

$$f(x, y) = 3x^2 + 5e^{-y} + 10$$

$$\frac{df(x, y)}{dx} = 6x$$

$$\frac{df(x, y)}{dy} = -5e^{-y}$$

$$\text{learning rate} = 0.153$$

$$\text{let } x_0 = 10, y_0 = 8.1$$

$$\text{grad at } x_0 = 6 \times 9.2 = 55.2$$

$$\text{grad at } y_0 = -5e^{-(8.1)} = -0.001517$$

ite-1:-

$$x_1 = x_0 - (\text{learning rate} \times \text{grad } f \text{ at } x_0)$$

$$y_1 = y_0 - (\text{learning rate} \times \text{gradient } f \text{ at } y_0)$$

$$y_1 = 8.1 - (0.153 \times (-0.001517))$$

$$= 8.1 - 0.00223$$

$$= 8.099767 \approx 8.10$$

$$\begin{aligned} x_1 &= 9.2 - (0.153 \\ &\quad \times 55.2) \\ &= 9.2 - 8.4456 \\ &= 0.7544 \end{aligned}$$

ite-2

$$x_2 = x_1 - (\text{learning rate} \times \text{grad } f \text{ at } x_1)$$

$$x_2 = 0.7544 - 1.426878$$

$$= 0.672478$$

$$y_2 = y_1 - (\text{learning rate} \times \text{grad } y \text{ at } y_1)$$

$$y_2 = 8.10023 - (0.153 \times$$

$$= 6.86 \quad \bullet 8.1)$$