Program 1 - FIND S

```
import csv
hypo=['%','%','%','%','%','%'];
with open('Training_examples.csv') as csv_file:
       readcsv = csv.reader(csv_file, delimiter=',')
       data = []
       print("\nThe given training examples are:")
       for row in readcsv:
               print(row)
               if row[len(row)-1].upper() == "YES":
                       data.append(row)
print("\nThe positive examples are:")
for x in data:
       print(x)
TotalExamples = len(data)
print("The steps of the Find-s algorithm are\n",hypo)
list = []
d=len(data[0])-1
for j in range(d):
       list.append(data[0][j])
hypo=list;
for i in range(TotalExamples):
       for k in range(d):
               if hypo[k]!=data[i][k]:
                       hypo[k]='?'
       print(hypo)
print("\nThe maximally specific Find-s hypothesis for the given training examples is");
print(hypo)
```

Sunny	Warm	Normal	Strong	Warm	Same	Yes
Sunny	Warm	High	Strong	Warm	Same	Yes
Rainy	Cold	High	Strong	Warm	Change	No
Sunny	Warm	High	Strong	Cool	Change	Yes

PROGRAM 2 – CANDIDATE PROGRAM

```
import numpy as np
import pandas as pd
data = pd.DataFrame(data=pd.read_csv('Training_examples.csv'))
print(data)
concepts = np.array(data.iloc[:,0:-1])
print("concepts",concepts)
target = np.array(data.iloc[:,-1])
print("target",target)
def learn(concepts, target):
  specific h = concepts[0].copy()
  print("initialization of specific_h and general_h")
  print(specific_h)
  general_h = [["?" for i in range(len(specific_h))] for i in range(len(specific_h))]
  print(general_h)
  for i, h in enumerate(concepts):
     if target[i] == "Yes":
       for x in range(len(specific_h)):
            if h[x] != specific h[x]:
             specific_h[x] = '?'
             general_h[x][x] = '?'
     if target[i] == "No":
       for x in range(len(specific_h)):
          if h[x] != specific_h[x]:
             general_h[x][x] = specific_h[x]
          else:
             general_h[x][x] = '?'
     print(" steps of Candidate Elimination Algorithm",i+1)
     print(specific_h)
     print(general_h)
  indices = [i for i, val in enumerate(general_h) if val == ['?', '?', '?', '?', '?', '?']]
  print("ind-----,indices)
  for i in indices:
    general_h.remove(['?', '?', '?', '?', '?', '?'])
  return specific_h, general_h
s final, g final = learn(concepts, target)
```

 $\begin{array}{l} print("Final\ Specific_h:",\ s_final,\ sep="\n")\\ print("Final\ General_h:",\ g_final,\ sep="\n") \end{array}$

C1	C2	C3	C4	C5	C6	C7
Sunny	Warm	Normal	Strong	Warm	Same	Yes
Sunny	Warm	High	Strong	Warm	Same	Yes
Rainy	Cold	High	Strong	Warm	Change	No
Sunny	Warm	High	Strong	Cool	Change	Yes

PROGRAM 3

```
import pandas as pd
from pandas import DataFrame
df tennis = pd.DataFrame(data = pd.read csv('tennis.csv'))
print("\n Given Play Tennis Data Set:\n\n",df_tennis)
def entropy(probs):
  import math
  return sum([-prob*math.log(prob, 2) for prob in probs])
def entropy of list(a list):
  from collections import Counter
  cnt = Counter(x for x in a_list) # Counter calculates the propotion of class
  num_instances = len(a_list)*1.0 # = 14
  probs = [x / num\_instances for x in cnt.values()] # x means no of YES/NO
  return entropy(probs) # Call Entropy:
total_entropy = entropy_of_list(df_tennis['PlayTennis'])
print("\n Total Entropy of PlayTennis Data Set:",total entropy)
def information_gain(df, split_attribute_name, target_attribute_name, trace=0):
  df_split = df.groupby(split_attribute_name)
  nobs = len(df.index) * 1.0
  df_agg_ent = df_split.agg({target_attribute_name : [entropy_of_list, lambda x: len(x)/nobs]
})#[target attribute name]
  df agg ent.columns = ['Entropy', 'PropObservations']
  # Calculate Information Gain:
  new_entropy = sum( df_agg_ent['Entropy'] * df_agg_ent['PropObservations'] )
  old_entropy = entropy_of_list(df[target_attribute_name])
  return old_entropy - new_entropy
print('Info-gain for Outlook is :'+str( information_gain(df_tennis, 'Outlook', 'PlayTennis')),"\n")
print('\n Info-gain for Humidity is: ' + str( information gain(df tennis, 'Humidity', 'PlayTennis')),"\n")
print('\n Info-gain for Wind is:' + str( information_gain(df_tennis, 'Wind', 'PlayTennis')),"\n")
print('\n Info-gain for Temperature is:' + str( information gain(df tennis,
"Temperature', 'PlayTennis')), "\n")
def id3(df, target_attribute_name, attribute_names, default_class=None):
  from collections import Counter
  cnt = Counter(x for x in df[target attribute name])# class of YES /NO
  if len(cnt) == 1:
     return next(iter(cnt)) # next input data set, or raises StopIteration when EOF is hit.
  elif df.empty or (not attribute names):
     return default_class # Return None for Empty Data Set
  else:
```

```
default_class = max(cnt.keys()) #No of YES and NO Class
     gainz = [information_gain(df, attr, target_attribute_name) for attr in attribute_names]
     index_of_max = gainz.index(max(gainz)) # Index of Best Attribute
     best_attr = attribute_names[index_of_max]
     tree = {best_attr:{}}
     remaining_attribute_names = [i for i in attribute_names if i != best_attr]
     for attr_val, data_subset in df.groupby(best_attr):
       subtree = id3(data subset,
               target attribute name,
              remaining_attribute_names,
               default_class)
       tree[best_attr][attr_val] = subtree
    return tree
attribute_names = list(df_tennis.columns)
print("List of Attributes:", attribute_names)
attribute_names.remove('PlayTennis')
print("Predicting Attributes:", attribute_names)
# Run Algorithm:
from pprint import pprint
tree = id3(df_tennis,'PlayTennis',attribute_names)
print("\n\nThe Resultant Decision Tree is :\n")
pprint(tree)
attribute = next(iter(tree))
print("Best Attribute :\n",attribute)
print("Tree Keys:\n",tree[attribute].keys())
```

	PlayTennis	Outlook	Temperature	Humidity	Wind
0	No	Sunny	Hot	High	Weak
1	No	Sunny	Hot	High	Strong
2	Yes	Overcast	Hot	High	Weak
3	Yes	Rain	Mild	High	Weak
4	Yes	Rain	Cool	Normal	Weak
5	No	Rain	Cool	Normal	Strong
6	Yes	Overcast	Cool	Normal	Strong
7	No	Sunny	Mild	High	Weak
8	Yes	Sunny	Cool	Normal	Weak
9	Yes	Rain	Mild	Normal	Weak
10	Yes	Sunny	Mild	Normal	Strong
11	Yes	Overcast	Mild	High	Strong
12	Yes	Overcast	Hot	Normal	Weak
13	No	Rain	Mild	High	Strong

PROGRAM 4 – BACKPROPOGATION ALGORITHM

```
import numpy as np
id = np.array([[2,9],[1,5],[3,6]], dtype=float)
eo = np.array([[92],[86],[89]], dtype = float)
id = id/np.amax(id,axis=0)
eo = eo/100
def sigmoid(x):
  return 1/(1+np.exp(-x))
def derivative_sigmoid(x):
  return x*(1-x)
epoch = 5
lr = 0.1
il\_neurons = 2
hd neurons = 3
ol neurons = 1
hw = np.random.uniform(size=(il_neurons,hd_neurons))
hb = np.random.uniform(size=(1,hd_neurons))
ow = np.random.uniform(size=(hd_neurons,ol_neurons))
ob = np.random.uniform(size=(1,ol_neurons))
print("Input :", id)
for i in range(epoch):
  hidden_input = np.dot(id,hw)
  hidden_input = hidden_input +hb
  hlo = sigmoid(hidden_input)
  outputlayer_input = np.dot(hlo,ow)
  outputlayer_input = outputlayer_input + ob
  olo = sigmoid(outputlayer_input)
  ol error = eo-olo
  ol_gradient = derivative_sigmoid(olo)
  ol_error_correction =ol_error*ol_gradient
  hl_error = ol_error_correction.dot(ow.T)
  hl gradient = derivative sigmoid(hlo)
  hl error correction= hl error*hl gradient
  ow+= hlo.T.dot(ol_error_correction)*lr
  hw+= id.T.dot(hl_error_correction)*lr
print("Expected Output", eo)
print("Actual Output", olo)
```

PROGRAM 5 – Naïve's Bayes Classifier

```
print("\nNaive Bayes Classifier for concept learning problem")
import csv
import random
import math
import operator
def safe_div(x,y):
  if y == 0:
     return 0
  return x / y
def loadCsv(filename):
        lines = csv.reader(open(filename))
        dataset = list(lines)
        for i in range(len(dataset)):
                dataset[i] = [float(x) for x in dataset[i]]
        return dataset
def splitDataset(dataset, splitRatio):
        trainSize = int(len(dataset) * splitRatio)
        trainSet = []
        copy = list(dataset)
        i=0
        while len(trainSet) < trainSize:
                trainSet.append(copy.pop(i))
        return [trainSet, copy]
def separateByClass(dataset):
        separated = \{\}
        for i in range(len(dataset)):
                vector = dataset[i]
                if (vector[-1] not in separated):
                        separated[vector[-1]] = []
                separated[vector[-1]].append(vector)
        return separated
def mean(numbers):
        return safe_div(sum(numbers),float(len(numbers)))
def stdev(numbers):
        avg = mean(numbers)
        variance = safe\_div(sum([pow(x-avg,2) for x in numbers]),float(len(numbers)-1))
        return math.sqrt(variance)
def summarize(dataset):
        summaries = [(mean(attribute), stdev(attribute)) for attribute in zip(*dataset)]
        del summaries[-1]
```

```
return summaries
```

```
def summarizeByClass(dataset):
        separated = separateByClass(dataset)
        summaries = {}
        for classValue, instances in separated.items():
                summaries[classValue] = summarize(instances)
        return summaries
def calculateProbability(x, mean, stdev):
        exponent = math.exp(-safe_div(math.pow(x-mean,2),(2*math.pow(stdev,2))))
        final = safe_div(1, (math.sqrt(2*math.pi) * stdev)) * exponent
        return final
def calculateClassProbabilities(summaries, inputVector):
        probabilities = {}
        for classValue, classSummaries in summaries.items():
                probabilities[classValue] = 1
                for i in range(len(classSummaries)):
                        mean, stdev = classSummaries[i]
                        x = inputVector[i]
                        probabilities[classValue] *= calculateProbability(x, mean, stdev)
        return probabilities
def predict(summaries, inputVector):
        probabilities = calculateClassProbabilities(summaries, inputVector)
        bestLabel, bestProb = None, -1
        for classValue, probability in probabilities.items():
                if bestLabel is None or probability > bestProb:
                        bestProb = probability
                        bestLabel = classValue
        return bestLabel
def getPredictions(summaries, testSet):
        predictions = []
        for i in range(len(testSet)):
                result = predict(summaries, testSet[i])
                predictions.append(result)
        return predictions
def getAccuracy(testSet, predictions):
        correct = 0
        for i in range(len(testSet)):
                if testSet[i][-1] == predictions[i]:
                        correct += 1
        accuracy = safe_div(correct,float(len(testSet))) * 100.0
        return accuracy
def main():
        filename = 'ConceptLearning.csv'
```

```
splitRatio = 0.75
        dataset = loadCsv(filename)
        trainingSet, testSet = splitDataset(dataset, splitRatio)
        print('Split {0} rows into'.format(len(dataset)))
        print('Number of Training data: ' + (repr(len(trainingSet))))
        print('Number of Test Data: ' + (repr(len(testSet))))
        print("\nThe values assumed for the concept learning attributes are\n")
        print("OUTLOOK=> Sunny=1 Overcast=2 Rain=3\nTEMPERATURE=> Hot=1 Mild=2
Cool=3\nHUMIDITY=> High=1 Normal=2\nWIND=> Weak=1 Strong=2")
        print("TARGET CONCEPT:PLAY TENNIS=> Yes=10 No=5")
        print("\nThe Training set are:")
        for x in trainingSet:
               print(x)
        print("\nThe Test data set are:")
        for x in testSet:
                print(x)
        print("\n")
        # prepare model
        summaries = summarizeByClass(trainingSet)
        # test model
        predictions = getPredictions(summaries, testSet)
        actual = []
        for i in range(len(testSet)):
               vector = testSet[i]
                actual.append(vector[-1])
        # Since there are five attribute values, each attribute constitutes to 20% accuracy. So if all
attributes match with predictions then 100% accuracy
        print('Actual values: {0}%'.format(actual))
        print('Predictions: {0}%'.format(predictions))
        accuracy = getAccuracy(testSet, predictions)
        print('Accuracy: {0}%'.format(accuracy))
main()
```

1	1	1	1	5
1	1	1	2	5
2	1	1	2	10
3	2	1	1	10
3	3	2	1	10
3	3	2	2	5
2	3	2	2	10
1	2	1	1	5
1	3	2	1	10
3	2	2	2	10
1	2	2	2	10
2	2	1	2	10
2	1	2	1	10
3	2	1	2	5
1	2	1	2	10
1	2	1	2	5

PROGRAM 6 – Naives Bayesian Classifier

```
from sklearn.datasets import fetch_20newsgroups from sklearn.metrics import confusion_matrix from sklearn.metrics import classification_report import numpy as np
```

```
categories = ['alt.atheism', 'soc.religion.christian', 'comp.graphics', 'sci.med']
twenty train = fetch 20newsgroups(subset='train',categories=categories,shuffle=True)
twenty test = fetch 20newsgroups(subset='test',categories=categories,shuffle=True)
print(len(twenty train.data))
print(len(twenty test.data))
print(twenty_train.target_names)
from sklearn.feature_extraction.text import CountVectorizer
count vect = CountVectorizer()
X_train_tf = count_vect.fit_transform(twenty_train.data)
from sklearn.feature_extraction.text import TfidfTransformer
tfidf_transformer = TfidfTransformer()
X train tfidf = tfidf transformer.fit transform(X train tf)
from sklearn.naive_bayes import MultinomialNB
from sklearn.metrics import accuracy_score
from sklearn import metrics
mod = MultinomialNB()
mod.fit(X_train_tfidf, twenty_train.target)
X_test_tf = count_vect.transform(twenty_test.data)
X_test_tfidf = tfidf_transformer.transform(X_test_tf)
predicted = mod.predict(X_test_tfidf)
```

print("Accuracy:", accuracy_score(twenty_test.target, predicted))
print(classification_report(twenty_test.target,predicted,target_names=twenty_test.target_names))
print("confusion matrix is \n",metrics.confusion_matrix(twenty_test.target, predicted))

PROGRAM 7 – Bayesian network

```
import numpy as np
from urllib.request import urlopen
import urllib
import sklearn as skl
import pandas as pd
import pgmpy
Cleveland_data_URL = 'http://archive.ics.uci.edu/ml/machine-learning-databases/heart-
disease/processed.hungarian.data'
#names = ['age', 'sex', 'cp', 'trestbps', 'chol', 'fbs', 'restecg', 'thalach', 'exang', 'oldpeak', 'slope', 'ca',
'thal', 'heartdisease']
names = ['1','2','3','4','5','6','7','8','9','10','11','12','13','heartdisease']
heartDisease = pd.read_csv(urlopen(Cleveland_data_URL), names = names) #gets Cleveland
data
from pgmpy.models import BayesianModel
from pgmpy.estimators import MaximumLikelihoodEstimator, BayesianEstimator
#model = BayesianModel([('age', 'trestbps'), ('age', 'fbs'), ('sex', 'trestbps'), ('sex', 'trestbps'),
                                 ('exang', 'trestbps'),('trestbps', 'heartdisease'),('fbs', 'heartdisease'),
                                ('heartdisease', 'restecg'), ('heartdisease', 'thalach'), ('heartdisease', 'chol')])
#
# Learing CPDs using Maximum Likelihood Estimators
model =
BayesianModel([('1','4'),('1','6'),('2','4'),('2','4'),('4','heartdisease'),('6','heartdisease'),('heartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdisease'),('bartdiseas
isease','7'),('heartdisease','8'),('heartdisease','5')])
model.fit(heartDisease, estimator=MaximumLikelihoodEstimator)
print(model.get_cpds('1'))
print(model.get_cpds('5'))
print(model.get_cpds('2'))
model.get_independencies()
# Doing exact inference using Variable Elimination
from pgmpy.inference import VariableElimination
HeartDisease_infer = VariableElimination(model)
# Computing the probability of bronc given smoke.
q = HeartDisease_infer.query(variables=['heartdisease'], evidence={'1': 22})
print(q['heartdisease'])
q = HeartDisease_infer.query(variables=['heartdisease'], evidence={'5': 128})
print(q['heartdisease'])
```

PROGRAM 8 -EM & k-Means

```
import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn.cluster import KMeans
import sklearn.metrics as sm
import pandas as pd
import numpy as np
iris = datasets.load_iris()
X = pd.DataFrame(iris.data)
X.columns = ['Sepal_Length', 'Sepal_Width', 'Petal_Length', 'Petal_Width']
#% matplotlib inline
11 = [0,1,2]
def rename(s):
        12 = []
        for i in s:
                if i not in 12:
                        12.append(i)
        for i in range(len(s)):
                pos = 12.index(s[i])
                s[i] = 11[pos]
        return s
iris = datasets.load_iris()
print("\n IRIS TARGET NAMES:\n",iris.target_names)
X = pd.DataFrame(iris.data)
X.columns = ['Sepal_Length', 'Sepal_Width', 'Petal_Length', 'Petal_Width']
y = pd.DataFrame(iris.target)
y.columns = ['Targets']
print("Actual Target is:\n", iris.target)
model = KMeans(n_clusters=3)
model.fit(X)
                      # computes k means clustering, model.labels_=returns clustered array
plt.figure(figsize=(14,7))
colormap = np.array(['red', 'lime', 'black'])
plt.subplot(1, 2, 1)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[y.Targets], s=40)
plt.title('Real Classification')
```

```
plt.subplot(1, 2, 2)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[model.labels_], s=40)
plt.title('K Mean Classification')
plt.show()
km = rename(model.labels_)
print("\nWhat KMeans thought: \n", km)
print("Accuracy of KMeans is ",sm.accuracy_score(y, km))
print("Confusion Matrix for KMeans is \n",sm.confusion_matrix(y, km))
from sklearn import preprocessing
scaler = preprocessing.StandardScaler()#Standardize features by removing the mean and scaling to unit
scaler.fit(X)
xsa = scaler.transform(X)
xs = pd.DataFrame(xsa, columns = X.columns)
print("\n",xs.sample(5))
from sklearn.mixture import GaussianMixture
gmm = GaussianMixture(n components=3)
gmm.fit(xs)
y_cluster_gmm = gmm.predict(xs)
plt.subplot(1, 2, 1)
plt.scatter(X.Petal_Length, X.Petal_Width, c=colormap[y_cluster_gmm], s=40)
plt.title('GMM Classification')
plt.show()
em = rename(y_cluster_gmm)
print("\nWhat EM thought: \n", em)
print("Accuracy of EM is ",sm.accuracy_score(y, em))
print("Confusion Matrix for EM is \n", sm.confusion_matrix(y, em))
```

Program 8 (version2)

```
import matplotlib.pyplot as plt
from sklearn.datasets import load iris
df = load_iris()
X = df["data"]
Y = df["target"]
from sklearn.cluster import KMeans
km_cluster = KMeans(n_clusters = 3)
km cluster.fit(X)
km_predictions = km_cluster.predict(X)
print("KM Thought")
print(km_predictions)
plt.scatter(X[:, 0], X[:, 1], c = km_predictions) # Sepal length vs Sepal width (in cm)
plt.show()
from sklearn.mixture import GaussianMixture
em cluster = GaussianMixture(n components = 3)
em cluster.fit(X)
em_predictions = em_cluster.predict(X)
print("EM Thought")
print(em_predictions)
plt.scatter(X[:, 0], X[:, 1], c = em\_predictions)
plt.show()
#Comparing their accuracies
from sklearn.metrics import accuracy_score, confusion_matrix
km_accuracy = accuracy_score(Y, km_predictions)
em_accuracy = accuracy_score(Y, em_predictions)
km_confusion = confusion_matrix(Y, km_predictions)
em_confusion = confusion_matrix(Y, em_predictions)
print("Accuracy of KMeans is ",km_accuracy)
print("Accuracy of EM is ",em_accuracy)
print("Confusion matrix of KMeans: \n", km_confusion)
print("Confusion matrix of EM: \n", em_confusion)
```

PROGRAM 9 – k – nearest neighbor algorithm

```
from sklearn.datasets import load iris
from sklearn.neighbors import KNeighborsClassifier
import numpy as np
from sklearn.model selection import train test split
iris_dataset=load_iris()
print("\n IRIS FEATURES \ TARGET NAMES: \n ", iris_dataset.target_names)
for i in range(len(iris_dataset.target_names)):
  print("\n[{0}]:[{1}]".format(i,iris_dataset.target_names[i]))
X_train, X_test, y_train, y_test = train_test_split(iris_dataset["data"], iris_dataset["target"],
random state=0)
print("\n X TRAIN \n", X_train)
print("\n X TEST \n", X_test)
print("\n Y TRAIN \n", y_train)
print("\n Y TEST \n", y_test)
kn = KNeighborsClassifier(n_neighbors=1)
kn.fit(X_train, y_train)
i=10
for i in range(len(X_test)):
  x = X \text{ test[i]}
  x_new = np.array([x])
  prediction = kn.predict(x_new)
  print("\n Actual : {0} {1}, Predicted
:{2}{3}".format(y_test[i],iris_dataset["target_names"][y_test[i]],prediction,iris_dataset["target_n
ames"][ prediction]))
print("\n TEST SCORE[ACCURACY]: {:.2f}\n".format(kn.score(X_test, y_test)))
```

PROGRAM 10 – Locally Weighted Regression

```
import numpy as np
from bokeh.plotting import figure, show
from bokeh.layouts import gridplot
def plot_lwr(tau):
  # prediction
  domain = np.linspace(-3, 3, num=300)
  prediction = [local_regression(x0, X, Y, tau) for x0 in domain]
  plot = figure(plot_width=400, plot_height=400)
  plot.title.text = 'tau=%g' % tau
  plot.scatter(X, Y, alpha=.3)
  plot.line(domain, prediction, line_width=2, color='red')
  return plot
def local_regression(x0, X, Y, tau):
  # add bias term
  x0 = np.r_{1}, x0 # r_{2} = Translates slice objects to concatenation along the first axis
  X = \text{np.c}[\text{np.ones}(\text{len}(X)), X] \# c_=> \text{Translates slice objects to concatenation along the}
second axis.
  # fit model: normal equations with kernel
  xw = X.T * radial kernel(x0, X, tau)
  beta = np.linalg.pinv(xw @ X) @ xw @ Y
  # predict value
  return x0 @ beta
def radial_kernel(x0, X, tau):
  return np.exp(np.sum((X - x0) ** 2, axis=1) / (-2 * tau * tau))
n = 1000
# generate dataset
X = np.linspace(-3, 3, num = n)
Y = np.log(np.abs(X ** 2 - 1) + .5)
# jitter X (Draw random samples from a normal (Gaussian) distribution)
X += np.random.normal(scale=.1, size=n)
show(gridplot([
  [plot_lwr(10.), plot_lwr(1.)],
  [plot_lwr(0.1), plot_lwr(0.01)]
]))
```

Program 10 (modified)

```
import math
import pylab as plt
import math
import numpy as np
n = 100
x = np.linspace(0, 2 * math.pi, n)[:,np.newaxis]
y = np.sin(x) + 0.3*np.random.randn(n)[:,np.newaxis]
print("len",x)
print("len2",len(y))
from sklearn.preprocessing import PolynomialFeatures
from sklearn.linear_model import LinearRegression
poly = PolynomialFeatures(degree = 5)
X_poly = poly.fit_transform(x)
poly.fit(X_poly, y)
lin2 = LinearRegression()
lin2.fit(X_poly, y)
plt.plot(x, y, color = 'blue', label='y noisy')
plt.plot(x, lin2.predict(poly.fit_transform(x)), color = 'red', label='y pred')
plt.title('Local Regression')
plt.legend()
plt.show()
```