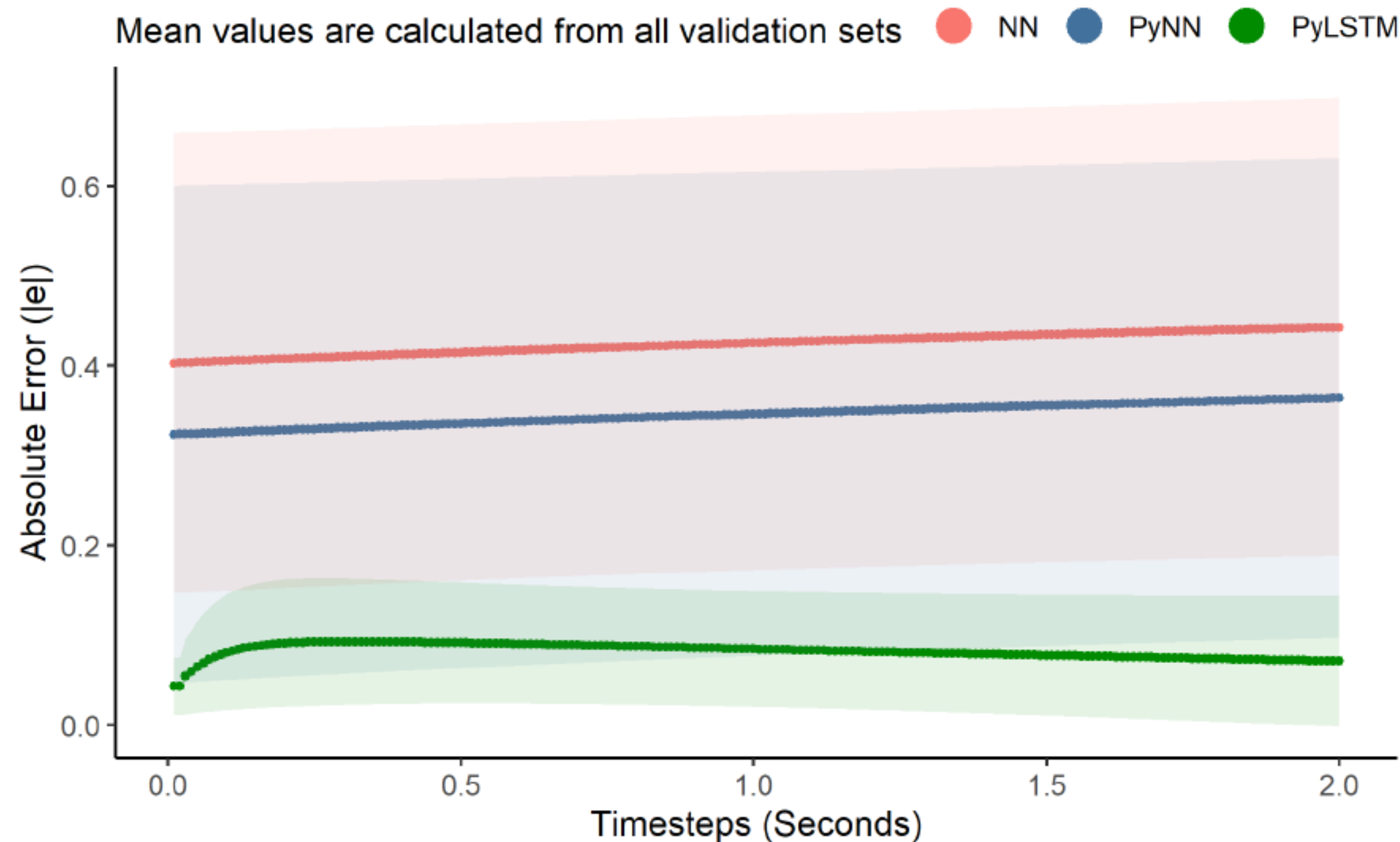
$$|e_i|_M = |V_{c,i} - \hat{V}_{c,i}^M|$$



Absolute error distribution for short-term (2 s) and long-term predictions (50 s)

Short term forecast errors in Neural Networks

Mean values are calculated from all validation sets

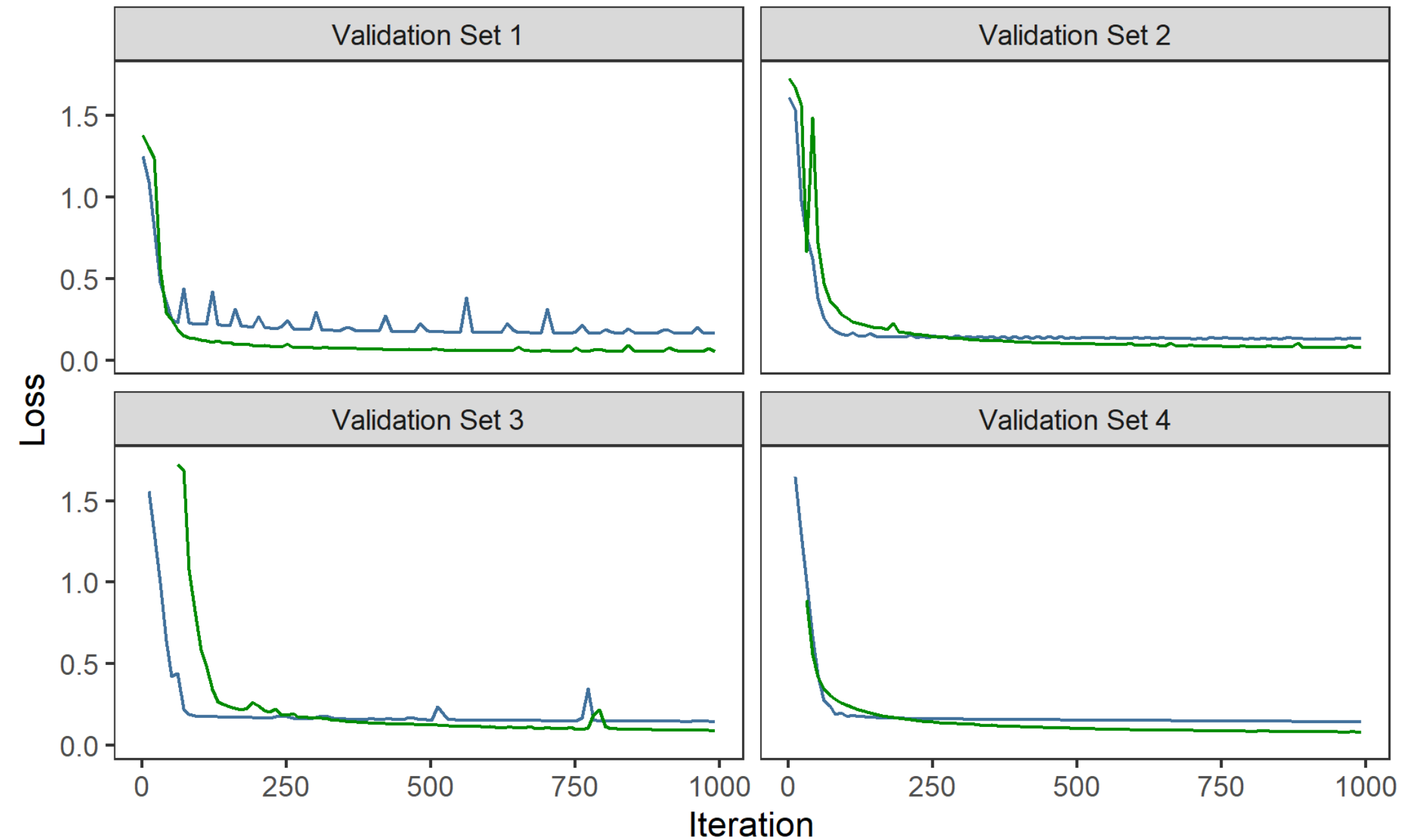


Absolute error for short-term predictions.

Loss for physics based networks

Average value of loss across all validation sets

— PyNN — PyLSTM



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